

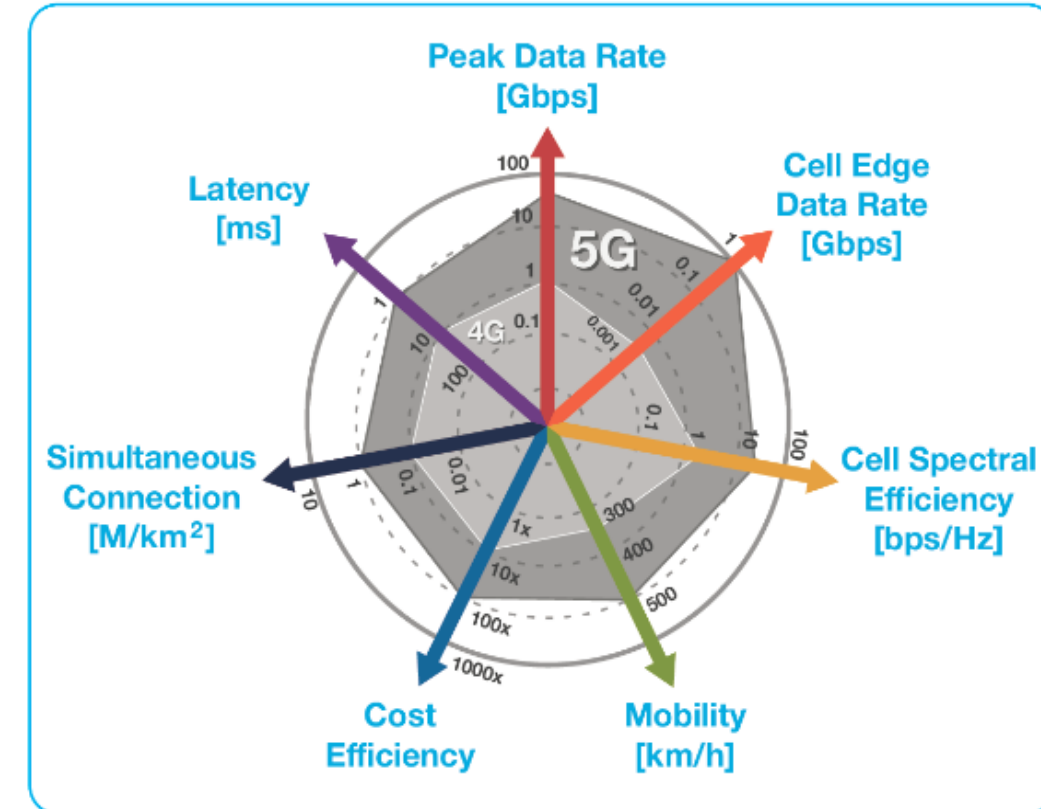
# A PROBABILISTIC INTERFERENCE DISTRIBUTION MODEL ENCOMPASSING CELLULAR LOS AND NLOS MMWAVE PROPAGATION



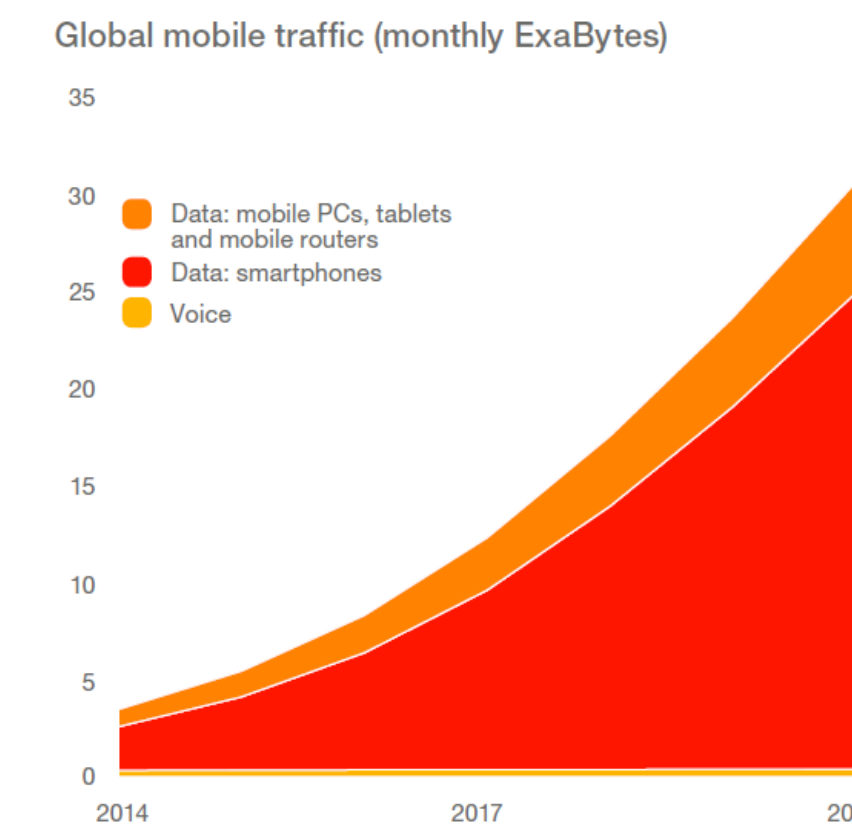
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## Introduction and Motivation



Samsung 5G Rainbow Requirements



Ericsson Mobility Report, 2015

- Scarce spectrum at the microwave band.
- Migration to mmWave (massive increase in bandwidth)
- Smaller cell radii leading to dense network deployments.
- Cellular networks are interference rather than noise limited.

## mmWave Channel Model and Features

- Channel propagation model:

$$\mathbf{H} = \sqrt{l(r)}\tilde{\mathbf{H}}$$

- Small-scale fading: non-parametric or parametric models.
- Probabilistic large-scale fading model

$$l(r) = \mathbb{B}(p(r)) L_l \beta_l r^{-\alpha_l} + (1 - \mathbb{B}(p(r))) L_n \beta_n r^{-\alpha_n}$$

$\mathbb{B}(\cdot)$ : Bernoulli random variable,  $L_i \sim \mathcal{N}(0, \sigma_i) \forall i \in \{l, n\}$

Floating intercept model:  $\beta_i$  floating intercept,  $\alpha_i$  linear slope

Close-in model:  $\beta_i$  is free space path loss  
 $\alpha_i$  is path loss exponent

- The probability that a link of length  $r$  is LOS

$$p(r) = \left[ \min\left(\frac{r_{BP}}{r}, 1\right) \left(1 - e^{-\frac{r}{\alpha}}\right) + e^{-\frac{r}{\alpha}} \right]^2$$

$r_{BP}$ : Breakpoint distance,  $\alpha$ : decay parameter

- Separate measurements/models for LOS and NLOS.

## Cellular Model based on Stochastic Geometry

- A multi-antenna cellular system.
- No intra-cell interference.
- Interferers distributed outside a cell of nominal radius  $R_0$ .
- LOS interferers distributed as a p.p.p.  $\Phi_L$  with intensity  $p(r)\lambda_1$ .
- NLOS interferers distributed as a p.p.p.  $\Phi_N$  with intensity  $(1 - p(r))\lambda_1$ .

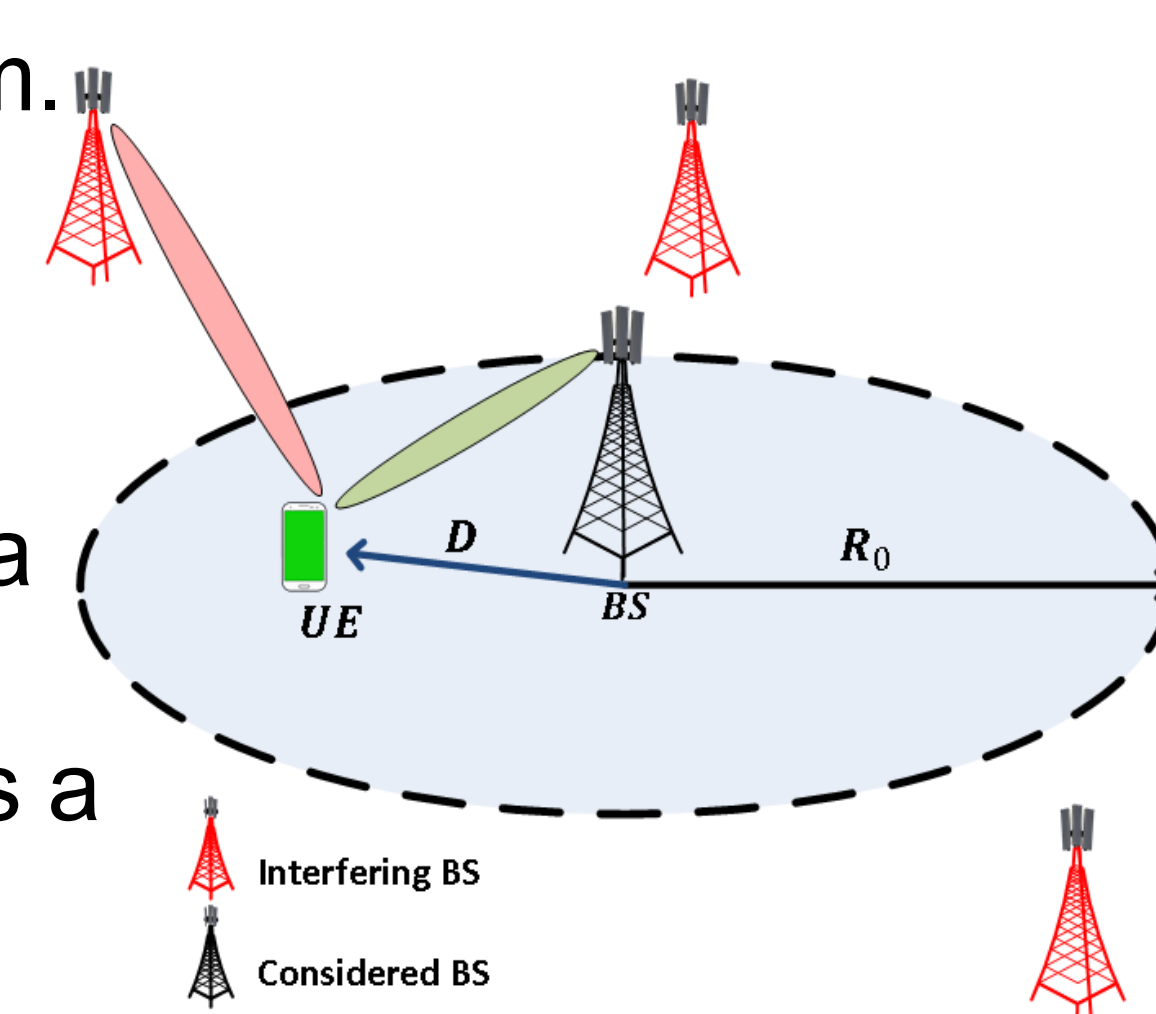


Fig. 1: System Model.

## Interference Modeling

- The interference vector  $\mathbf{v}_0$  at a UE at distance  $D$  from BS:

$$\mathbf{v}_0 = \sum_{z_k} \mathbf{H}_k \mathbf{w}_k x_k = \sum_{z_k} \sqrt{P_k l(\|z_k - \mathbf{t}_0\|_2)} \tilde{\mathbf{h}}_k U_k$$

$\mathbf{w}_k$ : unit-norm beamforming vector independent of  $\mathbf{H}_k$

$x_k = \sqrt{P_k} U_k$  is the transmitted signal with power  $P_k$

$\mathbf{t}_0$ : the 2-D location of the considered UE

- For a fixed fading and spatial realization,  $\mathbf{v}_0$  is  $\mathcal{CN}(\mathbf{0}, \mathbf{Q}_0)$ .
- The covariance matrix  $\mathbf{Q}_0$  is random.
- Diagonal elements  $q_0$  represent interference power.
- Assuming LOS probability independence, we separate the LOS and NLOS interference power modeling

$$q_0 = \sum_{z_k \in \Phi_L} l(\|z_k - \mathbf{t}_0\|_2) g_k P_k + \sum_{z_k \in \Phi_N} l(\|z_k - \mathbf{t}_0\|_2) g_k P_k$$

$g_k$ : the small-scale fading power gain from  $k^{th}$  interferer.

- Analytical expressions available for LOS and NLOS first two moments when the elements of  $\tilde{\mathbf{H}}$  are i.i.d.  $\mathcal{CN}(0,1)$ .

## Interference Power Candidate Distributions

- Consider 2-parameter candidates {Gamma (G), Inverse Gaussian (IG), and Inverse Weibull (IW)}.
- Characterized by shape and scale parameters.
- Few parameters to estimate.

## LOS Model as a Mixed Distribution

- The probability  $p(r)$  is a decreasing function of  $r$ .
- Only interferers in a limited area contribute to LOS part.
- Consider probability density function (PDF) as

$$\gamma_G(D) = \begin{cases} 0 & \text{with probability } p_0(D) \\ \tilde{\gamma}_G(D) & \text{with probability } 1 - p_0(D) \end{cases}$$

$p_0(D)$ : probability that LOS interference power is 0.

$\tilde{\gamma}_G(D)$ : Gamma distributed random variable

## NLOS Model as a Mixture Distribution

- The increasing function  $1 - p(r)$  suggests very low probability of NLOS interference power components around 0.
- Consider as a weighted mixture of IG and IW distributions.

$$f_Y(y|\theta) = w_1 f_{Y_{IG}}(y|\lambda) + w_2 f_{Y_{IW}}(y|c)$$

- After moment matching, only 3 parameters to estimate:
  - The distribution mixing weight, and
  - Shape parameter in each individual distribution.

## Models Parameters Estimation Approaches:

- Gamma moment matching (MM):
  - Match the first two moments analytically.
- Gamma Maximum Likelihood Estimation (MLE):
- Mixture distribution MLE:
  - Match the first moment, then develop an Expectation Maximization algorithm to estimate the parameters.

## Interference Models Evaluation

Visual verification:

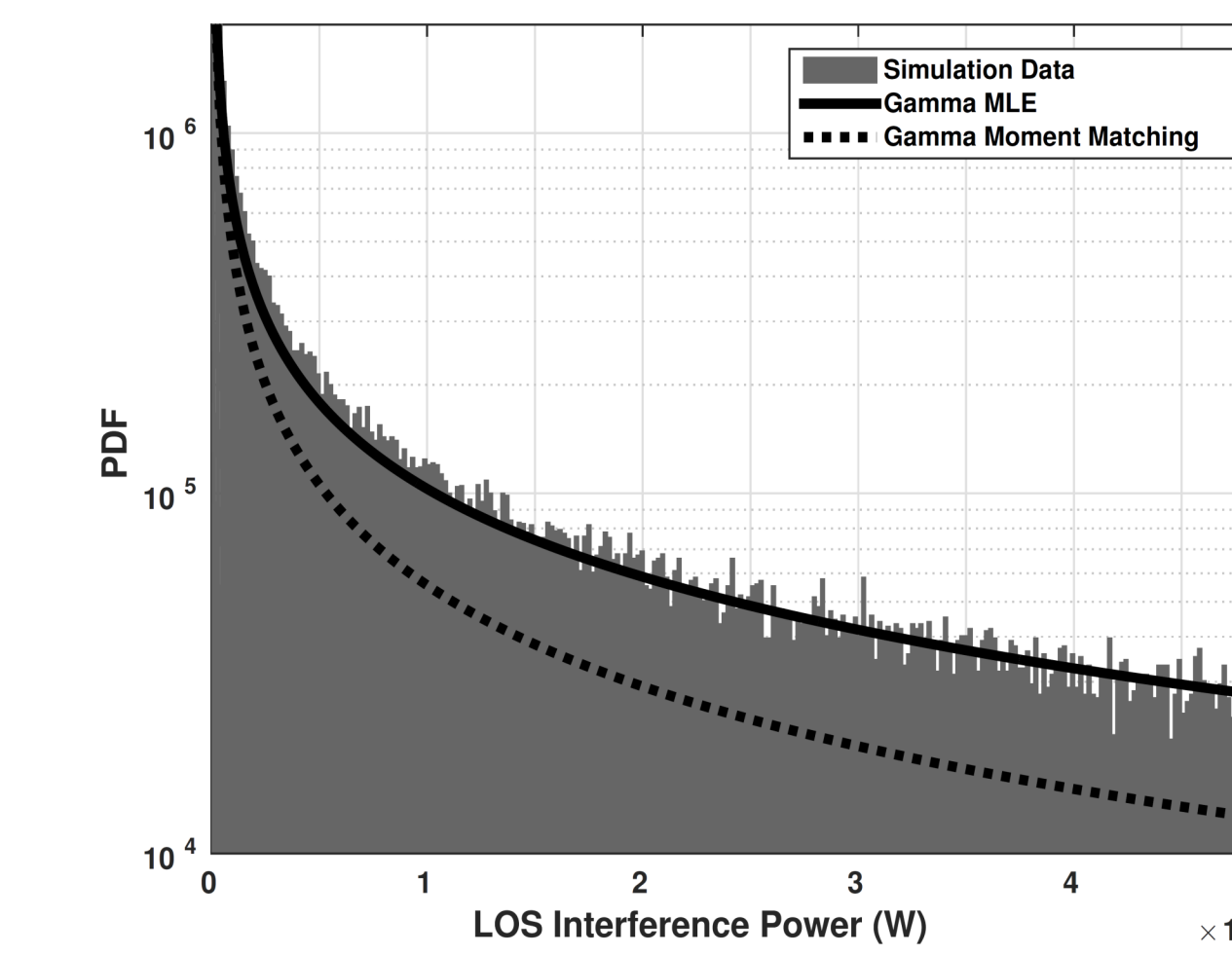


Fig. 3: LOS interference power PDF,  $\alpha_l = 3.5, \sigma_l = 4\text{dB}, (P_{max} = 30\text{dBm}, D = 75\text{m})$ .

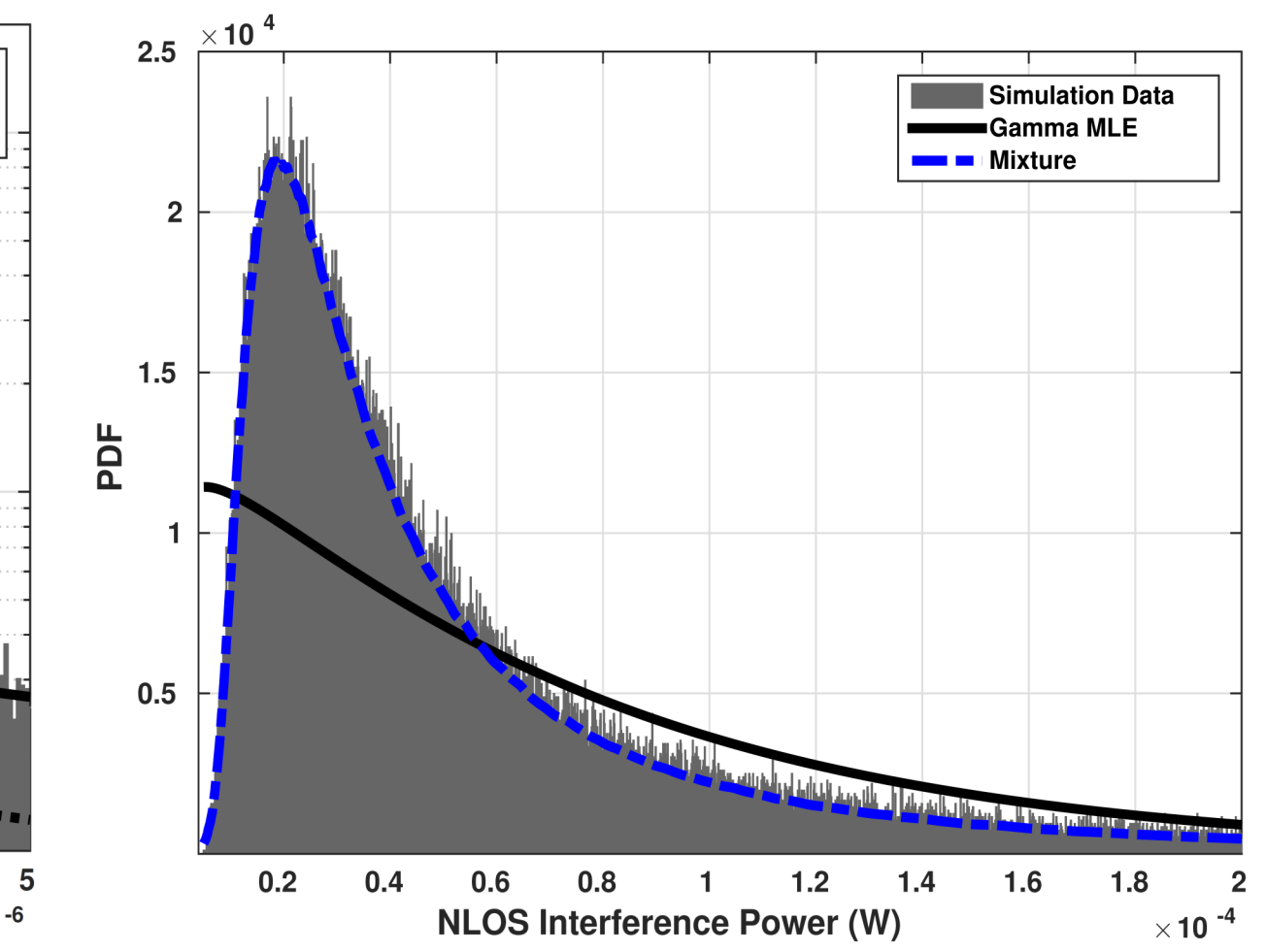


Fig. 4: NLOS interference power PDF,  $\alpha_n = 3.5, \sigma_n = 4\text{dB}, (P_{max} = 30\text{dBm}, D = 75\text{m})$ .

Kullback–Leibler (KL) divergence metric:

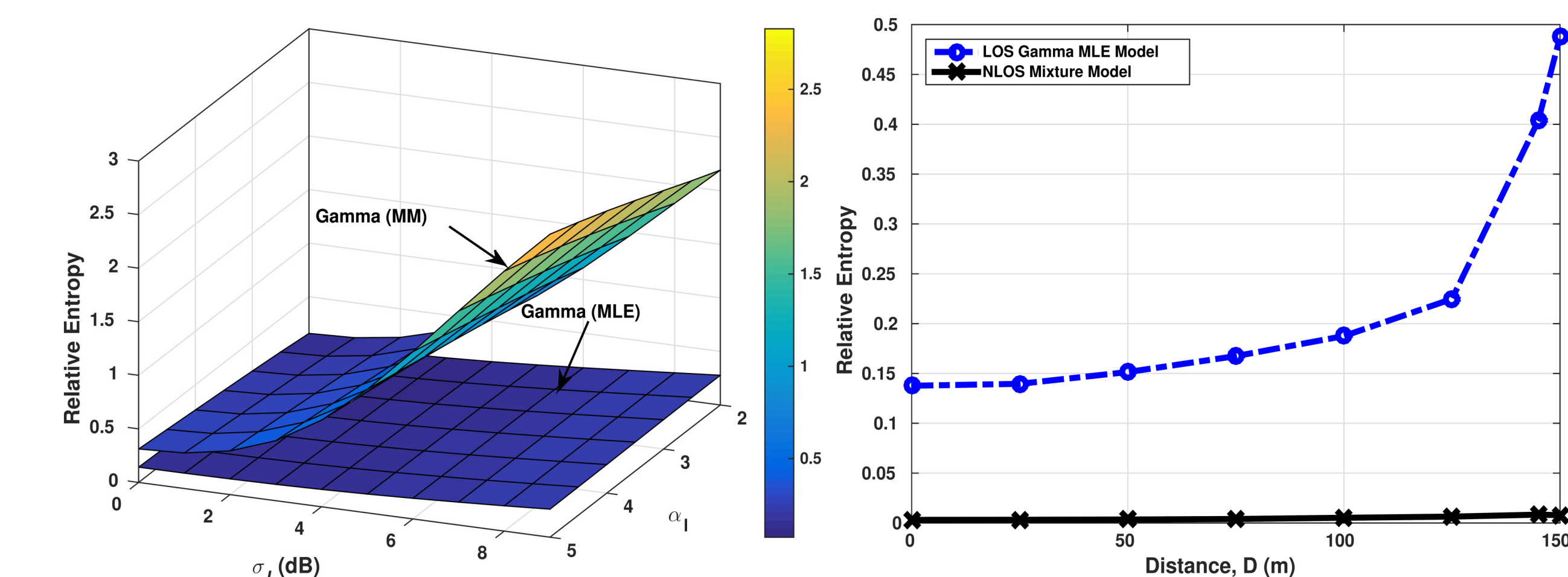


Fig. 5: KL metric of LOS models,  $D = 75\text{m}$ .

Fig. 6: KL metric versus distance  $D$  m, ( $\alpha_l = \alpha_n = 3.5, \sigma_l = \sigma_n = 4\text{dB}$ ).

## Conclusion and Future Work

- LOS MM model represents the simplest approach but fails to capture interference at high shadowing.
- Gamma MLE provides a good model for LOS interference power, but fails to model NLOS interference.
- Mixture MLE NLOS interference power model offers the best and most accurate fit.
- Future work:
  - Functional fitting as a simple way of modeling the mmWave interference directly.
  - Study models fitness under mmWave parametric channel model.