#### Hardware Implementation of FIR/IIR Digital Filters Using Integral Stochastic Computation

Arash Ardakani, Francois Leduc-Primeau and Warren J. Gross Department of Electrical and Computer Engineering McGill University Montreal, Quebec, Canada March 25, 2016



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## Introduction

- Stochastic Computing (SC) Provides some advantages over binary radix implementation:
  - Low-cost VLSI implementation
  - Fault tolerant hardware
- Despite its advantages, it introduces some challenges:
  - High processing time
  - Low accuracy
- Therefore, SC was viewed as not suitable for applications which require high accuracy such as digital filters.



# Stochastic Representation

In SC, a real value x ∈ [0, 1] is represented as a sequence of random bits, X<sub>i</sub> ∈ {0, 1}, i ∈ {1, 2, ..., N}, where N denotes the stream length. The number x corresponds to the expected value of an element of the sequence:

$$E[X_i] = x$$

This stochastic representation is known as the *unipolar* format. The *bipolar* format is also used for stochastic representation of a real number x ∈ [-1, 1] by setting:

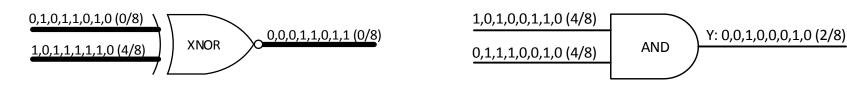
 $E[X_i] = (x + 1)/2$ 



# Computational Elements in SC

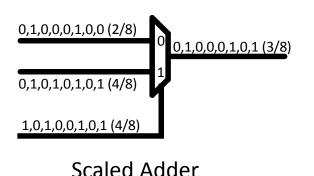
• Multiplication:

**Bipolar Multiplier** 



Unipolar Multiplier

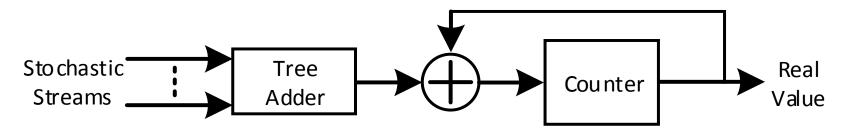
• Addition:



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#### Accumulative Parallel Counter (APC)

- It was introduced in [1]
- The APC uses a binary tree-adder to perform additions
- The output of APC is in binary radix domain
- The APC is restricted to the applications requiring information in binary domain after additions

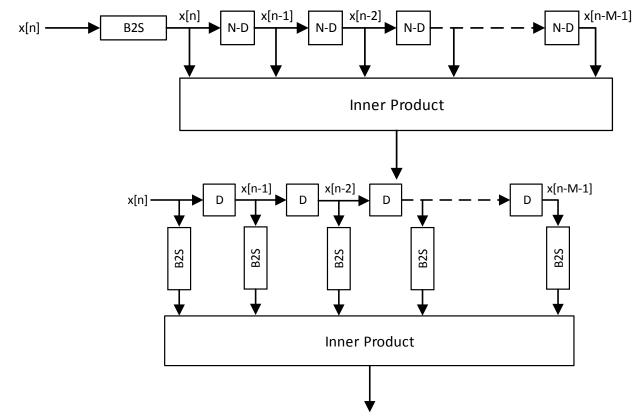


[1] Pai-Shun Ting and J.P. Hayes, "Stochastic Logic Realization of Matrix Operations," in 2014 17th Euromicro Conference on Digital System Design (DSD), Aug 2014, pp. 356–364.



#### Previously Proposed FIR Filter Based on SC

Two conventional approaches used for stochastic implementation of FIR filters by delaying (a) the stochastic sequence and (b) the binary numbers [2].



[2] Yun-Nan Chang and K.K. Parhi, "Architectures for digital filters using stochastic computing," in Proc. 2013 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), May 2013, pp. 2697–2701.

# **Integral Stochastic Computing**

- Integral SC was introduced in [3]
- Each element S<sub>i</sub> of the integer stochastic stream represents a real value s E [0, m]
- ISC can be generated by summing up m binary stochastic streams as follows: .

$$S_i = \sum_{j=1}^m X_i^j$$

- where  $X_i^j$  denotes an element of stochastic stream  $X^j$  representing the real value  $x^j \in [0, 1]$ . .
- Then, the expected value of the sequence element  $S_i$  is given by: .

$$s = E[S_i] = \sum_{j=1}^m x^j$$

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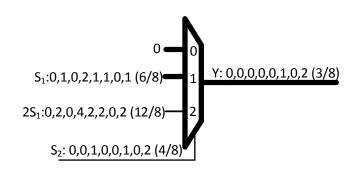
[3] A. Ardakani, F. Leduc-Primeau, N. Onizawa, T. Hanyu and W. J. Gross, "VLSI Implementation of Deep Neural Network Using Integral Stochastic Computing," CoRR, vol. abs/1509.08972, 2015. [Online]. Available: http://arxiv.org/abs/1509.08972.

# **ISC** Computational Elements

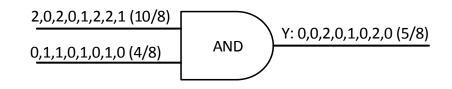
- It was shown that additions are performed by using binary adders, and multiplications can be performed by binary multipliers.
- Solutions to compensate the complexity of ISC multiplier:

S<sup>2</sup>: 1,2,2,1,1,1,2,2 (12/8)

Coefficient values mostly lie in [-2, 2] and multiplications are then performed using a multiplexer as follows:

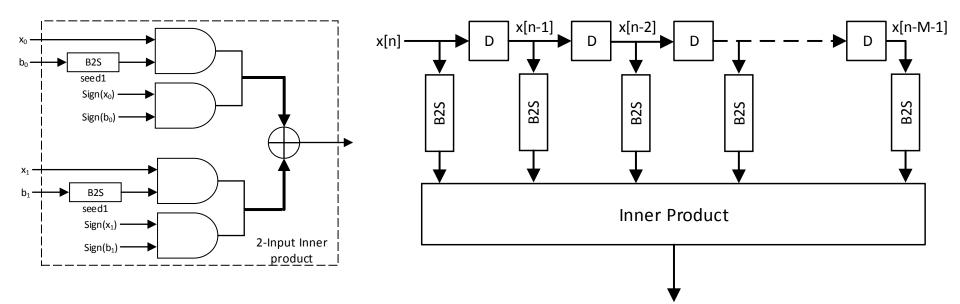


If one of the inputs is in SC format, multiplication can be performed using bit-wise AND gate



# The proposed FIR Filter

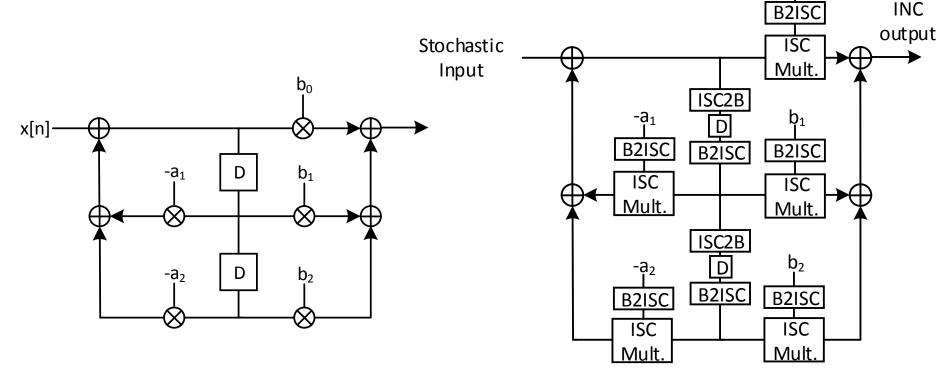
 Due to uncorrelated ISC addition, the proposed FIR filter only requires two LFSR units to perform computations as opposed to conventional stochastic filters





### The Proposed IIR Filter Based on ISC

 High-order filter can be achieved by cascading the proposed stochastic architecture of a second-order IIR filter using Integral SC.



The direct-form II structure for a second-order IIR filter.

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The proposed stochastic architecture of a secondorder IIR filter using Integral SC.

## FIR Filter Simulation Results

The output error-to-signal power ratio of the proposed stochastic FIR filters

Filter Order	Low-pass Cut-off Frequency				
	0.2π	0.4π	0.6π	0.8π	
45	0.0014	0.0012	2.9×10 <sup>-4</sup>	5.3×10 <sup>-4</sup>	
55	0.0012	0.0014	4.28×10 <sup>-4</sup>	5.3×10 <sup>-4</sup>	
Filter Order	High-pass Cut-off Frequency				
	0.2π	0.4π	0.6π	0.8π	
46	0.0012	0.0011	0.0012	0.0021	
56	2.8×10 <sup>-4</sup>	8.1×10 <sup>-4</sup>	0.0011	0.0018	



## **IIR Filter Simulation Results**

The output error-to-signal power ratio of the proposed stochastic IIR filters

Filter Type	Direct Form [2]	Proposed
Low-Pass	42.5721	0.0030
High-Pass	43.3597	0.0011

[2] Yun-Nan Chang and K.K. Parhi, "Architectures for digital filters using stochastic computing," in Proc. 2013 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), May 2013, pp. 2697–2701.



# Hardware Implementation Results

The hardware implementation in a 65 nm CMOS technology @ 400 MHz for a stream length of L.

Filter Type	FIR		IIR	
Implementatio n Type	ISC	Binary	ISC	Binary
Filter Order	56	56	6	6
Area (µm)	22,526	218,905	7,620	36,921
Latency (ns)	2.5 × L	2.5	2.5 × L	2.5



# Conclusion

- The proposed FIR filter uses the APC and AND gate as its main computational units to perform the additions and multiplications.
- The error rate of the proposed FIR architecture remains constant as the filter order increases.
- A second-order direct-form II structure of an IIR filter is proposed using the Integral SC.
- A high-order IIR filter can be obtained by cascading series of second-order direct-form II structures.
- The error-to-signal power ratio results of the proposed IIR filter showed a roughly 4 orders of magnitude improvement compared to the conventional structure.





