

Multiresolution Functional Connectivity Analysis Refines Functional Connectivity Networks in Individual Brains

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 - Voxel clustering
- Initial Results
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 - Other labs
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 - For network aggregation
- Enhanced Results
- Conclusions



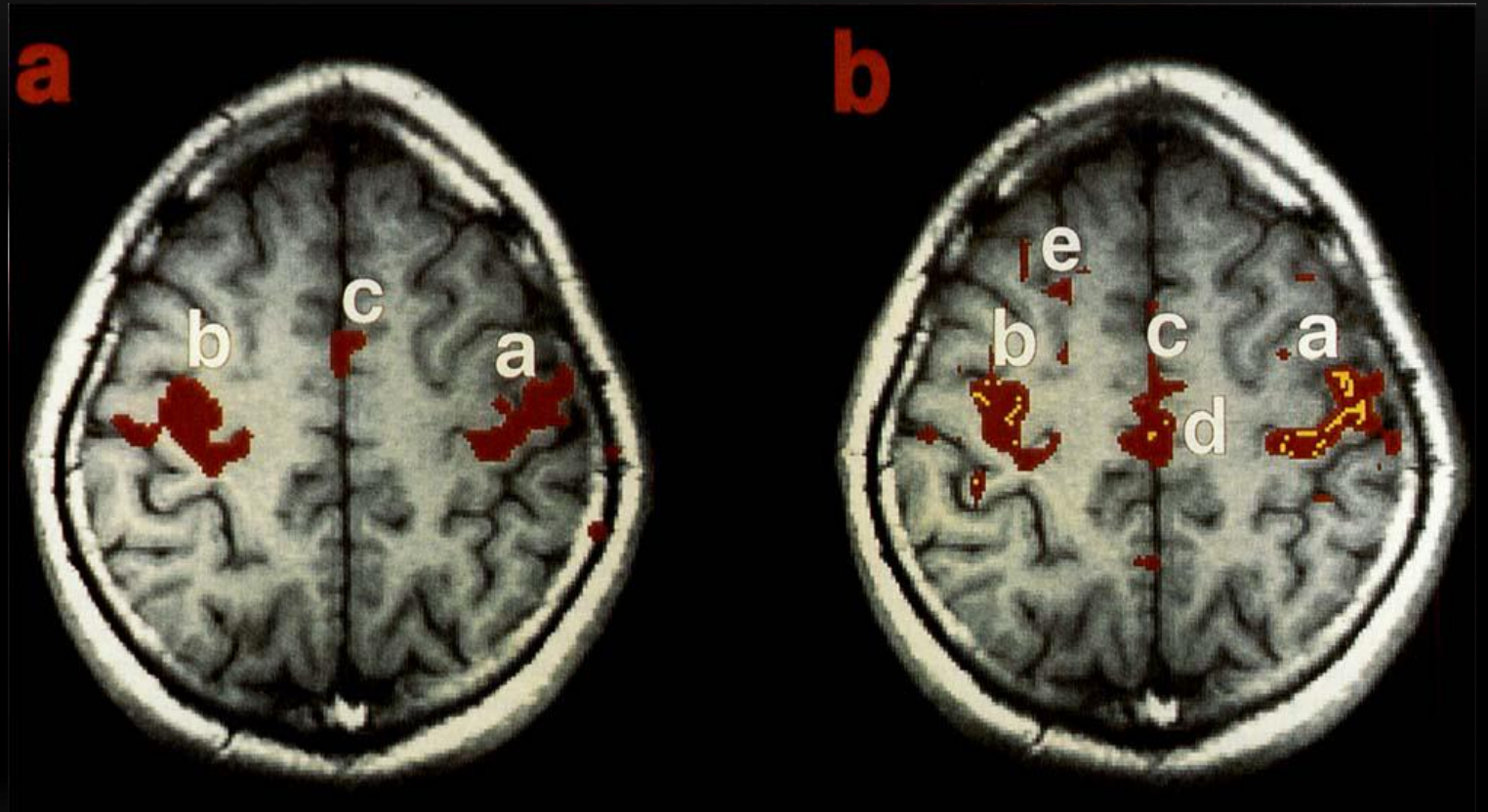
fc-fMRI

- Methodologically:

- Infers relationships between regions during particular states.
- Works with multiple datasets (EEG, LFP, fMRI, etc.)
- And multiple algorithmic approaches (seed-based correlation to graph-theory)

- In application

- Brain's intrinsic functional network architecture.
- Changes associated with disease
- Dynamic changes thru time



Biswal, B., et al. (1995). "Functional connectivity in the motor cortex of resting human brain using echo-planar MRI." *Magn Reson Med* **34**(4): 537-541.

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Initial Results

Enhanced Methods

Enhanced Results

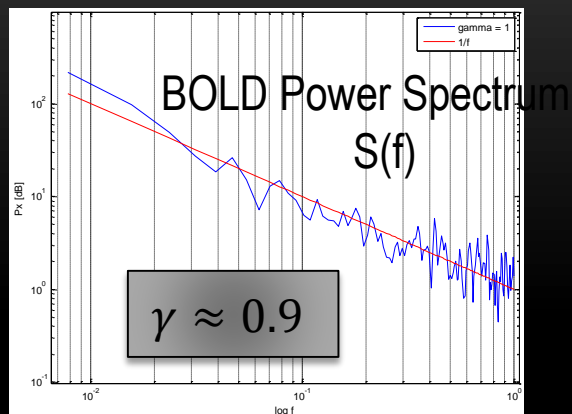
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Challenges and Proposed Solutions

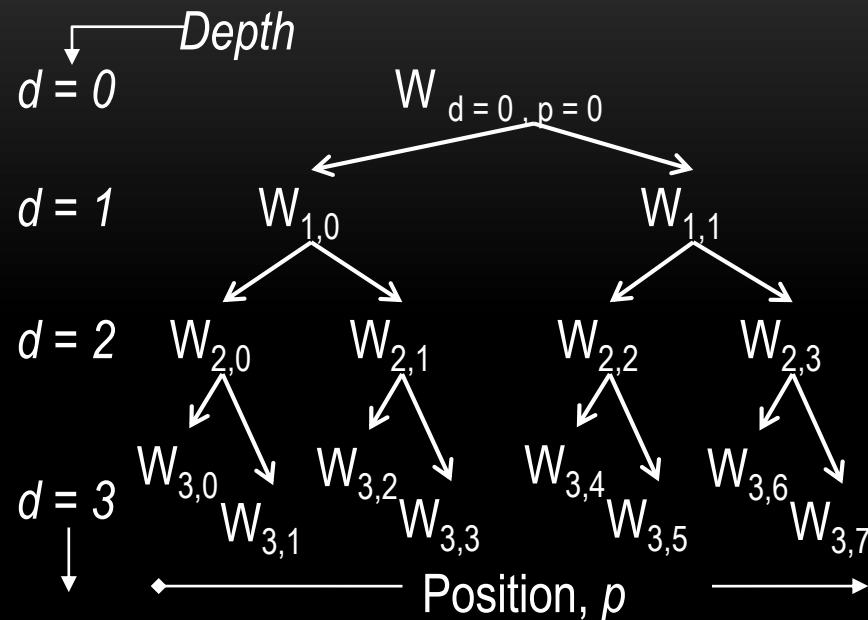
Challenges	Proposed solutions
Decouple overlapping BOLD signals	Signals should be transformed with a filter-bank: -wavelet packets
Depict network communications between both local and long range brain regions	Multi-spatial network analysis: -hierarchical clustering
Reduce manual work load interpreting multi-spatial and multi-spectral results	Features should be compared and aggregated into very similar feature sets: -wavelet entropy (signal level similarity) -mutual information (network level similarity)



Signal Fractionation via the Wavelet Packet Transform

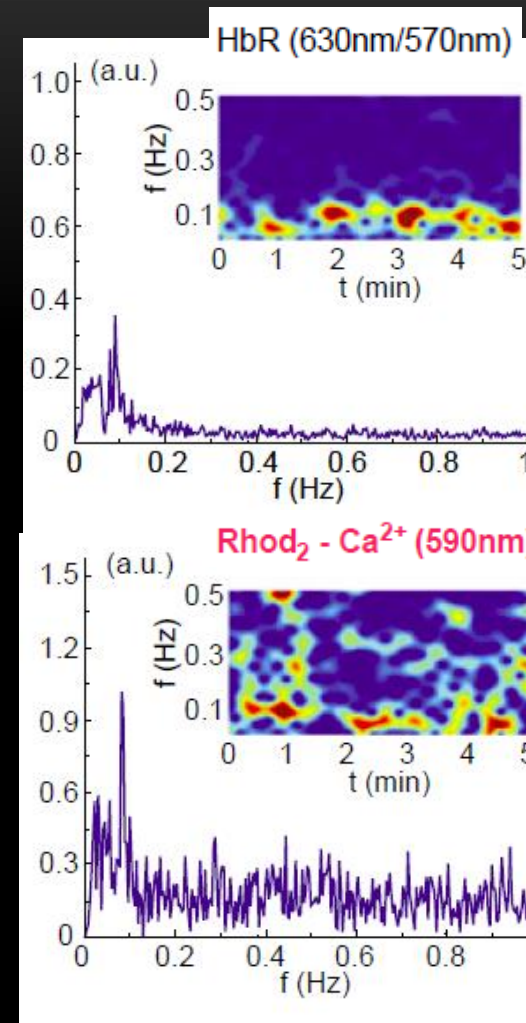
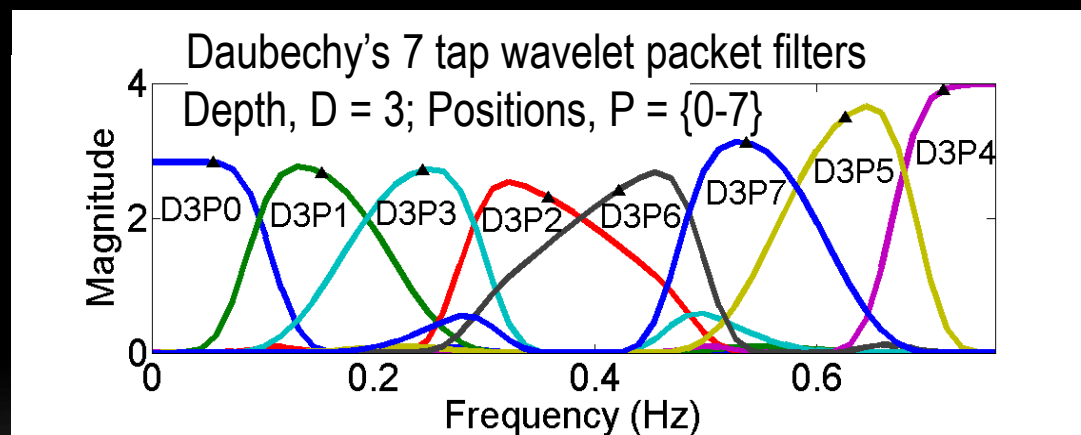


$$S(|f|) \approx \frac{1}{|f|^\gamma}$$



A. Medda, S. Keilholz. Wavelet Packet Based Clustering for the Study of Functional Connectivity in the Rat Brain. *Proceeding of the 46th Asilomar Conference on Signals, Systems, and Computers*; 2012 November 4, 2012; Pacific Grove, CA.

Wornell, G. W. (1993). "Wavelet-based representations for the $1/f$ family of fractal processes." *Proceedings of the IEEE* **81**(10): 1428-1450.



Du, C., et al. (2014). "Low-frequency calcium oscillations accompany deoxyhemoglobin oscillations in rat somatosensory cortex." *Proc Natl Acad Sci U S A* **111**(43): E4677-4686.

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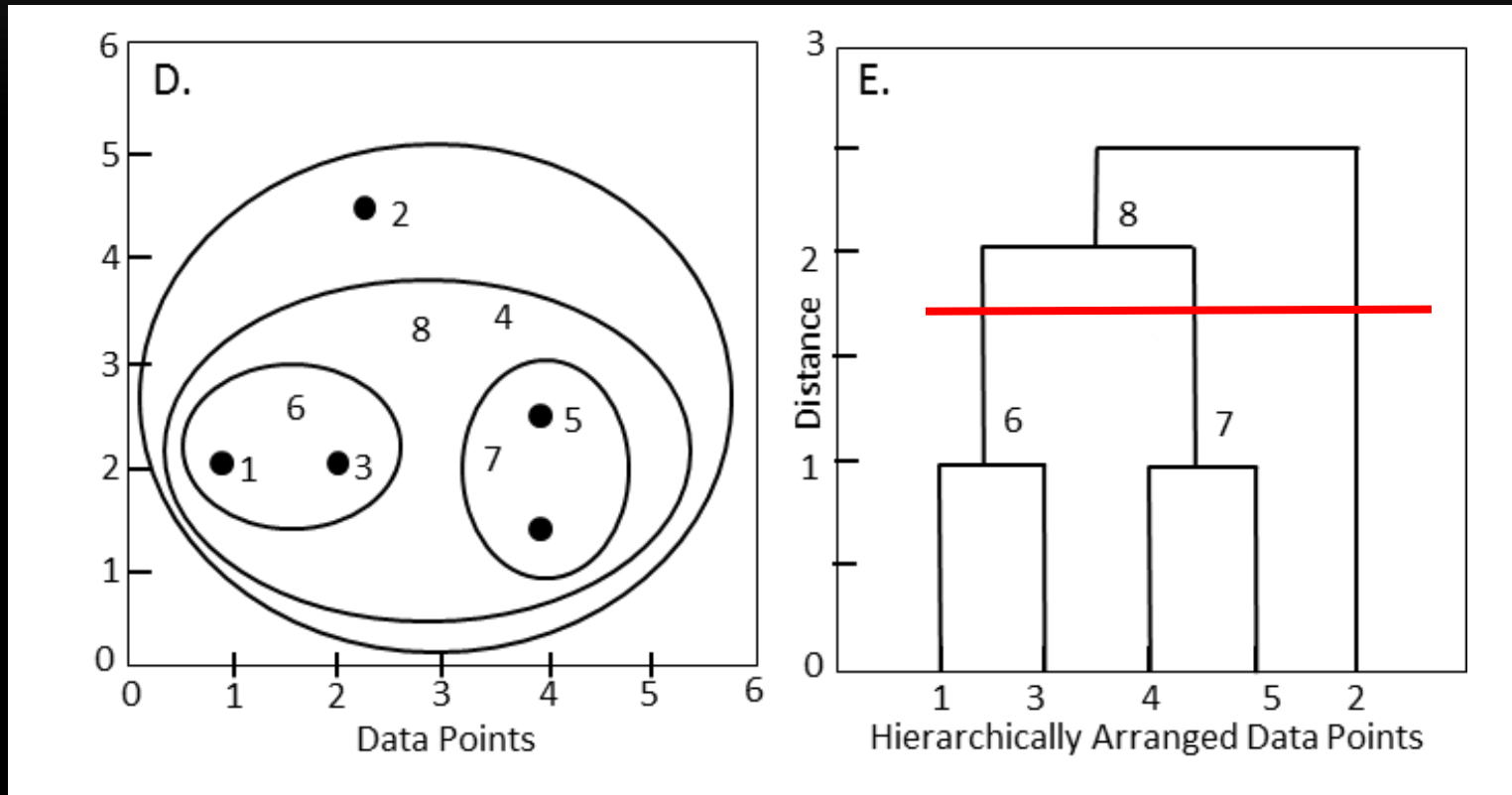
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Hierarchical Clustering: A general utility for clustering information



- Distance Metric

$$S1(i, j) = \sqrt{(V_{i \neq j} - V_j)(V_{i \neq j} - V_j)^T},$$

- Linkage Metric

$$S2(a, b) = \frac{1}{(n_a n_b)} \sum_{i=1}^{n_a} \sum_{j=1}^{n_b} S1(i \in a, j \in b).$$

- Generation of the k^{th} cluster

$$Y(k) = \min(S2_k)$$

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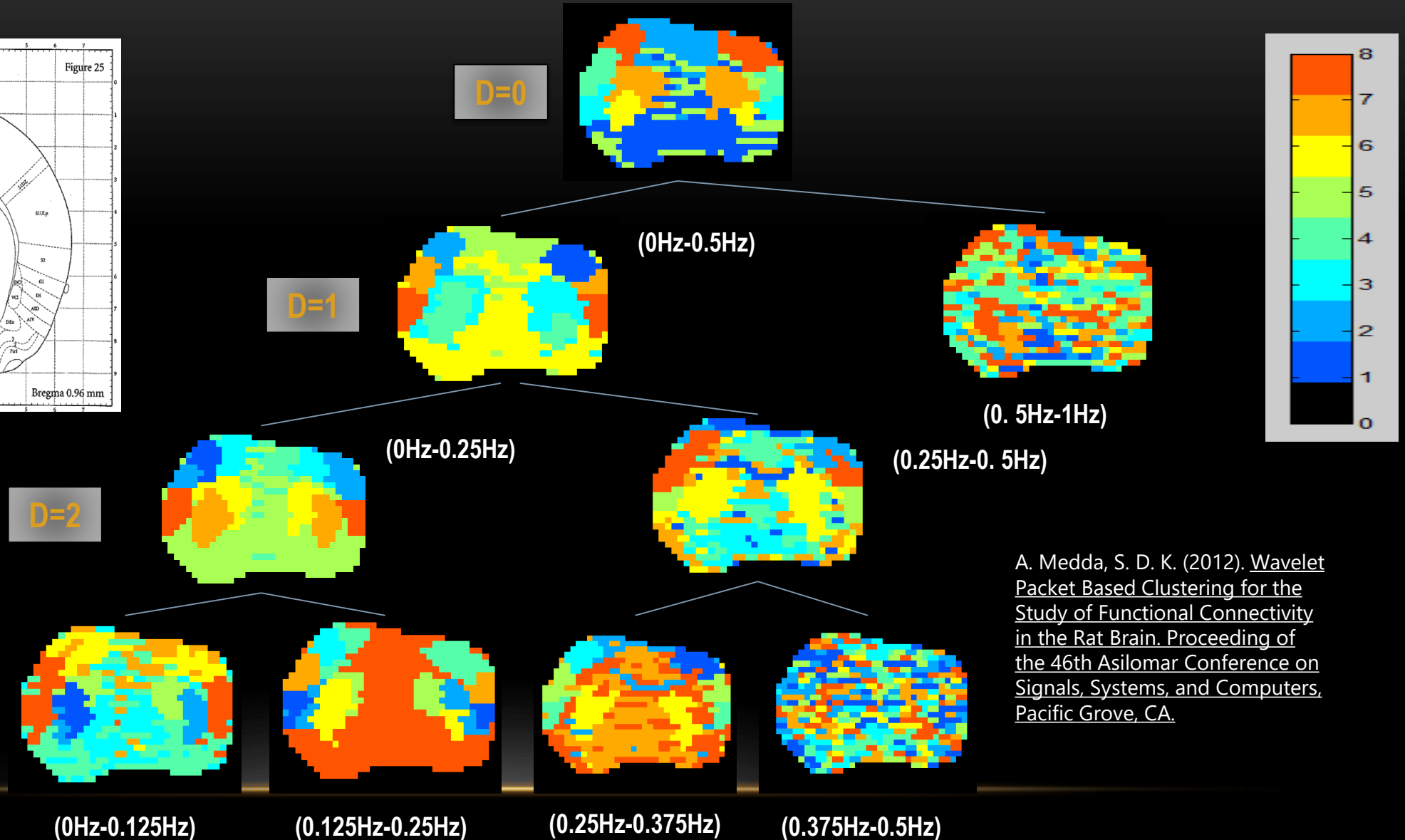
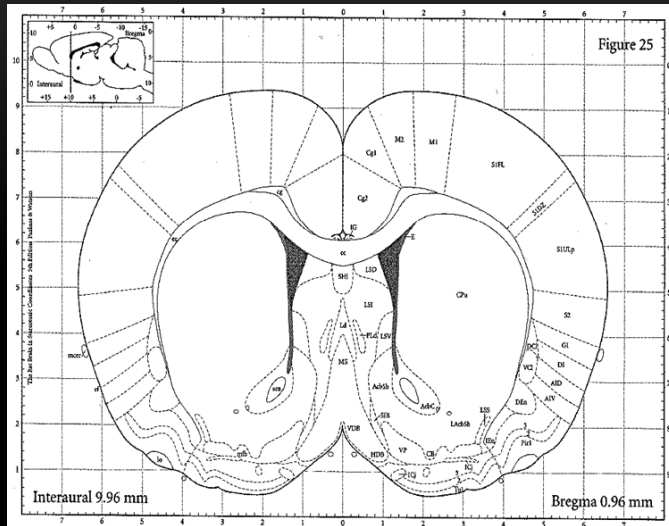
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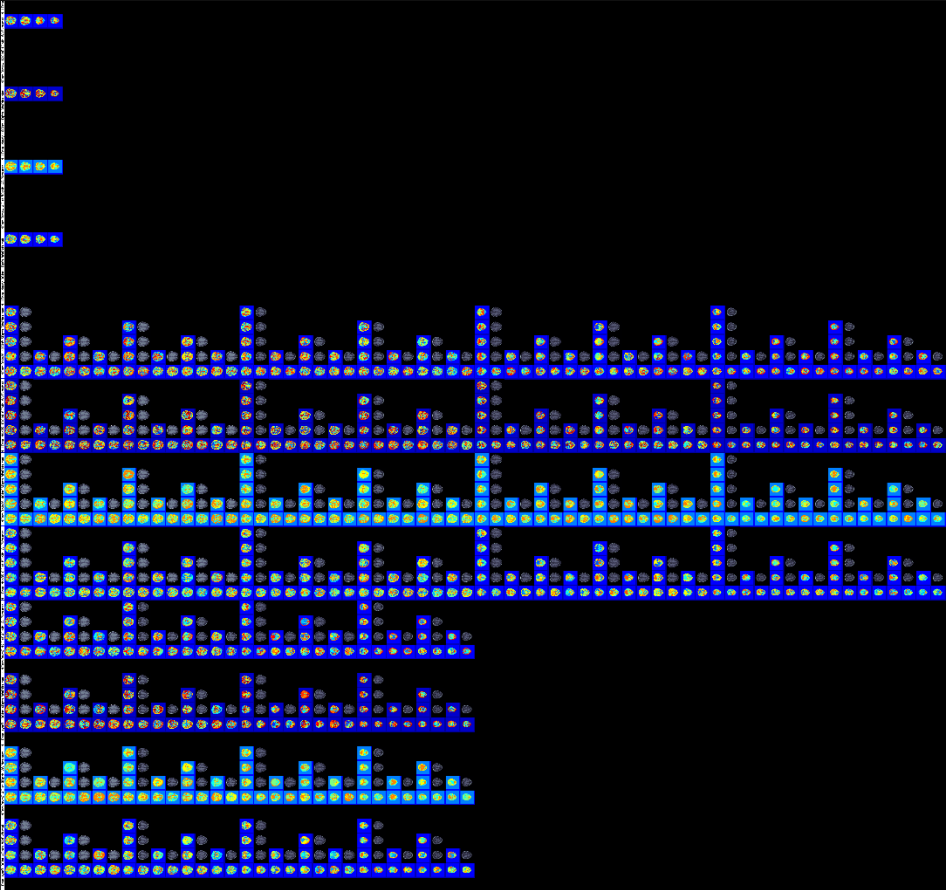
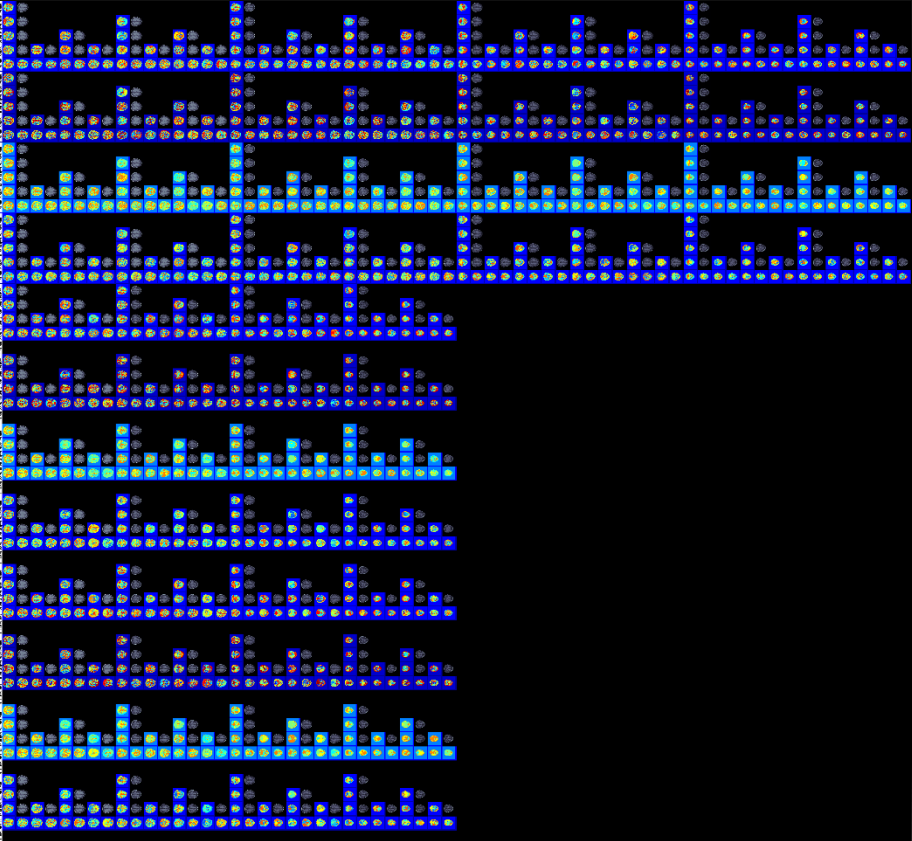
Initial results on single slice of rat brain



A. Medda, S. D. K. (2012). Wavelet Packet Based Clustering for the Study of Functional Connectivity in the Rat Brain. Proceeding of the 46th Asilomar Conference on Signals, Systems, and Computers, Pacific Grove, CA.



Process Explodes the Search Space for Functionally Relevant Networks



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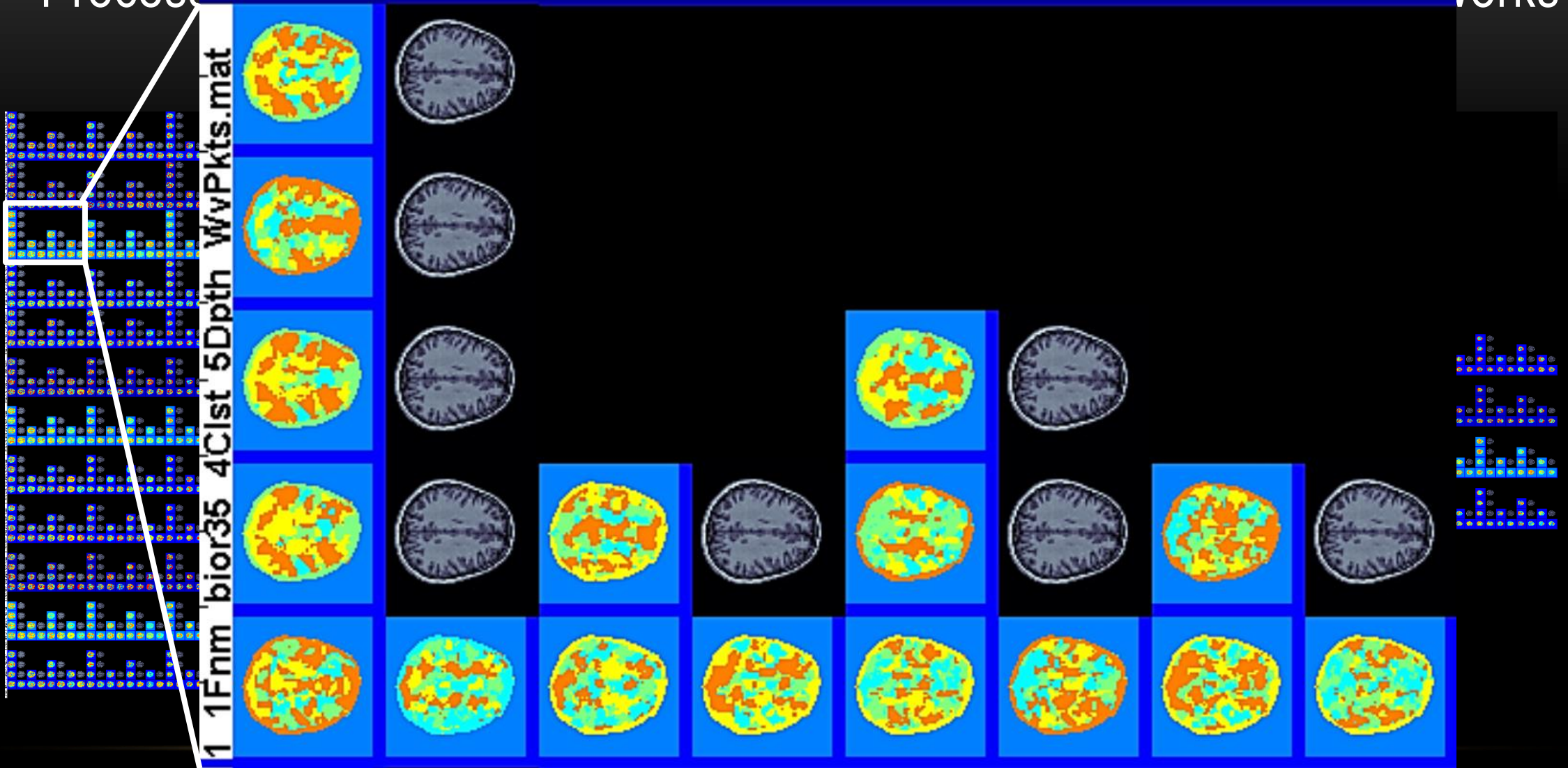
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Process Explodes the Search Space for Functionally Relevant Networks



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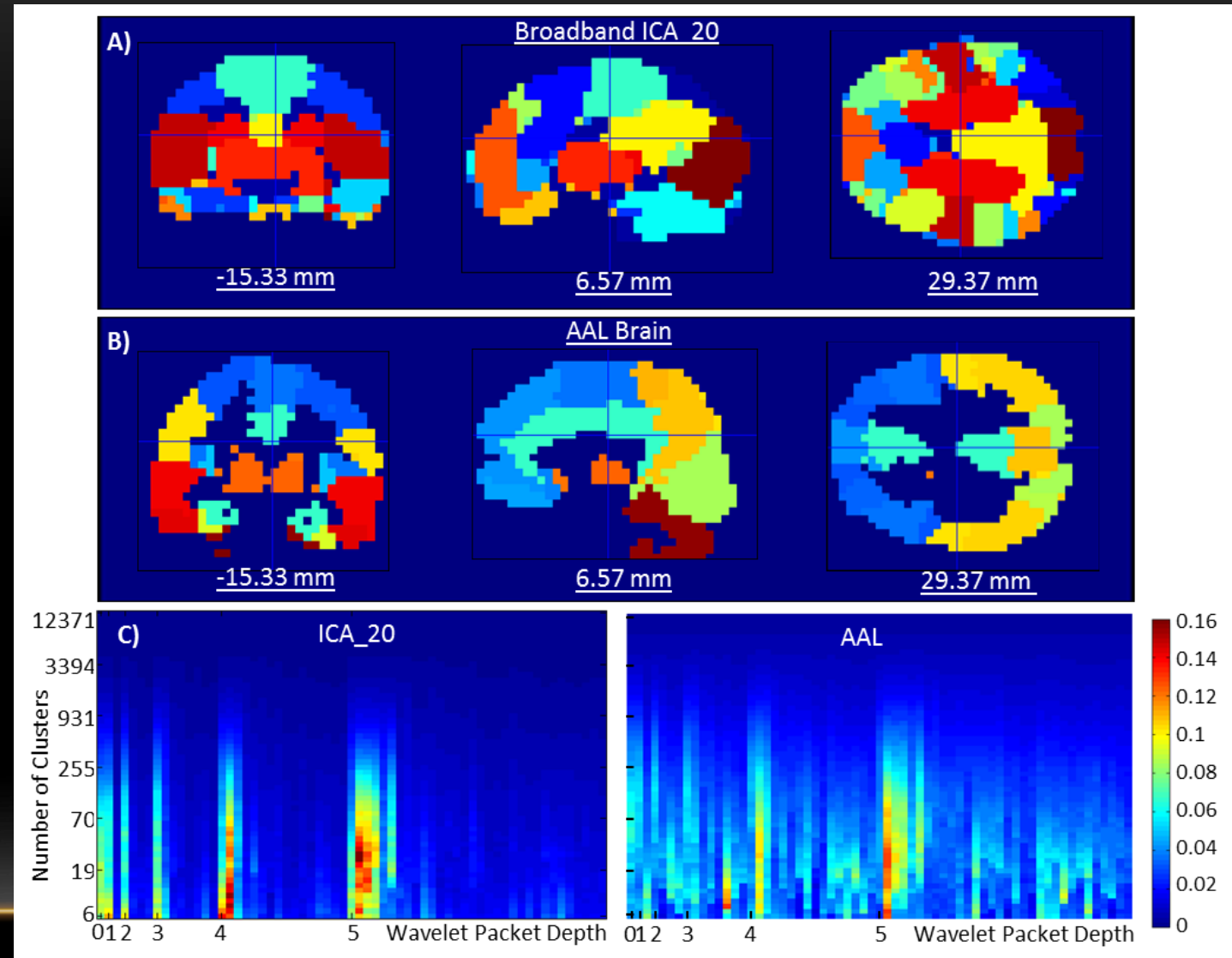
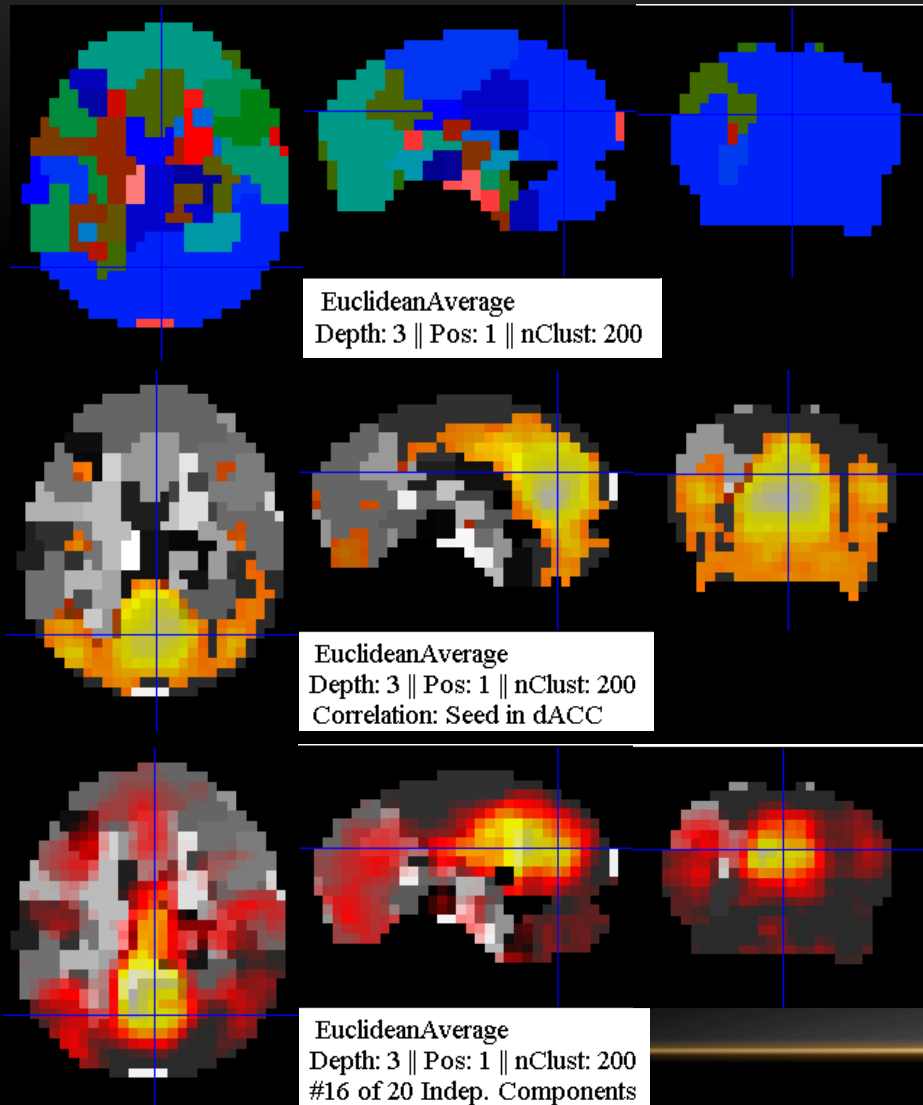
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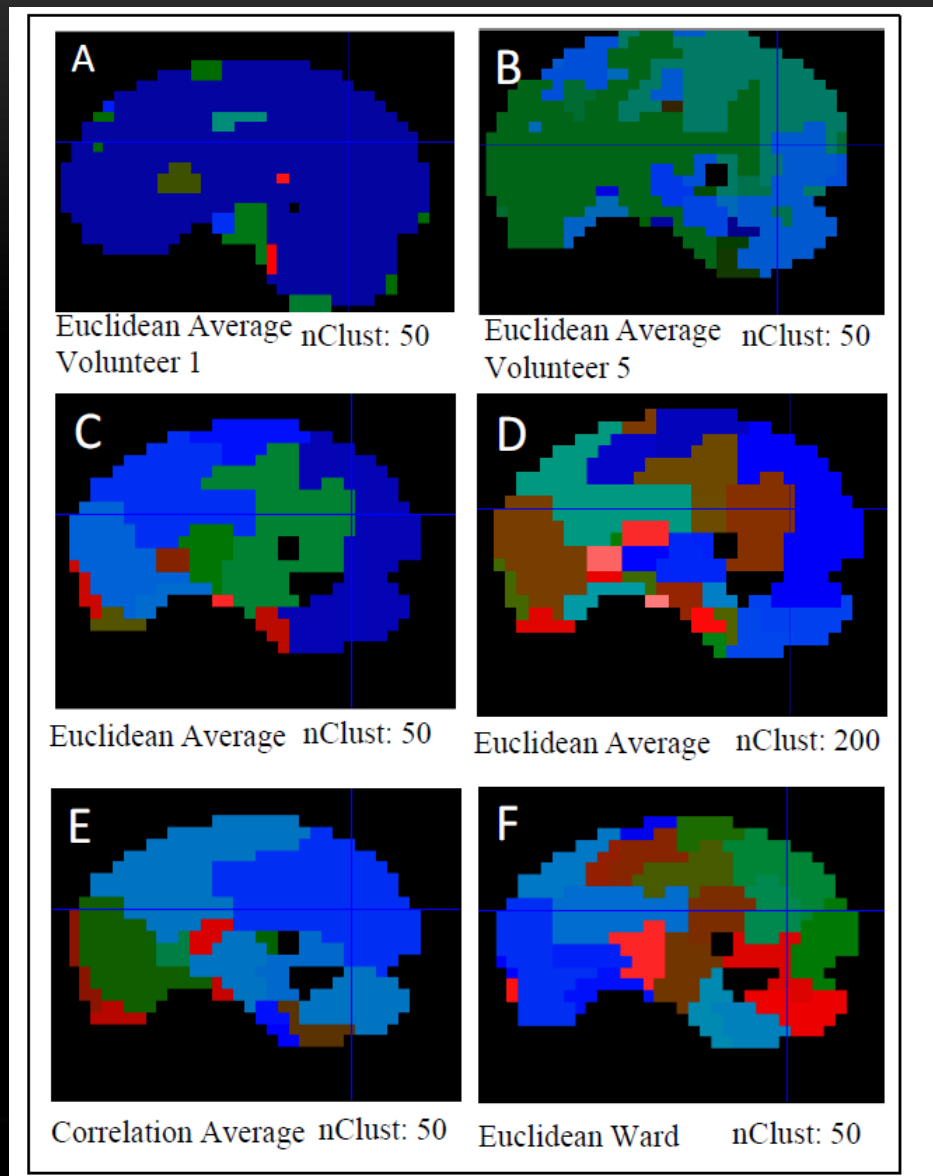
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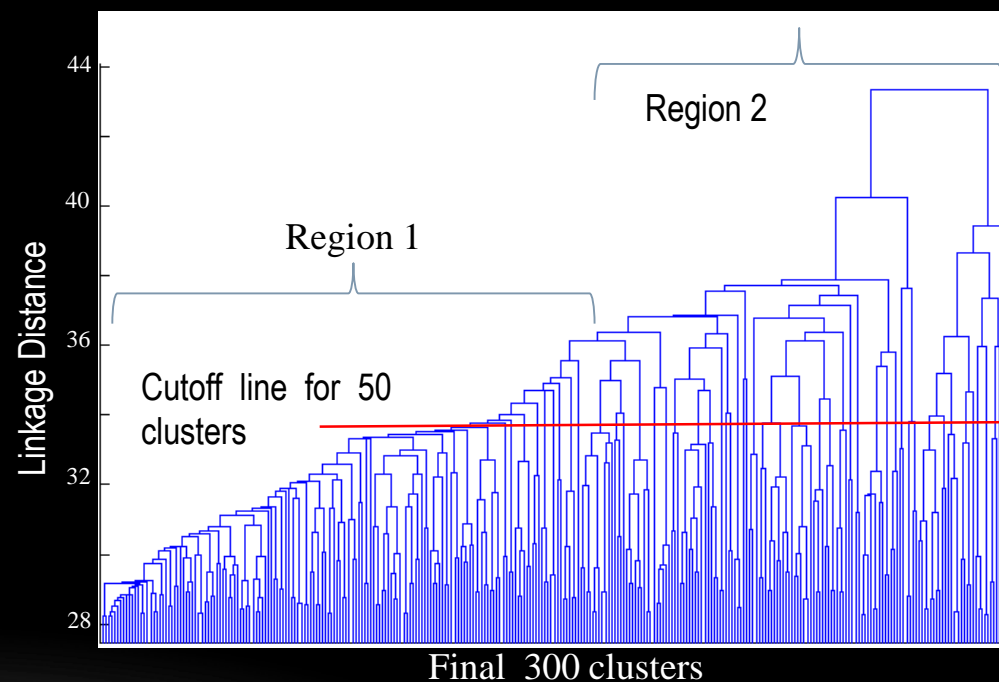
Wavelet Clustering fc-fMRI Compares Well with Alternative Techniques



Initial results in multi-slice human data



- Public resting-state BOLD dataset: NKI Enhanced Rockland Sample
- Hundreds of volunteers evenly sampled across demographic
- TR = 0.645 s, 3 mm isotropic, 10 minutes
- Standard preprocessing (SPM 8)



Billings, J. C. W., et al. (2013). Agglomerative clustering for resting state MRI. Neural Engineering (NER), 2013 6th International IEEE/EMBS Conference on.

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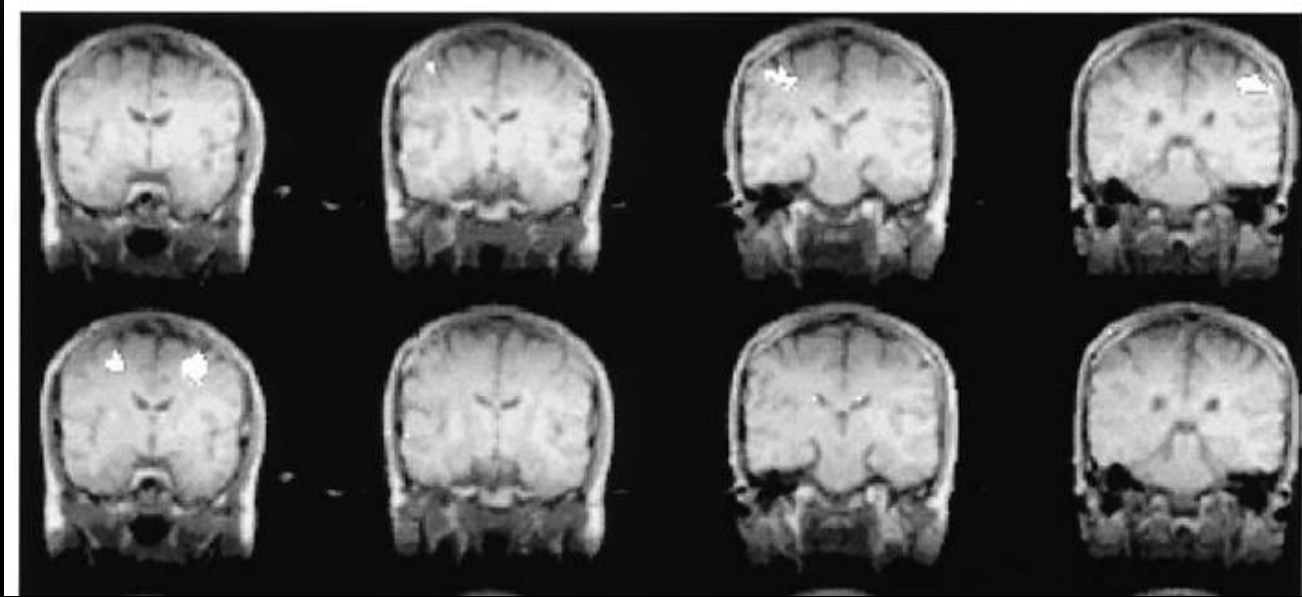
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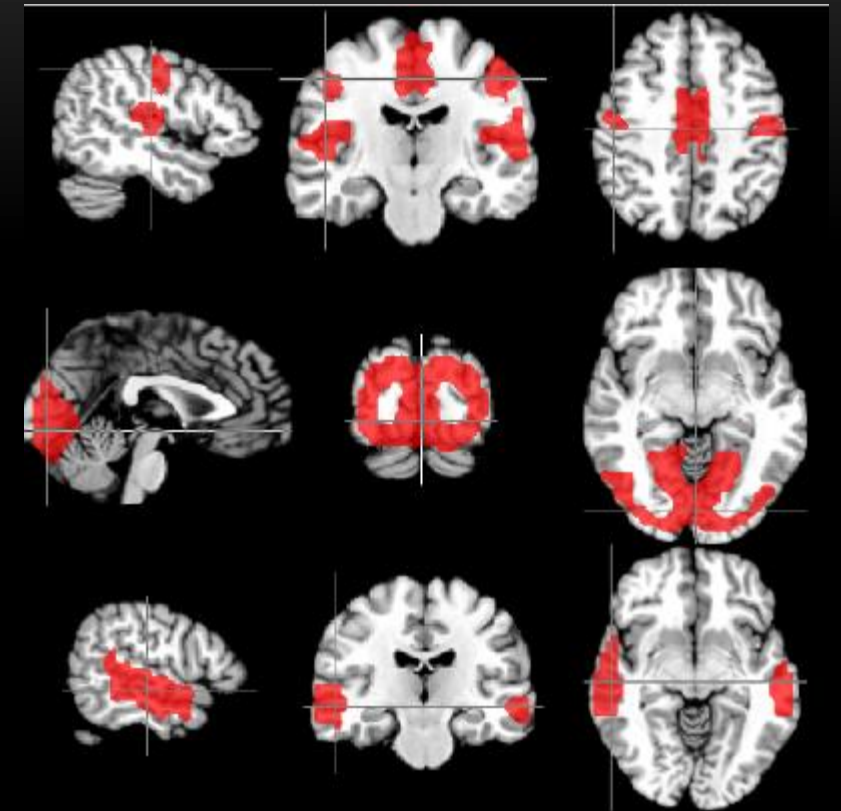
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Conclusions

Agglomerative clustering for whole-brain networks?



Cordes, D., et al. (2002). "Hierarchical clustering to measure connectivity in fMRI resting-state data." *Magnetic resonance imaging* **20**(4): 305-317.



Wang, Y. and T.-Q. Li (2013). "Analysis of Whole-Brain Resting-State fMRI Data Using Hierarchical Clustering Approach." *PLoS ONE* **8**(10): e76315.

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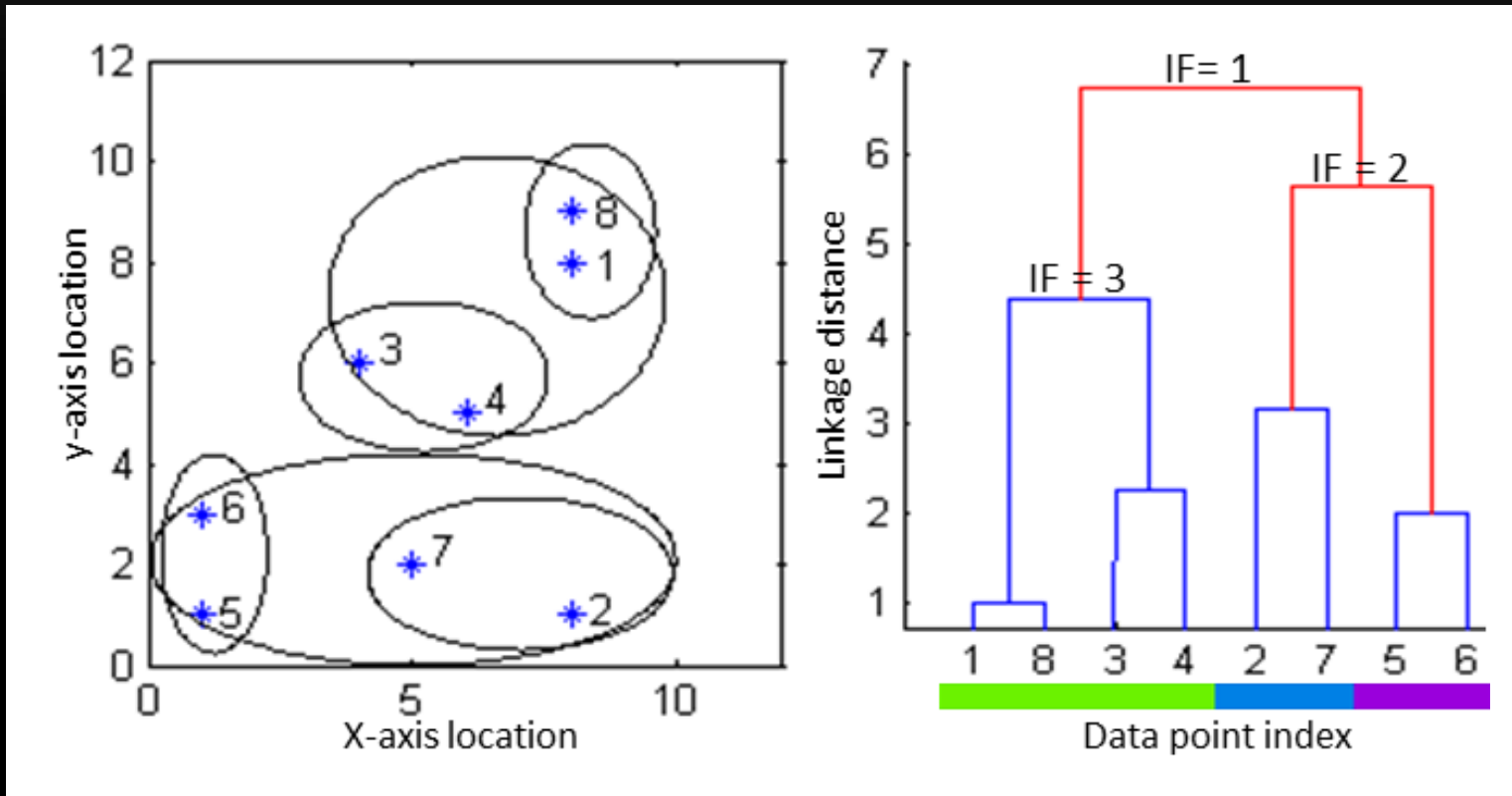
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An Improved Method for Cutting a Hierarchical Clustering Tree



- The inconsistency factor cuts the hierarchy
$$IF(Y_k) = (Y_k - \bar{Y}_g) / std(Y_g)$$

Subscript g is the number of links for which an average and standard deviation are calculated.

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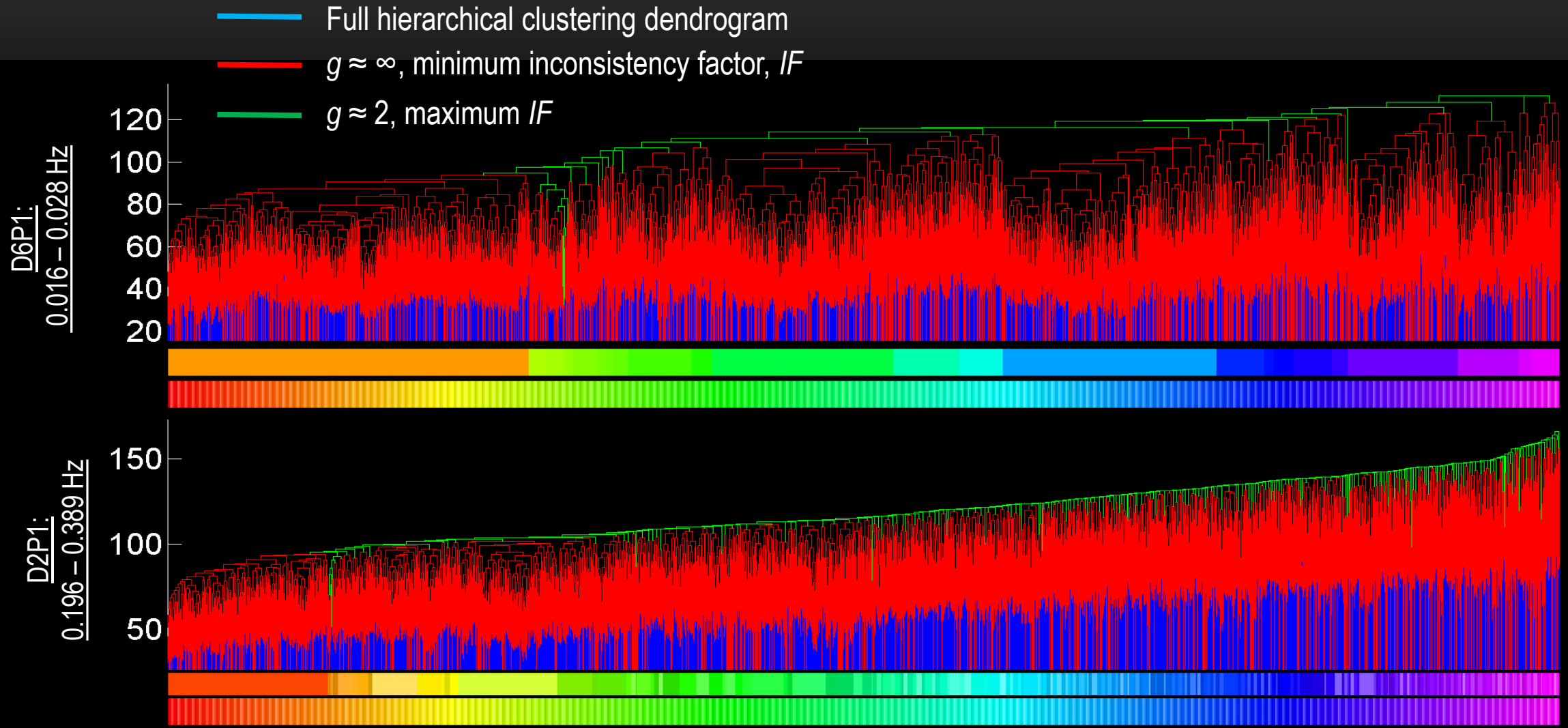
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The Hierarchical Clustering Dendrogram is a Natural Space for Conveying Network Multi-Scalability, $n = 112$



Feature comparison and aggregation

Signal comparisons

- *Non-normalized Shannon Entropy*

$$E(s) = - \sum_i s_i^2 \log(s_i^2)$$

With s_i being a voxel's wavelet coefficients

Network comparisons

- *Cluster Entropy:*

$$H(C) = - \sum_{i=1}^k P(i) \log_2 P(i),$$

$$\text{with } P(i) = \frac{|C_i|}{n},$$

C_i is a cluster of n parts.

- *Mutual information:*

$$I(C', C'') = \sum_{i=1}^k \sum_{j=1}^l P(i, j) \log_2 \frac{P(i, j)}{P(i)P(j)},$$

$$\text{where } P(i, j) = \frac{|C_i \cap C_j|}{n}.$$

- *Variation in information:*

$$VI(C', C'') = [H(C') - I(C', C'')] + [H(C'') - I(C', C'')]$$

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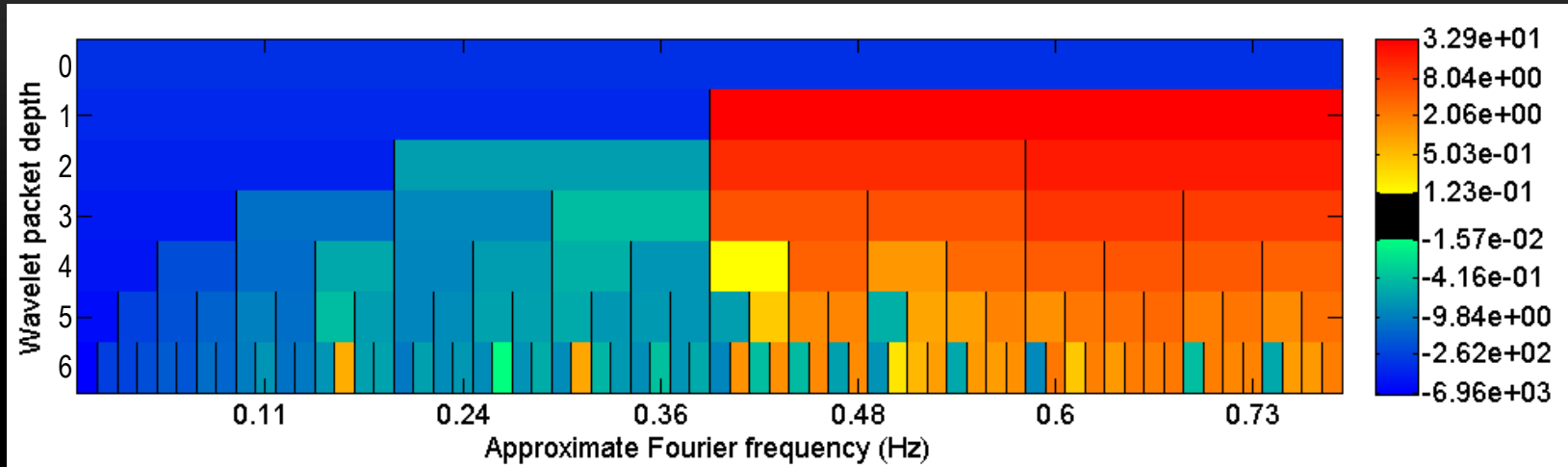
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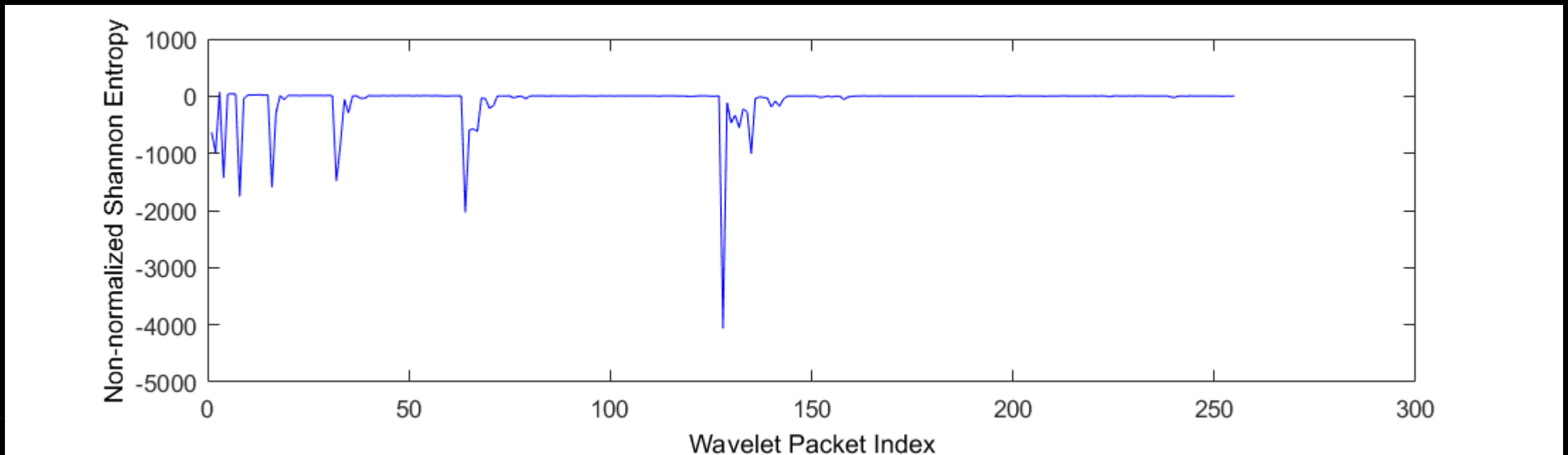
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Entropy values across spectra, N = 112



Non-normalized Shannon Entropy

$$E(s) = - \sum_i s_i^2 \log(s_i^2)$$



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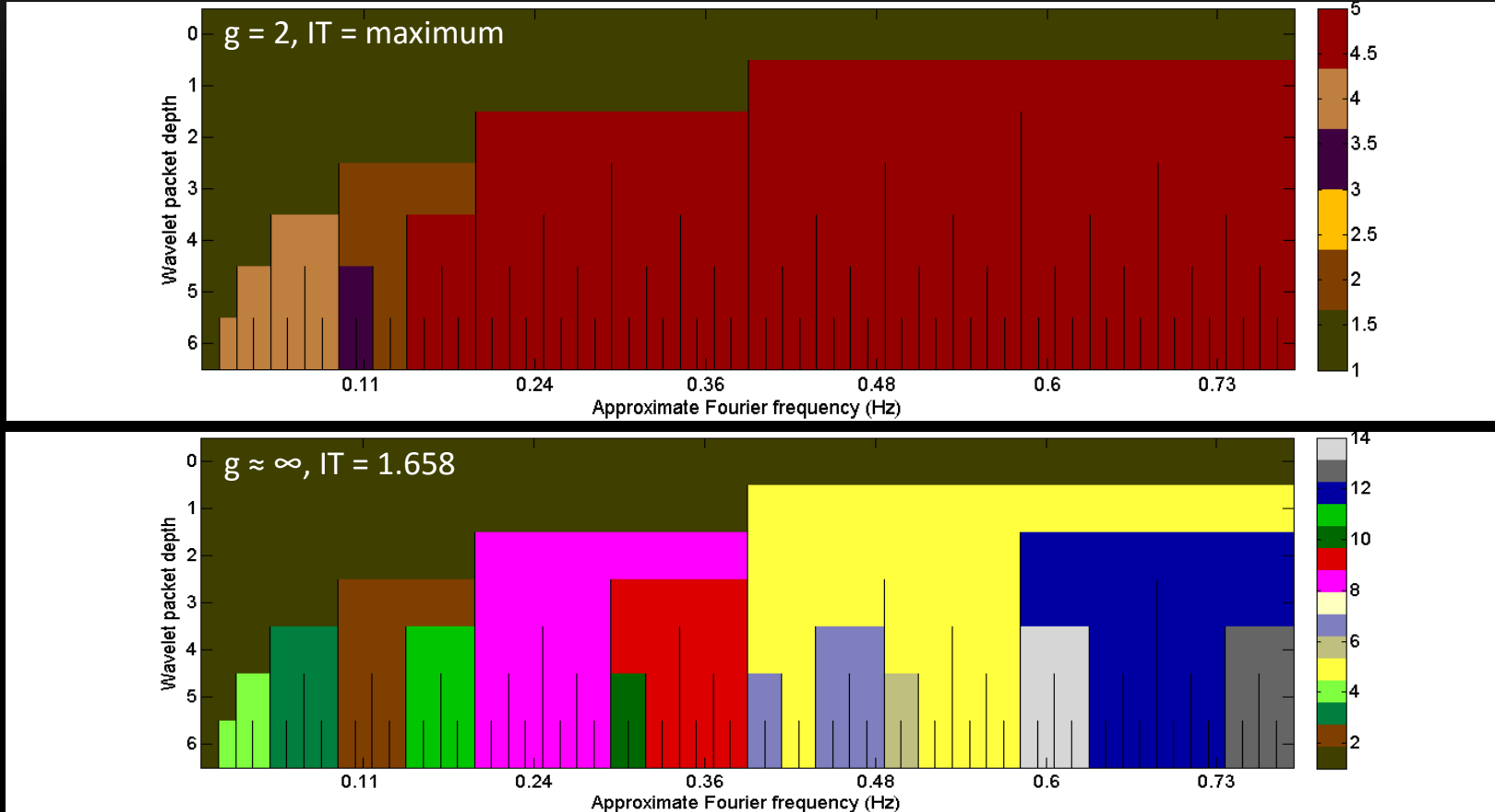
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Network Spectral Similarity as Identified Through Mutual Information



Entropy:

$$H(C) = - \sum_{i=1}^k P(i) \log_2 P(i),$$

with $P(i) = \frac{|C_i|}{n}$,

C_i is a cluster of n parts.

Mutual information:

$$I(C', C'') =$$

$$\sum_{i=1}^k \sum_{j=1}^l P(i, j) \log_2 \frac{P(i, j)}{P(i)P(j)},$$

where $P(i, j) = \frac{|C_i \cap C_j|}{n}$.

Variation in information:

$$VI(C', C'') =$$

$$[H(C') - I(C', C'')] + [H(C'') - I(C', C'')].$$

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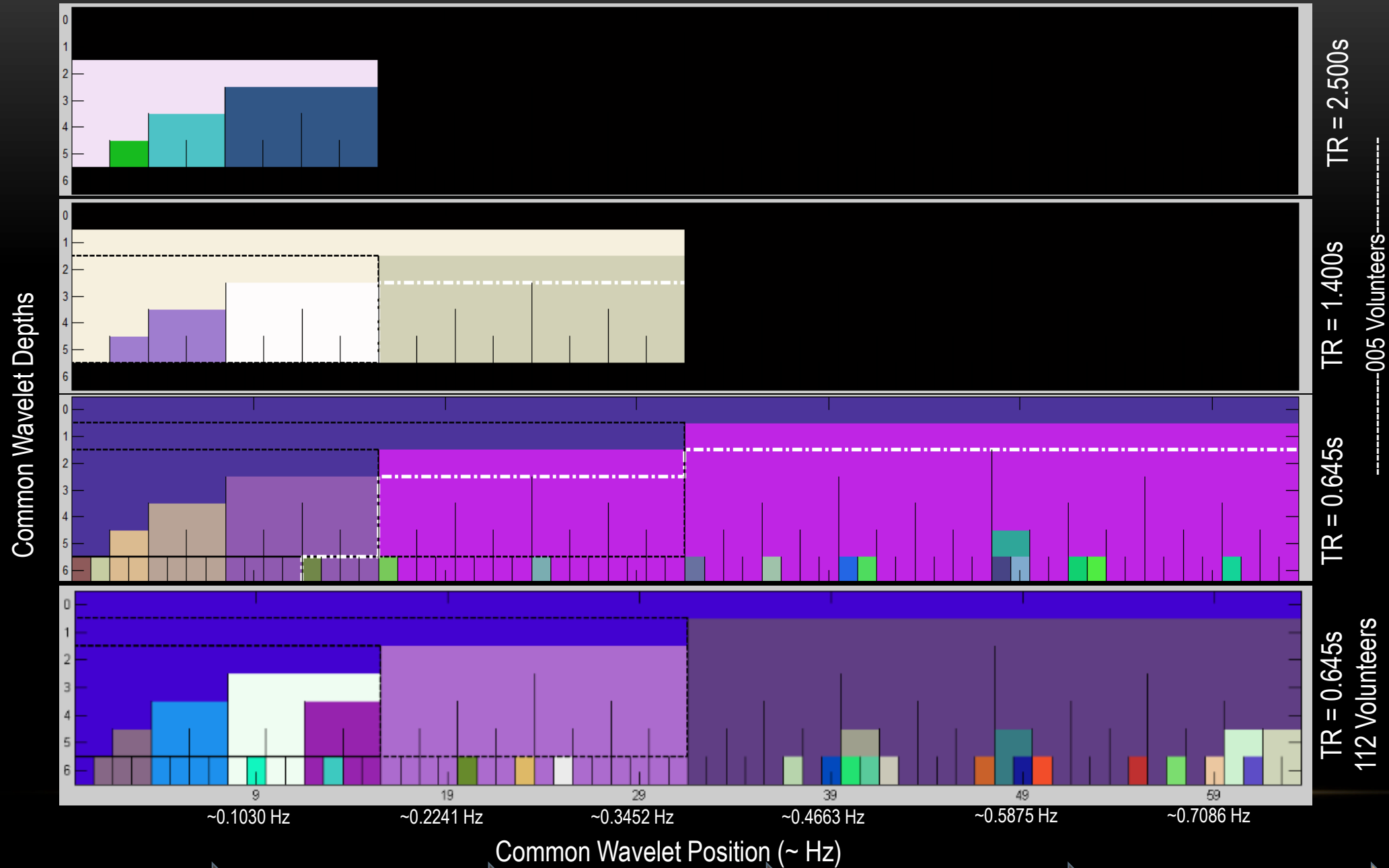
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Network Spectral Similarity as Identified Through Mutual Information



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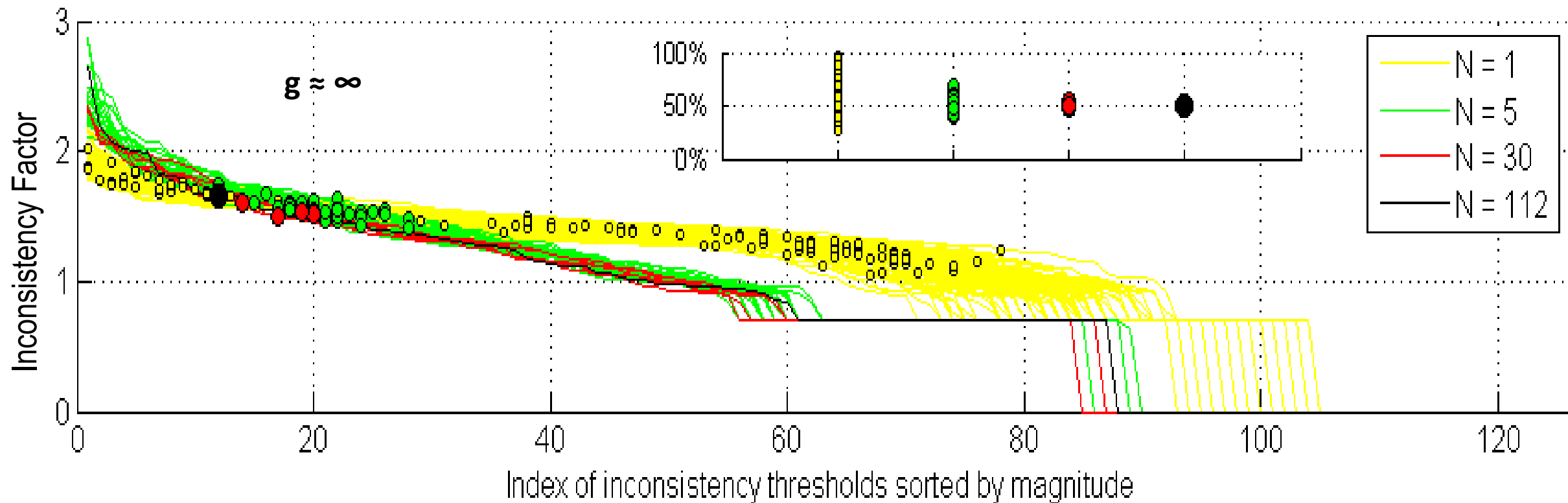
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The Low-frequency Fluctuation Domain Separates into Distinct Networks at the 50% Point of All Inconsistency Factors



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Broadband:
0.003 – 0.745

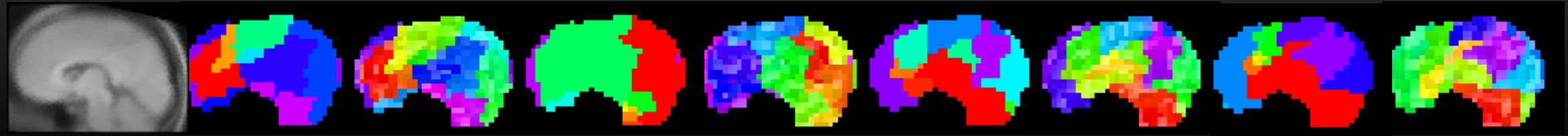
D6P0 Packet:
0.003-0.016 Hz

D6P1 Packet:
0.016-0.028 Hz

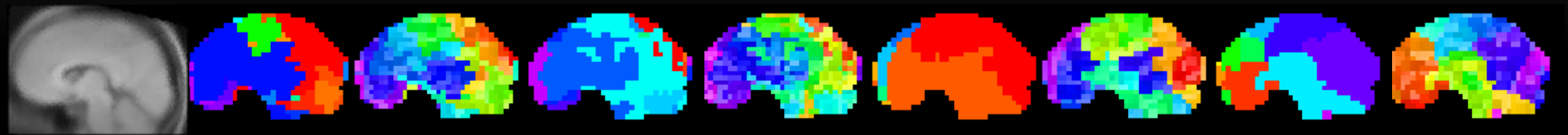
D5P1 Packet:
0.028-0.052 Hz

Anatomical

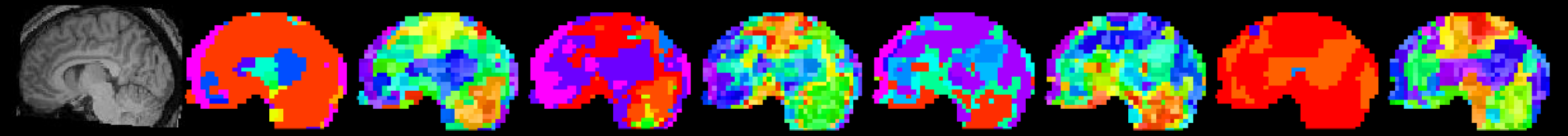
G_112



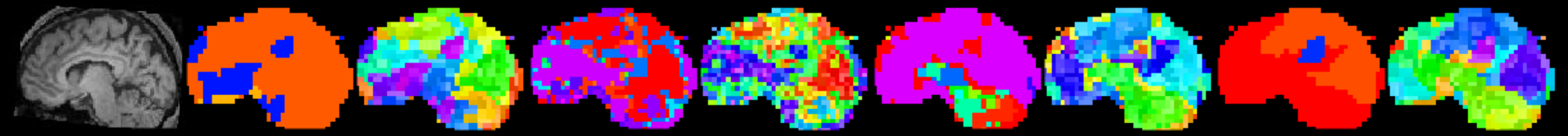
G_005



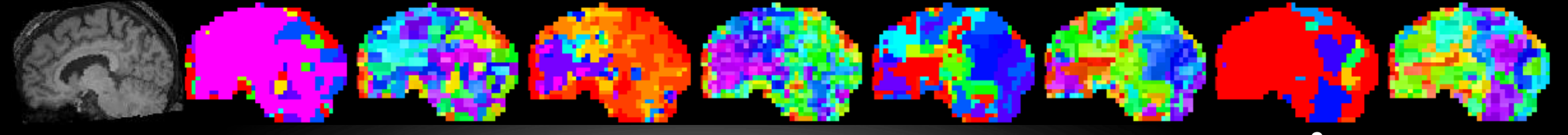
V_001



V_002



V_003



G_###: Group dataset with ### volunteers

V_###: Volunteer ###

$g = 2$
max IF

$g \approx \infty$
min IF

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- BOLD signal <0.1 Hz has a high probability of containing a large amount of noise
- Best BOLD networks in the low-frequency fluctuation range between 0.01 and 0.1 Hz
- Frequency range may be subdivided into to build quantitatively distinct networks
- Functional connectivity networks exist at several spatial scales who complimentarily address whole brain connectivity
- Network connectivity in groups produce well known functional architecture
- Individual networks demonstrate a mixture of highly variant architectures in addition to well known network features
- Equivalent findings observed independent of acquisition parameters



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