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# BEM-based UKF Channel Estimation for 5G-enabled V2V Channel

Xuanfan Shen<sup>1</sup>, Yong Liao<sup>1</sup> and Xuewu Dai<sup>2</sup>

1 Chongqing University, Chongqing, China

2 Northumbria University, Newcastle upon Tyne, United Kingdom

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# PART ONE

# Background

# Background



## High-Speed Environment

### Doubly-selective channel:

- Multipath effects
- Doppler effects

### Challenge:

Time and frequency selective fading

### Solution:

Time domain channel estimation method

### Non-stationary channel:

- The Channel Impulse Response (CIR) is changing during an OFDM symbol
- Time correlation coefficients are time-varying

### Solution:

Joint estimating the CIR and time correlation coefficients



# Background

## BEM

The Basis Expansion Model (**BEM**) is used to compresses the CIR into a low-dimensional space based on a series of base vectors, which effectively **reduce the space complexity** of time domain channel estimation.

## UKF

The Unscented Kalman Filter (**UKF**) is a more effective state estimation method for non-linear state space model. For certain systems, the resulting UKF filter **more accurately** estimates the true mean and covariance.





# PART TWO

# System Model

# System Model



## Frame Structure and pilot pattern

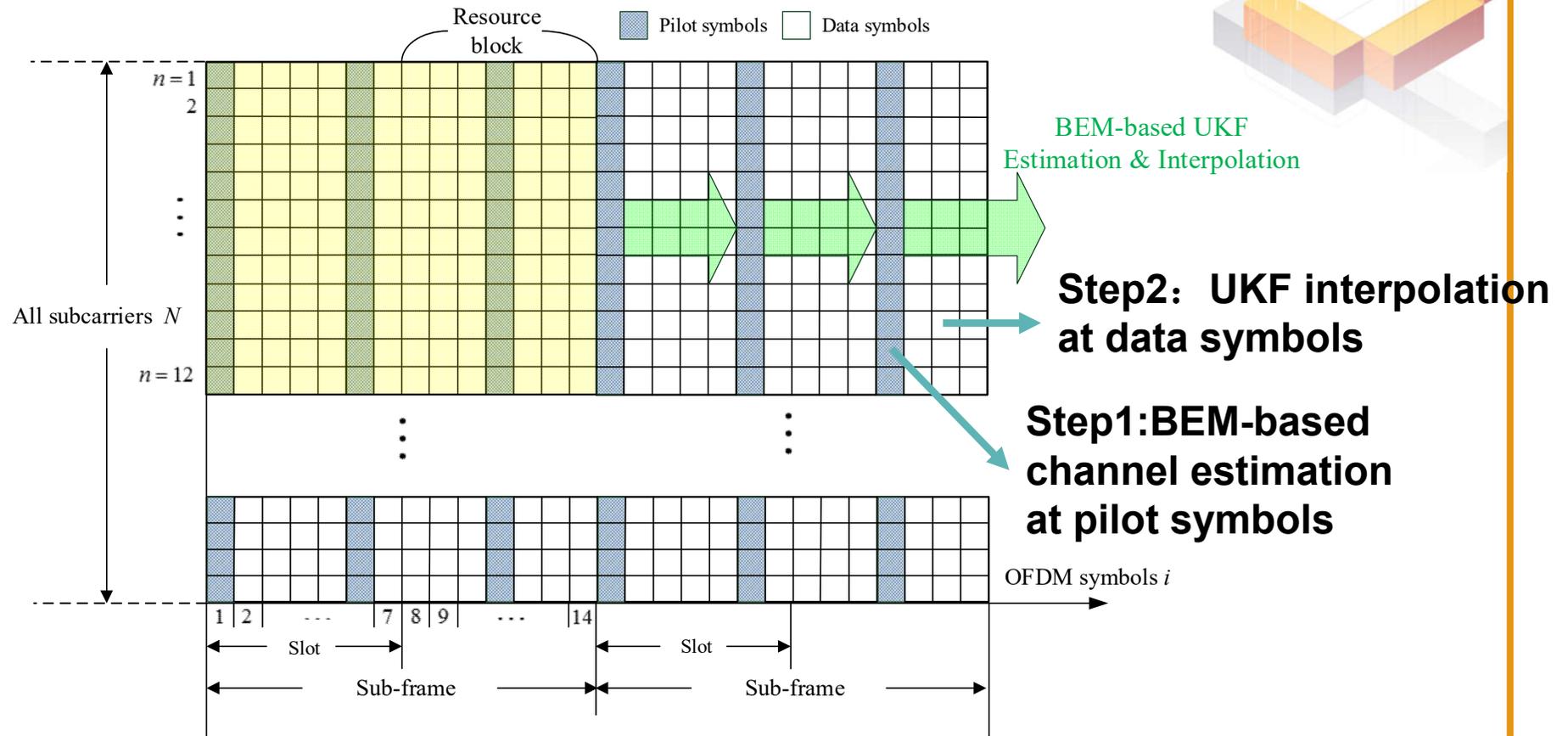


Fig. 1 Frame structure and pilot pattern.



# System Model



## BEM Channel Model:

The CIR matrix:  $\mathbf{g}_i = \begin{bmatrix} h_i(0,0) & 0 & \dots & h_i(0,L-1) & \dots & h_i(0,1) \\ h_i(1,1) & h_i(1,0) & 0 & \dots & \dots & h_i(1,2) \\ \vdots & \ddots & \ddots & \ddots & \ddots & \vdots \\ 0 & \dots & 0 & h_i(N-1,L-1) & \dots & h_i(N-1,0) \end{bmatrix}$



The N-1 th CIR sample point whose delay is L-1 on i th OFDM symbol

$$h_i(k,l) = \sum_{q=0}^{Q-1} b_{k,q} c_{i,l}^q = \mathbf{b}_k^T \mathbf{c}_{i,l}$$

The base vectors of BEM  
(the Complex Exponential  
BEM is used)

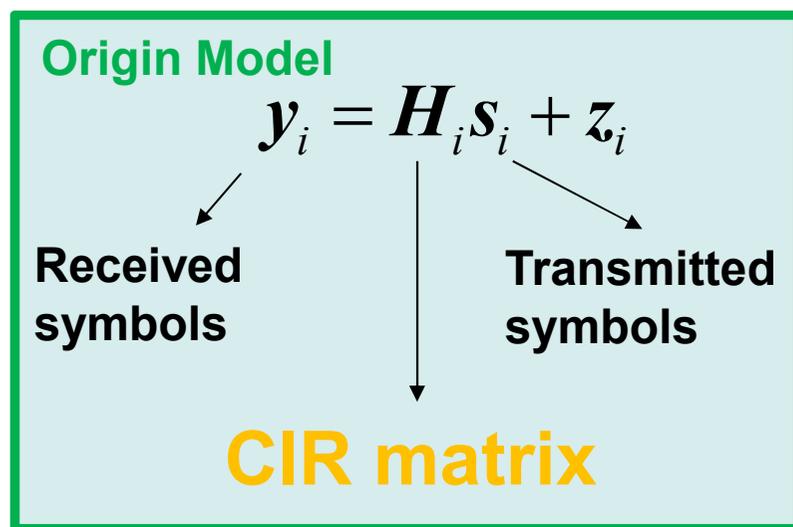
The coefficients of BEM  
(The state of channel)

$$\mathbf{h}_i = \left[ \mathbf{h}_{i,0}^T, \dots, \mathbf{h}_{i,L-1}^T \right]^T = \mathbf{B} \mathbf{c}_i$$

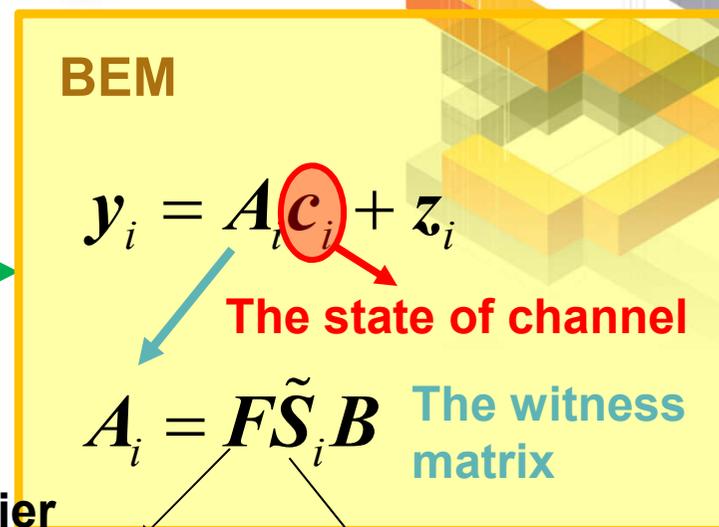
The base matrix  $\mathbf{B}$  is constant, so the CIR could be described by  $\mathbf{c}_i$ .



# System Model



**BEM**



The Fourier transforming matrix  $F$

Cyclic form of transmitted sequence  $\tilde{S}_i$

**TV-AR (time-varying auto regression) Channel Model:**

$$c_{i+1} = R_i c_i + v_i$$

where  $R_i$  is the correlation matrix of coefficients of BEM for adjacent OFDM symbols,  $v_i$  is the process noise with variance  $\sigma_v^2$ . And the correlation matrix is a diagonal matrix under CE-BEM.





# PART THREE

# BEM-based UKF



# BEM-based UKF

## Non-linear state space model

System model with BEM:

$$y_i = A_i c_i + z_i$$

TV-AR model:

$$c_{i+1} = R_i c_i + v_i$$

State space model:

$$\begin{cases} r_{i+1} = r_i + w_i \\ c_{i+1} = R_i c_i + v_i \\ y_i = A_i c_i + z_i \end{cases}$$

AR Model

$$r_i = \text{vec}(R_i)$$

Time-varying correlation matrix

Redefine the state variable

$$x_i = \begin{bmatrix} r_i & c_i \end{bmatrix}^T$$

Non-linear state space model:

$$\begin{cases} x_{i+1} = f(x_i) + u_i \\ y_i = \begin{bmatrix} 0 & A_i \end{bmatrix} x_i + z_i \end{cases}$$

$$f(x_i) = \begin{bmatrix} r_i \\ R_i c_i \end{bmatrix} = \begin{bmatrix} r_i \\ \text{diag}(r_i) c_i \end{bmatrix}$$



# BEM-based UKF



## State Prediction

1. **Generating sigma points.**
2. **Substituting the sigma points into the transformation equation.**
3. **Calculating the means of the *a priori* state variable and covariance matrix.**

## State Updating

1. **Generating sigma points.**
2. **Substituting.**
3. **Calculating the mean, covariance matrix and cross covariance matrix of measurement variable.**
4. **Computing the gain of fileting and the a posterior estimates and covariance matrix of state variable.**





# PART FOUR

# Simulation and Analysis

# Simulation Parameters



Table 1 Parameters of Simulation System

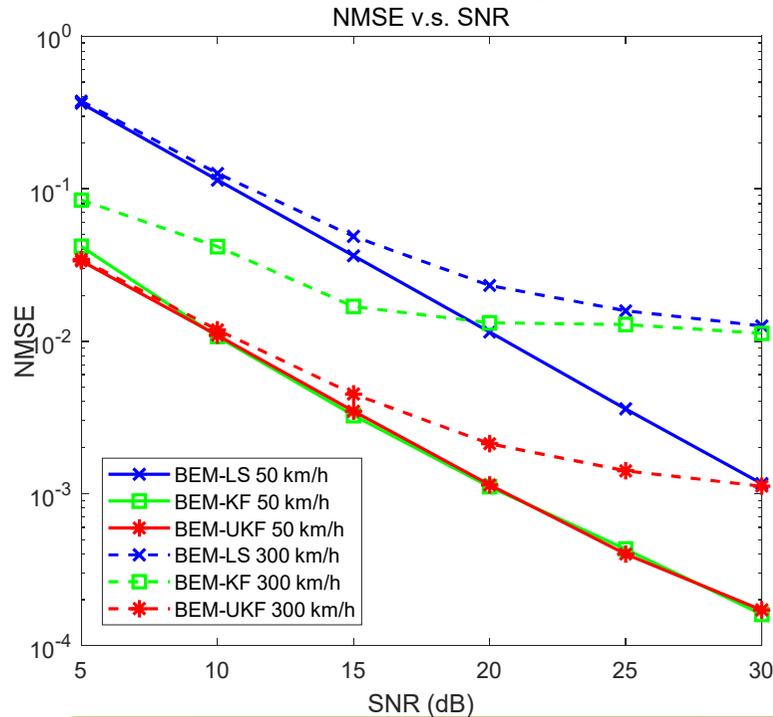
Parameters	Value
Frequency of carrier	2.8 GHz
Bandwidth	5 MHz
Number of subcarriers	300
Length of FFT	512
Length of CP	36
Dimension of base vectors $Q$	16
Modulation	QPSK
Non-stationary channel	WINNER-II D2a



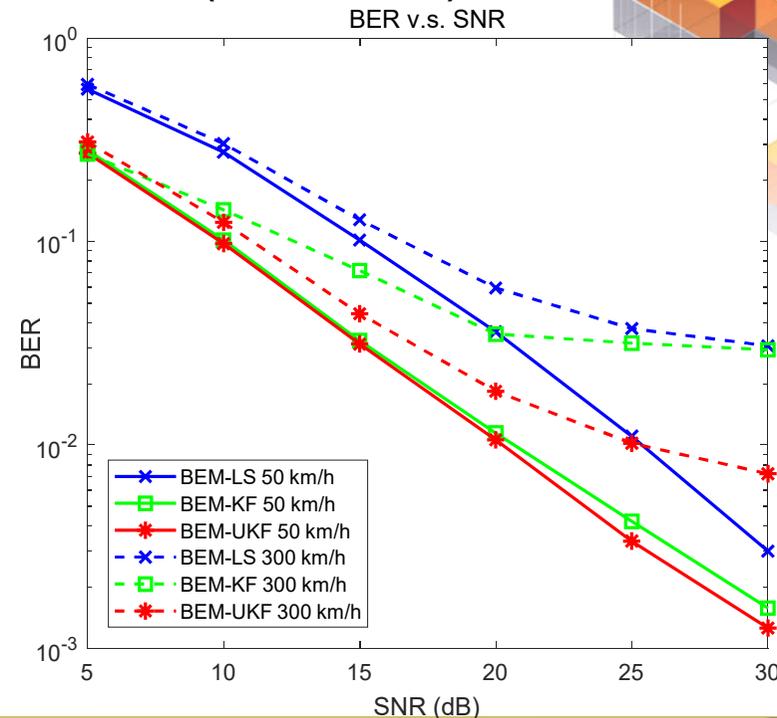
# Simulation



## NMSE(normalized mean squared error)

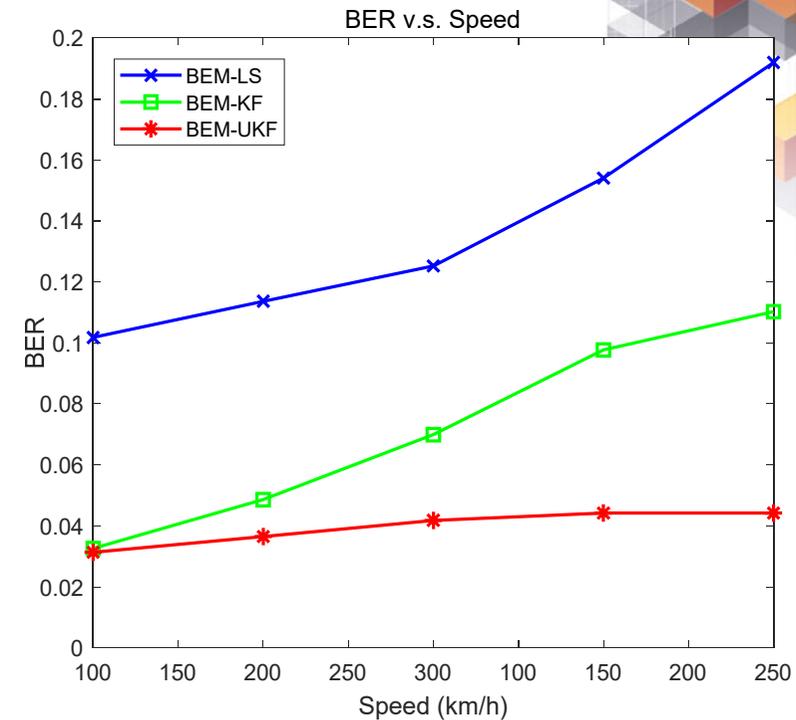
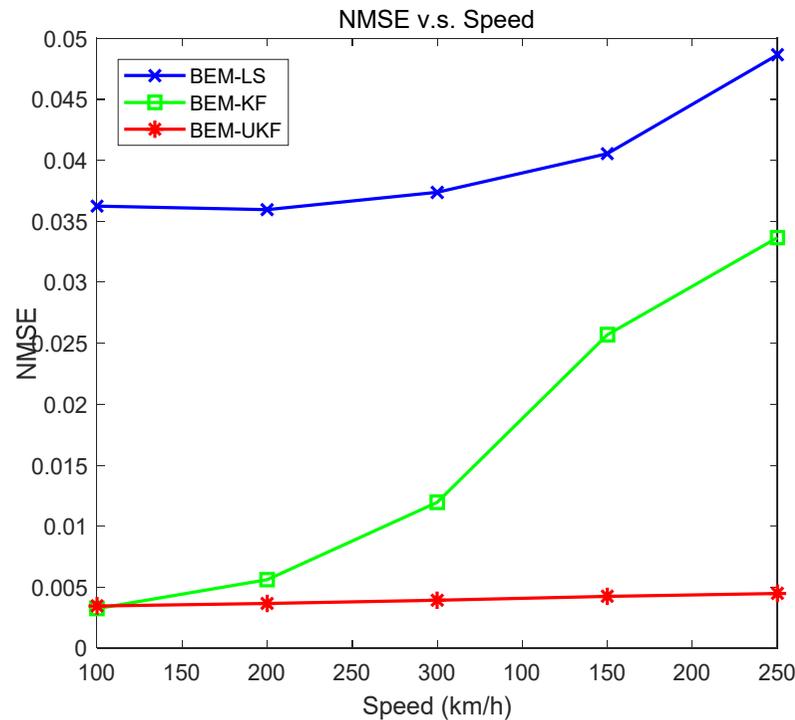
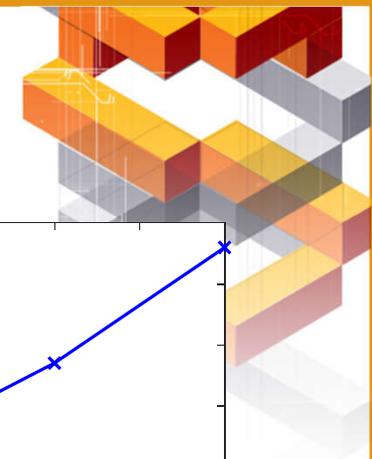


## BER(bit error rate)



- (1) Obviously, the BER and NMSE performances of BEM-UKF is better than other two traditional methods, namely, BEM-LS (Least Square), and BEM-KF (Kalman Filter)
- (2) Performance improvement is more significant in the high speed environments.

# Simulation Velocity



The lines of BEM-UKF are flat in two graphs, the NMSE and BER performances of BEM-UKF are rarely influenced by the increasing velocity. It is obvious that the robustness of BEM-UKF is stronger than BEM-LS and BEM-KF.





# Conclusion & Future work

# Conclusion



- The BEM is adopted to reduce the complexity of channel estimation and eliminate the ICI (inter-carrier interference).
- An UKF-based method is proposed to jointly estimate CIR and time-varying time correlation coefficients in a non-linear state space model.
- The performances of proposed BEM-based UKF channel estimation and interpolation method in different speed environments is analyzed.



# Future work



- **Attempt to apply Artificial Intelligence (AI) to channel estimation in high-speed mobile environment.**
- **Research Channel estimation based on superimposed pilot and data symbols.**





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A large, complex 3D geometric graphic on the left side of the slide. It consists of numerous rectangular blocks in shades of orange, yellow, and red, arranged in a staggered, isometric pattern. A circular button with an orange arrow pointing right is overlaid on one of the blocks.

**Thank You !**