

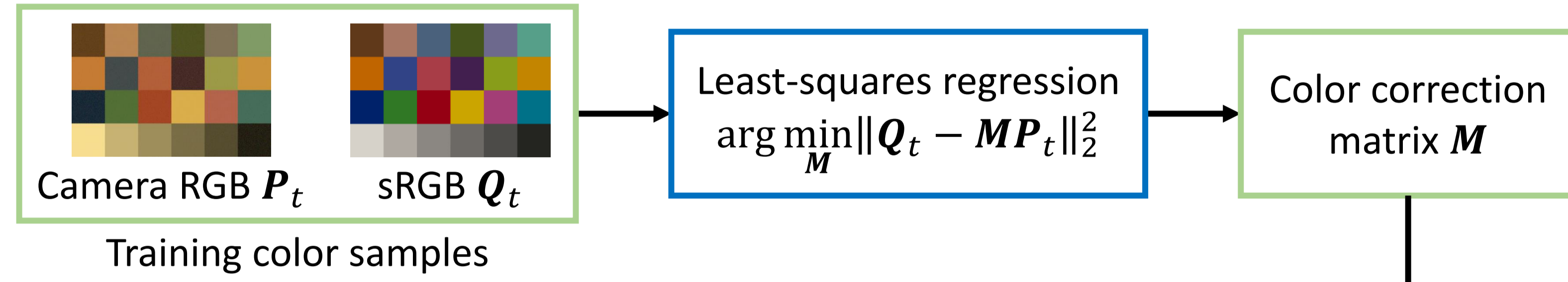
# Tunable Color Correction Between Linear and Polynomial Models For Noisy Images

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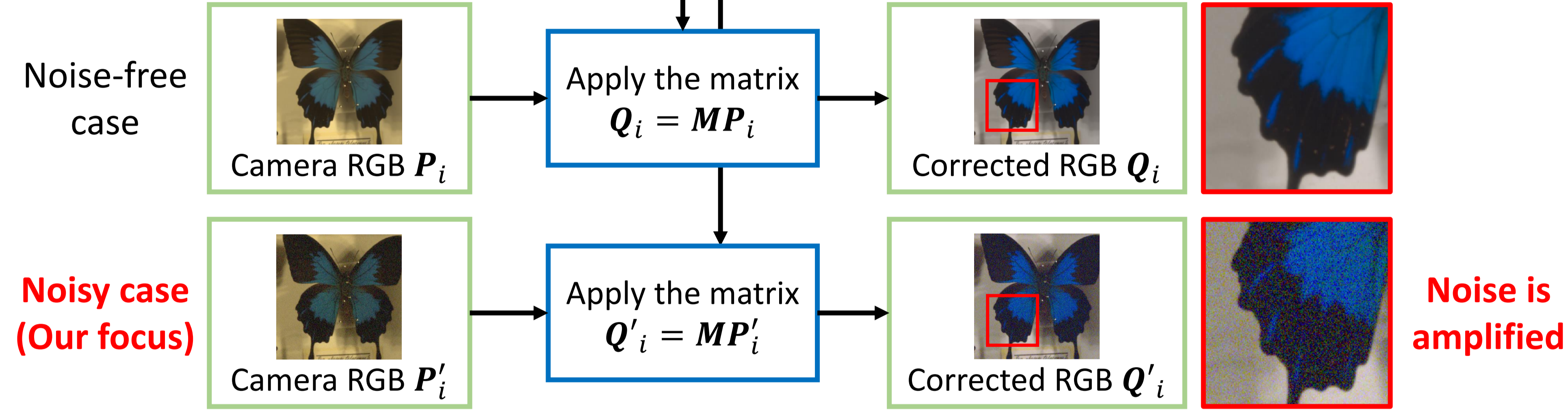
## Introduction: Color correction for noisy images

### Color correction process

Step 1: Train color correction matrix



Step 2: Apply color correction matrix



### Linear color correction (LCC) [1]

$$q_{LCC} = M_{LCC} p_{LCC}$$

$$p_{LCC} = [1, p_r, p_g, p_b]^T$$

$p_i$ : Camera RGB value

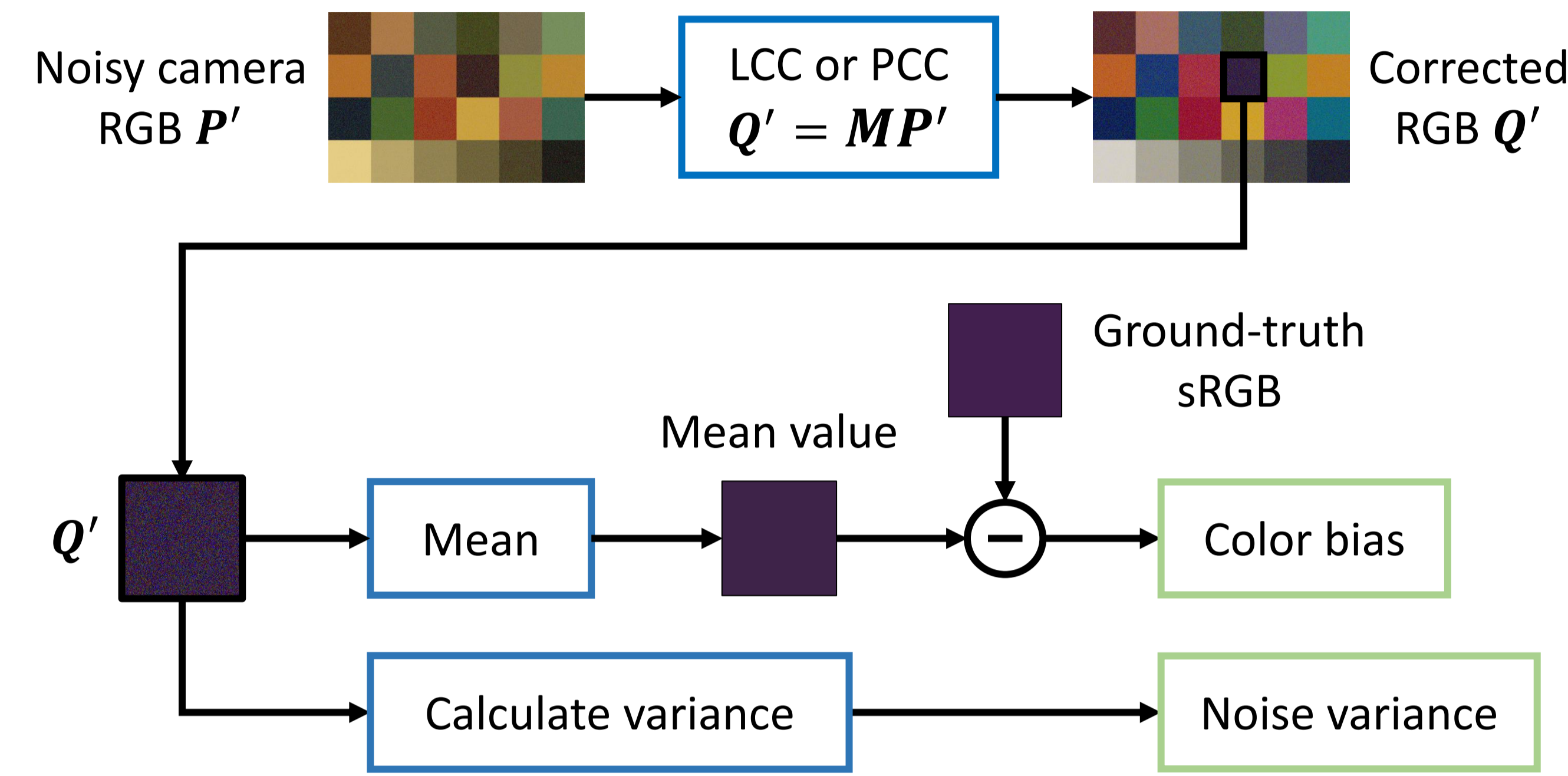
### Polynomial color correction (PCC) [2]

$$q_{PCC} = M_{PCC} p_{PCC}$$

$$p_{PCC} = [1, p_r, p_g, p_b, p_{rg}, p_{gb}, p_{br}, p_{r^2}, p_{g^2}, p_{b^2}]^T$$

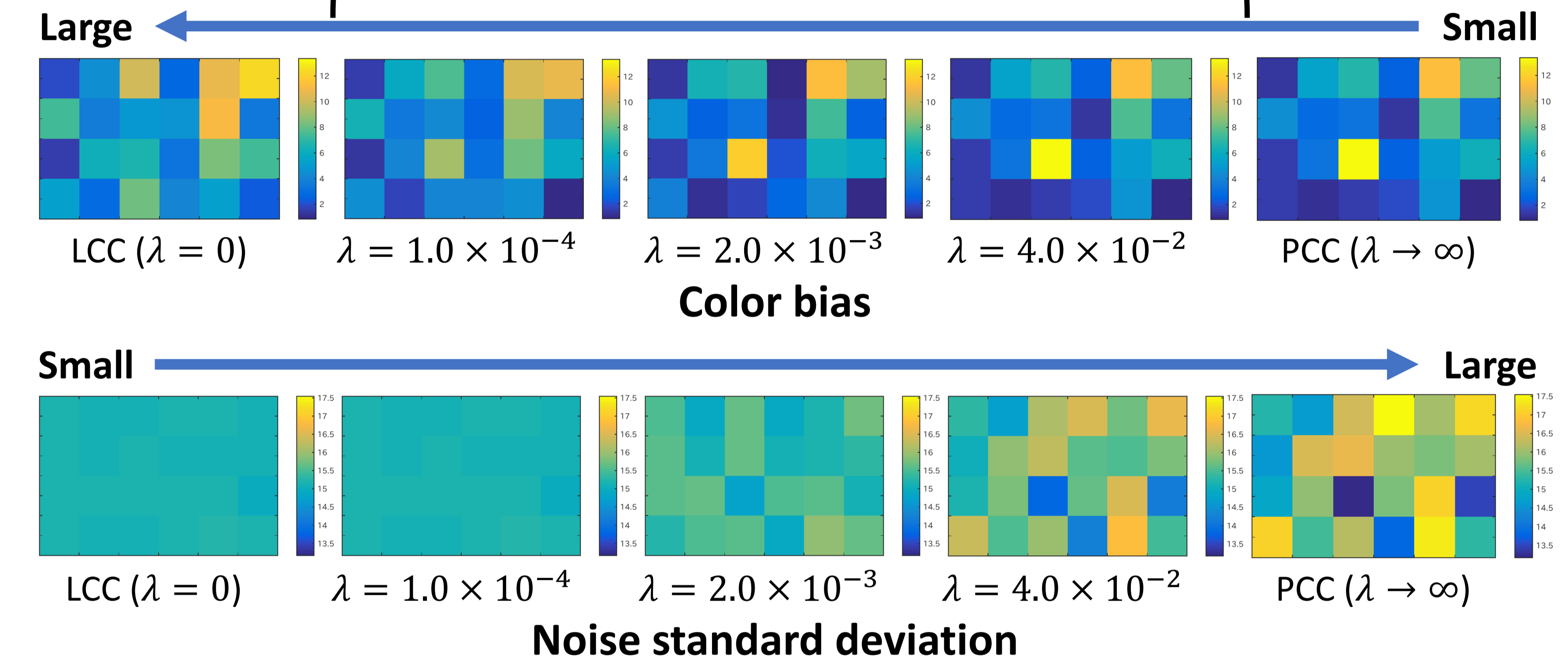
Use high-order terms (Our focus is 2<sup>nd</sup>-order PCC)

### Color correction error analysis



### Proposed tunable color correction (TCC)

Tune the color correction matrix between LCC and PCC models and optimize the balance of the trade-off.



## Proposed tunable color correction (TCC)

### Cost function of training matrix

$$\hat{M}(\lambda) = \arg \min_M \left( \underbrace{\|Q_t - MP_t\|_F^2}_{\text{Data term}} + \frac{1}{\lambda} \underbrace{\|W \circ M\|_F^2}_{\text{Constraint term}} \right)$$

Element-wise product

### Key properties of TCC

$$\lim_{\lambda \rightarrow 0} \hat{M}(\lambda) = [M_{LCC} \mid \mathbf{0}]$$

$$\lim_{\lambda \rightarrow \infty} \hat{M}(\lambda) = M_{PCC}$$

### Optimized matrix of TCC

$$M_{TCC} = \hat{M}(\hat{\lambda})$$

$\hat{\lambda}$ : Optimized tuning parameter value

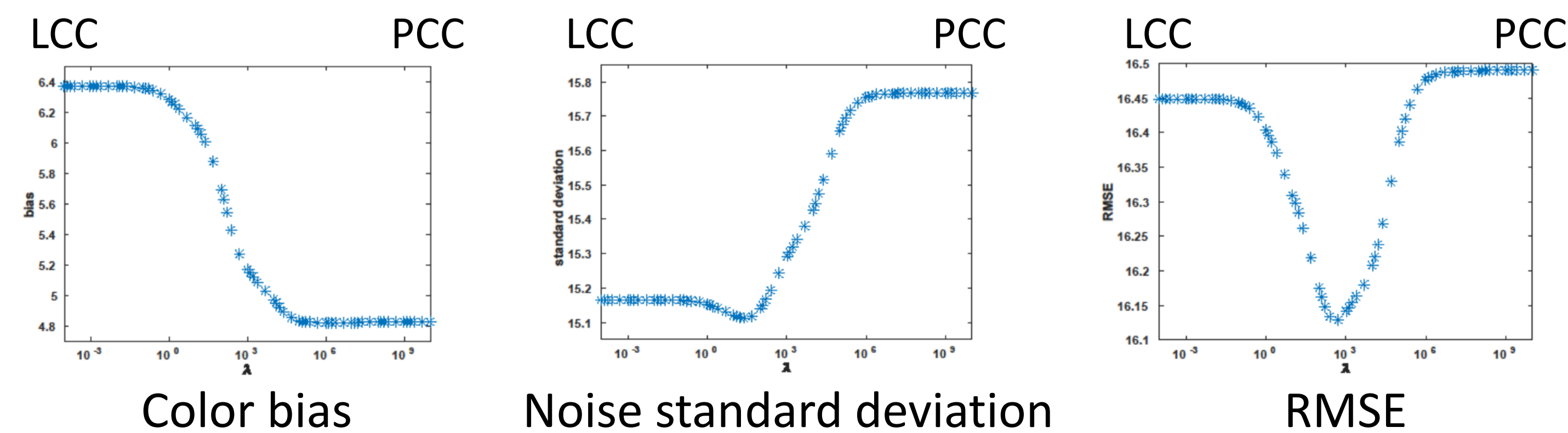
### Data term

$$Q_t - MP_t = \begin{bmatrix} q_R \\ q_G \\ q_B \end{bmatrix} - M_{3 \times 10} \begin{bmatrix} 1 p_R p_G p_B p_{RG} p_{GB} p_{BR} p_R^2 p_G^2 p_B^2 \\ \vdots \\ \vdots \end{bmatrix}^T$$

### Constraint term: Constraint on the 2<sup>nd</sup>-order terms of the matrix $M$ .

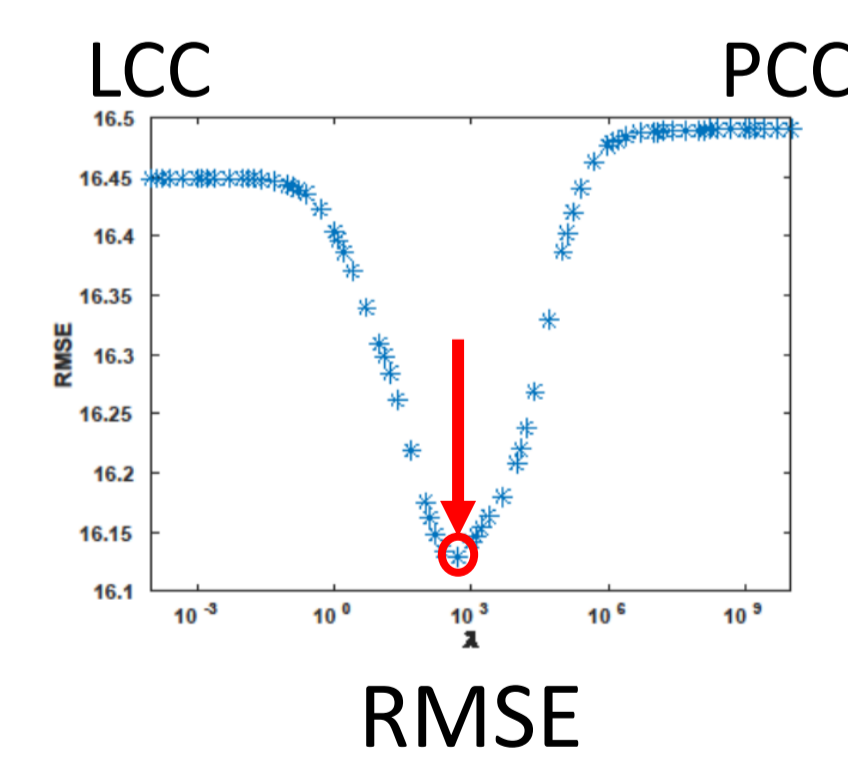
$$W \circ M = \begin{bmatrix} 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \circ \begin{bmatrix} 1 m_{1,R} m_{1,G} m_{1,B} m_{1,RG} m_{1,GB} m_{1,BR} m_{1,R^2} m_{1,G^2} m_{1,B^2} \\ 1 m_{2,R} m_{2,G} m_{2,B} m_{2,RG} m_{2,GB} m_{2,BR} m_{2,R^2} m_{2,G^2} m_{2,B^2} \\ 1 m_{3,R} m_{3,G} m_{3,B} m_{3,RG} m_{3,GB} m_{3,BR} m_{3,R^2} m_{3,G^2} m_{3,B^2} \end{bmatrix}$$

### Simulation results with different parameter values for SG chart



### Optimize tuning parameter value

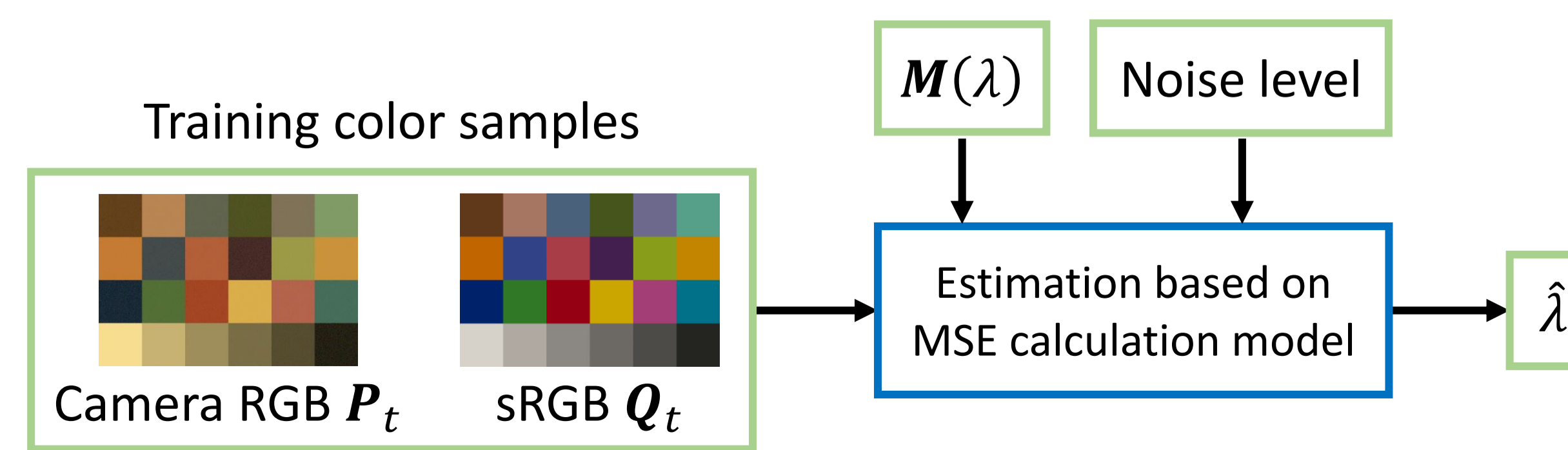
Find the optimal parameter value in terms of RMSE



$$\hat{\lambda} = \arg \min_{\lambda} MSE(\lambda)$$

$$= \arg \min_{\lambda} ((\text{color bias})^2 + (\text{noise variance}))$$

The optimal value is calculated based on the MSE calculation model we derived (see the paper for details).



## Experimental results

### Setups

Training data: SG chart (96 patches)  
Test data: SG chart (96 patches)  
Hyperspectral images (30 scenes) [3]  
Illumination: CIE A  
Camera sensitivity: Olympus E-PL2 [4]

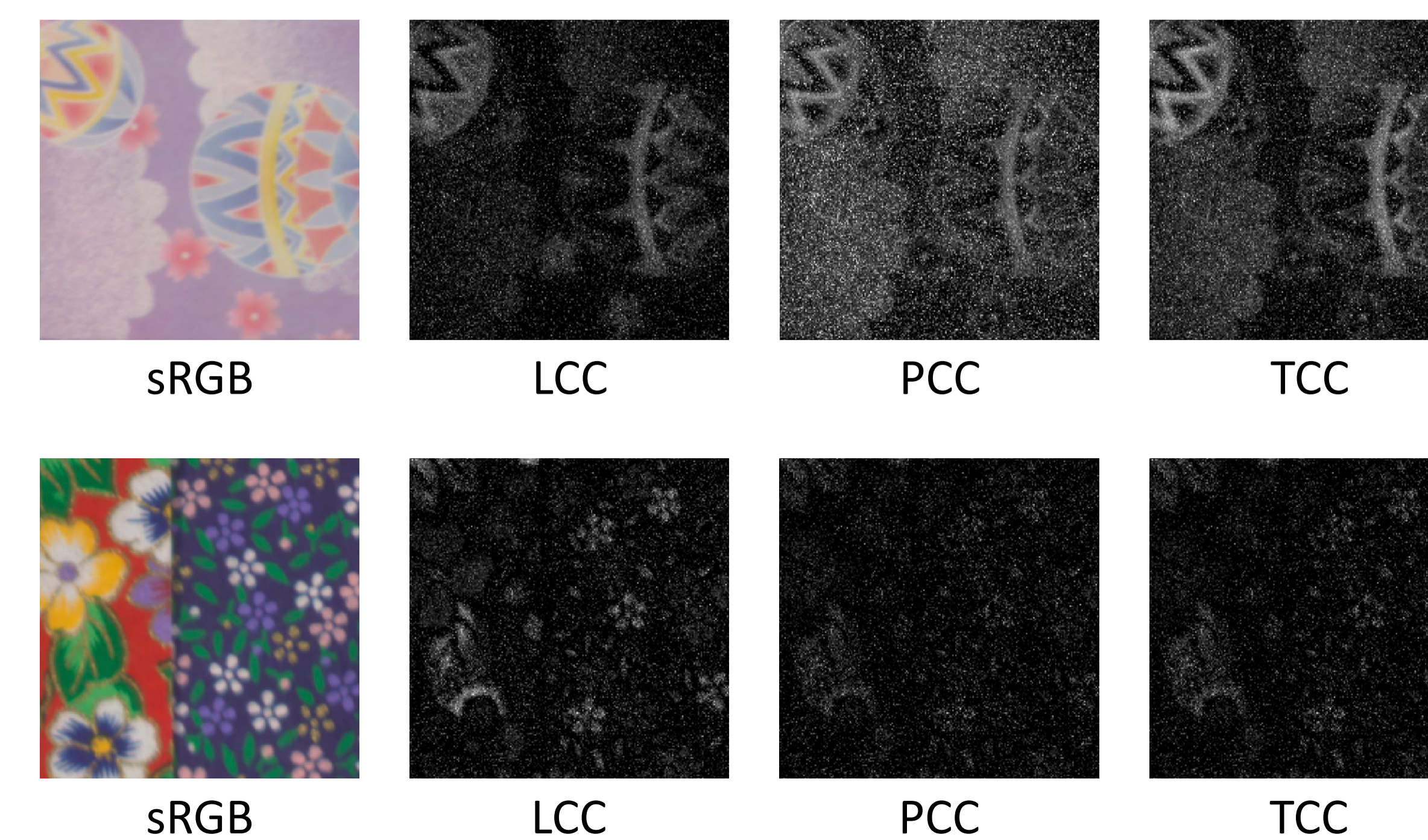
### Numerical comparison: Average RMSE

(Training data – Test data)

$\sigma$	SG chart - SG chart			SG chart - Hyperspectral		
	LCC	PCC	TCC	LCC	PCC	TCC
0	6.37	4.81	4.81	11.30	10.65	10.65
2	9.91	9.24	9.17	13.61	13.24	13.29
4	16.45	16.49	16.13	18.91	19.00	18.83
6	23.62	24.17	23.41	25.40	25.92	25.32
8	31.00	31.99	30.81	32.37	33.30	32.25
10	38.43	39.88	38.23	39.57	40.94	39.44

### Visual comparison for hyperspectral images:

RMSE map ( $\sigma = 2$ )



## References

- [1] P. M. Hubel, J. Holm, G. D. Finlayson, and M. S. Drew, "Matrix calculations for digital photography," Proc. of Color and Imaging Conference (CIC), pp. 105–111, 1997.
- [2] G. Hong, M. R. Luo, and P. A. Rhodes, "A study of digital camera colorimetric characterisation based on polynomial modelling," Color Research and Application, vol. 26, no. 1, pp. 76–84, 2001.
- [3] Y. Monno, S. Kikuchi, M. Tanaka, and M. Okutomi, "A practical one-shot multispectral imaging system using a single image sensor," IEEE Trans. on Image Processing, vol. 24, no. 10, pp. 3048–3059, 2015.
- [4] J. Jiang, D. Liu, J. Gu, and S. Süstrunk, "What is the space of spectral sensitivity functions for digital color cameras?," Proc. of Workshop on Applications of Computer Vision (WACV), pp. 168–179, 2013.