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Overview

# The Concept

Semi-Supervised Classification model using Selective Pixel Removal and APGL Inpainting.

- **1** Hand-Select/work with pre-known endmembers.
- 2 Using a PCA scheme, remove parts of pixels that are not within a threshold distance of an endmember.
- **3** Using APGL and a modified APGL algorithm for matrix completion, reconstruct the hyperspectral image
- Classification can now be done for each pixel using the direct Euclidean distance from the endmembers

# **PCA** Initialization

- Order the pixels (rows) based on distance to nearest endmember.
- 2 Order bands (columns) of each pixel pseudo-randomly based on top PCA bands.



### **PCA** Initialization

**2** Top 20% is kept as index set.



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**3** Lower [x]% is cut (adjustable to dataset).



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-PCA Initialization

# PCA Initialization-Band by Band





PCA Initialization

### PCA Initialization-Band by Band





PCA Initialization

# PCA Initialization-Band by Band





# APGL: Original Algorithm

The APGL (Accelerated Proximal Gradient with Linesearch) algorithm minimizes a problem of the form:

$$\arg \min_{X} \quad \frac{1}{2} ||\mathcal{A}(X) - b||_{2}^{2} + \mu ||X||_{*}$$

- A is a linear operator that can be thought of as the index set from X, the original image that we're trying to reconstruct, to b, the partial image that we observe.
- 3 Minimizing the rank of X corresponds to the stipulation that each pixel is the linear combination of a small set of endmembers.

# APGL-Hyp Algorithm

- Add a penalization term for distance of inpainted pixels from endmembers.
- **2** Instead of minimizing:

$$\arg\min_{X} \frac{1}{2} ||\mathcal{A}(X) - b||_{2}^{2} + \mu ||X||_{*}$$

we minimize

$$\arg\min_{X} \quad \frac{1}{2} ||\mathcal{A}(X) - b||_{2}^{2} + \mu ||X||_{*} + \frac{\lambda}{2} ||X - CX||_{F}^{2}$$

where "CX" is a projection of each pixel onto the nearest endmember.

# APGL Algorithm: Proximal Gradient Method

Solve a minimization problem of the form:

$$F(X) = f(X) + P(X)$$

- P is proper, convex, lower, semicontinuous: ||X||<sub>\*</sub> is an acceptable P.
- f is convex, smooth, and continuously differentiable on domP
- Use iterative interpolation:

$$\begin{cases} X^k = S_{\tau^k}(G^k) \\ G^{k+1} = X^k - (\tau^k)^{-1} \mathcal{A}^*(\mathcal{A}(X^k) - b) \end{cases}$$

# APGL Hyperspectral Algorithm

#### APGL\_Hyp Algorithm

- 1. Let  $\mu > 0$  be a fixed regularization parameter, let  $\eta \in (0,1)$  be a given constant. Let  $X^0 = X^1 = 0 \in \mathbb{R}^{m \times n}$ , let  $t^0 = t^{-1} = 1$  and let  $\tau^0 = 1 + \lambda$ .
- Repeat the following loop until convergence: for k = 0, 1, 2, ..., generate X<sup>k+1</sup> according to the following iteration:
  - (a) Set  $Y^k = X^k + \frac{t^{k-1}-1}{t^k}(X^k X^{k-1})$
  - (b) Calculate  $CX^{k-1}$ .
  - (c) Set  $\widehat{\tau}_0 = \eta \tau^{k-1}$
  - (d) For j=0, 1, 2, ...
    - Set  $G = Y^k (\hat{r}_j)A^*(\mathcal{A}(Y^k) b) + \lambda(X^k CX^{k-1}).$ Compute  $S_{\hat{r}_j}(G) = U\text{Diag}(\sigma - \mu/\hat{r}_j)_+V^T$ If  $F(S_{\hat{r}_j}(G)) \leq Q_{\hat{r}_j}(S_{\hat{r}_j}(G)),$ Set  $\tau^k = \hat{r}_c$ , break
      - Else,

Set  $\widehat{\tau}_{i+1} = \min\{\eta^{-1}\widehat{\tau}_i, \tau^0\}$ 

end

end

(f) Set 
$$t^{k+1} = \frac{1+\sqrt{1+4(t^k)^2}}{2}$$
.

Data-Sharpening Effects

## Datasets

### 1 Kiwi Dataset

- Close-up on a kiwi fruit, taken using a Specim AISA Hyperspectral Sensor.
- original image 848 bands of wavelengths between 391.52 and 1007.37 nm taken from 0.7 to 0.76 nanometers apart, we worked with bands 250 to 449
- 250 × 351 × 200
- 2 Chemical Plume Dataset
  - Chemical plume imaged from long wave infrared spectrometers placed 2km away by the John Hopkins University Applied Physics Laboratory
  - 128 × 320 × 129
- 3 Salinas-A Dataset
  - subscene of the Salinas dataset, taken by the AVIRIS sensor over Salinas Valley
  - 86 × 83 × 204

Data-Sharpening Effects

# **Pixel-Smoothing**



Pictured above: comparison of a pixel from the Kiwi Dataset with the same pixel from the APGL and APGL-Hyp sharpened datacube.

Data-Sharpening Effects

### Band-by-Band Sharpening



#### APGL Inpainted



#### APGL\_Hyp Inpainted



Classification Results

Salinas-A Dataset

### Salinas-A Dataset







APGL\_Hyp

80



Classification Results

└─ Salinas-A Dataset

### Salinas-A Dataset

Algorithm	Time	Accuracy
K-Means	1.04	69.52 %
H2NMF	2.41	70.08 %
NLTV	53.83	80.42 %
APGL	29.98	76.93 %
$APGL_Hyp$	65.95	69.60 %

Classification Results

└─ Salinas-A Dataset

### Salinas-A Dataset: 10 % Pixels Replaced





APGL

APGL\_Hyp

80



Classification Results

└─ Salinas-A Dataset

## Salinas-A Dataset: 10% Pixels Replaced

Algorithm	Time	Prior Accuracy	Accuracy 10% Replaced
K-Means	4.60	69.55%	50.90%
H2NMF	1.75	70.08 %	58.36%
NLTV	54.23	80.42%	71.02%
APGL	33.57	76.93 %	76.78 %
APGL_Hyp	77.73	69.60%	72.57%

Classification Results

└─Kiwi Dataset

### Kiwi Dataset













Classification Results

└─Kiwi Dataset

### Kiwi Dataset

Algorithm	Time	Accuracy
K-Means	9.5964	64.14%
H2NMF	7.2750	58.72%
NLTV	251.1266	77.54%
APGL	220.3274	85.63%
APGL_Hyp	416.0232	86.63%

Classification Results

└─Kiwi Dataset

# Kiwi Dataset: 10% Pixels Replaced













Classification Results

└─Kiwi Dataset

### Kiwi Dataset: 10% Pixels Replaced

Algorithm	Time	Prior Accuracy	Accuracy 10% Replaced
K-Means	10.0953	64.14%	53.07%
H2NMF	8.0856	58.72%	45.14%
NLTV	279.1046	77.54%	52.24%
APGL	206.0447	85.63%	79.78%
APGL_Hyp	572.2304	86.63%	79.30%

- Classification Results
  - Chemical Plume Dataset

### **Chemical Plume Dataset**















Classification Results

Chemical Plume Dataset

### Chemical Plume Dataset

Algorithm	Time	Accuracy
K-Means	2.4594	81.44%
H2NMF	1.9909	63.42%
NLTV	92.4825	66.21%
APGL	27.6438	87.44%
APGL_Hyp	49.1695	87.24%

Classification Results

Chemical Plume Dataset

## Chemical Plume Dataset: 10 % Pixels Replaced





Classification Results

Chemical Plume Dataset

### Chemical Plume Dataset: 10% Pixels Replaced

Algorithm	Time	Prior Accuracy	Accuracy 10% Replaced
K-Means	N/A	81.44%	N/A
H2NMF	2.2981	63.42%	36.23%
NLTV	99.6240	66.21%	66.53%
APGL	44.1697	87.44%	85.43%
APGL_Hyp	49.1466	87.24%	85.29%

Classification Results

Additional Effects

### Full Pixel Removal







APGL Hyp,25% Full Pixels Removed



APGL Hyp,30% Full Pixels Removed



APGL Hyp,35% Full Pixels Removed



Classification Results

Additional Effects

### Full Pixel Removal



300

300

300

300

Classification Results

Additional Effects

### Full Pixel Removal



Classification Results

Additional Effects

### Full Pixel Removal

Percent Pixel Removal	Accuracy: APGL	Accuracy: APGL_Hyp
10%	85.99%	85.83%
20%	85.31%	85.36%
30%	81.85%	83.45%
40%	71.08%	81.77%
50%	60.66%	69.80%
60%	50.66%	63.42%
70%	48.61%	51.95%
80%	43.94%	44.36%



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