

# Multi-step Online Unsupervised Domain Adaptation

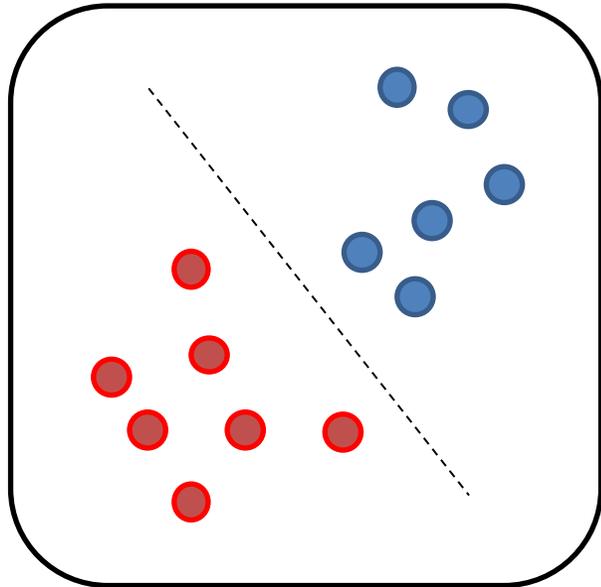
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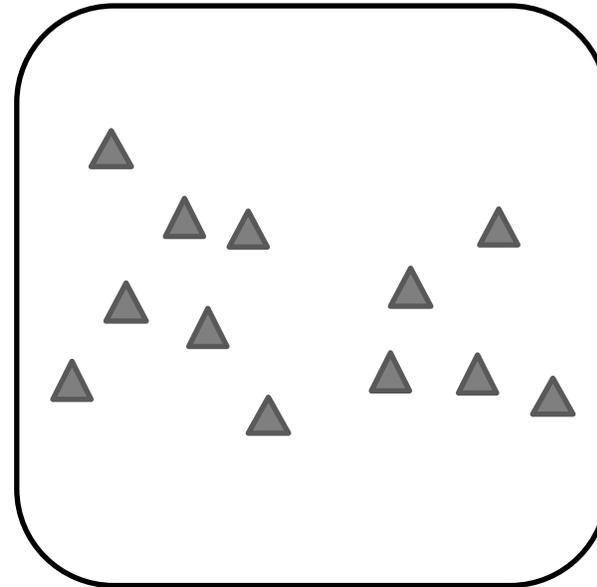
- Introduction
- Main steps of proposed method
  - Subspace Representation
  - Averaging Mean-target Subspace
  - Domain Adaptation
  - Recursive Feedback
- Experimental Results
- Conclusion

# *Introduction*

Source Domain

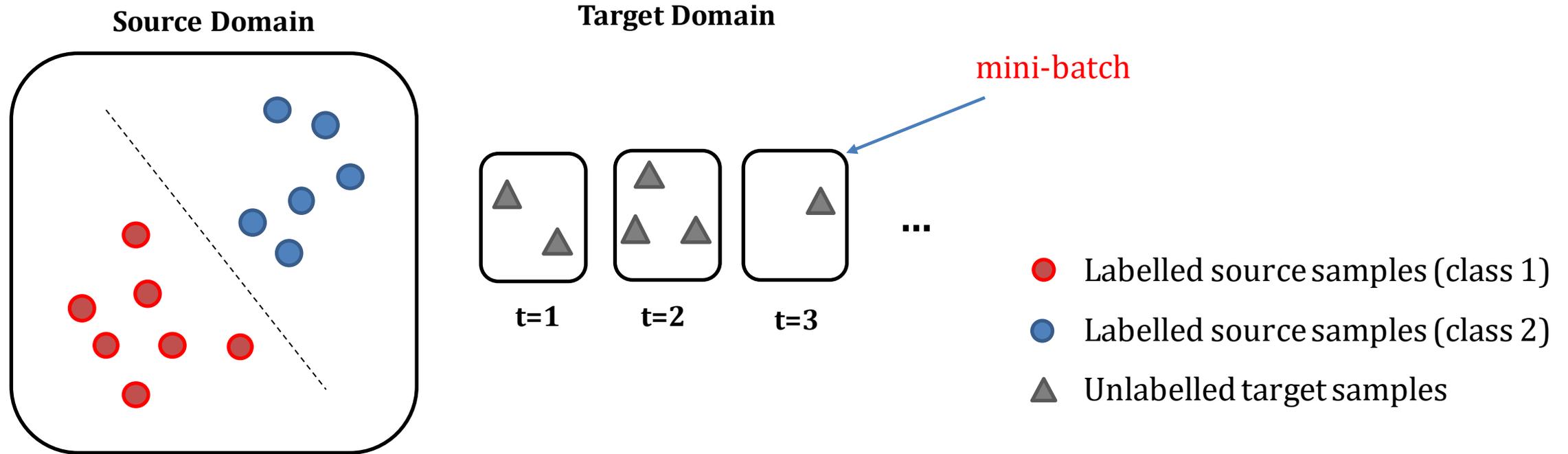


Target Domain



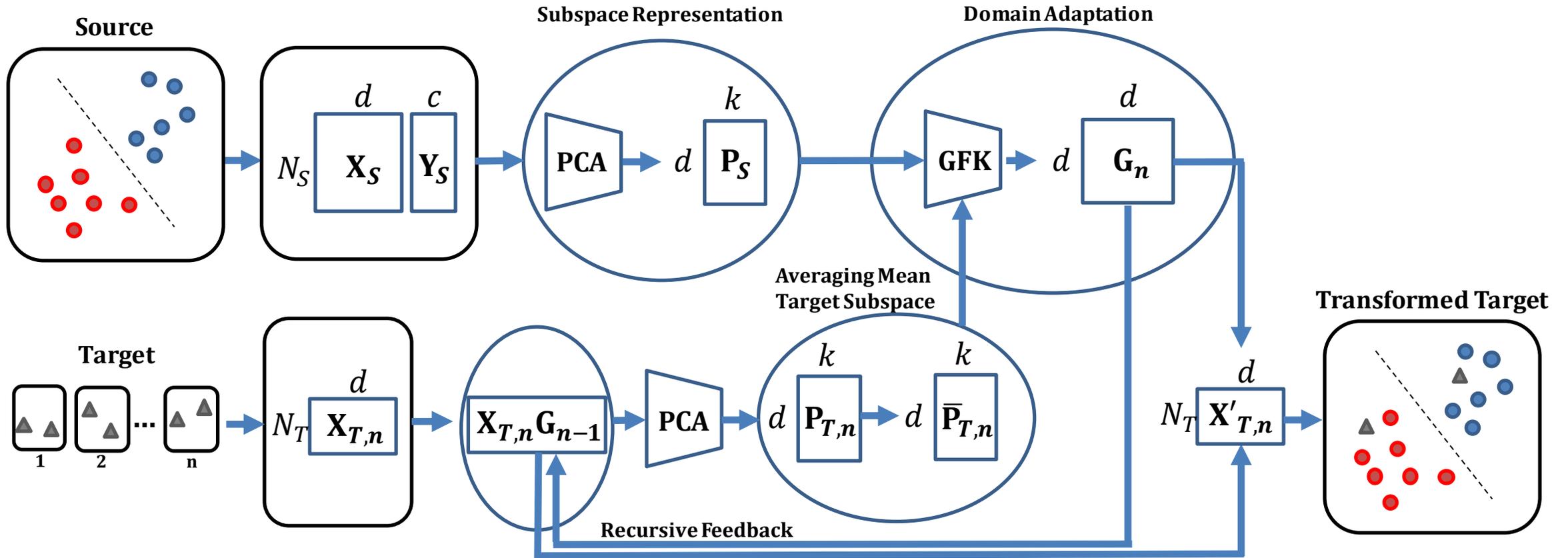
- Labelled source samples (class 1)
- Labelled source samples (class 2)
- ▲ Unlabelled target samples

- Unsupervised Domain Adaptation (UDA) transfers the knowledge from the labelled source domain to the unlabelled target domain
- Source and target samples are in batch



- Online Unsupervised Domain Adaptation (OUDA) is a more challenging problem than a traditional UDA problem
- Target samples arrive in online fashion (each mini-batch)

- Subspace Representation
- Averaging Mean-target Subspace
- Domain Adaptation
- Recursive Feedback



# *Each Step of the Proposed Framework*

# *1. Subspace Representation*

**Labelled Source**



$X_S$

**Unlabelled Target**

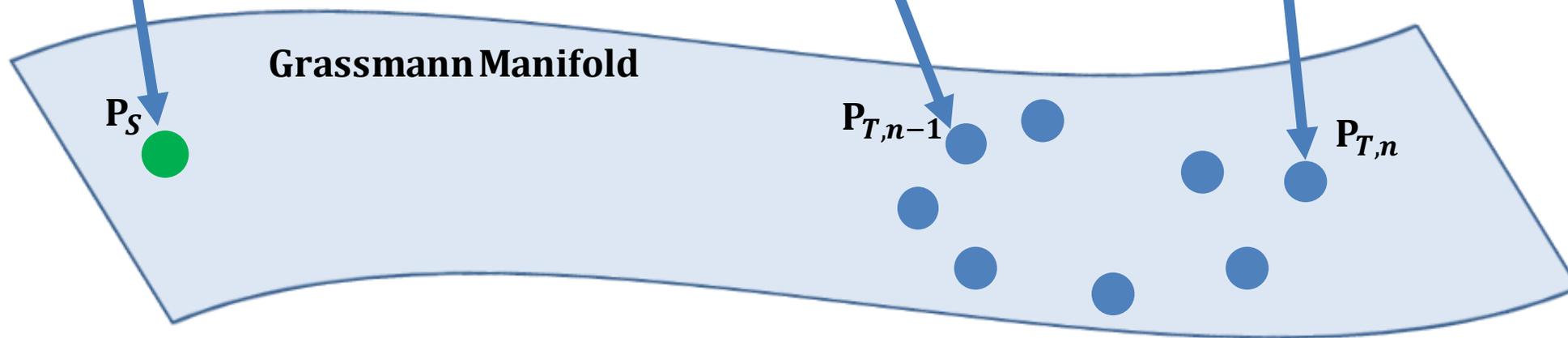


$X_{T,n-1}$



$X_{T,n}$

Mini-batch



## *2. Averaging Mean-target Subspace*

**Labelled Source**



$X_S$

**Unlabelled Target**

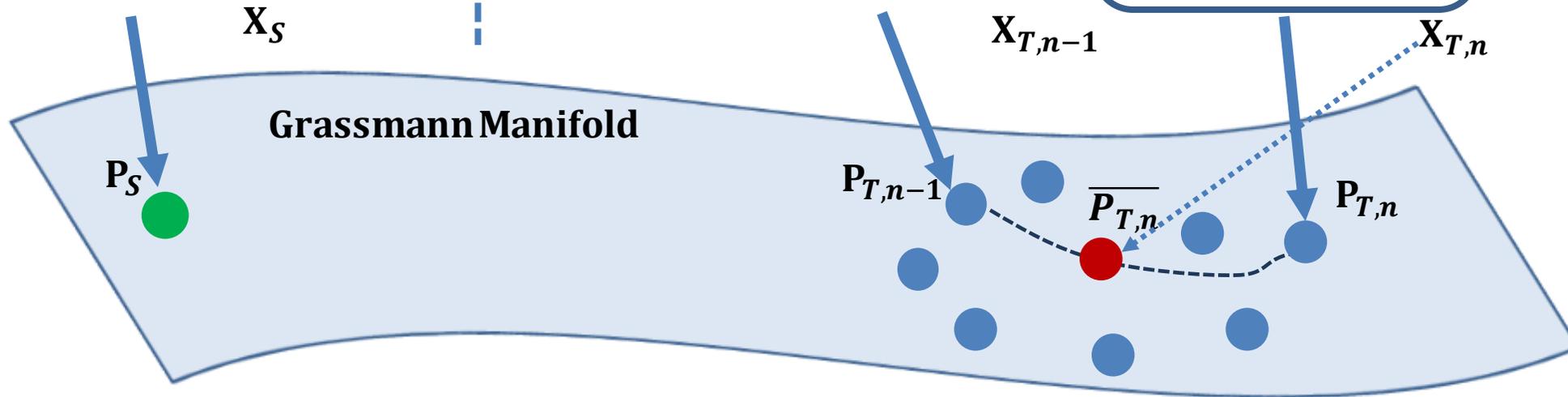


$X_{T,n-1}$

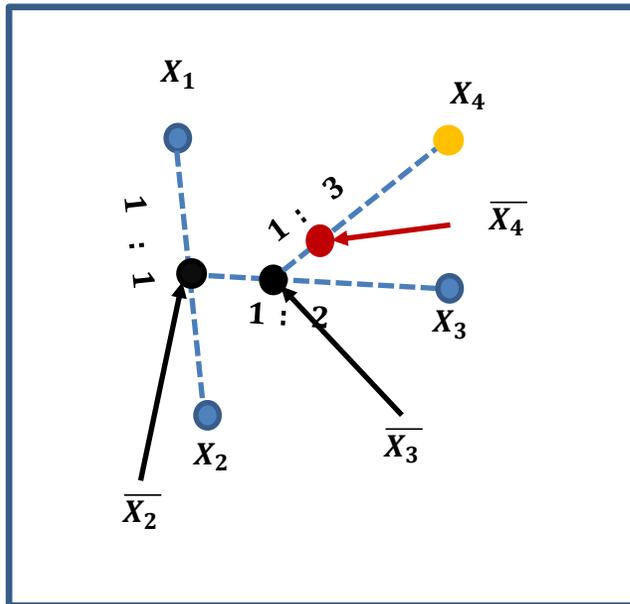


$X_{T,n}$

Mini-batch

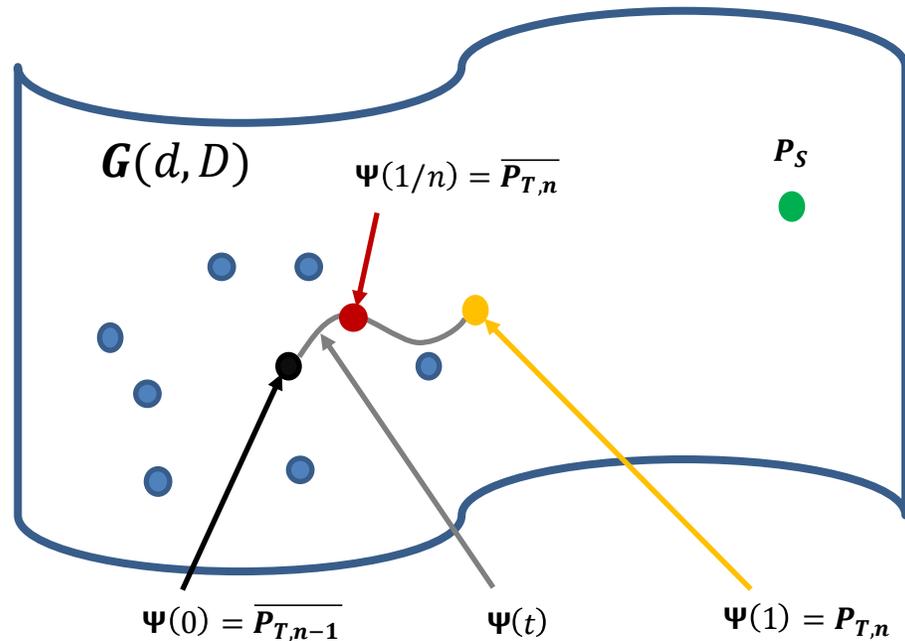


*Euclidean Space*



$$\overline{X}_n = \frac{(n-1)\overline{X}_{n-1} + X_n}{n}$$

*Grassmann Manifold*



- $P_S$ : Source Subspace
- $P_{T,i}$ :  $i$ 'th Target Subspace
- $\overline{P_{T,n-1}}$ : Mean of  $n - 1$  Subspaces
- $P_{T,n}$ :  $n$ 'th Target Subspace
- $\overline{P_{T,n}}$ : Mean of  $n$  Target Subspaces
- ~  $\Psi(t)$ : Geodesic Curve from  $\overline{P_{T,n-1}}$  to  $P_{T,n}$

- $\Psi(0) = \overline{P_{T,n-1}}$
- $\Psi(1) = P_{T,n}$
- $\Psi(1/n) = \overline{P_{T,n}}$

## *3. Domain Adaptation*

**Labelled Source**



$X_S$

**Unlabelled Target**

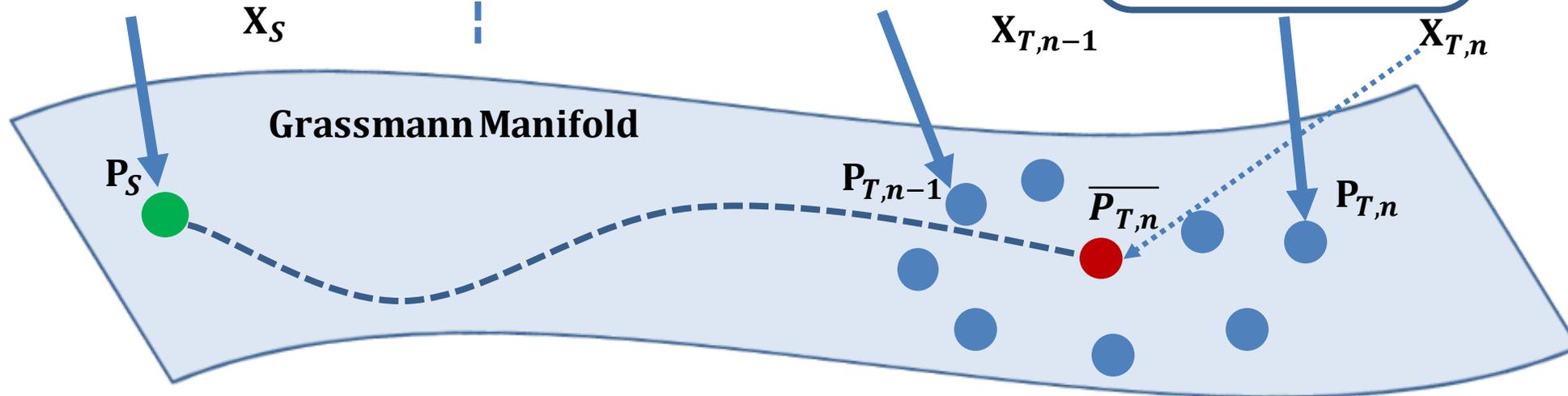


$X_{T,n-1}$

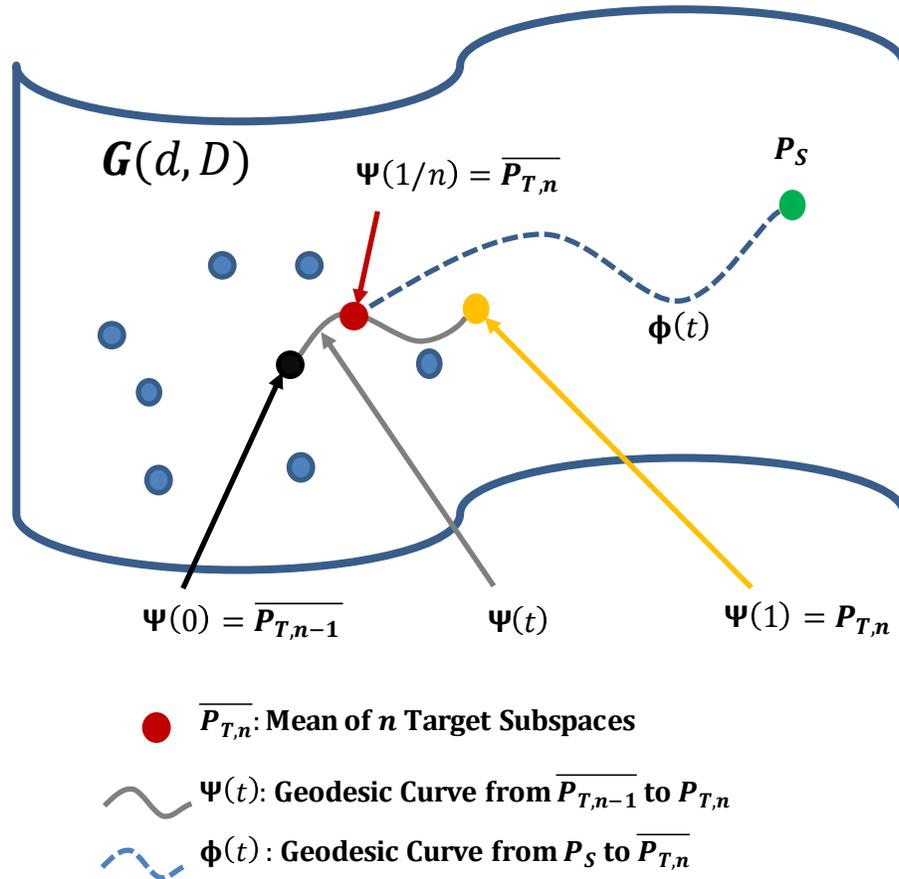


$X_{T,n}$

Mini-batch



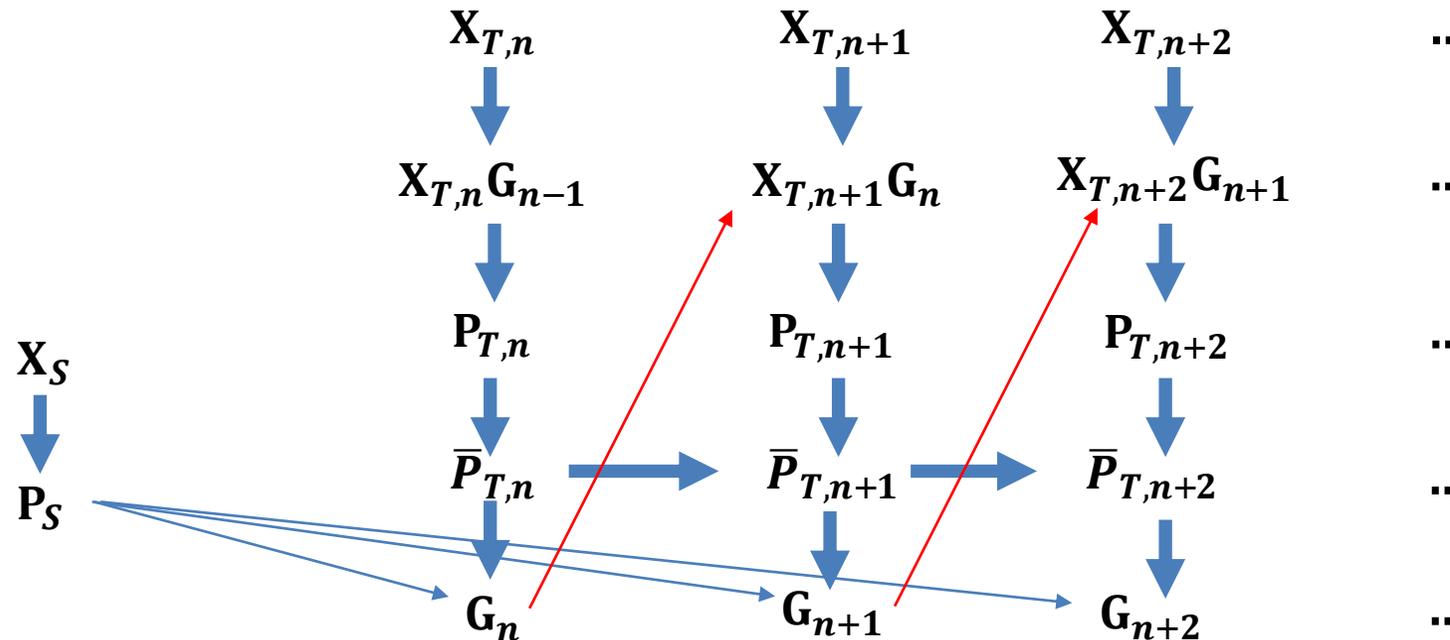
Grassmann Manifold



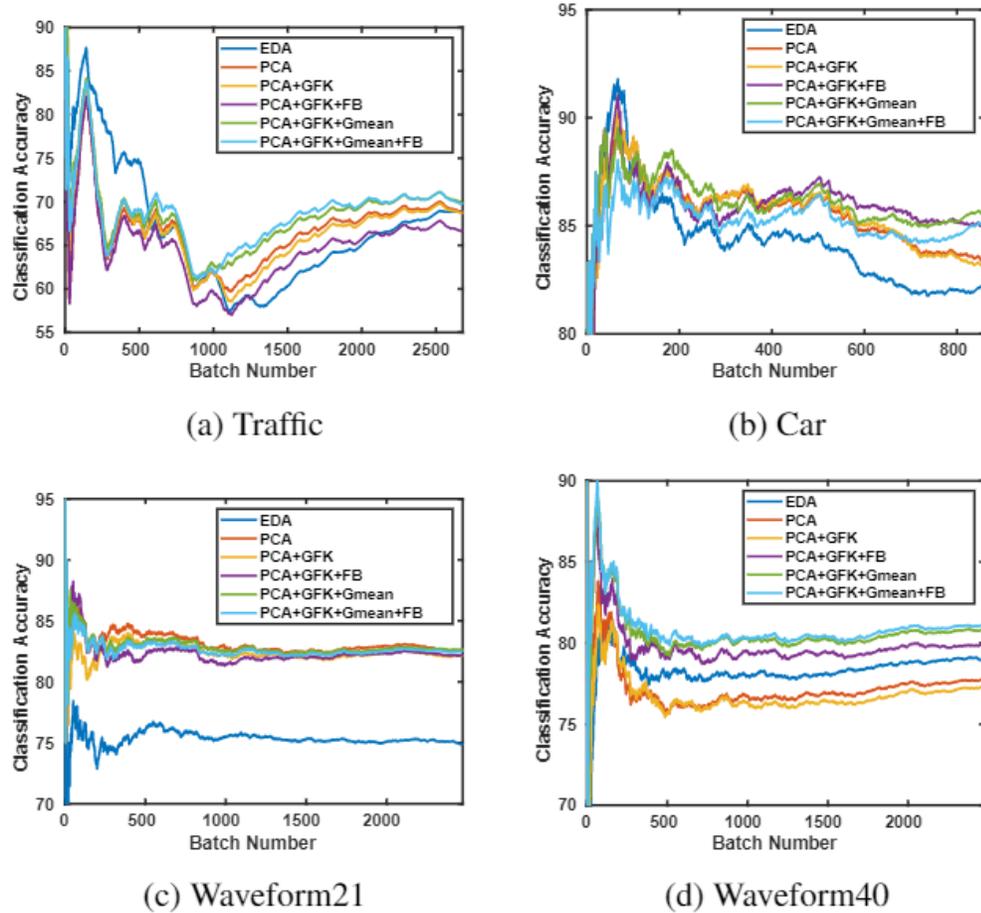
- Transformation matrix  $\mathbf{G}_n$  from the target domain to the source domain using the Geodesic Flow Kernel (GFK)

- $$\mathbf{G}_n = \int_0^1 \boldsymbol{\Phi}(\alpha) \boldsymbol{\Phi}(\alpha)^T$$

## *4. Recursive Feedback*



- Based on the computed transformation matrix  $G_n$ , modify the  $(n+1)$ th target mini-batch  $X_{T,n+1}$  to  $X_{T,n+1}^{pre} = X_{T,n+1}G_n$  before subspace representation step.



**Fig. 4:** Accuracy of the previous method (EDA) and variants of the proposed method.

**Table 1:** Accuracy (%) of Various Methods(Vanilla AE)

| Method           | Classifier | Traffic      | Car          | Waveform21   | Waveform40   |
|------------------|------------|--------------|--------------|--------------|--------------|
| CMA+GFK          | KNN        | 63.22        | 82.50        | 72.48        | 66.85        |
|                  | SVM        | 68.87        | 82.73        | 69.15        | 68.77        |
| CMA+SA           | KNN        | 41.33        | 56.45        | 33.19        | 33.09        |
|                  | SVM        | 41.33        | 56.45        | 33.84        | 33.05        |
| EDA              | ISSL       | 69.00        | 82.59        | 74.65        | 79.66        |
| PCA              | KNN        | 63.05        | 82.50        | 71.07        | 66.08        |
|                  | SVM        | 68.85        | 83.31        | 82.55        | 77.74        |
| PCA+GFK          | KNN        | 64.02        | 82.44        | 70.55        | 65.76        |
|                  | SVM        | 68.71        | 83.08        | 82.10        | 77.23        |
| PCA+GFK+FB       | KNN        | 61.77        | 81.28        | 72.65        | 66.85        |
|                  | SVM        | 66.67        | 84.88        | 82.18        | 79.86        |
| PCA+GFK+Gmean    | KNN        | 56.42        | 82.73        | 72.22        | 67.11        |
|                  | SVM        | <b>69.94</b> | <b>85.52</b> | <b>82.69</b> | 80.79        |
| PCA+GFK+Gmean+FB | KNN        | 57.03        | 82.44        | 72.38        | 67.90        |
|                  | SVM        | 69.77        | 85.00        | 82.51        | <b>81.07</b> |

**Table 2:** Comparison of Computation Time (sec)

| Method          | Traffic | Car  | Waveform21 | Waveform40 |
|-----------------|---------|------|------------|------------|
| EDA             | 105.7   | 2545 | 22.32      | 23.42      |
| Proposed method | 57.45   | 5503 | 3.188      | 4.410      |

- We proposed a multi-step framework to solve the OUDA problem.
- We incrementally computed the mean-target subspace on a Grassmann manifold.
- Our method outperformed the previous OUDA methods in terms of classification accuracy and computation time.