

# Robust Detection of Jittered Multiply Repeating Audio Events Using Iterated Time-Warped ACF

Frank Kurth, Kevin Wilkinghoff

## 1. Introduction

### Goal

- Robust detection of multiply "almost repeating" (jittered) events in time series
- Model: Repeating onset times  $(t_0, t_0 + \lambda, \dots, t_0 + K\lambda) + (\delta_0, \delta_1, \dots, \delta_K)$ ,  $\max(|\delta_i|) < \lambda/2$

### Approach

- Combine *shift-ACF*, a variant of classical ACF, with *Dynamic Time Warping (DTW)*

### Evaluation

- Newly introduced *ITW-ACF* outperforms ACF and shift-ACF on bioacoustics datasets

## 2. Shift-Method and Shift-ACF

**Shift-product:** (for integer  $s$ )

$$\mathbb{O}_s^0[x](k) := P_s[x](k) := x(k) \cdot \overline{x(k-s)}$$

emphasizes repeating components.

$$\text{Binary version: } \mathbb{O}_s^0[x, y](k, l) := x(k) \cdot \overline{y(l-s)}$$

**Shift-minimum:**

$$\mathbb{O}_s^1[x](k) := M_s[x](k) := \min(|x(k)|, |x(k-s)|)$$

suppresses non-repeating components

**General shift-method framework:**

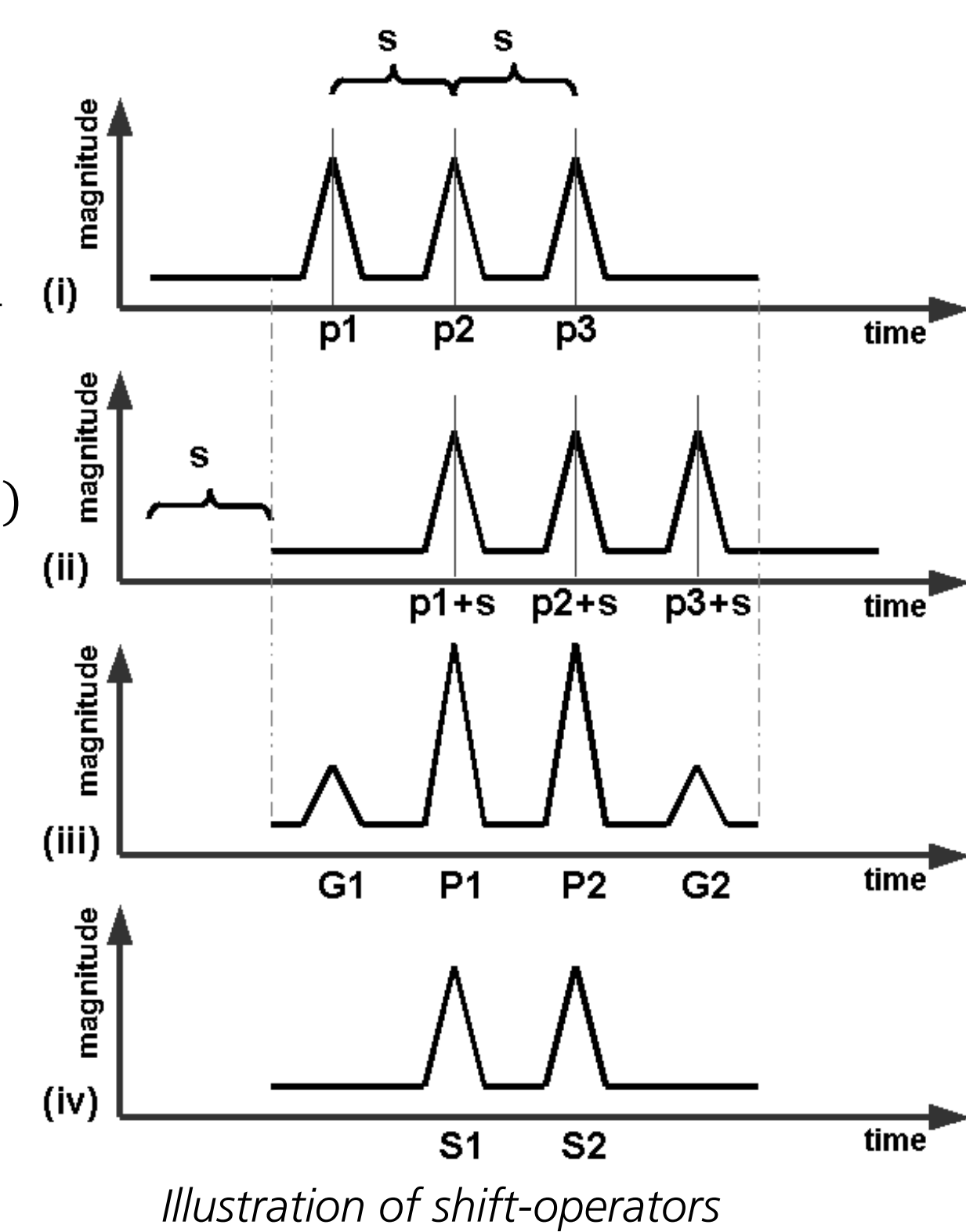
$$\mathbb{O}_s^t := \mathbb{O}_s^{t_1} \circ \dots \circ \mathbb{O}_s^{t_n}, \quad t = (t_1, \dots, t_n) \in \{0, 1\}^n$$

**Shift Operations ("ShOps"):**

$$\mathbb{O}_s^t[x] \text{ is called ShOp, } (\mathbb{O}_s^t[x])_s \text{ ShOp-matrix}$$

**Shift-ACF of type  $t$ :**

$$ACF^t[x](s) := \sum_{k \in \mathbb{Z}} \mathbb{O}_s^t[x](k)$$

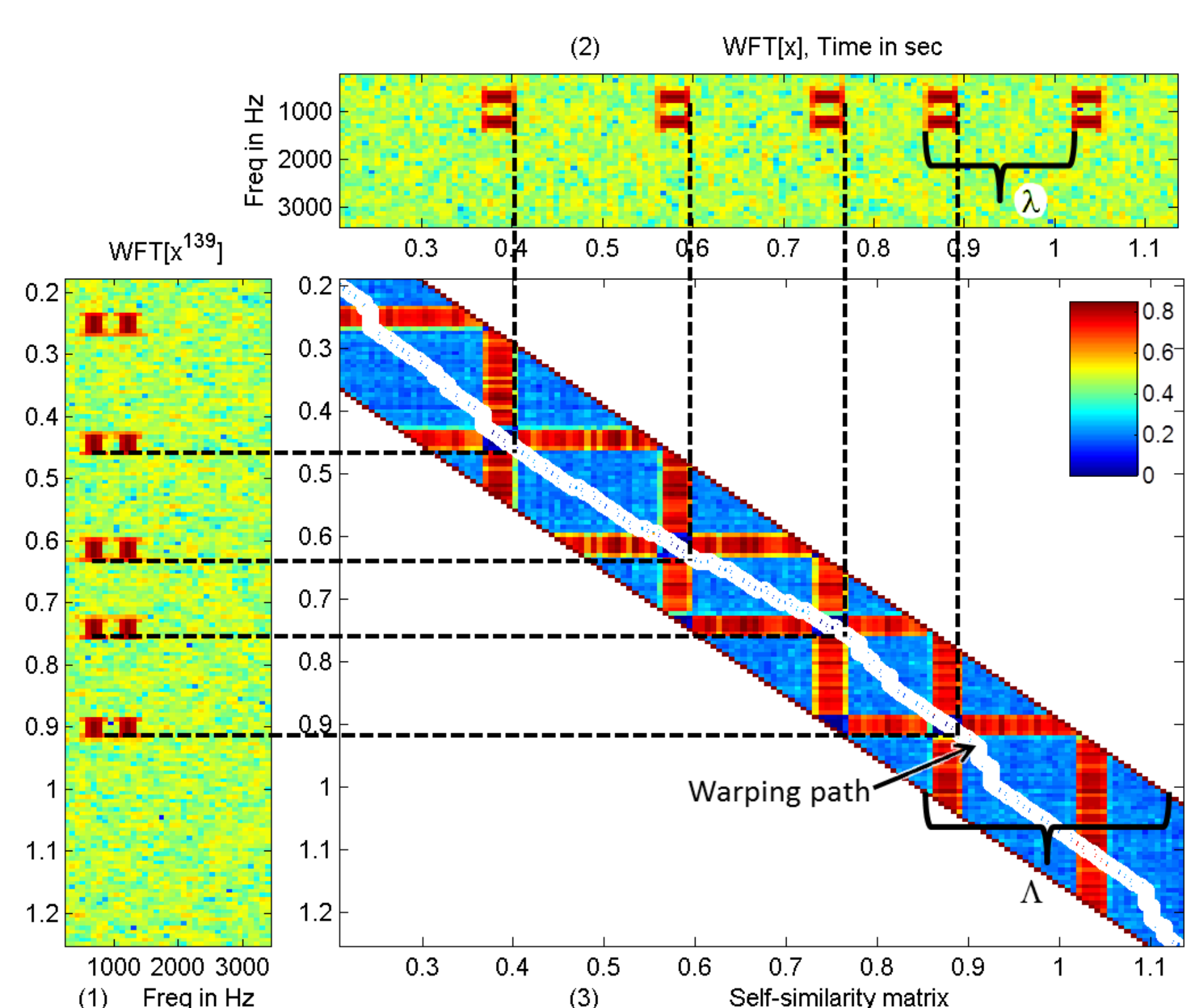


## 3. Jittered Multiply Repeating Events and DTW

(1) Spectrogram  $WFT[x]$  of DTMF Signal  $x$ .  $x$  contains multiply "almost repeating" (jittered) events.

(2) Spectrogram of same signal as in (1) delayed by 139 samples, i.e.  $WFT[x^{139}]$ .

(3) Warping path between  $WFT[x]$  and  $WFT[x^{139}]$  obtained by DTW restricted to Sakoe-Chiba-band.



## 4. Iterated Time-Warped ACF (ITW-ACF)

### Main Idea

- Perform shift-operations  $\mathbb{O}_s^0$  and  $\mathbb{O}_s^1$  along warping path between  $x$  and  $x^s$
- Iteration for fixed shift  $s$  along shift type  $t = (t_1, \dots, t_n) \in \{0, 1\}^n$

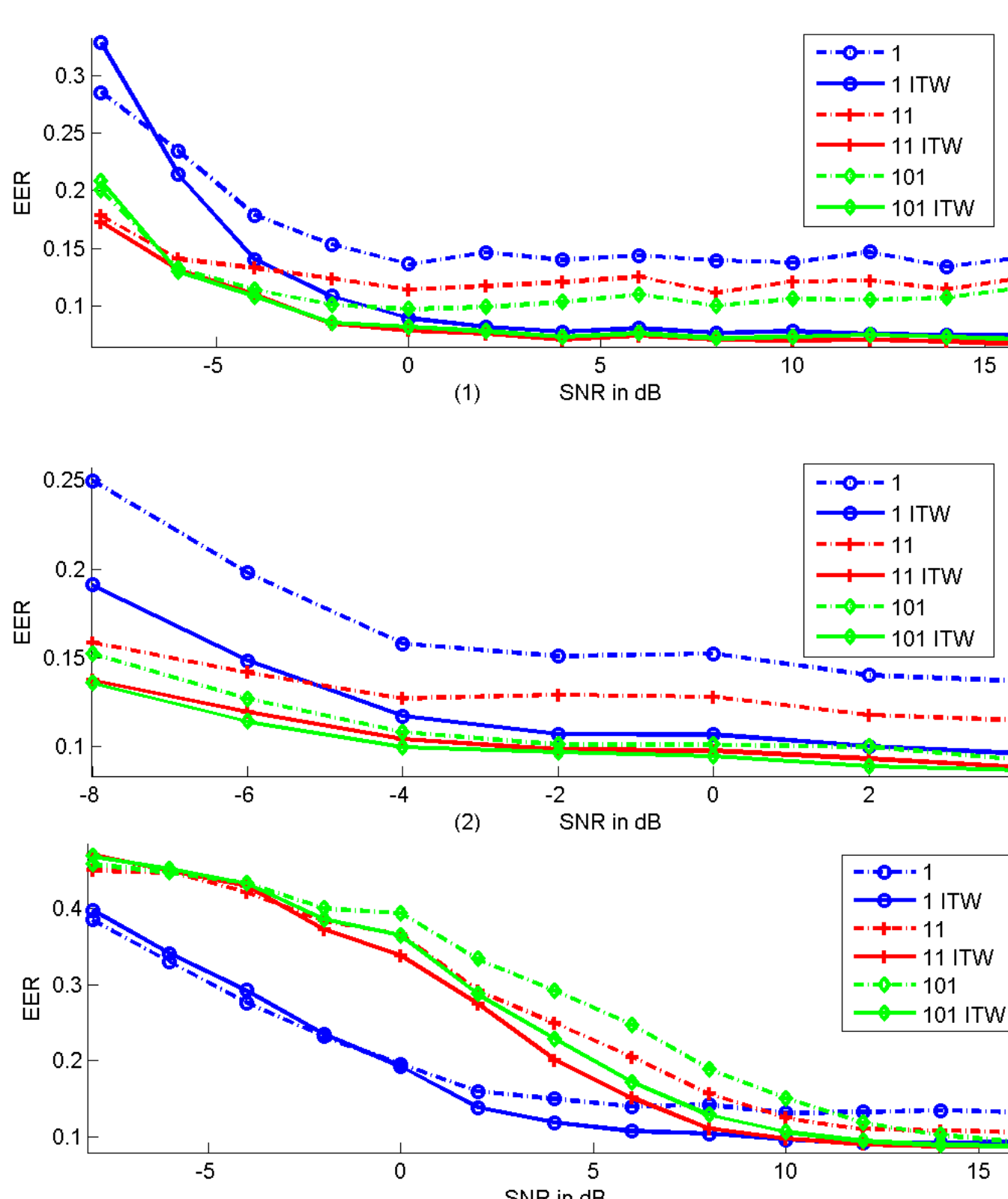
In step  $1 \leq i \leq n$

- Compute band-restricted DTW of  $x$  and  $x^s$  yielding warping path  $((a_1, b_1), \dots, (a_p, b_p))$
- Compute warped  $t_i$ -operation  $y(k) := \mathbb{O}_0^{t_i}[x, x^s](a_k, b_k)$  for  $1 \leq k \leq p$
- Unwarp  $y$  using back-projection to  $(a_1, \dots, a_p)$ , yielding warped ShOp  $\tilde{\mathbb{O}}_s^{t_i}[x]$

Iterated time-warped ACF is defined as

$$ITW-ACF^t[x](s) := \sum_{k \in \mathbb{Z}} \tilde{\mathbb{O}}_s^{t_i}[x](k)$$

## 5. Evaluation



Detection equal error rates (EER) for:

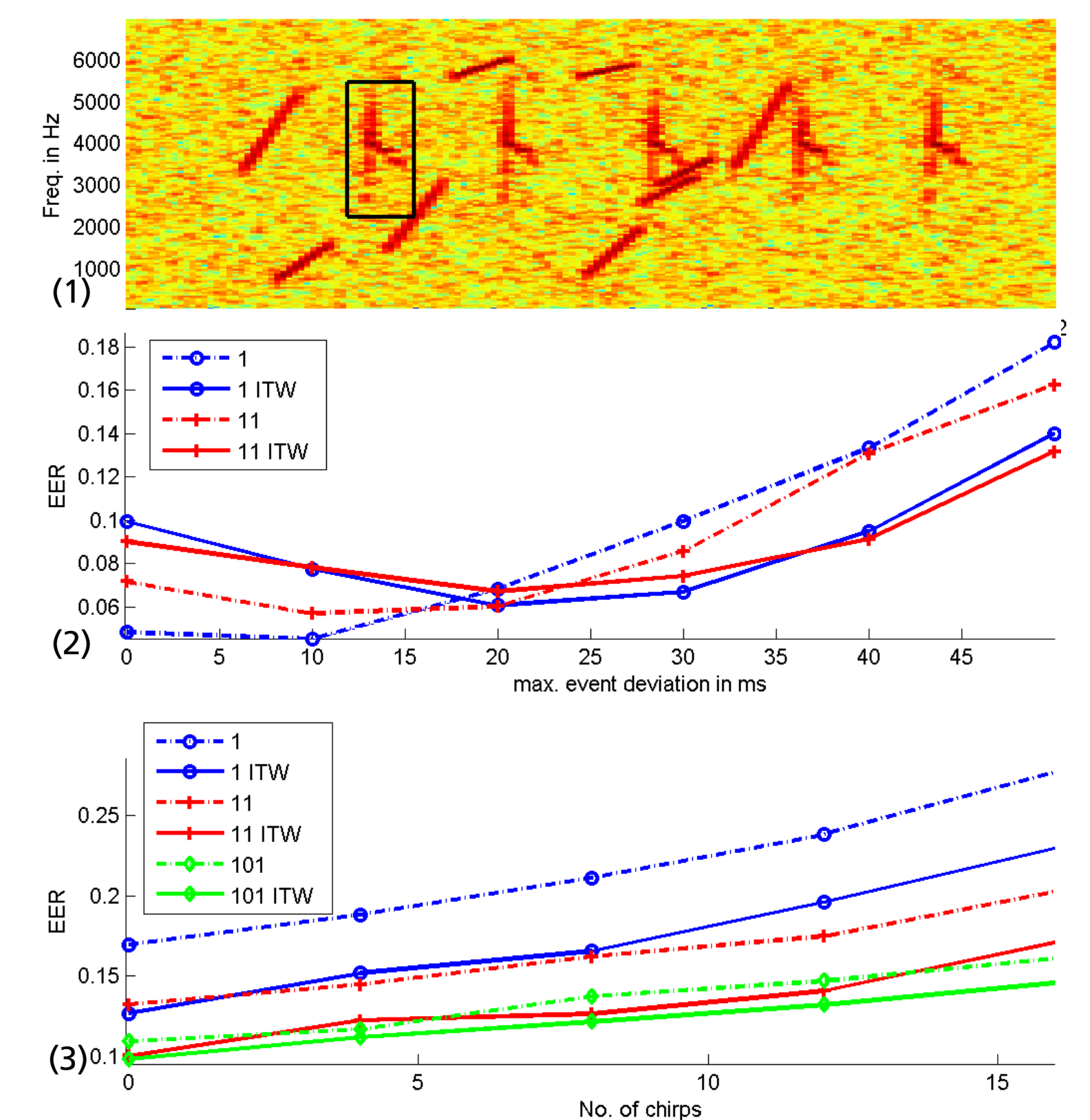
- DTMF-signals depending on SNR-level of added Gaussian noise. (5 DTMF-tones repeated at initial (random) IOI in [80, 200] ms. Jitter: maximum individual deviation of 20 ms.)
  - Bioacoustic events depending on SNR-level of added Gaussian noise.
  - bioacoustic events depending on SNR-level of added realistic bioacoustic background noise.
- (Counting of TPs and FPs is detailed below, see Evaluation.)

(1) 5-fold repeated bioacoustic event\* (framed) with 9 added chirps at 0 dB Gaussian background noise.

(2) Detection-EERs for bioacoustic events with added realistic bioacoustic background noise at 10 dB, depending on maximum event deviation in ms.

(3) Detection-EERs for bioacoustic events with added Gaussian noise at -5 dB for different numbers of added chirp signals.

- \*Bioacoustic events taken from
  - Reference System of Animal Vocalisations of Museum für Naturkunde Berlin, <http://www.animalsoundarchive.org/RefSys/>
  - xeno-canto, <https://www.xeno-canto.org/>



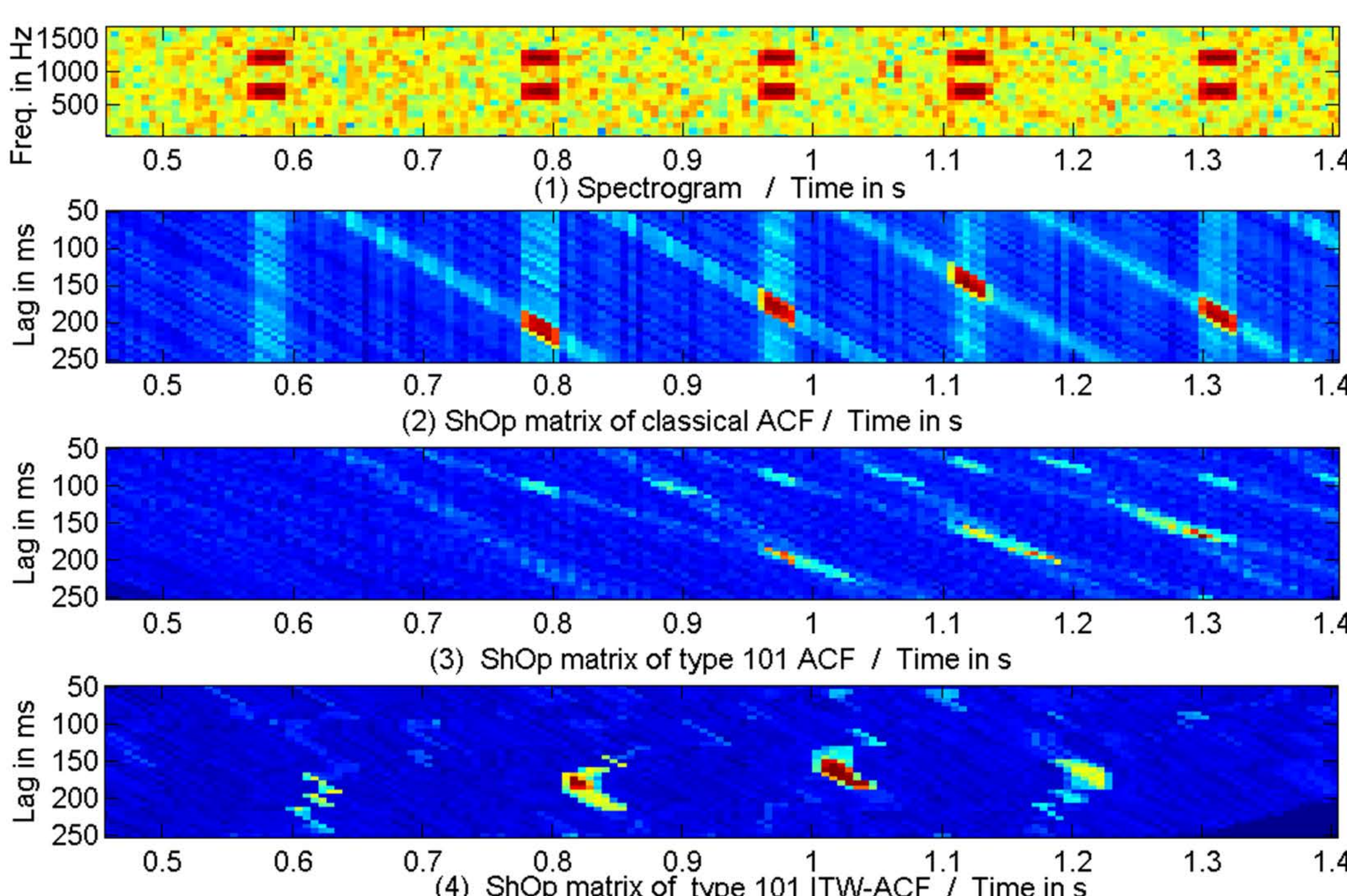
## Comparison of standard ACF, Shift-ACF, and proposed Iterated Time-Warped ACF

(1) Spectrogram of signal  $x$  containing 5 subsequent DTMF-tones.

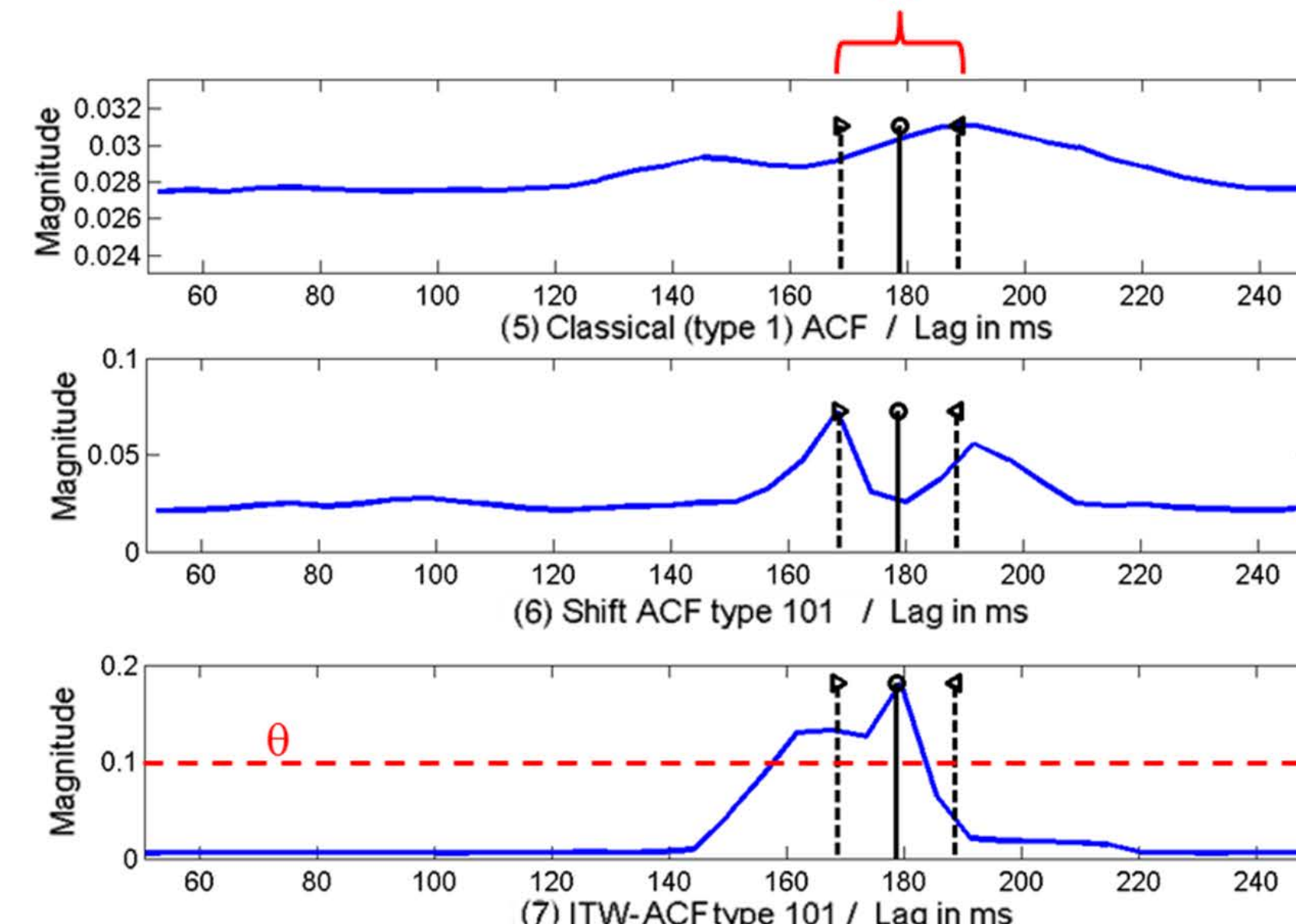
(2) ShOp-matrix  $(\mathbb{O}_s^0[x])_s$ , i.e., for classical ACF.

(3) ShOp-matrix  $(\mathbb{O}_s^{101}[x])_s$ .

(4) ShOp-matrix for proposed ITW-ACF, i.e.,  $(\tilde{\mathbb{O}}_s^{101}[x])_s$ .



**Evaluation:** TPs are lags inside dashed region of width  $\Delta$  around known basic IOI (circles) with  $ACF > \theta$ . FPs: lags outside dashed region with  $ACF > \theta$ .



Different ACFs corresponding to (2)-(4):

- standard (type 1) ACF
- type 101 shift-ACF,
- Proposed warped ACF of type 101

Ground truth IOI (circle) and 20 ms tolerance region (dashed lines) are indicated in black.

Note that only ITW-ACF exceeds threshold  $\theta = 0.1$