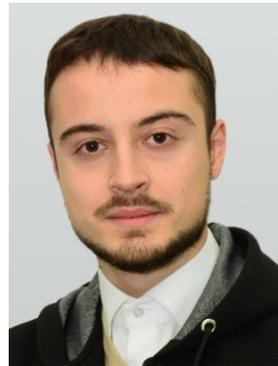
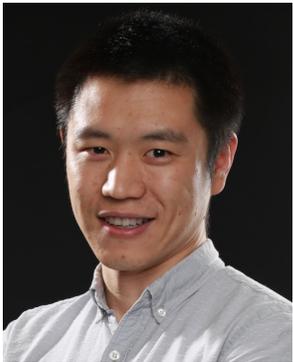


Delay-aware backpressure routing using Graph Neural Networks



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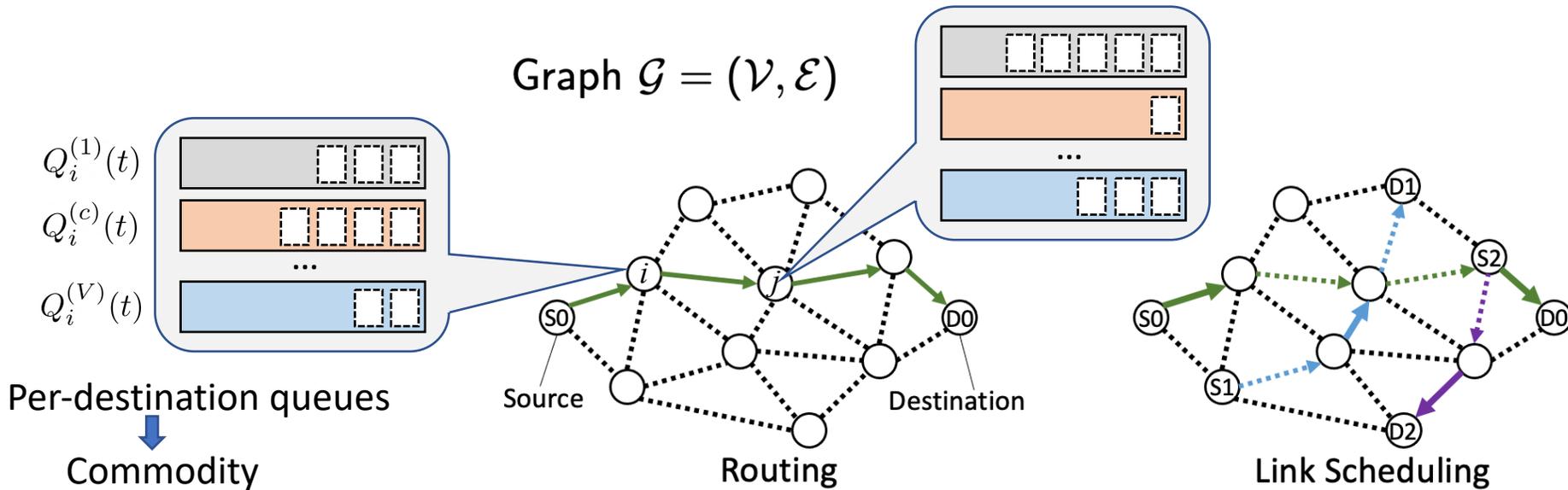
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2023 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)

Rhodes Island, Greece, June 4-10, 2023

Backpressure Routing*



- ✓ Distributed Routing
- ✓ Congestion prevention
- ✓ Throughput optimality
- ✗ Poor latency performance
 - ✗ Slow start
 - ✗ Loop
 - ✗ Last-packet problem

1. Select optimal commodity

$$c_{ij}^*(t) = \operatorname{argmax}_{c \in \mathcal{V}} \{U_i^{(c)}(t) - U_j^{(c)}(t)\}$$

$$U_i^{(c)}(t) = Q_i^{(c)}(t)$$

Vanilla BP

2. Find link gradient

$$w_{ij}(t) = \max\{U_i^{(c_{ij}^*(t))}(t) - U_j^{(c_{ij}^*(t))}(t), 0\}$$

3. MaxWeight scheduling

$$\mathbf{l}^{BP}(t) = \operatorname{argmax}_{\mathbf{l}(t) \in \{0,1\}^{|\mathcal{E}|}} \mathbf{l}(t)^\top \cdot [\mathbf{r}(t) \odot \mathbf{w}(t)]$$

$$U_i^{(c)}(t) = Q_i^{(c)}(t) + B_i^{(c)}$$

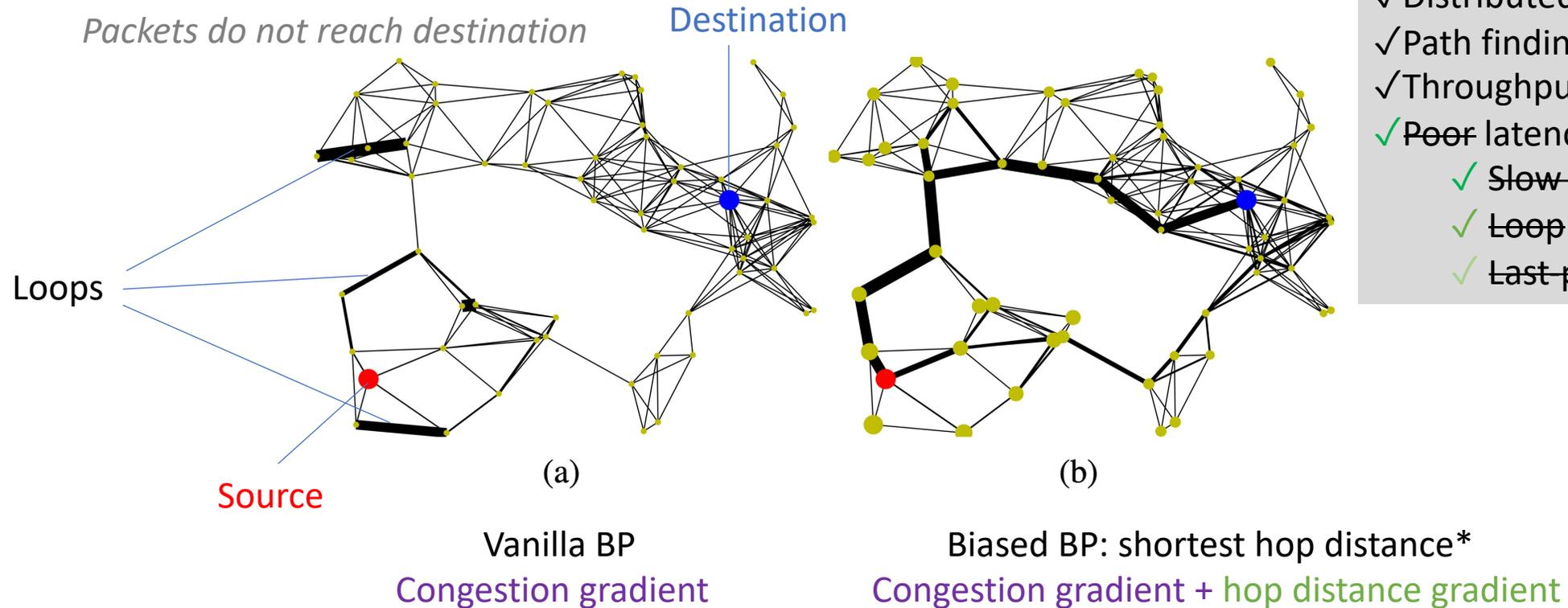
Biased BP

4. Assign link capacity

$$\mu_{ij}^{(c)}(t) = \begin{cases} r_{ij}(t), & \text{if } c = c_{ij}^*, w_{ij} > 0 \\ 0, & \text{otherwise} \end{cases}$$

Shortest path-aware bias

Vanilla v.s. biased BP routing



Route visualization: Normalized number of packets over links in 500 steps

Can we do better than shortest hop distance bias?

Delay-aware shortest path bias based on link duty cycle

How likely a link is scheduled under current network topology and traffics

Link duty cycle

$$0 < x_e \leq 1 \quad e \in \mathcal{E}$$

Per hop distance

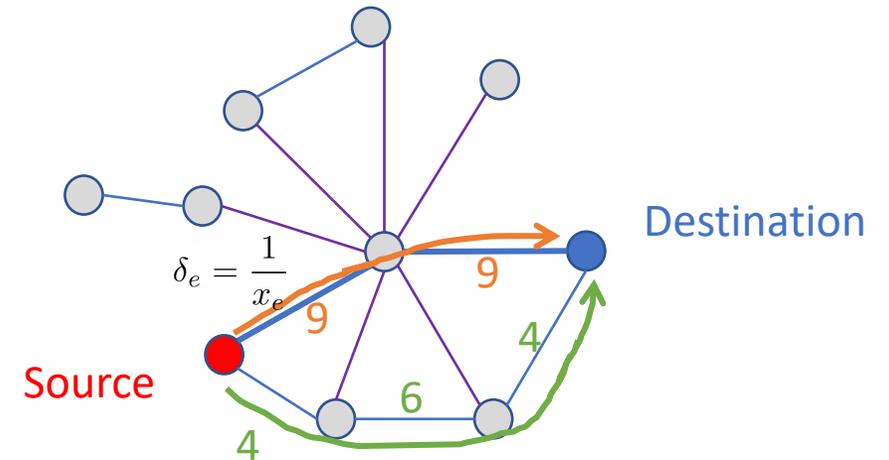
$$\delta_e = \frac{1}{x_e}$$

Per hop distance with link rate

$$\delta_e = \frac{\bar{r}}{x_e r_e}$$

Link duty cycle estimated by an L-layer graph convolutional neural network (GCNN)

$$\mathbf{x} = \Psi_{\mathcal{G}^c}(\mathbf{1}; \boldsymbol{\omega})$$



Fully distributed execution

$$\mathbf{x}_{e^*}^l = \sigma_l \left(\mathbf{x}_{e^*}^{l-1} \boldsymbol{\Theta}_0^l + \left[\mathbf{x}_{e^*}^{l-1} - \sum_{u \in \mathcal{N}_{\mathcal{G}^c}(e)} \frac{\mathbf{x}_{u^*}^{l-1}}{\sqrt{d(e)d(u)}} \right] \boldsymbol{\Theta}_1^l \right)$$

Properties of delay-aware shortest path bias

- Complexity

- GCNN $\mathcal{O}(L)$
- Single source shortest path (SSSP)
- All pairs shortest path (APSP)

Distributed weighted SSSP and APSP

$$\mathcal{O}(V)$$

GCNN and SP algorithms only need to run once a while, when topology changes

- Throughput Optimality

- Shortest path bias is non-negative and constant
- Throughput optimality holds

BP algorithm can stabilize the queues in the network as long as the arrival rates of flows are within the network capacity region

Training of GCNN

- Draw a network instance
- Find delay-aware shortest path bias with GCNN and APSP
- Run BP routing and collect schedules of each time slot
- Update parameters of GCNN with loss function

Connectivity graph $\mathcal{G}^n(k)$, *Conflict graph* $\mathcal{G}^c(k)$, *Flows* $\mathcal{F}(k)$, *Flow arrivals* $\mathbf{A}(k)$, *Link rates* $\mathbf{R}(k)$

$$(\mathcal{G}^n(k), \mathcal{G}^c(k), \mathcal{F}(k), \mathbf{A}(k), \mathbf{R}(k)) \sim \Omega.$$

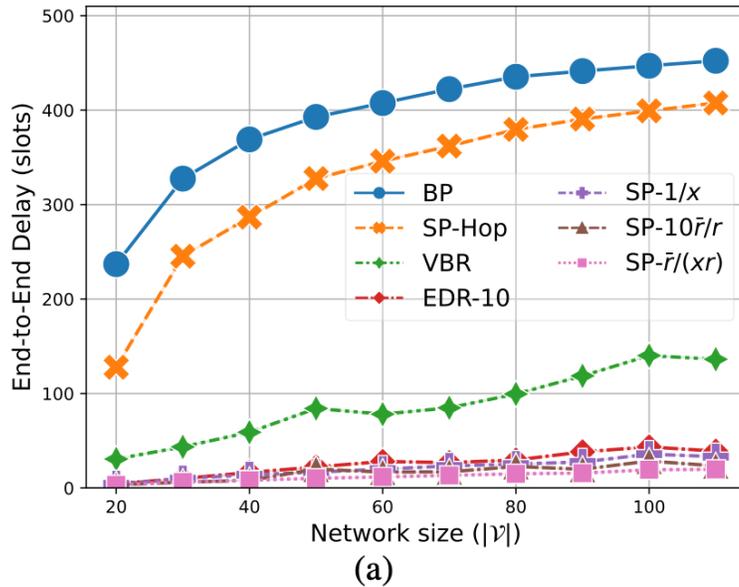
Per-link distance $\mathbf{x}(k) = \Psi_{\mathcal{G}^c(k)}(\mathbf{1}; \boldsymbol{\omega})$,
Shortest path bias $\mathcal{B}(k)$

Empirical schedule $\mathbf{s}^k(t) \in \{0, 1\}^{|\mathcal{E}|}$

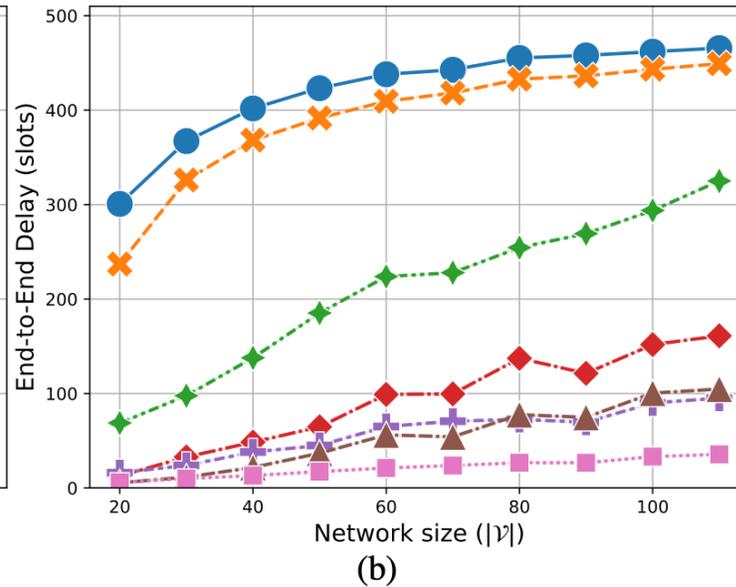
$$\ell(\boldsymbol{\omega}) = \mathbb{E}_{\Omega} [MSE(\mathbf{x}(k), \mathbb{E}_t(\mathbf{s}^k(t)))]$$

Performance

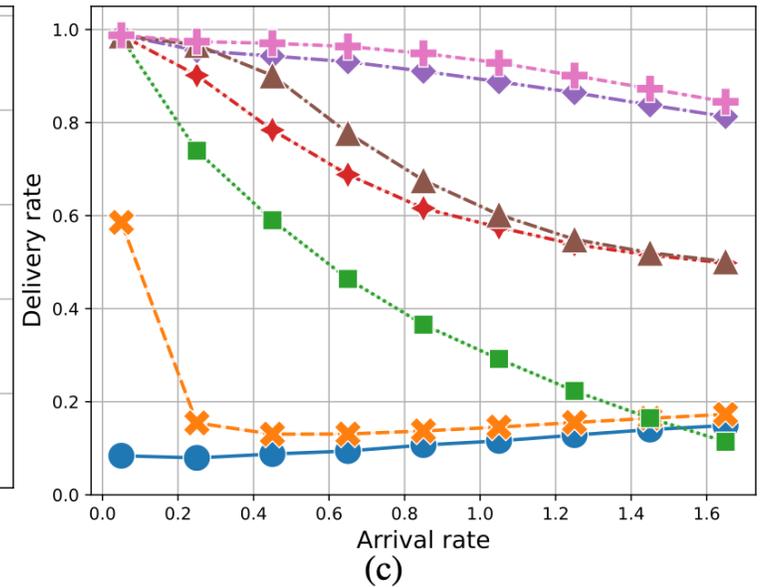
On 100 random graphs from **2D point process model**
 T=1000



Interface conflict model,
 e.g., mmWave networks



Unit-disk conflict model,
 e.g., wireless sensor/ad-hoc
 networks



Delivery rate under unit-disk
 conflict model with 100 nodes

Conclusion & Future directions

- Delay-aware per-hop distance for biased backpressure routing
 - Link duty cycle
 - Conflict-aware (adaptive to network density)
 - Significantly improve **end-to-end delay & delivery rate**
- Keep advantages of shortest hop distance bias
 - Fully distributed execution
 - Minimal increase in complexity
 - Simplicity
 - Low overhead (update only once a while)
- Apply to other routing schemes
- Improved training method