



## Introduction

- Eyes represent the most distinctive features of the human face, while their position and movements are a significant source of information about the cognitive and affective state of humans.
- Precise eye center localization constitutes a challenging problem in many human-computer interaction applications.
- An automatic method is introduced for the precise eye center localization, based on a modified version of the Fast Radial Symmetry Transform<sup>1</sup>.
- Experiments performed in two publicly available face databases, where there is a wide variety of ages, ethnicities, poses, lighting conditions, shadows, presence of occlusions (hair, glasses) and reflections.
- The results demonstrate the superior performance and enhanced accuracy of this technique against the state-of-the-art methods.

## Proposed Method

The proposed method consists of the following steps (Fig. 1):

- Firstly, the face is detected and the two eye Regions Of Interest are selected.
- An edge-preserving filter is applied to enhance the circular shape of the eyes and separate them from the skin.
- Then, a modified Radial Symmetry Transform (RST)<sup>1</sup> is used to localize the eye centers. Specifically, its magnitude component results from the red color component of the original image while its orientation component from a properly filtered version of the original one. Finally, the superposition of their normalized counterparts denotes the position of the eyes centers.

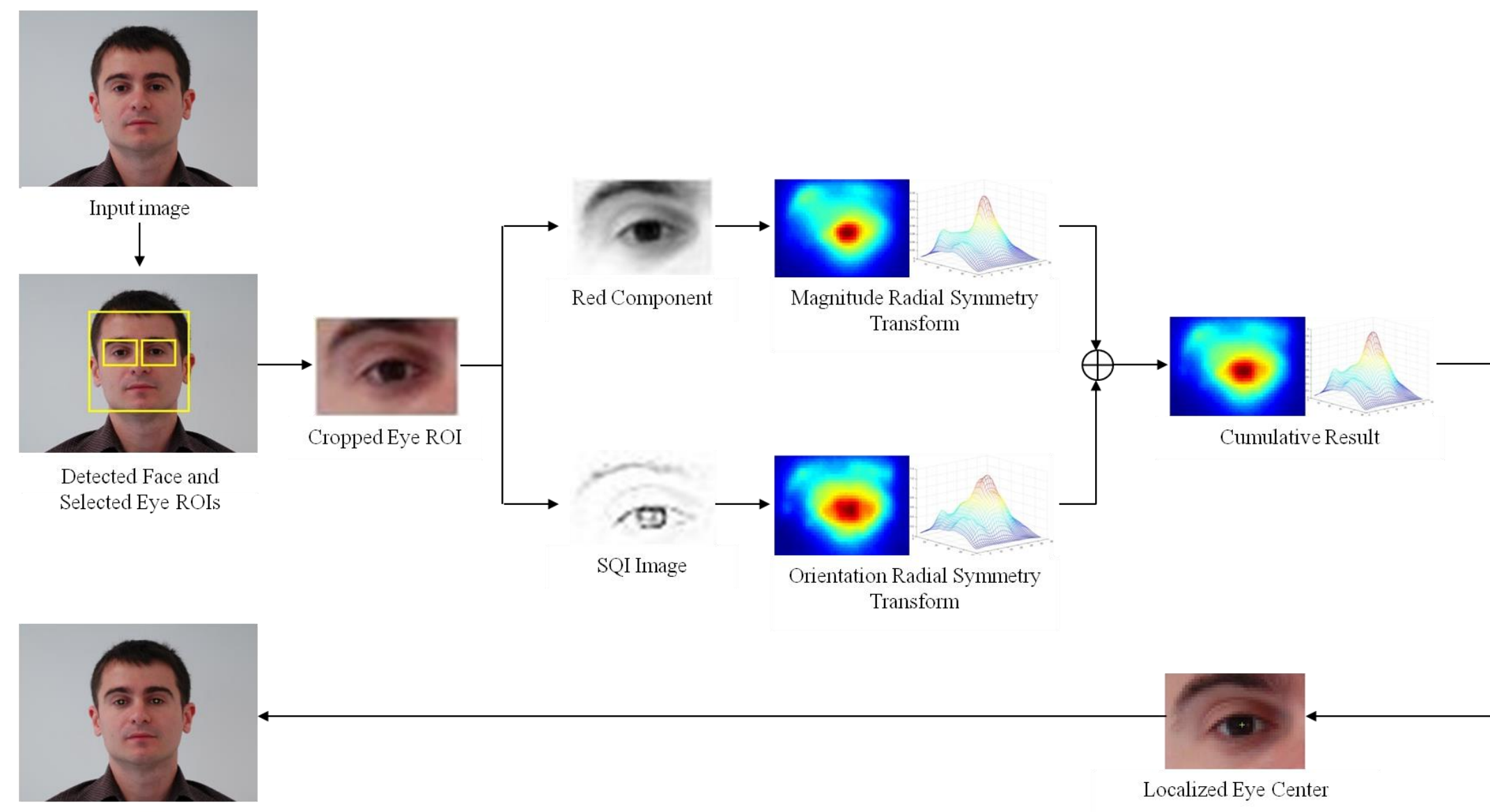


Fig. 1: Overview of the stages of the proposed system.

## Edge Preserving Filtering

### Self-Quotient Image (SQI)

- Observation:** Illumination is considered as one of the main limitations in the eye localization problem.
- Goal:** SQI aims to construct a lighting invariant representation of the image which can effectively removes the shadow for any type of lighting sources.
- Proposal:** The use of the SQI that is defined as the ratio of the input image and its smoothed version, i.e.:

$$Q(x) = \frac{I(x)}{I_\sigma(x)}, \quad \text{where:} \quad I_\sigma(x) = I(x) * G_\sigma(x)$$

### Denoising Scheme

- Observation:** SQI suffers from noise because of the division operation.
- Goal:** The elimination of this undesirable amplification of the noise.
- Step 1.** A sigmoid correction is applied to the SQI to suppress the noise:

$$T(x) = S(Q(x)), \quad \text{where:} \quad S(x) = \frac{1}{1 + e^{-a(x-x_0)}}$$

- Step 2.** A convolutional Gaussian kernel is used to smooth the image:

$$Q_f(x) = T(x) * G_\sigma(x)$$

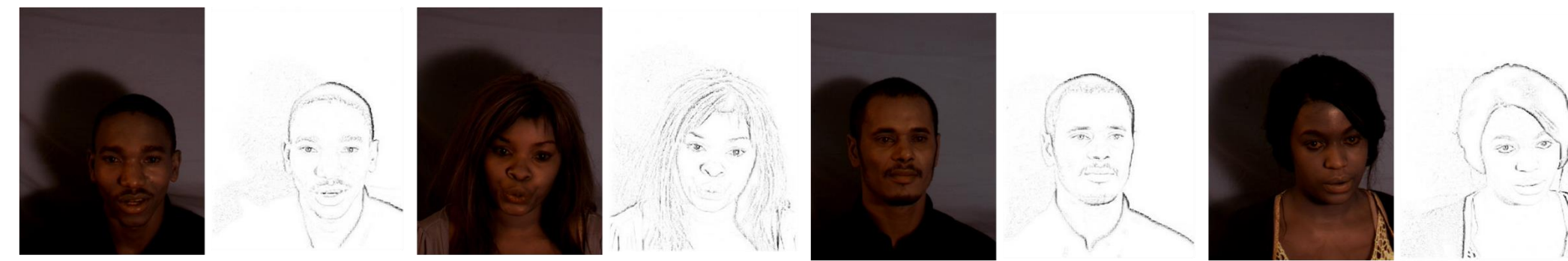


Fig. 2: Face images with strong illumination distortions and their shadow-free results

## Modified Radial Symmetry Transform

- Observation:** Symmetry constitutes one of the primary properties of the eyes.
- Proposal:** Separation of the RST into two parts and exploit the Red component and the SQI image to precisely detect the eye centers.
- Definition:** The affected pixels are determined based on the gradient direction:

$$P_{affected}(r) = p + \text{round}\left(\frac{\nabla I(p)}{\|\nabla I(p)\|_2} r\right)$$

### Magnitude Radial Symmetry Transform

- Goal:** Exploit the enhanced contrast existing between the eyes and the skin.
- Proposal:** Selection of the Red component only to apply the Magnitude RST.
- Definition:** For each radius, a "Magnitude Projection Image" is constructed:

$$M_r(p_{affected}) = M_r(p_{affected}) + \|\nabla I(p)\|$$

The contribution is convolved with a Gaussian kernel and summed:

$$S_M = \sum_{r \in N} (M_r * G_r)$$

### Orientation Radial Symmetry Transform

- Goal:** Exploit the shadow-free image from the edge-preserving filtering.
- Proposal:** Application to the SQ Image and counting only on the orientation of the gradient to distinguish the eye shape.
- Definition:** For each radius an "Orientation Projection Image" is constructed:

$$O_r(p_{affected}) = O_r(p_{affected}) + 1$$

The contribution is convolved with a Gaussian kernel and summed:

$$S_O = \sum_{r \in N} (O_r * G_r)$$

### The optimization problem

- The location of the eye centers results from the solution of the problem:

$$p^* = \arg \max_p (S_{M,norm} + S_{O,norm})$$

## Parameters Specification

- Selection of the set of radii:** It is selected based on the expected iris size in relation to the face dimensions:

$$r_{min} = \max\left\{\frac{FaceWidth}{60}, 3\right\}, \quad r_{max} = \frac{FaceWidth}{6}$$

## Experimental Setup

- The performance of the proposed method is evaluated in two publicly available face databases: **MUCT** (3755 color images, **BioID** (1521 gray-scale images).
- Definition:** The normalized error, quantifying the worst eye estimation:

$$e = \frac{\max(\|\tilde{C}_L - C_L\|_2, \|\tilde{C}_R - C_R\|_2)}{\|C_L - C_R\|_2}$$

## Experimental Results

- The proposed method achieves high accuracy and robustness in localizing the eye centers (Fig. 3).
- This method deals successfully under the most challenging circumstances, including shadows, pose variations, occlusions by hair or strong reflections, out-of-plane rotations, and presence of glasses (Fig. 3).
- The contents of the Tables 1, 2 provide supporting evidence of the superior performance of the proposed method.
- Points with  $e \leq 0.25$  belong to a disk with its center located to the eye center and its periphery to the eye corner, points with  $e \leq 0.1$  belong to the disk of the iris while points with  $e \leq 0.05$  belong to the pupil area.

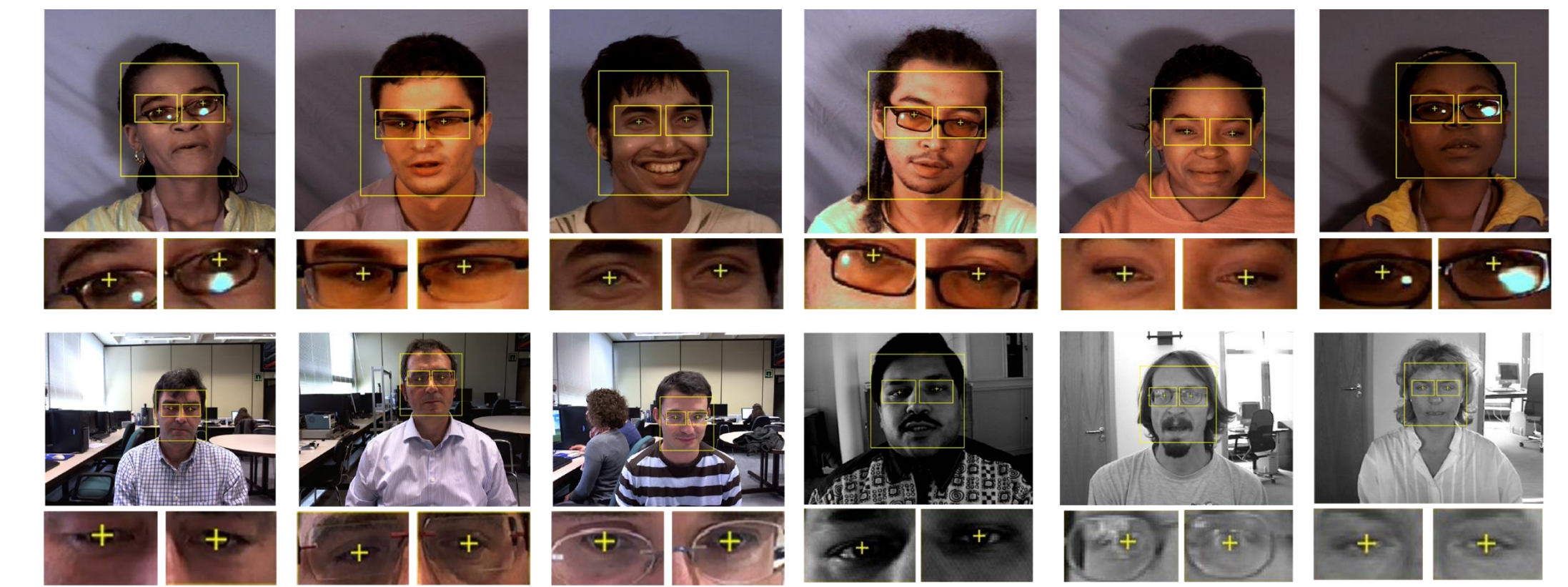


Fig. 3: Our method localizes precisely the eye centers under challenging conditions

Method	Accuracy (%)			Method	Accuracy (%)		
	e≤0.05	e≤0.1	e≤0.25		e≤0.05	e≤0.1	e≤0.25
<b>Proposed</b>	<b>94.43</b>	<b>98.53</b>	<b>99.62</b>	<b>Proposed</b>	<b>87.10</b>	<b>98.00</b>	<b>100</b>
Skodras <sup>3</sup>	92.9	97.2	99.0	Valenti <sup>6</sup>	86.1	91.67	97.87
Timm <sup>4</sup>	78.6	94.9	98.6	Timm <sup>4</sup>	82.5	93.4	98.0
Yang <sup>5</sup>	81.6	89.5	94.5	Leo <sup>7</sup>	80.7	87.3	94.0
Valenti <sup>6</sup>	63.1	76.7	94.1	Cristinacce <sup>8</sup>	57.0	96.0	97.1

Table 1: Accuracy vs normalized error in MUCT Table 2: Accuracy vs normalized error in BioID

## Conclusions

- A new, fully automatic, non-intrusive eye center localization method is proposed, based on a modified version of Radial Symmetry Transform.
- The proposed technique combines simplicity with high precision to provide accurate localization under the most challenging circumstances.
- This method was tested among the most challenging face databases and outperformed in accuracy the compared state-of-the-art techniques.

## References

- G. Loy and A. Zelinsky, "Fast radial symmetry for detecting points of interest," IEEE Transactions on Pattern Analysis and Machine Intelligence, vol. 25, pp. 959973, August 2003.
- P. Viola and M. Jones, "Robust real-time face detection," Int. Journal on Computer Vision, vol. 57, pp. 137–154, February 2004.
- Skodras E. and N. Fakotakis, "Precise localization of eye centers in low resolution color images," Image and Vision Computing Journal, Elsevier, 2015.
- F. Timm and E. Barth, "Accurate eye centre localization by means of gradients," in VISAPP, 2011, pp. 125–130.
- P. Yang, B. Du, S. Shan, and W. Gao, "A novel pupil localization method based on gabor eye model and radial symmetry operator," in International Conference on Image Processing (ICIP'04). IEEE, 2004, p. 6770.
- Valenti R. and T. Gevers, "Accurate eye center location through invariant isocentric patterns," IEEE Transactions on Pattern Analysis and Machine Intelligence, vol. 34, pp. 17851798, Sep
- M. Leo, D. Cazzato, T. De Marco, and C. Distante, "Unsupervised eye pupil localization through differential geometry and local self-similarity matching," in In Proceedings of PLOS, 2014.
- D. Cristinacce, T. Cootes, and I. Scott, "A multi-stage approach to facial feature detection," in In Proceedings of BMVC, 2004, p. 277286.