



Joint source localization and dereverberation by sound field interpolation using sparse regularization

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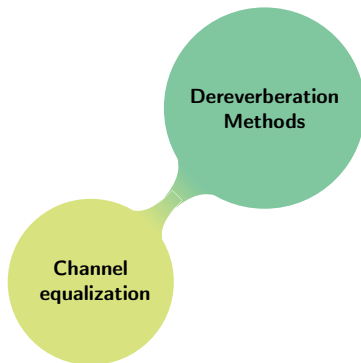
1. Introduction
2. Acoustic models
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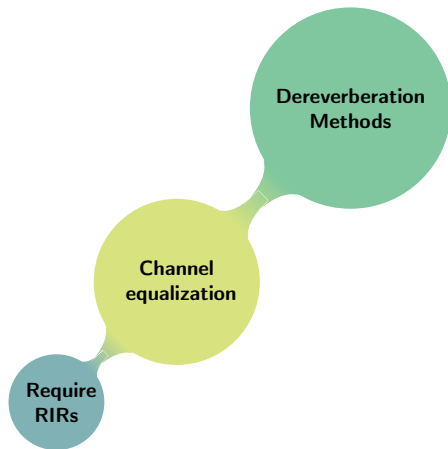


**Dereverberation
Methods**

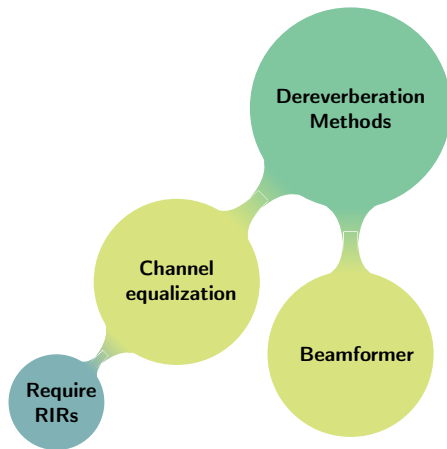
Reverberant environments reduce speech intelligibility



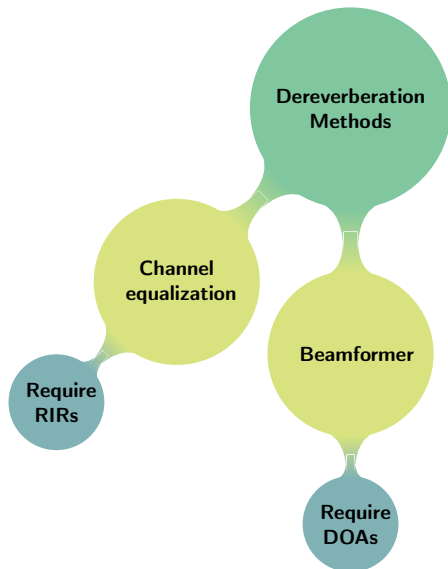
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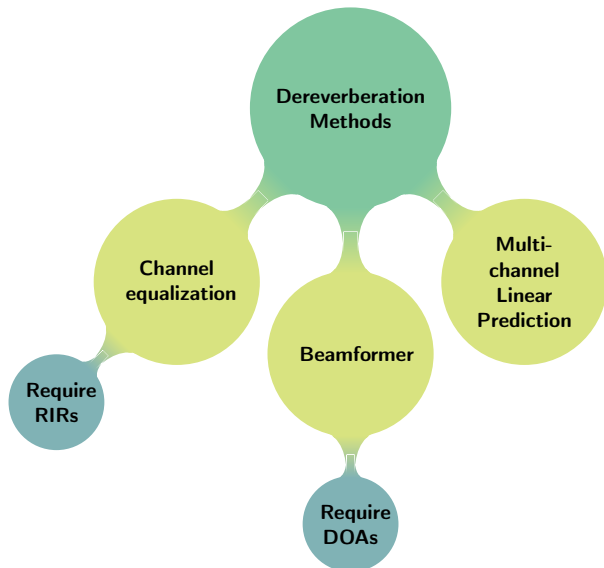
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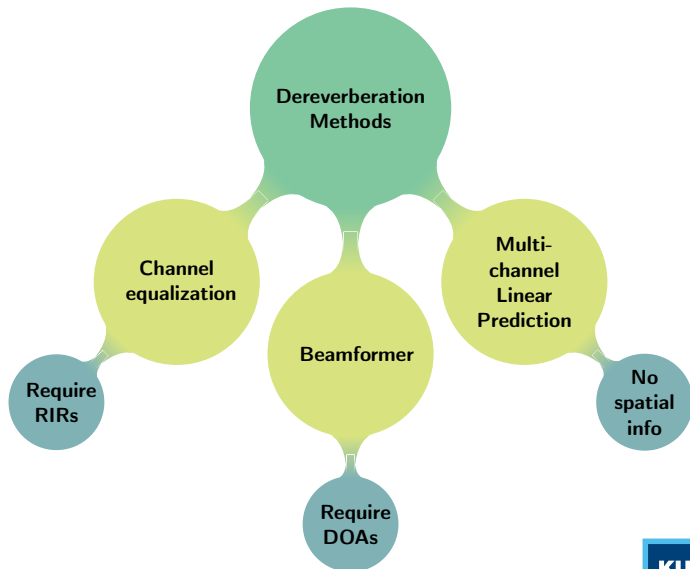
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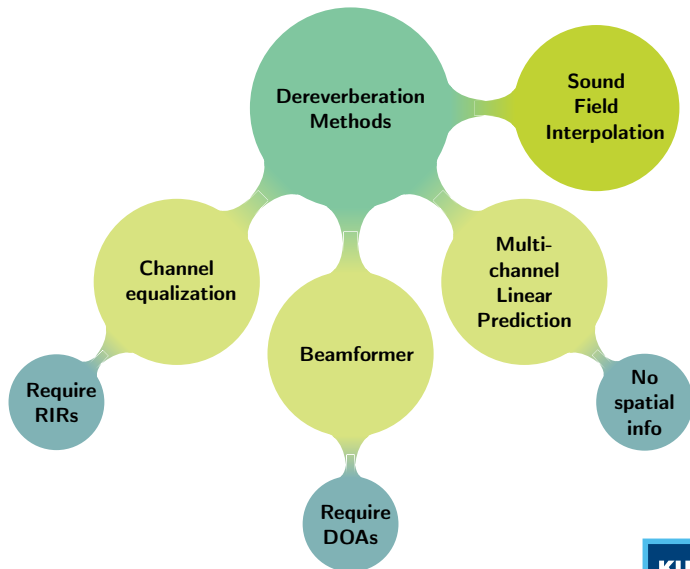
Reverberant environments reduce speech intelligibility



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Reverberant environments reduce speech intelligibility



- ▶ Localization and dereverberation formulated jointly

Novel method

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 - ▶ Time-domain Equivalent Source Model (TESM)

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 - Sparse prior
 - ▶ spatial sparsity
 - ▶ spatio-temporal sparsity
 - ▶ spatio-spectral sparsity

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 - ▶ spatio-spectral sparsity
- ▶ Large-scale nonsmooth optimization problem:
 - accelerated variant of Proximal Gradient (PG) algorithm
 - Weighted Overlap-Add (WOLA) procedure

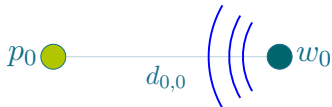
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Time-domain equivalent source model (TESM)

Time-domain spherical wave definition (Green's function):

$$p(t, \mathbf{x})|_{\mathbf{x}=\mathbf{x}_m} = \frac{1}{4\pi d_{l,m}} \delta\left(t - \frac{d_{l,m}}{c}\right) * w(t),$$

where $w(t)$ is a *weight signal* driving the *equivalent source*.

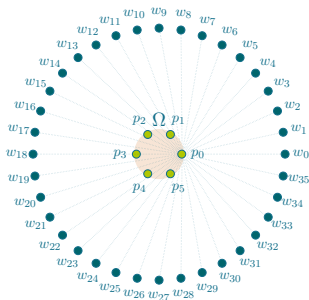


Time-domain equivalent source model (TESM)

Using many equivalent sources and discretizing over time:

$$p(\mathbf{x}, t)|_{\mathbf{x}=\mathbf{x}_m} = \sum_{l=0}^{N_w-1} \frac{1}{4\pi d_{l,m}} \delta\left(t - \frac{d_{l,m}}{c}\right) * w_l(t), \quad \mathbf{x}_m \in \Omega,$$

any sound pressure inside source-free volume Ω can be modeled.

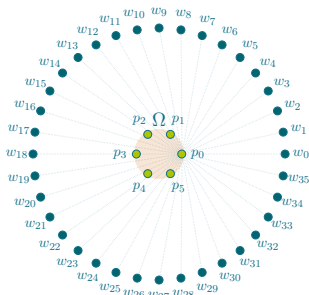


Time-domain equivalent source model (TESM)

Generalizing for many mic positions:

$$\mathbf{P} = \mathbf{D}_t \mathbf{W}$$

where $\mathbf{D}_t : \mathbb{R}^{N_t \times N_w} \rightarrow \mathbb{R}^{N_t \times N_m}$ *dictionary of spherical waves*.

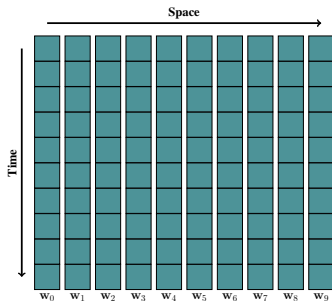


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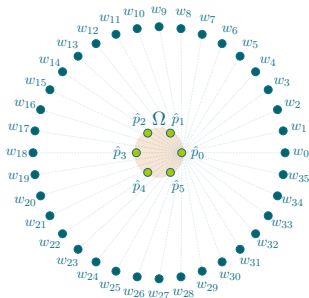


Plane wave decomposition model (PWDM)

Same using many plane waves (frequency domain):

$$\hat{p}(\mathbf{x}, f)|_{\mathbf{x}=\mathbf{x}_m} \approx \sum_{l=0}^{N_w-1} e^{-ik_f d_{l,m}} \hat{w}_l(f) \text{ for } \mathbf{x}_m \in \Omega,$$

any sound pressure inside source-free volume Ω can be modeled.

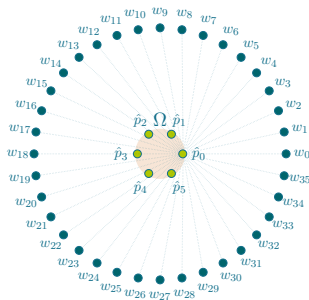


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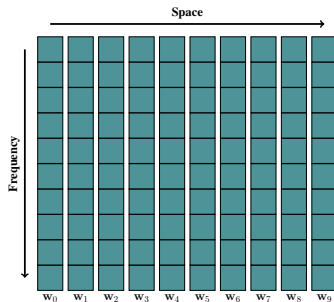


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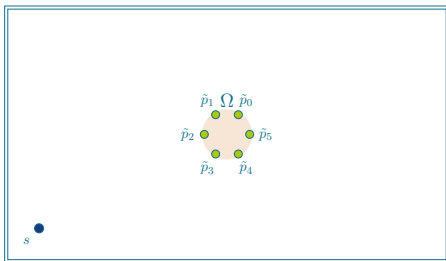
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The inverse problem

Sound field created by *far field* source is recorded by an array of N_m mics.

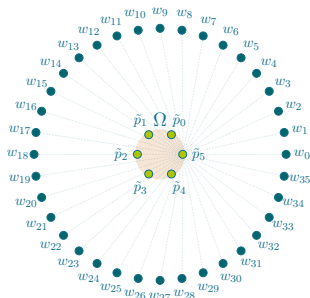


The inverse problem

Optimal weight signals \mathbf{W}^* found by solving:

$$\mathbf{W}^* = \underset{\mathbf{W}}{\operatorname{argmin}} f(\mathbf{W}) = \frac{1}{2} \|\mathbf{D}\mathbf{W} - \tilde{\mathbf{P}}\|_F^2$$

heavily *ill-posed problem* \rightarrow **over-fitting**

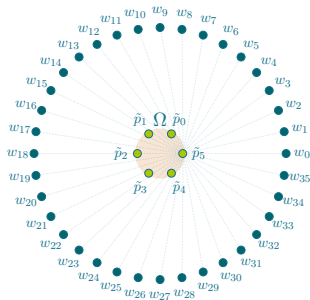


The inverse problem

Optimal weight signals \mathbf{W}^* found by solving:

$$\mathbf{W}^* = \underset{\mathbf{W}}{\operatorname{argmin}} \quad \frac{1}{2} \|\mathbf{D}\mathbf{W} - \tilde{\mathbf{P}}\|_F^2 + \lambda g(\mathbf{W})$$

regularize using a sparsity inducing *regularization term* g .

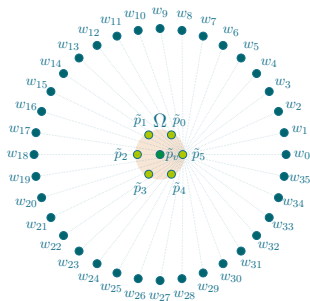


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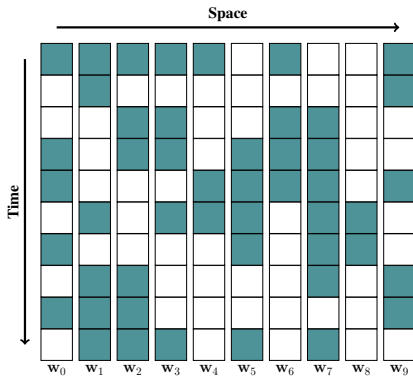
regularize using a sparsity inducing *regularization term* g .
Use additional mic \tilde{p}_v for tuning regularization parameter λ .



Spatio-temporal sparsity

Model: TESM

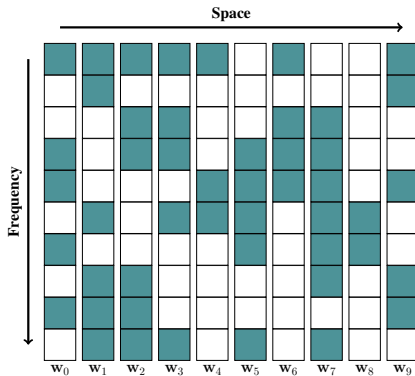
Regularization: $g(\mathbf{W}) = \|\mathbf{W}\|_1$



Spatio-spectral sparsity

Model: PWDM

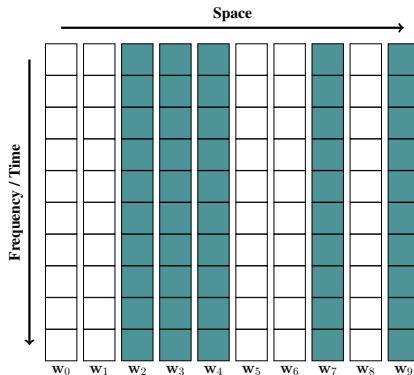
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Spatial sparsity

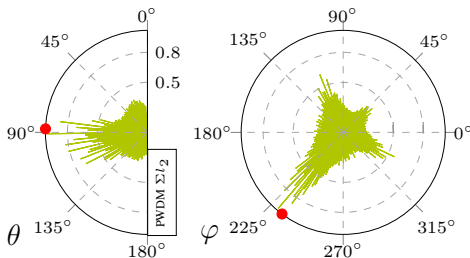
Model: both PWDM and TESM

Regularization: $g(\mathbf{W}) = \sum_{l=0}^{N_w-1} \|\mathbf{w}_l\|_2$



Joint Dereverberation & Localization

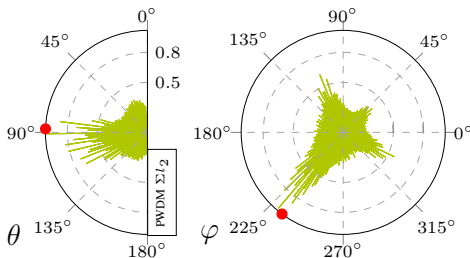
After solving inverse problem obtain \mathbf{W}^*



Plot energy of columns of \mathbf{w}_i^* as a function of azimuthal (φ) and polar (θ) angles.

Joint Dereverberation & Localization

After solving inverse problem obtain \mathbf{W}^*



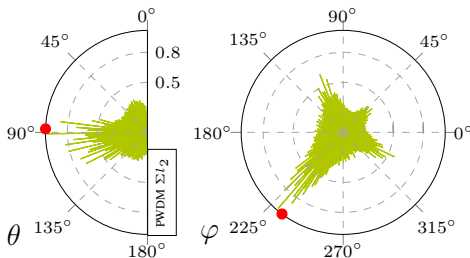
Localization

Find d -th column of \mathbf{W}^* with strongest energy.

This corresponds to equivalent source with specific DOA.

Joint Dereverberation & Localization

After solving inverse problem obtain \mathbf{W}^*



Dereverberation

Dereverberated signal readily available: \mathbf{w}_d^*

Reverberation is spatially distributed among equivalent sources

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Optimization algorithm

Inverse problem: nonsmooth cost function

- ▶ f is smooth
- ▶ g nonsmooth

Proximal Gradient (PG) algorithm

- ▶ can deal with nonsmooth terms
- ▶ cheap iterations
- ▶ suitable for large scale problems
- ▶ can be accelerated using quasi Newton methods[†]

[†] N. Antonello, L. Stella, P. Patrinos and T. van Waterschoot, "Proximal gradient algorithms: applications in signal processing", arXiv:1803.01621, 2018.

github.com/kul-forbes/StructuredOptimization.jl

Optimization algorithm

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Optimization problem may still be intractable:

- ▶ if $N_w = 500$ $N_t = 16000$ (2 s $F_s = 8$ kHz) $\rightarrow 8 \cdot 10^6$
optimization variables

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Weighted Overlap-Add procedure:

- ▶ split $\tilde{\mathbf{P}}$ into overlapping frames of $N_\tau = 512 \rightarrow 256 \cdot 10^3$
optimization variables *sub-problem*

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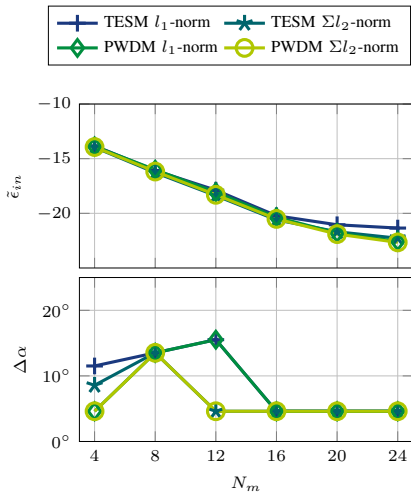
Set-up

- ▶ RIRs simulated with Randomized Image Method¹
 - $T_{60} = 1$ s
 - $[L_x, L_y, L_z] = [7.34, 8.09, 2.87]$ m
- ▶ Mic signals created with male speech signal (sensor noise SNR = 40dB)
- ▶ Spherical microphone array with N_m
- ▶ $N_w = 500$ equivalent sources on a Fibonacci Lattice radius 2.9 m

¹E. De Sena, N. Antonello, M. Moonen, and T. van Waterschoot, "On the Modeling of Rectangular Geometries in Room Acoustic Simulations", IEEE Transactions of Audio, Speech Language Processing, vol. 21, no. 4, 2015.

github.com/nantonel/RIM.jl

Interpolation error & DOA estimate



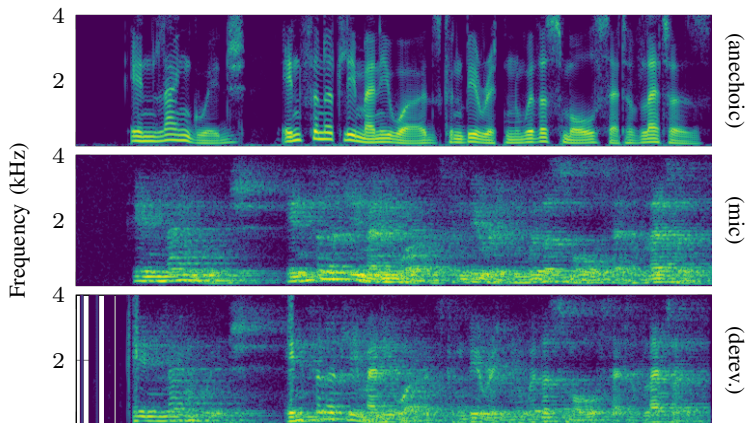
▶ Average interpolation error $\bar{\epsilon}_{in}$

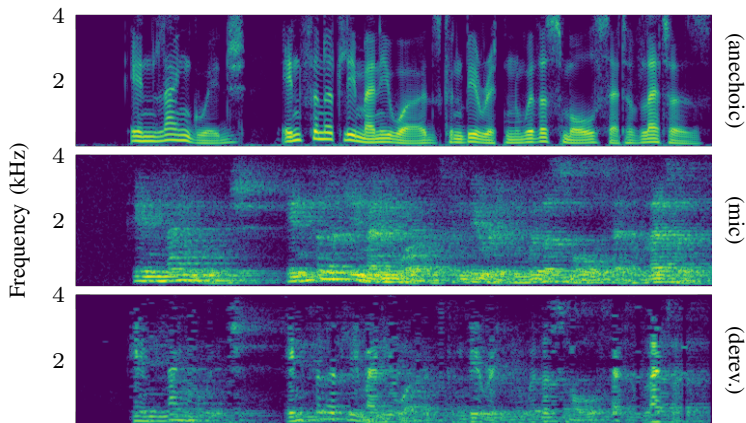
- Similar performances
- Spatio-temporal sparsity slightly worse

▶ DOA estimate

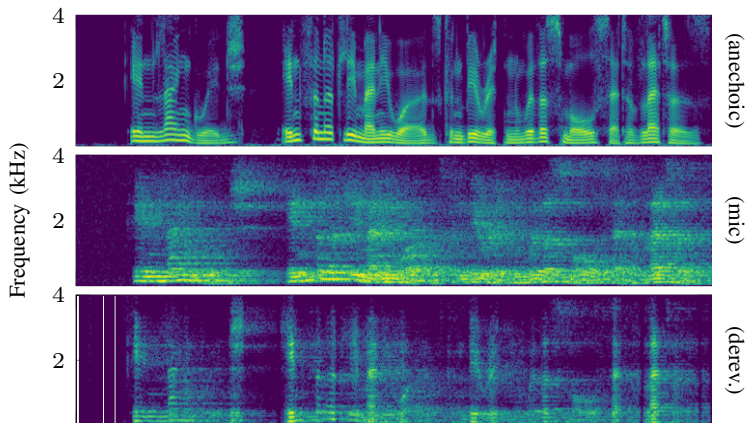
- good performance even with few mics
- minimum angular distance of 4.5° due to finite number of directions

→ more mics, better results

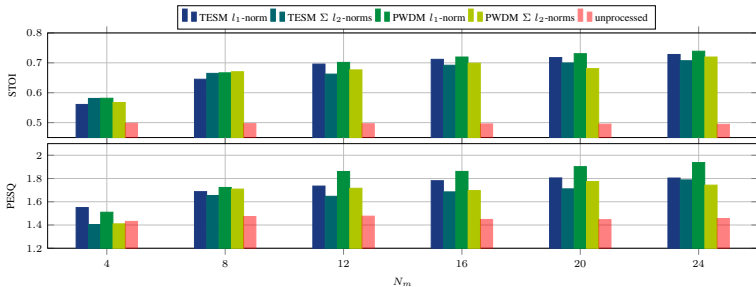




Dereverberation - Spatial sparsity sparsity $N_m = 16$



Objective measures



- ▶ Speech intelligibility (STOI) & Speech Quality (PESQ) scores
- ▶ In line with interpolation error and DOA estimates
- ▶ Better performance with spatio-spectral sparsity
- ▶ Informal listening test: worse results are with spatio-temporal sparsity
- ▶ Sound samples

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- ▶ Novel method for joint source localization and dereverberation
 - Inverse problem rely on acoustic model and sparse prior
 - ▶ Spatio-temporal sparsity (TESM + l_1 -norm)
 - ▶ Spatio-spectral sparsity (PWDM + l_1 -norm)
 - ▶ Spatial sparsity (Σl_2 -norm)
 - Solve with accelerated PG algorithm & WOLA procedure
- ▶ Simulation results
 - good DOA estimates with few mics
 - Better dereverberation as more mics are used