

# REFLECTANCE-BASED SURFACE SALIENCY

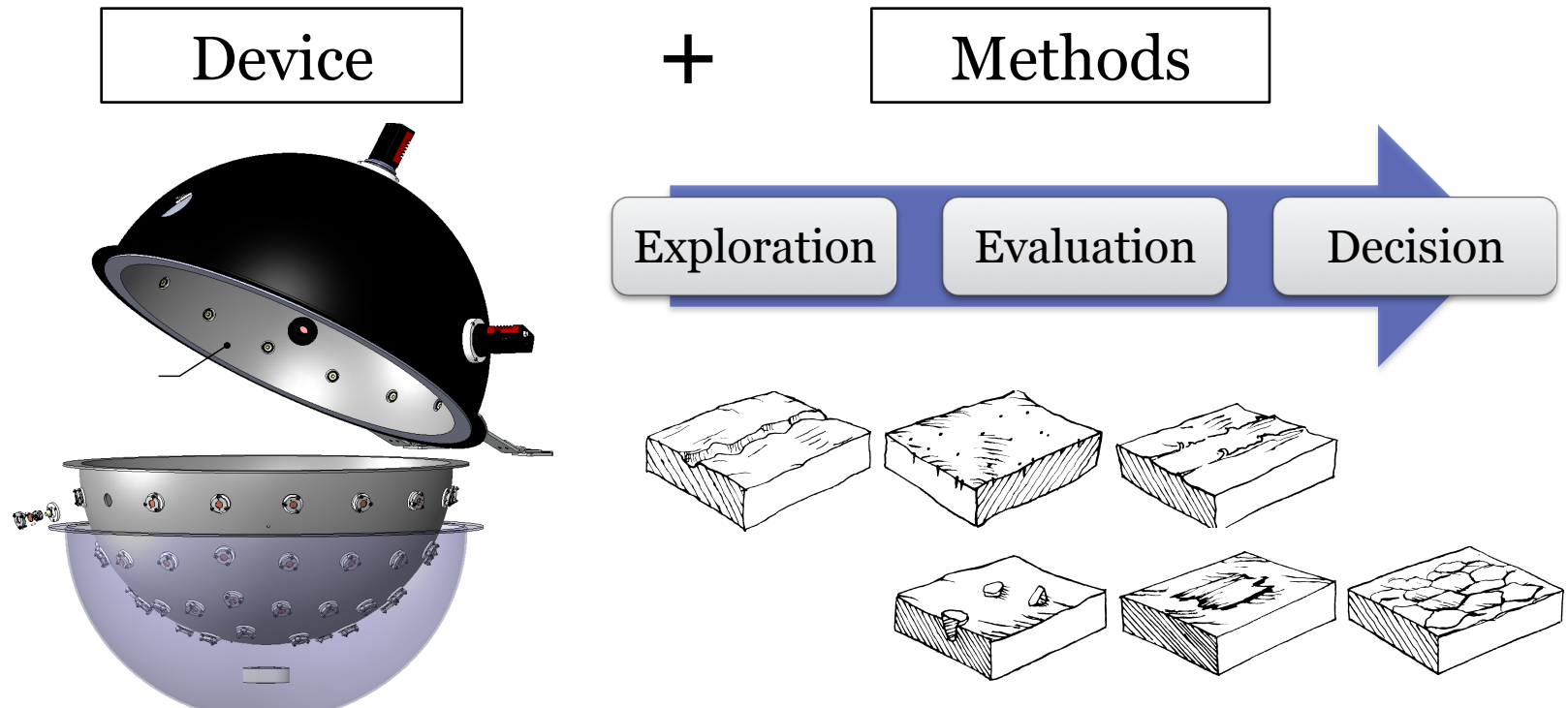
Gilles Pitard, Gaëtan Le Goïc, Alamin Mansouri, Hugues Favrelière,  
Maurice Pillet, Sony George, and Jon Yngve Hardeberg



The Norwegian  
Colour and Visual Computing  
Laboratory



# Scope and Objectives



## Main aim

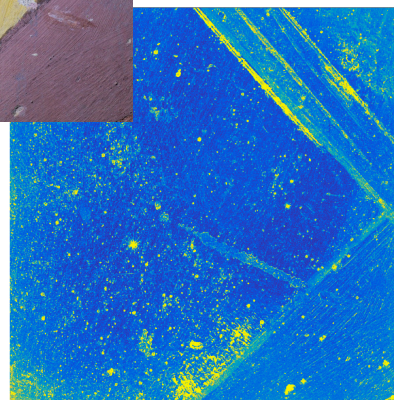
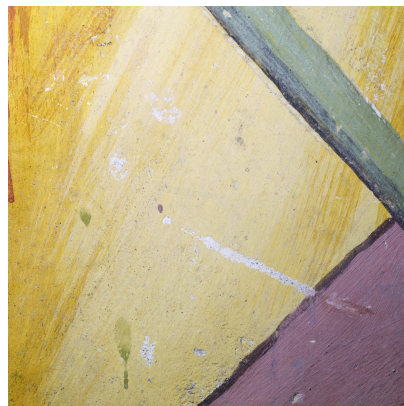
→ Develop an automatic inspection vision system to measure the quality of industrial products



# Enlarging the scope to other applications

➔ Detect and quantify the salient features (such as changes and degradations) on the cultural heritage objects using new imaging modalities

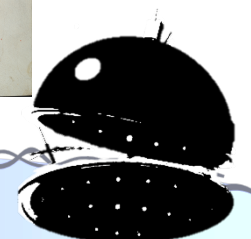
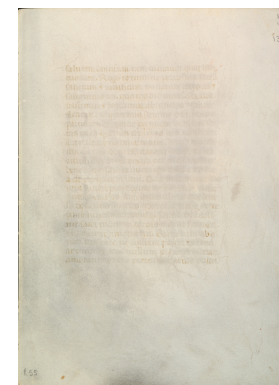
## Wall paintings



## Fossils



## Palimpsests



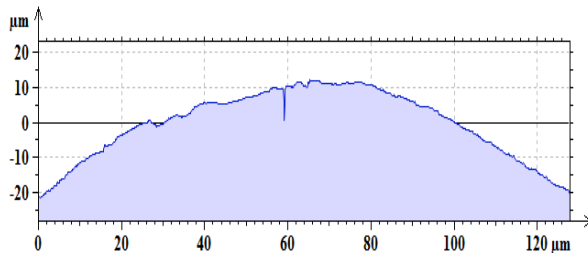
# 3 ways to address this challenge

## Measuring, modeling and controlling:

①

### Geometry

Altitudes, normals, and curvatures



②

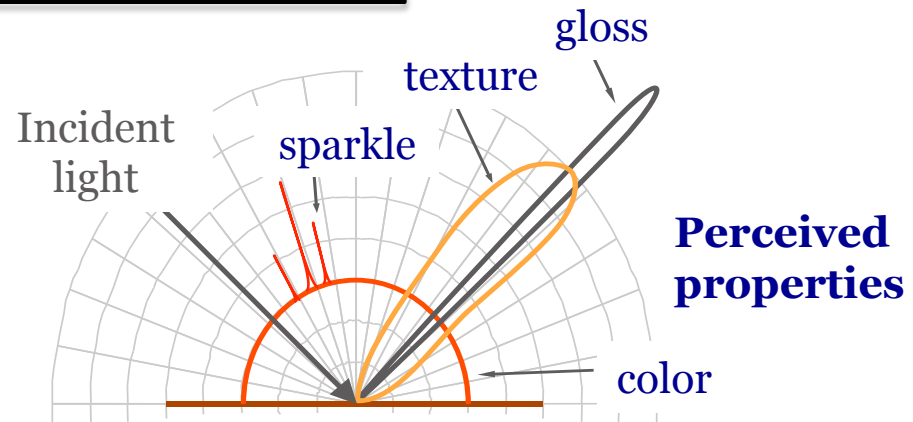
### Spatial BRDF

Angular distribution of the reflected light

③

### Spectral BRDF

Wavelengths



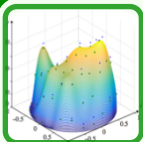
B.R.D.F : Bidirectionnall Reflectance  
Distribution Function





## 1. Reflectance Transformation Imaging

- ⊕ Related works
- ⊕ RTI Devices



## 2. Modeling the angular reflectance

- ⊕ Angular reflectance modeling
- ⊕ Discrete Modal Decomposition



## 3. Computing the saliency maps

- ⊕ Rotation-invariant representation
- ⊕ Multivariate analysis



## 4. Conclusion

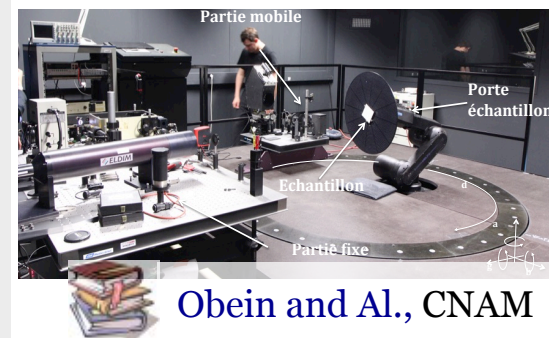


# 1. REFLECTANCE TRANSFORMATION IMAGING

## Approaches for BRDF assessment

Methods	Principle	Advantages/ disadvantages
<b>Measuring the BRDF</b>	measures using a goniospectrophotometer	<ul style="list-style-type: none"> <li>😊 complete characterization of an infinitesimal area element of the surface</li> <li>😞 total amount of data</li> <li>😞 data acquisition time</li> </ul>
<b>Model-based rendering</b>	analytical BRDF Models, eg. Phong, Cook-Torrance,...	<ul style="list-style-type: none"> <li>😞 not suitable for the rendering of real-world surfaces</li> </ul>
<b>Image-based rendering</b>	reflectance estimated from photometric stereo data	<ul style="list-style-type: none"> <li>😊 rapid acquisition</li> <li>😊 not require knowledges of physical and geometrical properties</li> </ul>

→ e.g. Reflectance Transformation Imaging



Obein and Al., CNAM

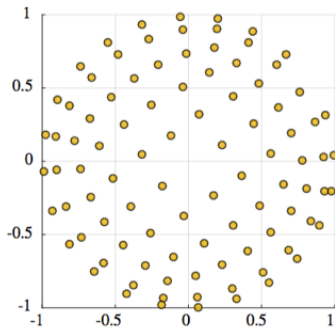


# 1. REFLECTANCE TRANSFORMATION IMAGING

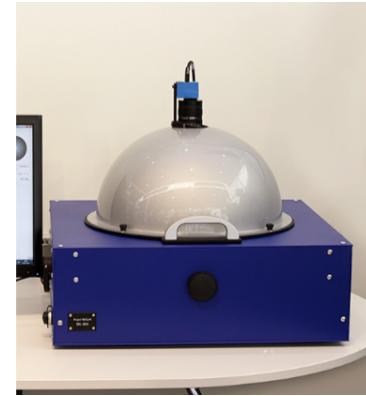
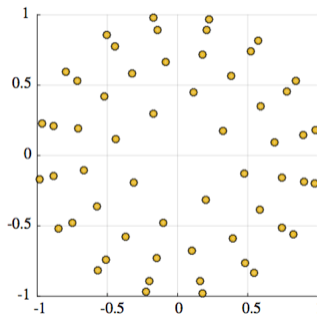
RTI devices → photometric stereo acquisition



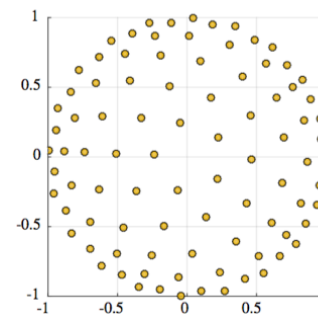
Dome v.1  
 ∅ 900mm  
 1 digital camera  
 96 light sources



MeSurA Sphere  
 ∅ 650mm  
 4 cameras  
 112 light sources



Dome Opto  
 ∅ 320mm  
 1 camera  
 90 light sources

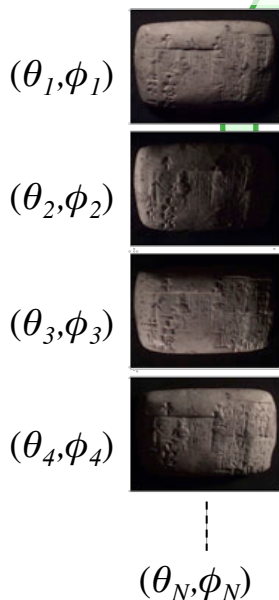


# 1. REFLECTANCE TRANSFORMATION IMAGING

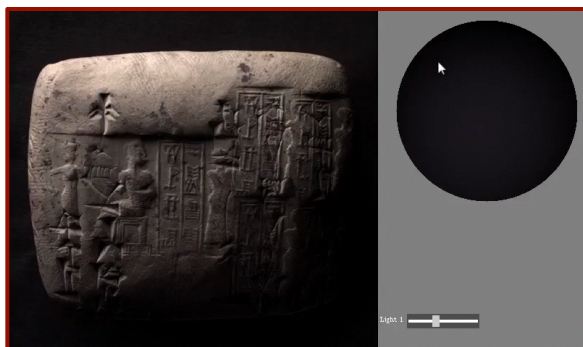
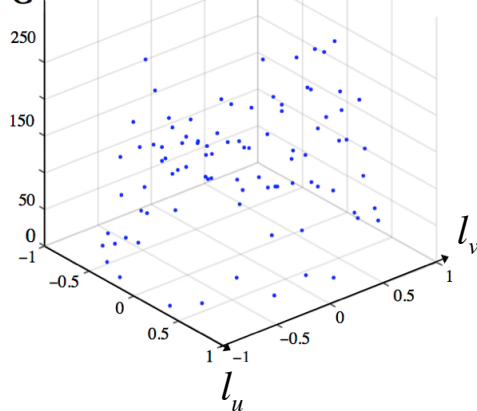
## PTM Polynomial Texture Mapping

### 1 – Acquisition

Set of  $N$  images



For each pixel:  
 $N$  values of luminance

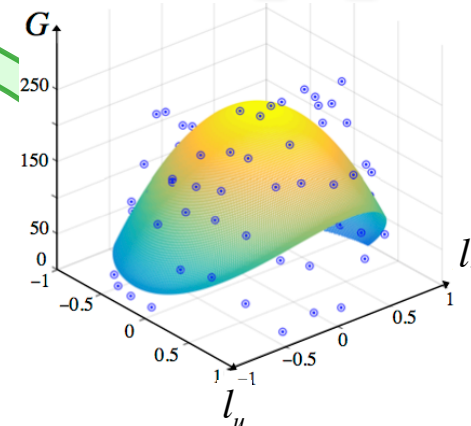


### 3 – Rendering

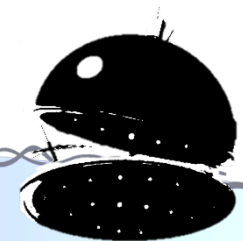
Interpolate and re-lighting the object under a new lighting direction chosen by the user

### 2 – Modeling

6 polynomial coefficients  
noted  $a_0$  to  $a_5$



$$L(l_u, l_v) = a_0 + a_1 l_u + a_2 l_v + a_3 l_u l_v + a_4 l_u^2 + a_5 l_v^2$$

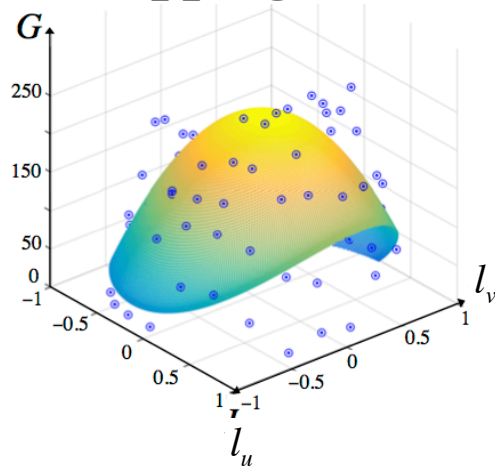




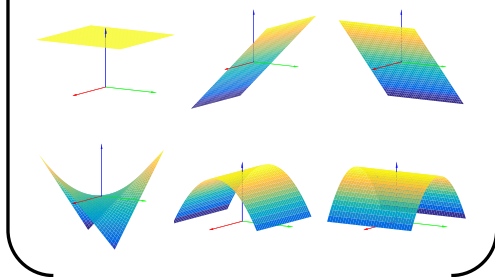
# 1. REFLECTANCE TRANSFORMATION IMAGING

## Existing models

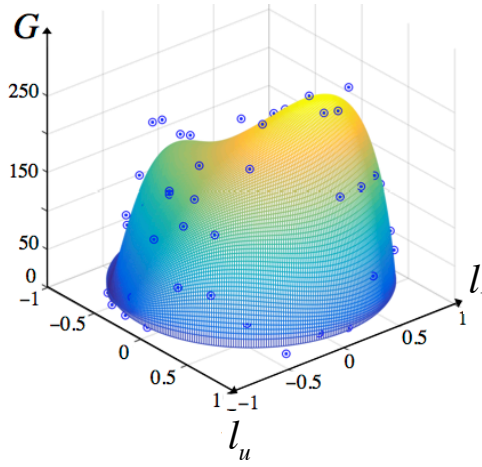
### Polynomial Texture Mapping **PTM**



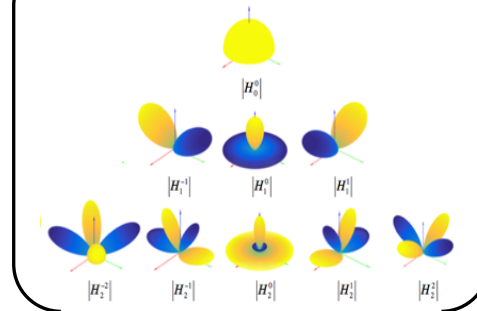
PTM basis



### Hemispherical Harmonics **HSH**

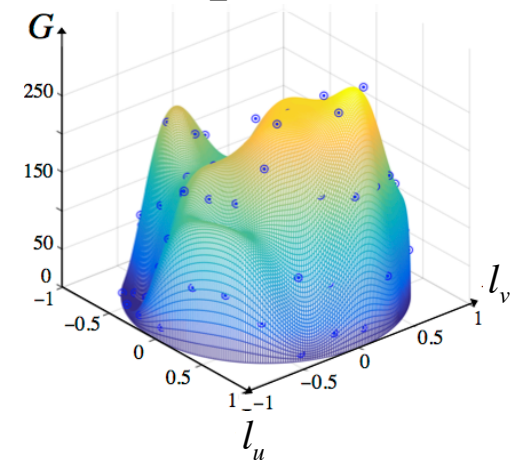


HSH basis

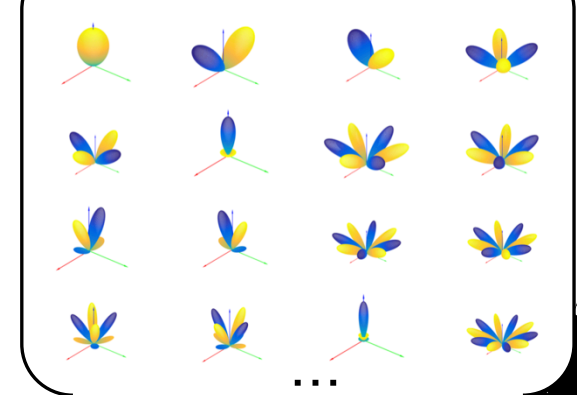


## Proposed model

### Discrete Modal Decomposition **DMD**



DMD basis

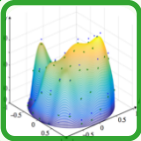


**GILLES PITARD**, et al. “Discrete Modal Décomposition: ...”.  
*Machine Visions and Applications, 2017*



## 1. Reflectance Transformation Imaging

- ⊕ Related works
- ⊕ RTI Devices



## 2. Modeling the angular reflectance

- ⊕ Angular reflectance modeling
- ⊕ Discrete Modal Decomposition



## 3. Computing the saliency maps

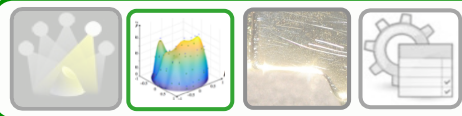
- ⊕ Rotation-invariant representation
- ⊕ Multivariate analysis

→ Proposal for a new R.T.I method,



## 4. Or called « Discrete Modal Decomposition »

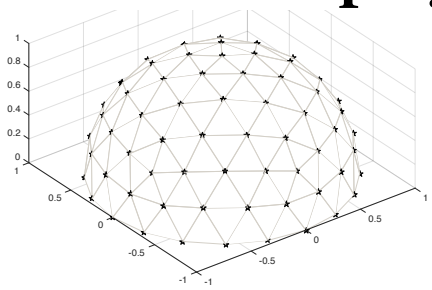




# 2. MODELING THE ANGULAR REFLECTANCE

## ↘ Basis of projection called « Reflectance Modal Basis »

Discretization of the nominal surface geometry



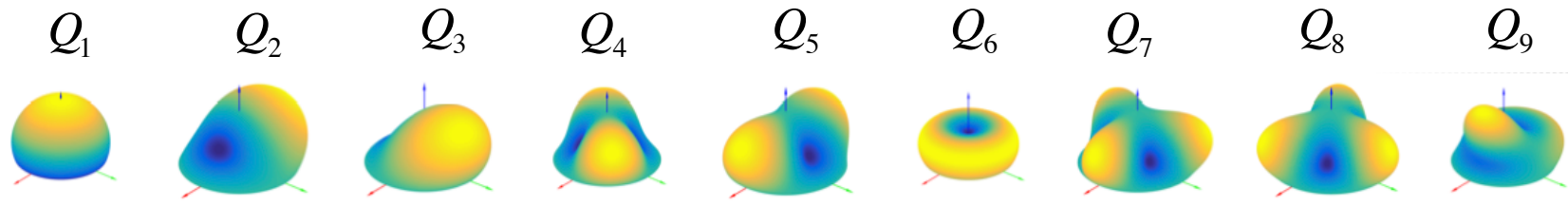
Classical equations of motion

$$M.\ddot{q} + K.q = 0 \quad \text{avec} \quad q = q(\theta, \phi, t)$$

$$q(\theta, \phi, t) = \sum_{k=1}^{+\infty} Q_k \cos(w_k t)$$

$$(M^{-1}K - \frac{1}{w_k^2} I) Q_k = 0$$

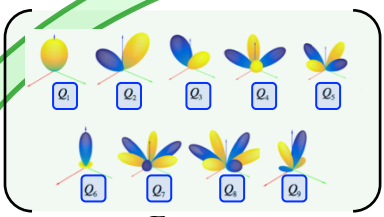
Calculation of modes  $Q_k$  with the pulsation  $w_k$



# 2. MODELING THE ANGULAR REFLECTANCE

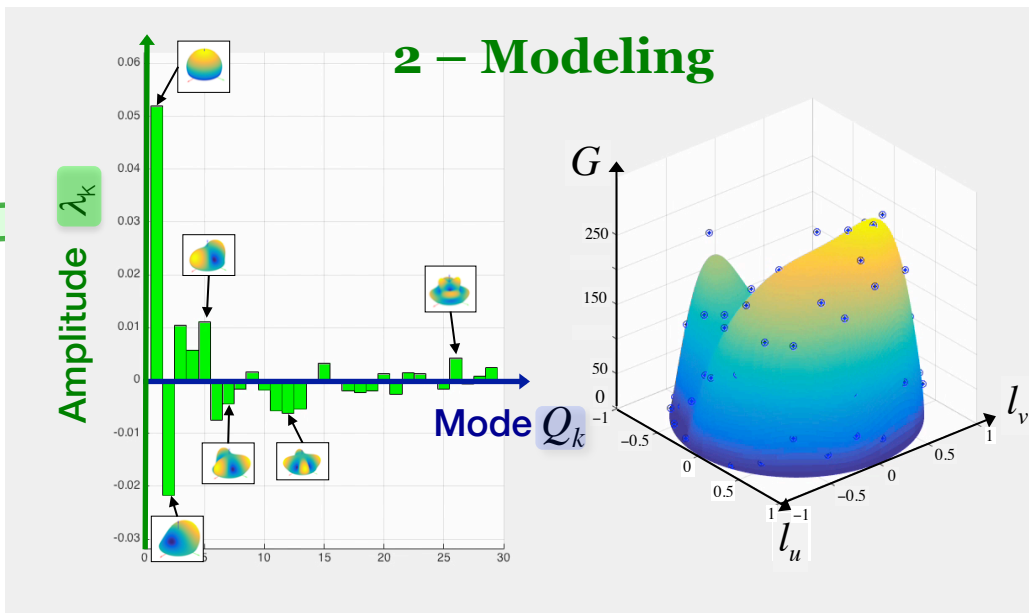
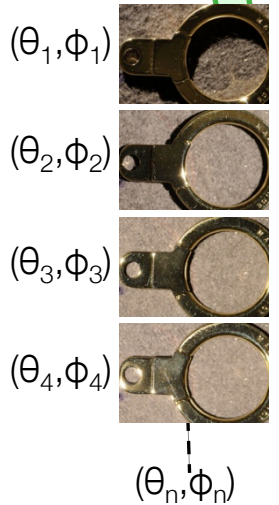
For each pixel:

$\lambda_k$  modal coefficients obtained by projecting the measured luminances  $L$  onto each mode  $Q_k$  of the basis

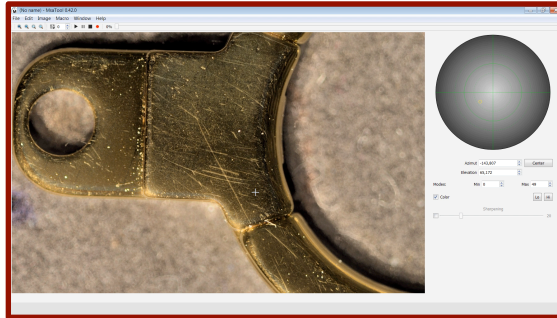


Reflectance Modal Basis Q

## 1 - Acquisition



$$f_{(\theta_v, \phi_v)}(\theta_i, \phi_i) = \sum_{k=1}^n \lambda_k(\theta_v, \phi_v) Q_k(\theta_i, \phi_i) + R_n$$



## 3 - Rendering



## 2. MODELING THE ANGULAR REFLECTANCE

### ✦ Assessing the image quality of the reconstructed images

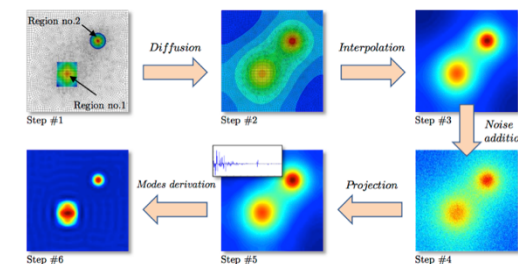
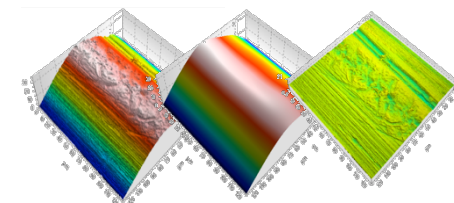
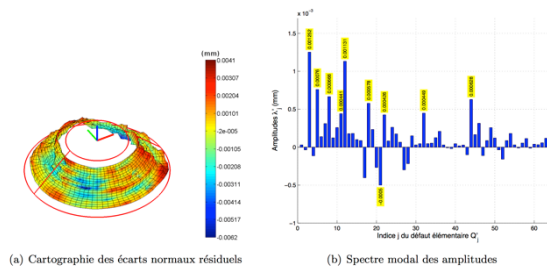


## 2. MODELING THE ANGULAR REFLECTANCE

### Discrete Modal Decomposition

From [mechanical vibrations](#), DMD has notably been applied for:

1. **Characterization and specification of geometric deviations in form**, in the field of geometric tolerancing [1]
2. **The 3D multi-scale topographic measurements of roughness analysis** (form, waviness and roughness) [2]
3. **The estimation of spacial term of a heat diffusion problem** [3]
4. **The assessment of the angular distribution of reflectance from RTI data** [4]



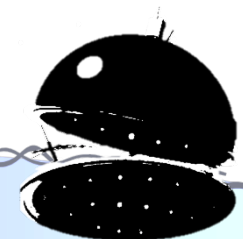
Works initiated by **Serge Samper** at SYMME Laboratory and continued by:

[1] H. Favreliere, Modal Tolerancing : From metrology to specifications, Ph.D. thesis, 2009

[2] G. Le Goic and Al., Multi scale modal decomposition of primary form, waviness and roughness of surfaces, Scanning, 2011

[3] T. Pottier and Al., Proposition of a modal filtering method to enhance heat source computation..., IEJS, 2014

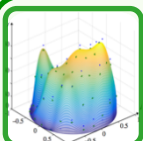
[4] G. Pitard and Al., Discrete Modal Decomposition for surface appearance modelling and rendering, Optical Metrology SPIE, 2015





## 1. Reflectance Transformation Imaging

- ⊕ Related works
- ⊕ RTI Devices



## 2. Modeling the angular reflectance

- ⊕ Angular reflectance modeling
- ⊕ Discrete Modal Decomposition

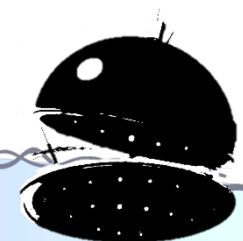


## 3. Computing the saliency maps

- ⊕ Rotation-invariant representation
- ⊕ Multivariate analysis

## 4. Ongoing works

→ Change the DMD parametrization in a rotation-invariant representation to ease the detection



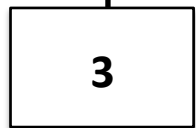
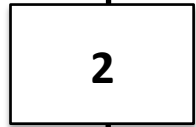
### 3. COMPUTING THE SALIENCY MAPS

#### ✦ Proposal

- ❖ aim: creation of a detection method based on the modal spectra
- ➔ Detecting the significant deviations in the angular reflectance

RTI DATA  
(dataset of  
images)

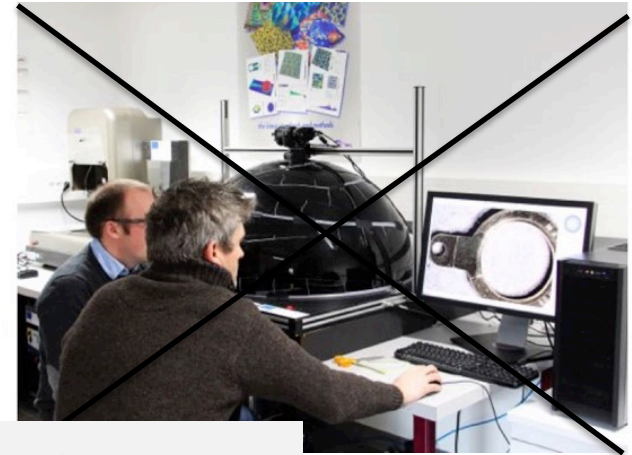
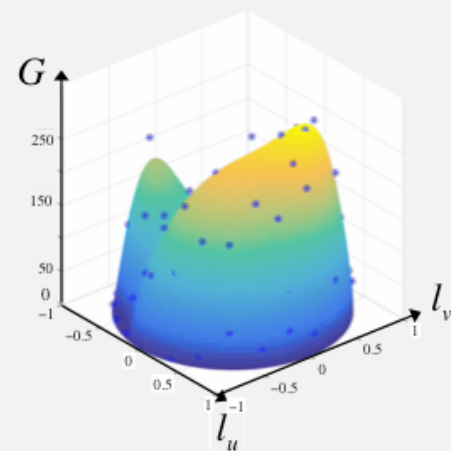
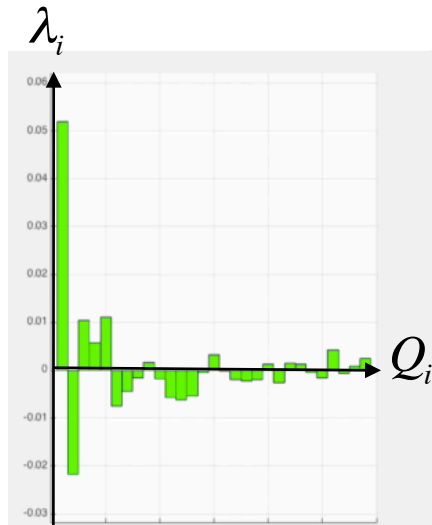
**Step 1:**  
Discrete Modal Decomposition



$D_M$   
**Saliency  
map**

$\lambda_i$

$\lambda'_j$



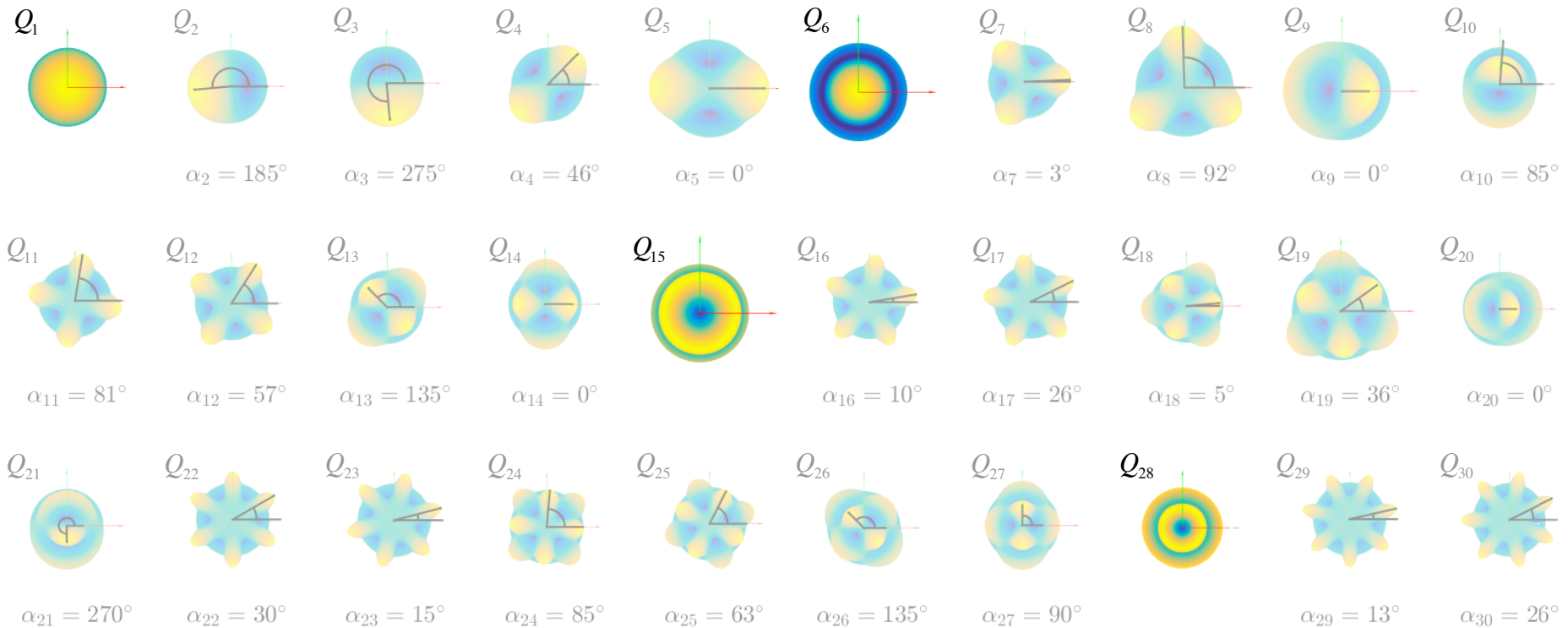


### 3. COMPUTING THE SALIENCY MAPS

#### Two families of modes in the RMB

□ **Simple modes** → rotation invariants

□ **Congruent modes**

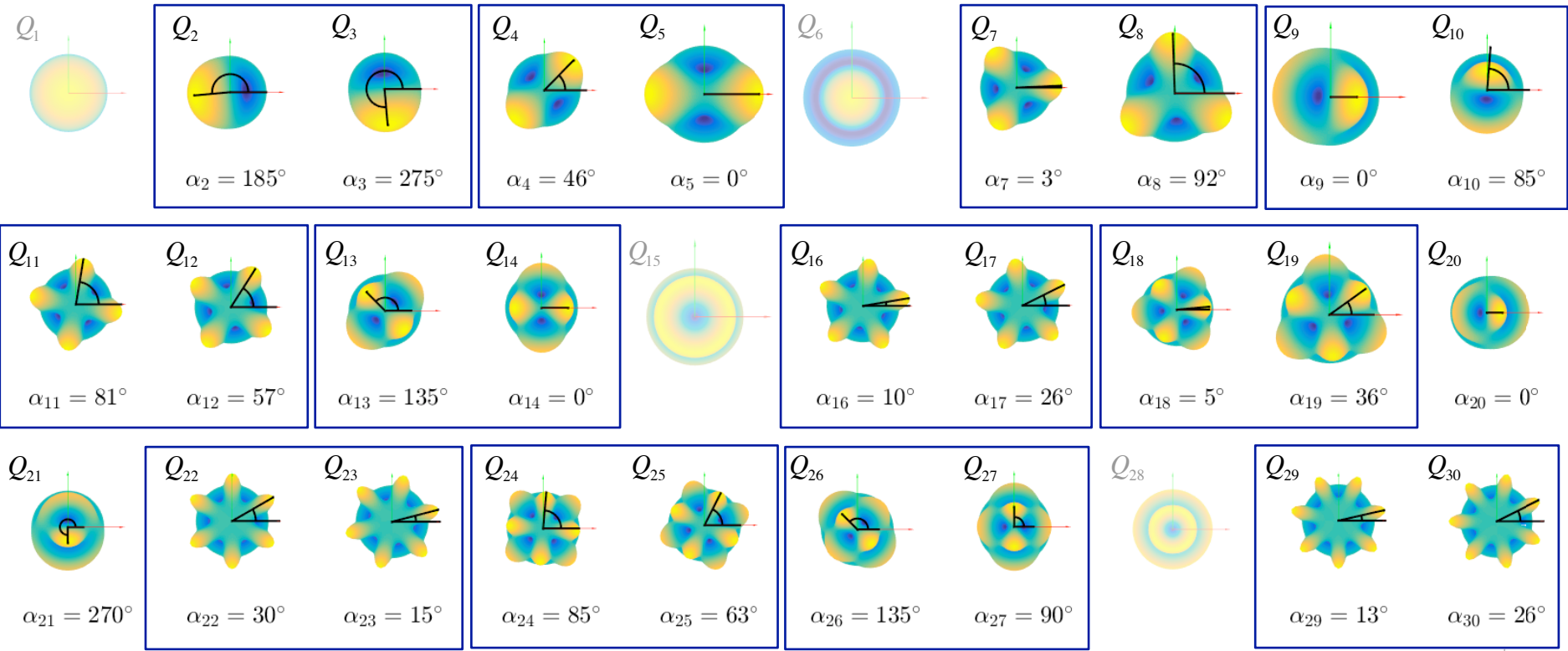


# 3. COMPUTING THE SALIENCY MAPS

## Two families of modes in the RMB

Simple modes

**Congruent modes** → pair with the same shape but oriented differently



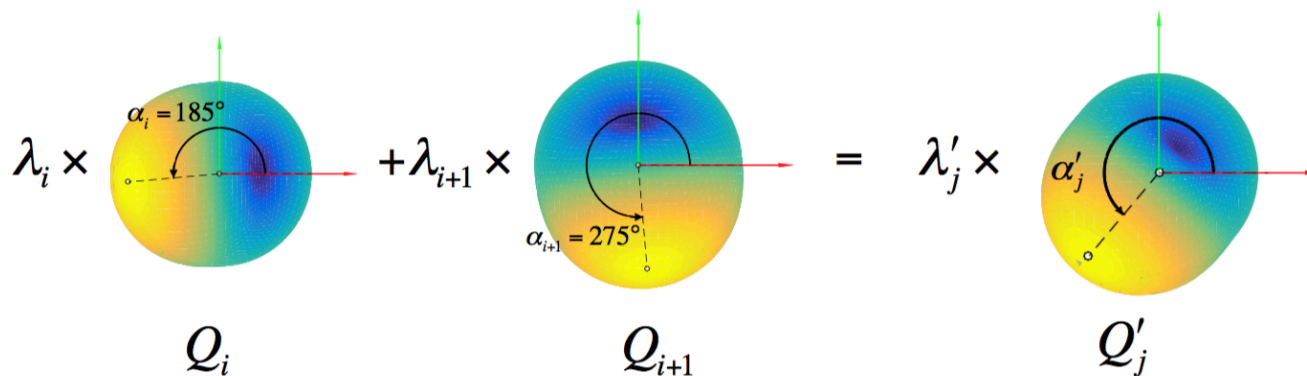
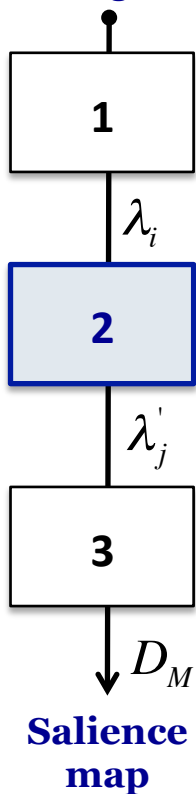
### 3. COMPUTING THE SALIENCY MAPS

↘ **Step 2: changing the parameterization for the congruent modes**

➔ Separating *phase-angle* and *amplitude* components

RTI DATA

(dataset of images)



□ **Amplitude**  $\lambda'_j = \sqrt{\lambda_i^2 + \lambda_{i+1}^2}$  ➔ Rotational invariant component

□ **Phase-angle**  $\alpha'_j = \alpha_i + \arctan \frac{\lambda_{i+1} \sin(\alpha_{i+1} - \alpha_i)}{\lambda_i + \lambda_{i+1} \cos(\alpha_{i+1} - \alpha_i)}$

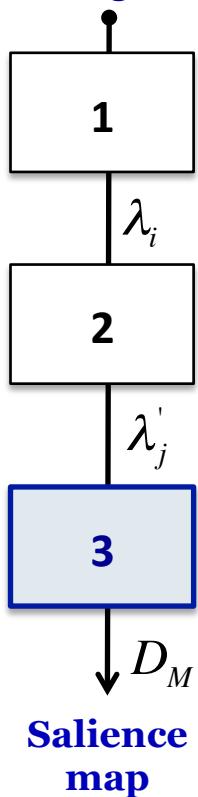
Saliency map



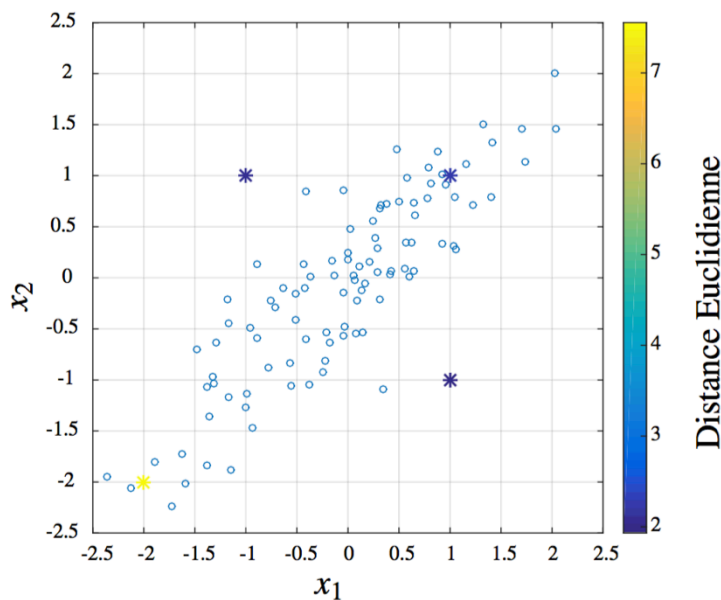
### 3. COMPUTING THE SALIENCY MAPS

#### Step 3: multivariate analysis of modal amplitudes $\lambda_j'$

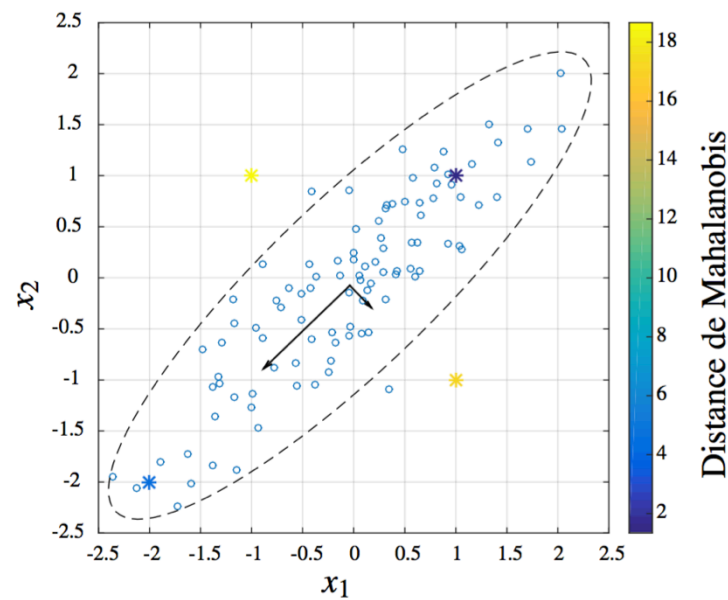
RTI DATA  
(dataset of  
images)



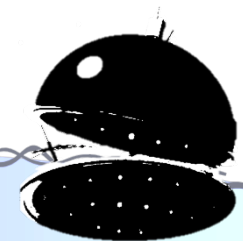
- ✓ **Mahalanobis distance:** taking into account the variance of data, the different scales between the variables, and their correlations



$$d(x) = \|x - \mu\|$$

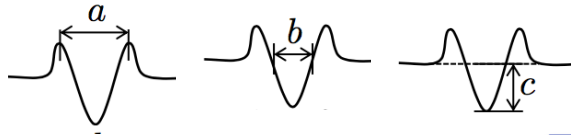
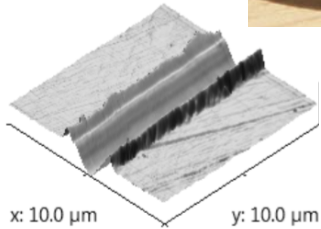
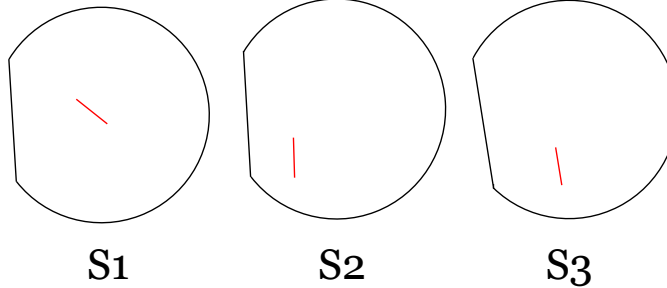
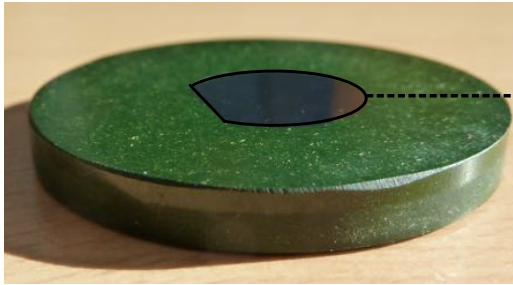


$$D_M(x) = \sqrt{(x - \mu)^T \Sigma^{-1} (x - \mu)}$$

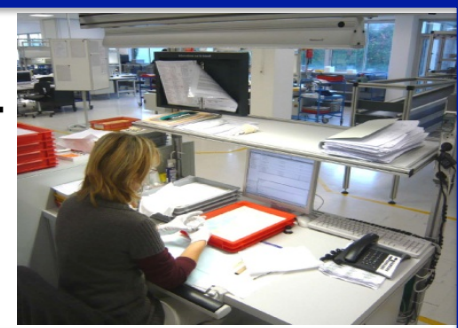


### 3. COMPUTING THE SALIENCY MAPS

↘ **Samples: 3 polished surfaces**



Sample	$a$ ( $\mu\text{m}$ )	$b$ ( $\mu\text{m}$ )	$c$ ( $\mu\text{m}$ )	Visibility (%)
$S_1$	1.25	0.75	58.32	64.6
$S_2$	0.98	0.61	43.57	14.5
$S_3$	0.68	0.44	26.1	5

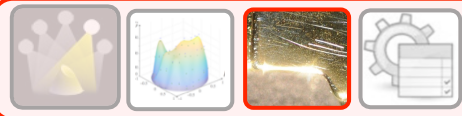


Psychophysical experiments



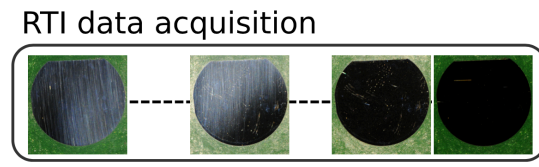
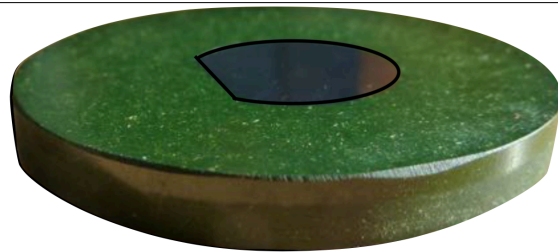
T. Puntous, et al. "Ability of quality controllers to detect standard scratches on polished surfaces," *Precision Engineering*, 2013



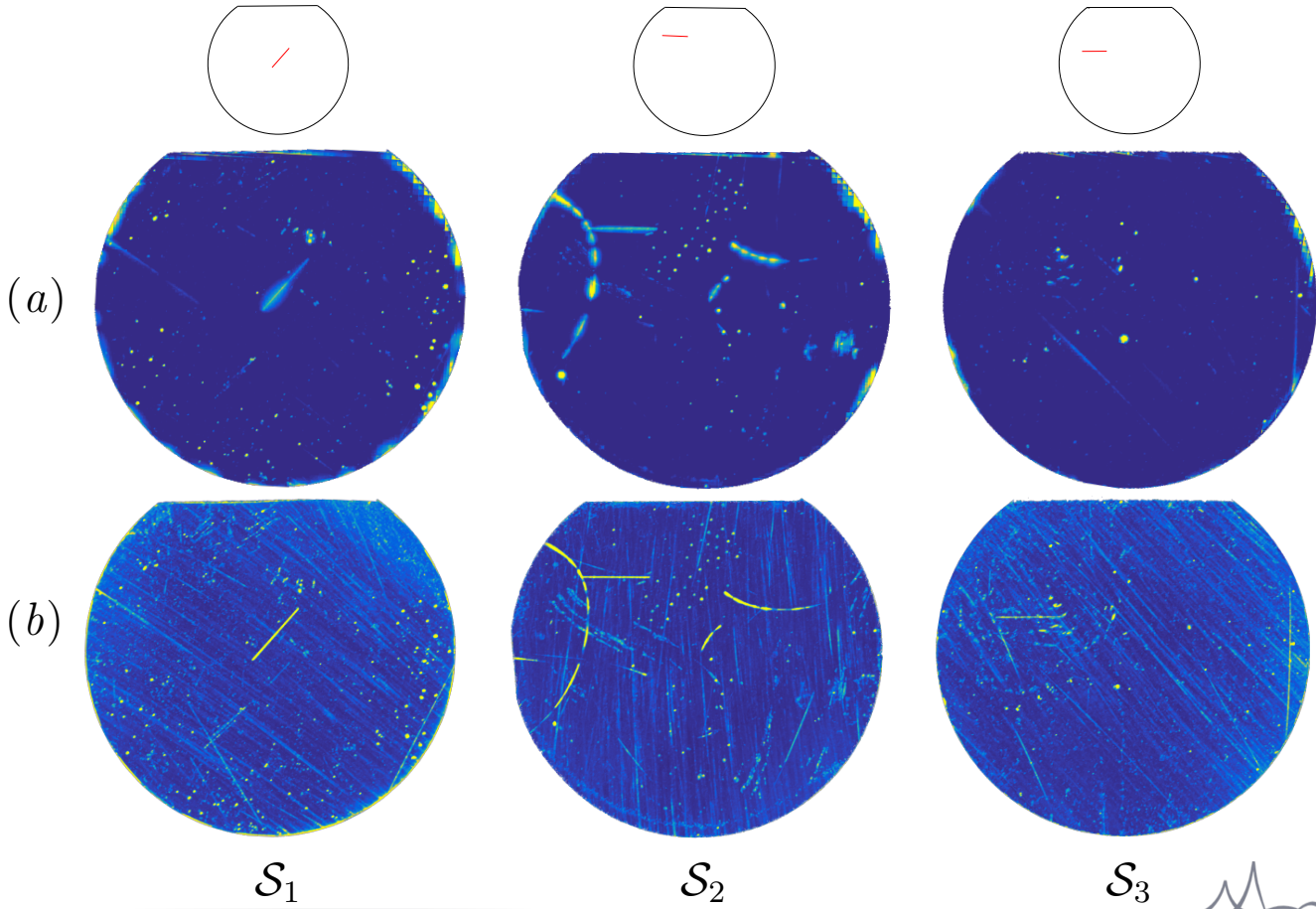
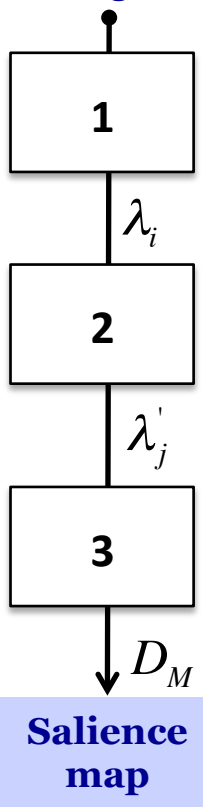


# 3. COMPUTING THE SALIENCY MAPS

## Results



RTI DATA  
(dataset of images)



Itti's method

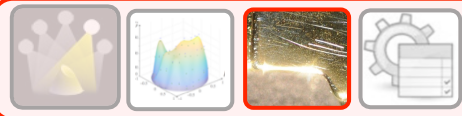
Our  
(speedup  $\approx 150$  times)

$S_1$

$S_2$

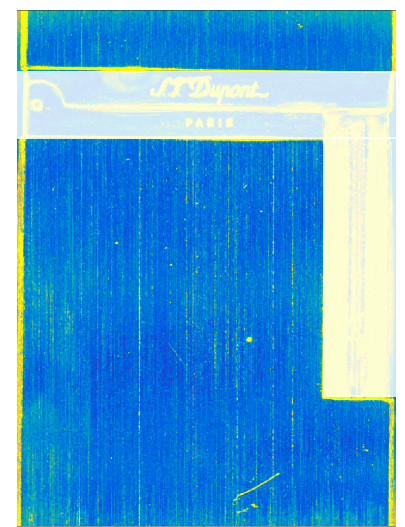
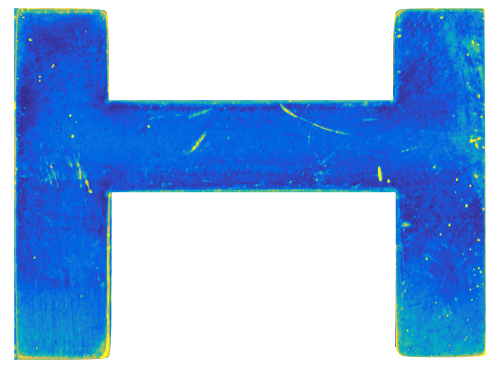
$S_3$





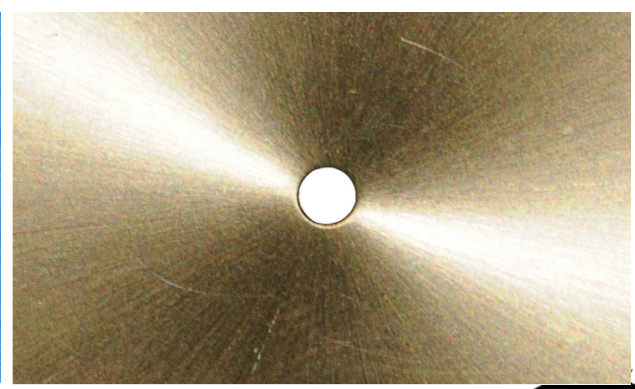
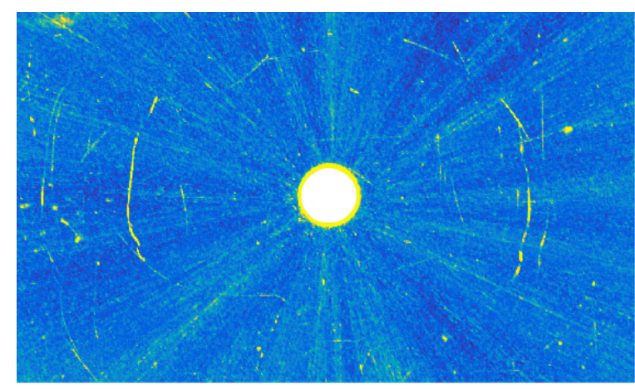
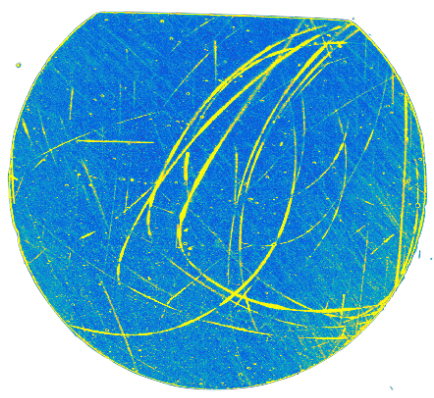
### 3. COMPUTING THE SALIENCY MAPS

↘ Saliency maps obtained from our methodology



Link in a watch bracelet

Lighter body



Highly polished surface

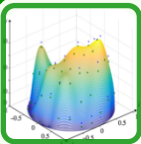
Sunray pattern dial watch





## 1. Reflectance Transformation Imaging

- ⊕ Related works
- ⊕ RTI Devices



## 2. Modeling the angular reflectance

- ⊕ Angular reflectance modeling
- ⊕ Discrete Modal Decomposition



## 3. Computing the saliency maps

- ⊕ Rotation-invariant representation
- ⊕ Multivariate analysis



## 4. Conclusion





## 4. CONCLUSION

### ✦ We claim:

- **A change in the DMD parametrization** of angular reflectances for the comparison of reflectance shapes independently from their spatial orientation
- **Detection and location of changes (saliency maps) in reflectance shape** over the inspected by performing a multivariate analysis in this rotation-invariant space

### ✦ Ongoing tasks:

- **Evaluation of the criticality of the detected anomalies** by using several modalities (reflectance, geometry, spectral response)



# THANKS !

