





## **DOA Estimation Using Amateur Drones Harmonic Acoustic Signals**

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## Abstract

In this paper, we consider the problem of the direction-of-arrival (DOA) estimation of amateur drones.

- We formulate the acoustic signals of amateur drones by a harmonic model;
- We improve MUSIC algorithm under the harmonic model to estimate the DOAs of amateur drones;
- We conduct a real-life drone tracking platform integrating the algorithm to track amateur drones.

## **Security Threats About Amateur Drones Intrusions**



Drone crash-landed in front of the



Drone landed on the roof of the



Drone crashed on the South Lawn



Drone flew in the vicinity of

German Chancellor in Sept. 2013.

Japanese Prime Minister's office in April 2015.

-50

-100

150

-60

-100

-120

of the White House in Jan. 2015.

Hangzhou International Airport in Jan. 2017.

## Harmonic Model Formulation of Drone Acoustic Signals

**Time-frequency** 



### Model acoustic signals as the sum of harmonics

$$x_m(k) = \sum_{p=1}^{P} \sum_{i=1}^{N} d_{ip}(k) \gamma_i^k \kappa_{ip}^{m-1} + v_{mp}(k)$$

 $\chi_m$ : The received signal of m-th sensor

 $d_{ip}$ : The Fourier coefficient of p-th drone associated with i-th harmonic  $\gamma_i = e^{j2\pi f_i}, \kappa_{ip} = e^{-j2\pi f_i\Delta\sin\theta_p/c}$ 

 $f_i$ : The frequency corresponding to i-th harmonic of p-th drone

P: The number of amateur drone N: The number of harmonics

 $v_{mp}$ : Spatially and temporally white Gaussian noise

### In a vector form

x(k) = As(k) + v(k)

### **DOA estimation problem of drones is formulated**

Given K snapshots of data vector x(k), estimate  $\theta_p$  for p = 1, ..., P.

# **DOA Estimation By Using MUSIC Algorithm Under Harmonic Model**

**Theorem:** A and  $U_{M\times Q}$  are orthogonal as  $a_i^H(\theta)U_{M\times Q} = 0$ , where  $a_i$  is the j-th column of A,  $U_{M \times Q}$  is the eigenvectors associated with Q = M - NP smallest eigenvalues of  $R(k) = E[x(k)x^H(k)]$ , and j = 1, ..., NP.

Search the peaks in the following cost function

$$P(\theta) = \frac{1}{\sum_{j=1}^{N} a_j^H(\theta) U_{M \times Q} U_{M \times Q}^H a_j(\theta)}$$

## **Real-life Drone DOA Tracking Experiments**







#### **DOA estimation results when DJI**









#### **Acoustic sensor**

