

# Full-Duplex Relaying in MIMO-OFDM Frequency-Selective Channels with Optimal Adaptive Filtering

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# Full-Duplex Relaying in MIMO-OFDM Frequency-Selective Channels with Optimal Adaptive Filtering

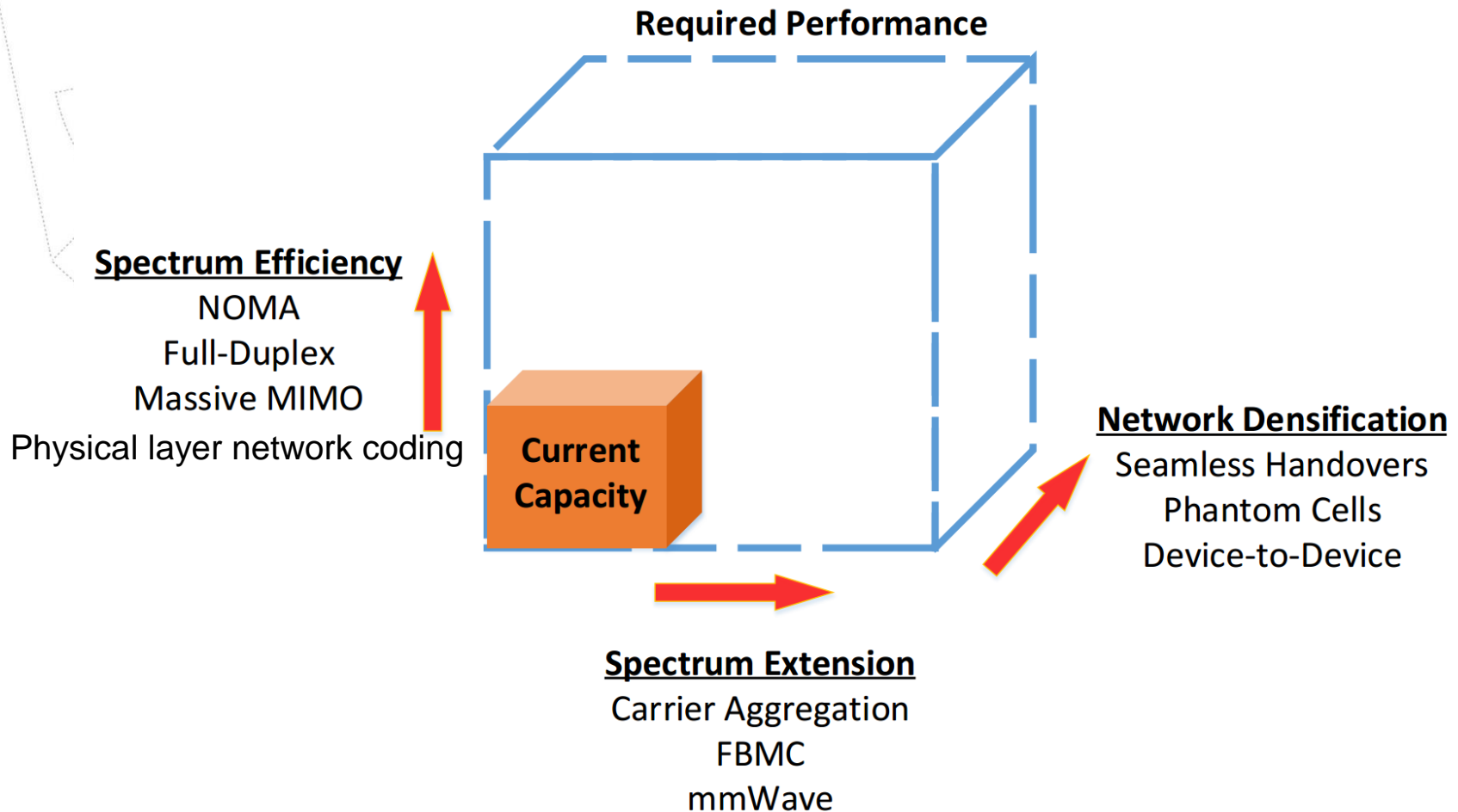
## 1- Context

2- Proposed System Model

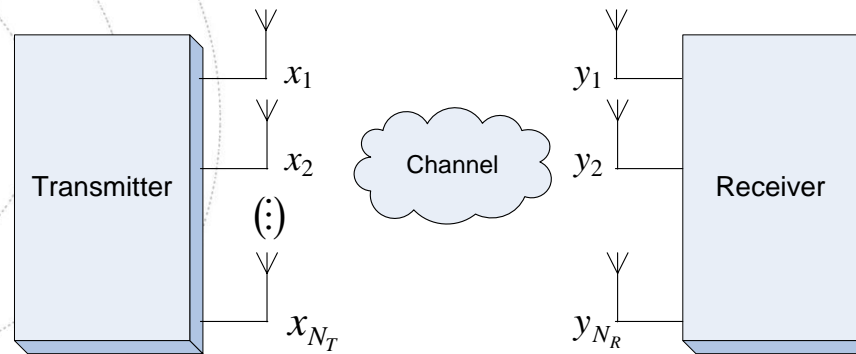
3- Results

4- Conclusions

# How to offer more?



# Multiple-input multiple-output (MIMO) detection



$$\begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \vdots \\ \mathbf{y}_{N_R} \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & \cdots & h_{1N_T} \\ h_{21} & h_{22} & \cdots & h_{2N_T} \\ \vdots & \vdots & \ddots & \vdots \\ h_{N_R 1} & h_{N_R 2} & \cdots & h_{N_R N_T} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \\ \vdots \\ \mathbf{x}_{N_T} \end{bmatrix} + \begin{bmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \\ \vdots \\ \mathbf{n}_{N_R} \end{bmatrix}$$

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n}$$

$$\hat{\mathbf{x}}_{ML} = \min_{\mathbf{x}} \left\{ \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 \right\}$$

## Recent state-of-the-art in radio science

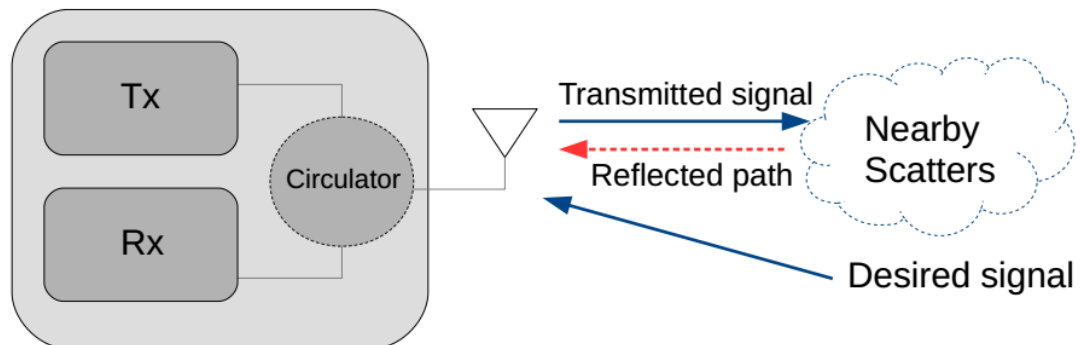
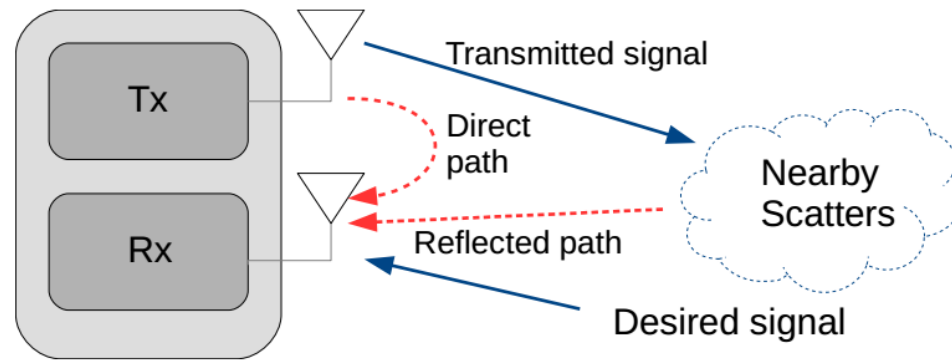
*“It is generally not possible for radios to receive and transmit on the same frequency band because of the interference that results.”*



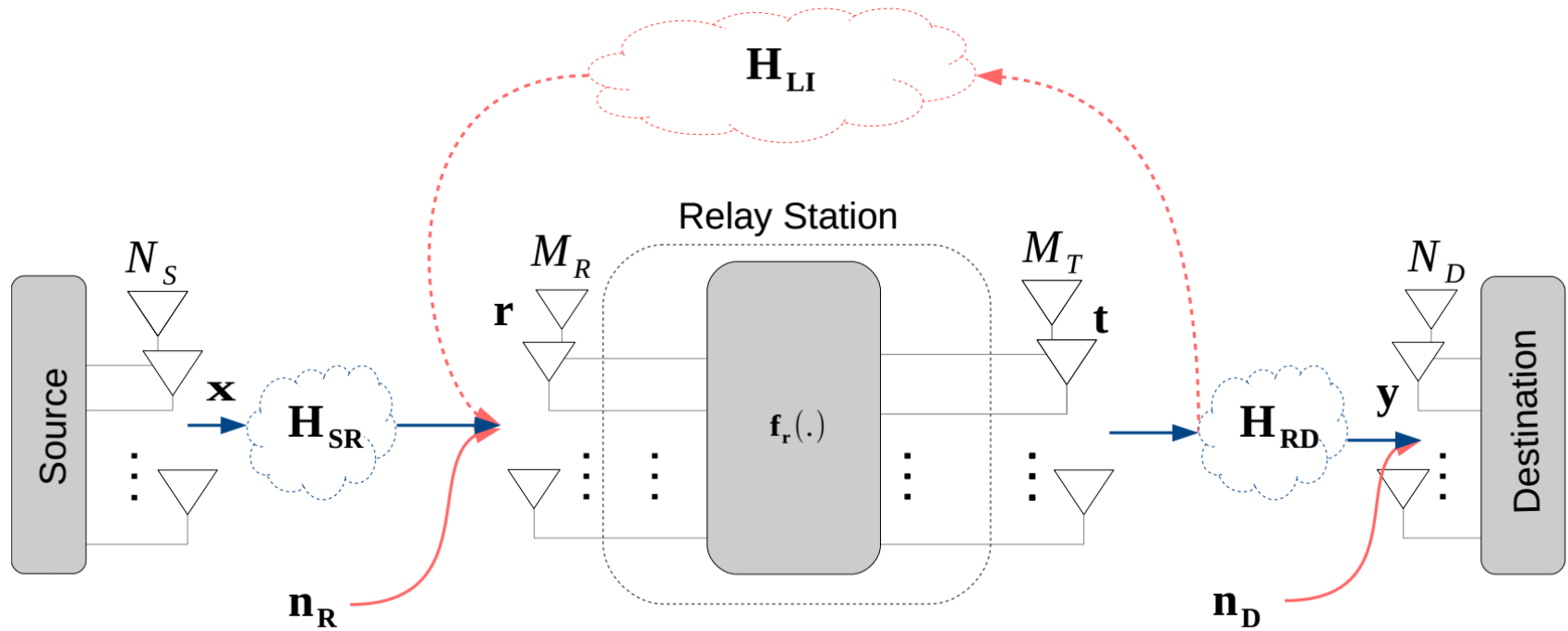
Andrea Goldsmith,

In *Wireless Communications*, Cambridge University Press, p. 454, 2003

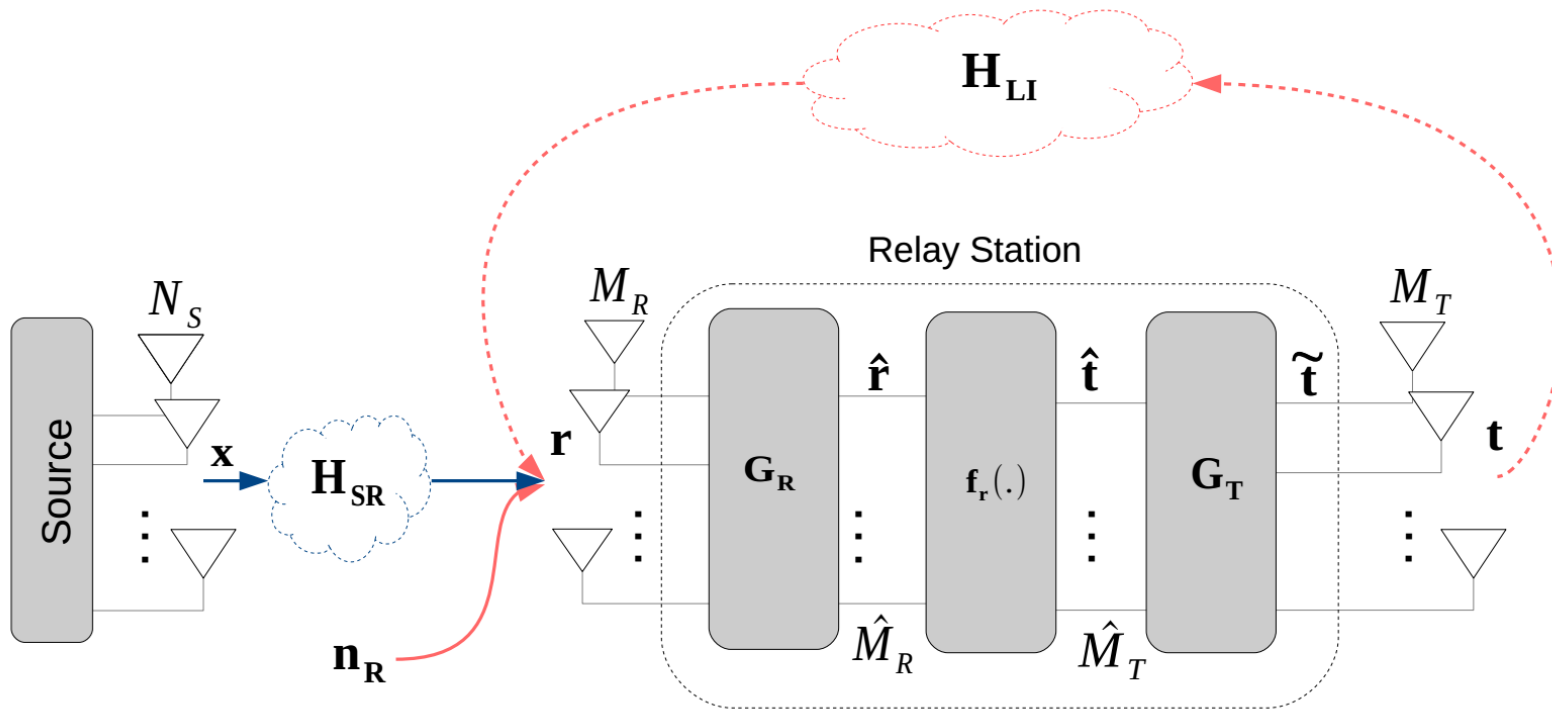
# Two possible antenna setups



# System model for in-band full-duplex with a relay station

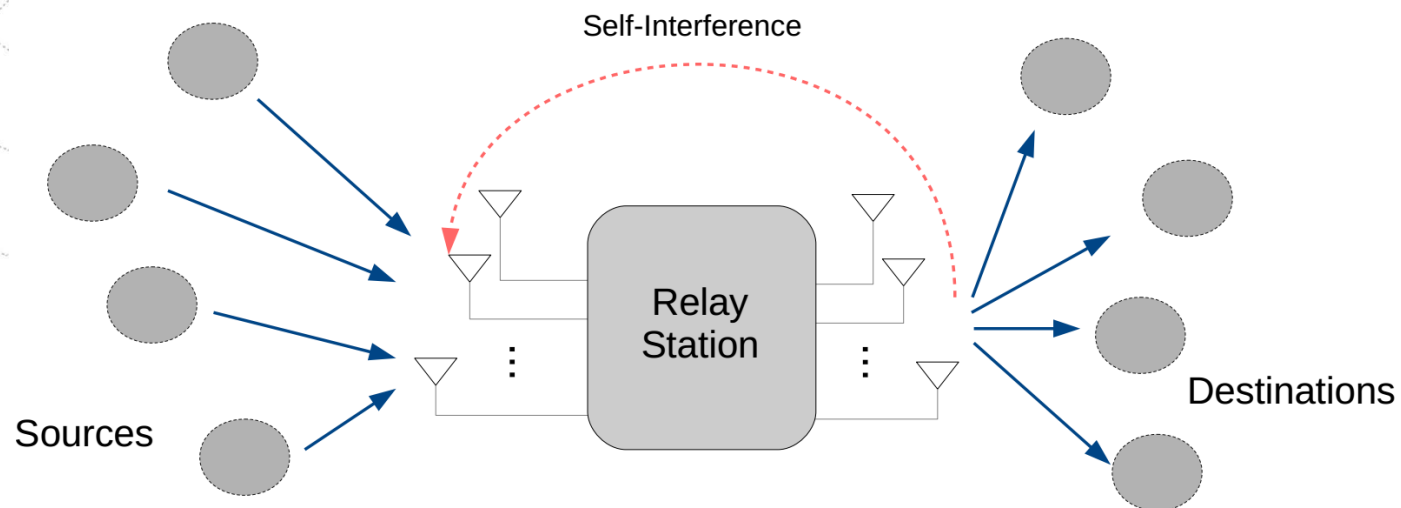


# Linear filter design for time-domain cancellation: receive filters and transmit filters



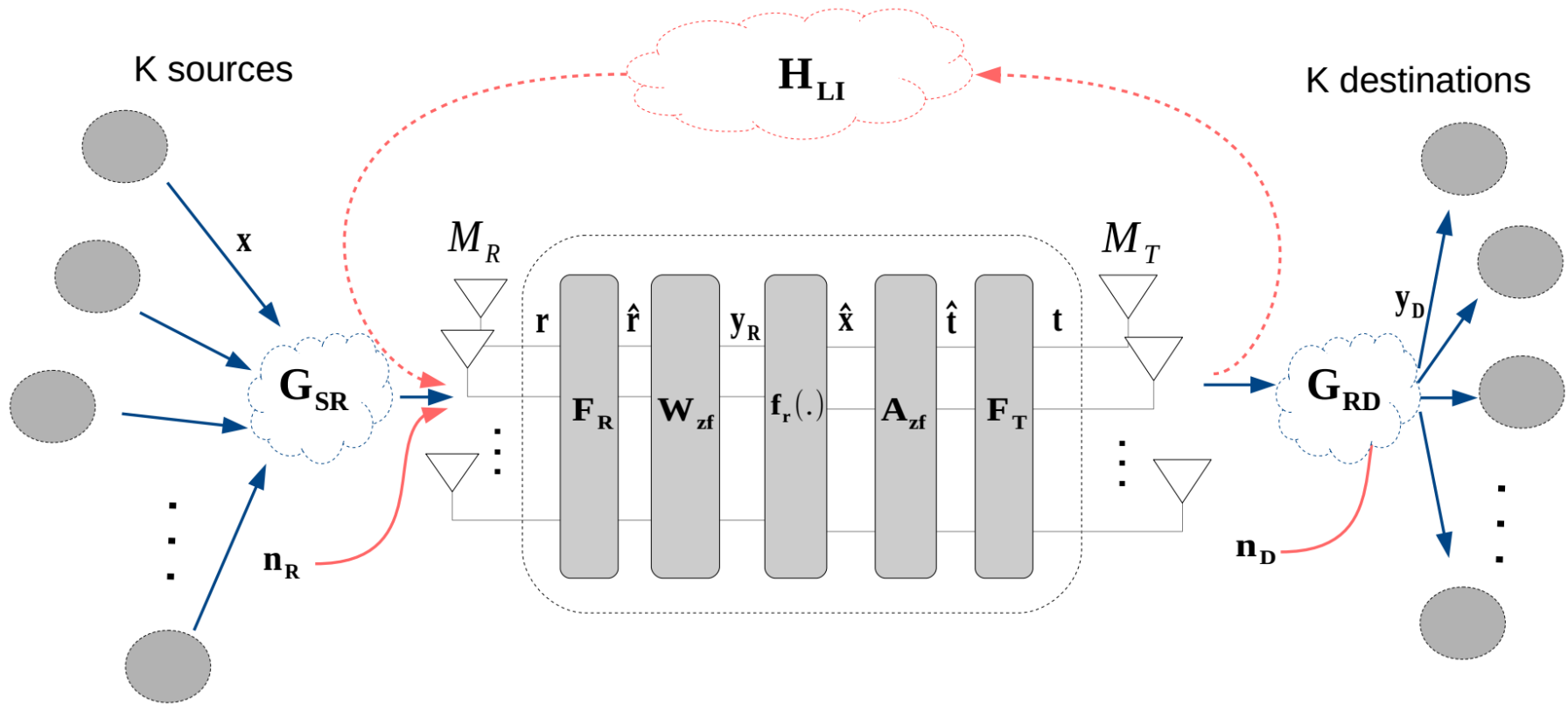


# Alternative application: multi-pairs with a full-duplex relay (1/2)



See e.g., [J. S. Lemos, F. Rosário, F. A. Monteiro, J. Xavier, A. J. Rodrigues, "**Massive MIMO Full-Duplex Relaying with Optimal Power Allocation for Independent Multipairs**", in Proceedings of SPAWC 2015, Stockholm, Sweden, June 2015.]

# Alternative application: multi-pairs with a full-duplex relay (2/2)



# Full-Duplex Relaying in MIMO-OFDM Frequency-Selective Channels with Optimal Adaptive Filtering

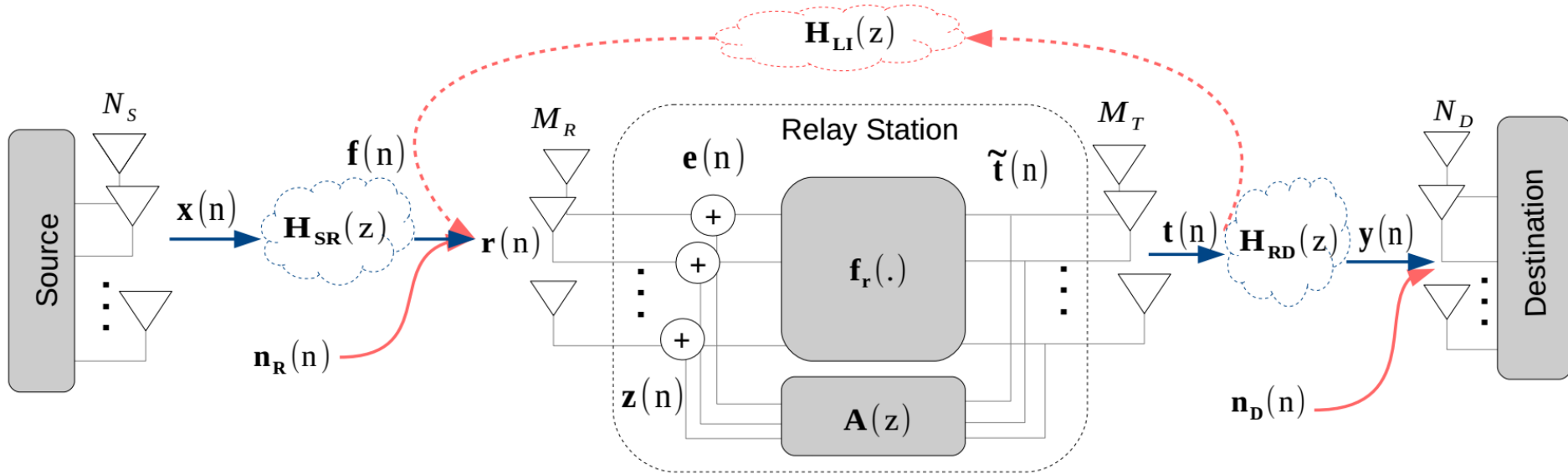
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# Proposal: feedback filtering for interference cancellation



$$\mathbf{q}(n) = \mathbf{H}_{SR}(z)\mathbf{x}(n) + \mathbf{H}_{LI}(z)\mathbf{t}(n) + \mathbf{n}_R(n),$$

$$\mathbf{y}(n) = \mathbf{H}_{RD}(z)\mathbf{t}(n) + \mathbf{n}_D(n),$$

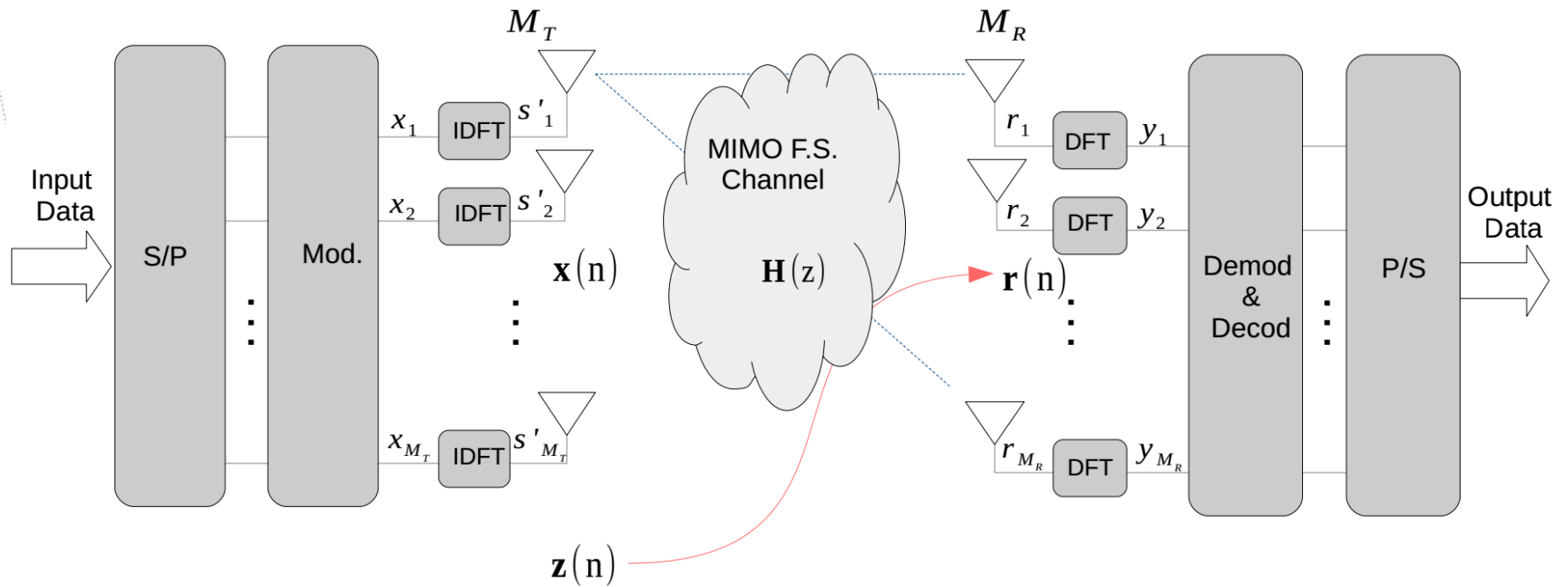
Minimum squared error

$$\widehat{MSE}_{RLS}(n, \mathbf{A}(z)) =$$

“Forgetting” factor

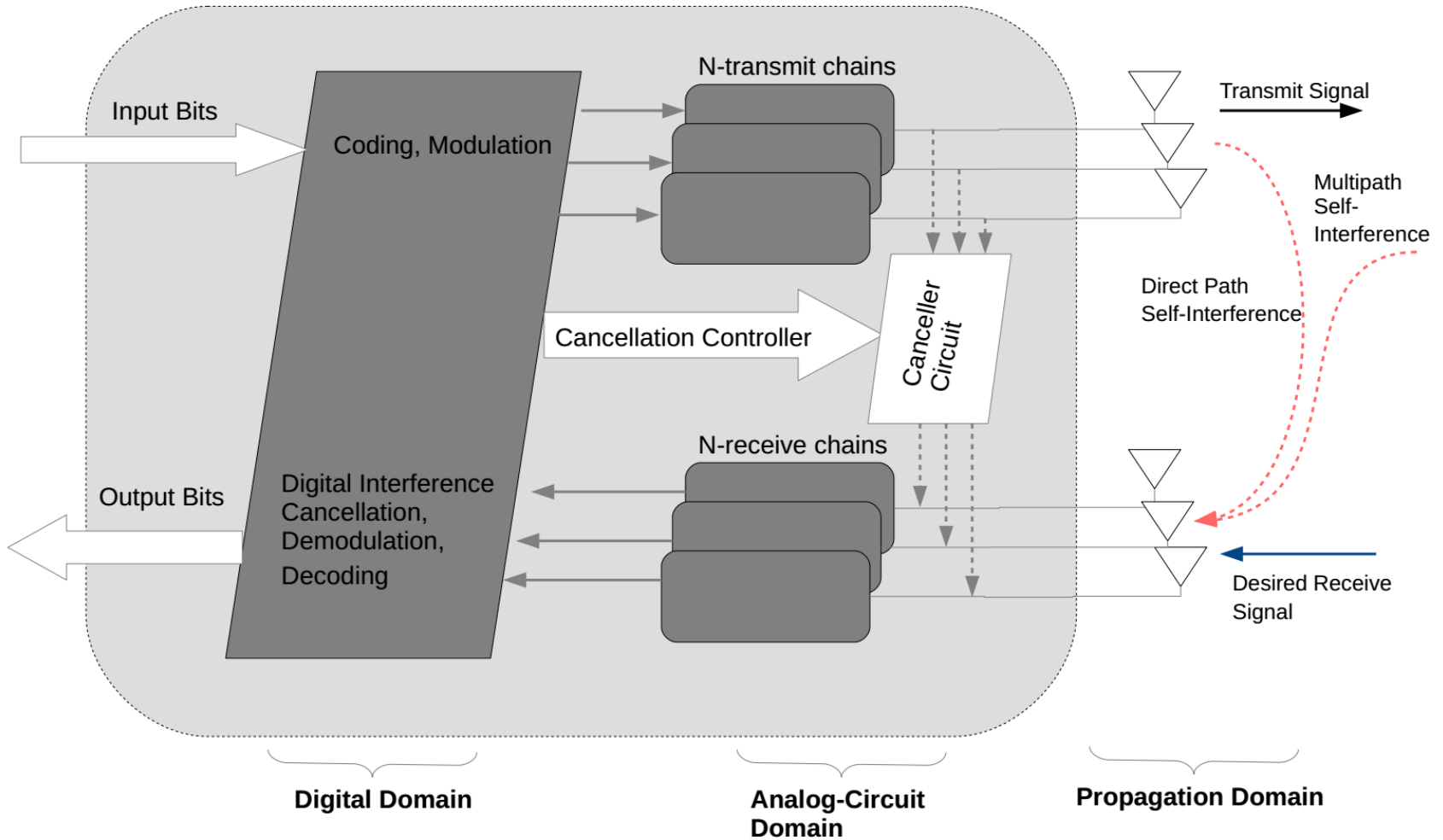
$$= \sum_{k=1}^n \lambda^{n-k} (\mathbf{f}(k) - \mathbf{A}(z)\tilde{\mathbf{t}}(k))^H (\mathbf{f}(k) - \mathbf{A}(z)\tilde{\mathbf{t}}(k))$$

# OFDM-MIMO is used in our scheme



# MIMO full-duplex device

## In-Band Full-Duplex Terminal



# Full-Duplex Relaying in MIMO-OFDM Frequency-Selective Channels with Optimal Adaptive Filtering

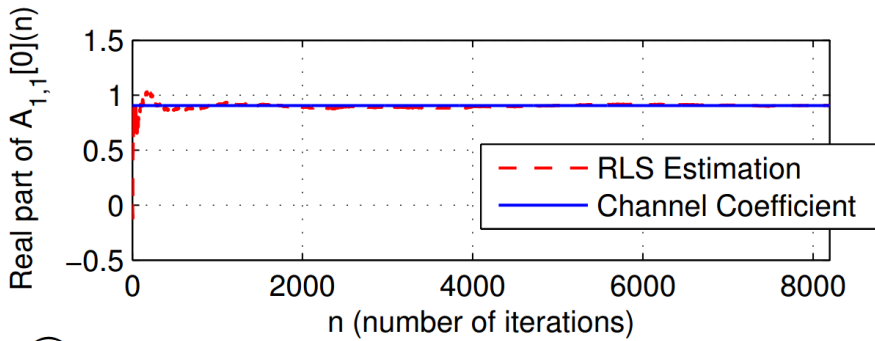
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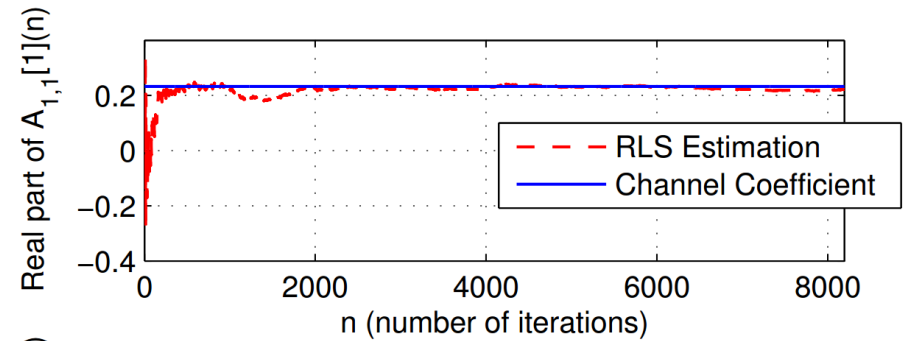
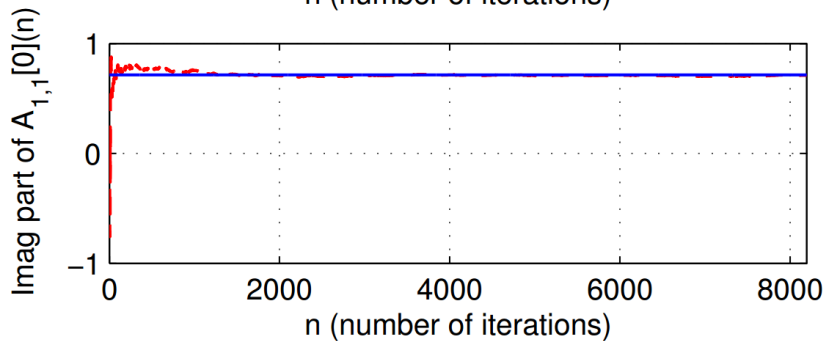
**3- Results**

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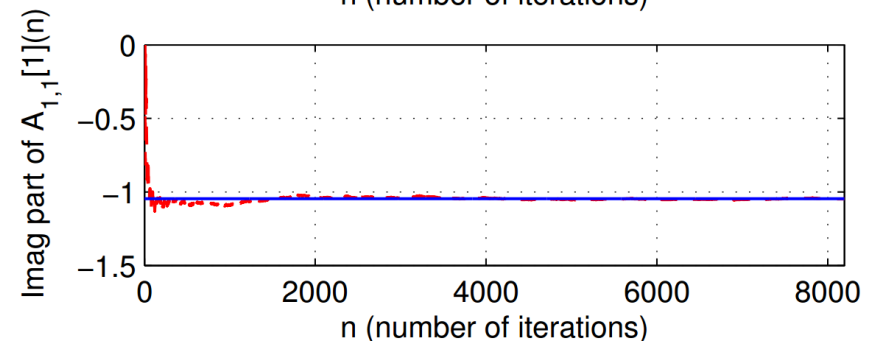
# RLS estimation of self-interference matrix coefficients (with 16-QAM)



(a)  $k = 0$



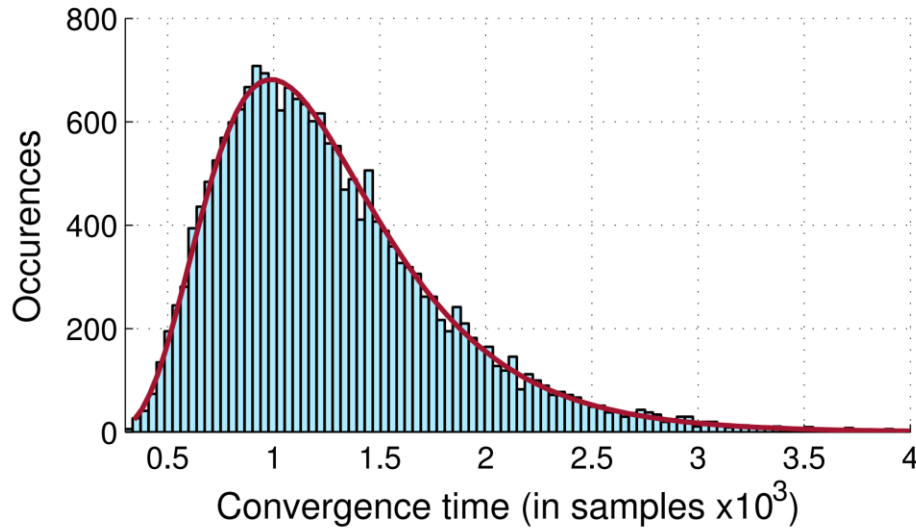
(b)  $k = 1$



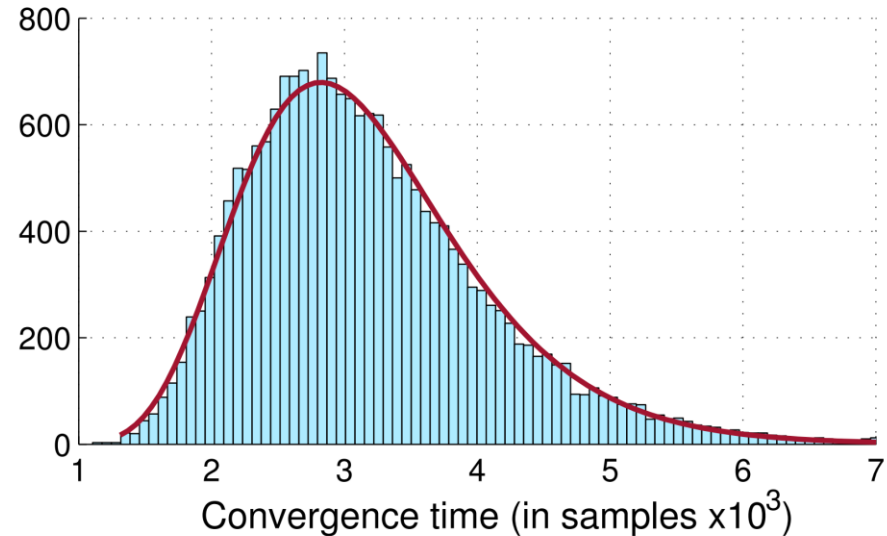
Note: the algorithms *always* converges.  
(Proof in the paper)



# Convergence “time” with 16-QAM



(a)  $L = 1$



(b)  $L = 3$

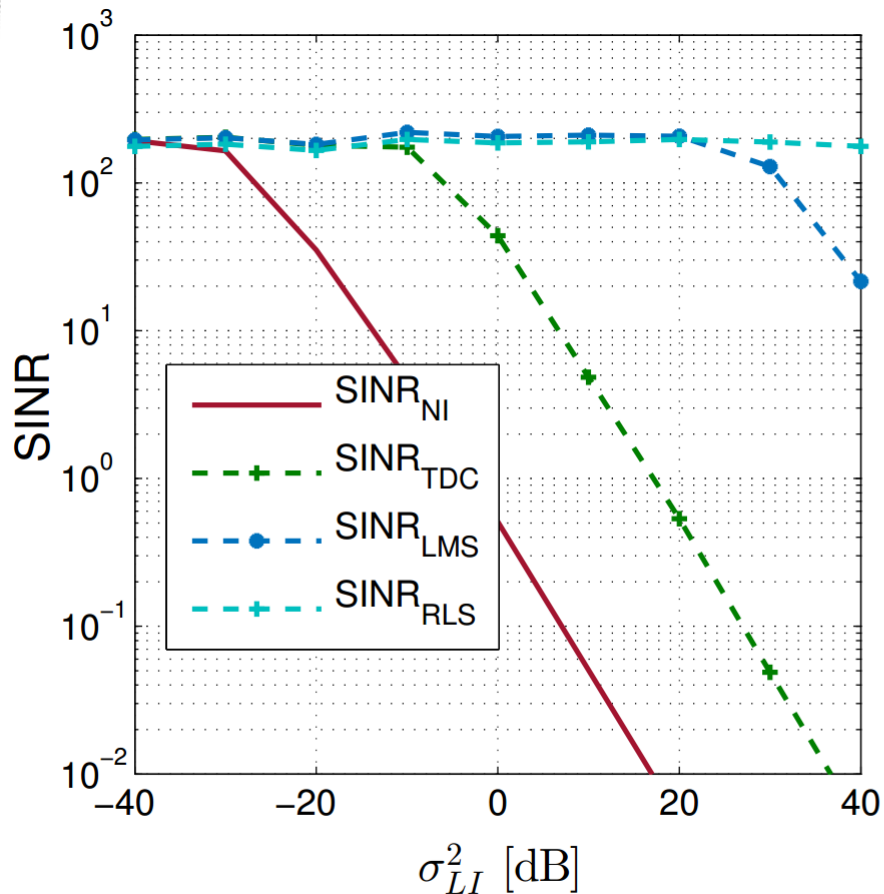
Error metric:

$$EM \leq \frac{\|\hat{\mathbf{A}}_{*,n} - \mathbf{H}_{\text{LI},*}\|_F^2}{\|\mathbf{H}_{\text{LI},*}\|_F^2}$$

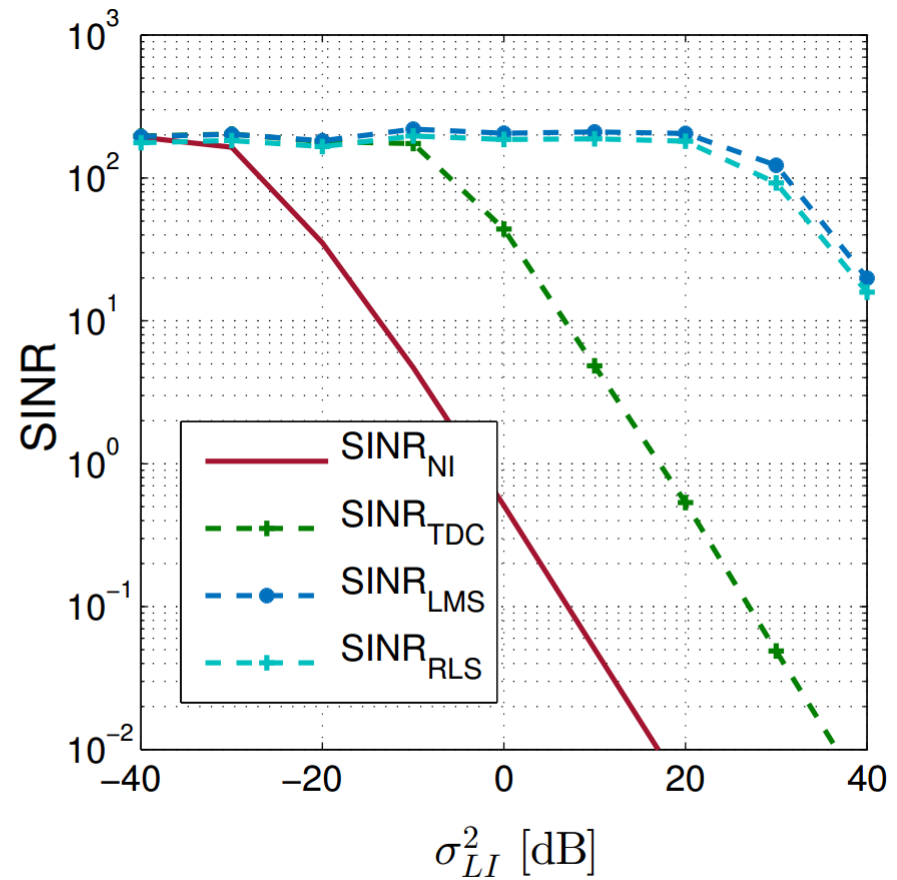
Notes:

- i) the  $EM$  for the steady state is  $-42$  dB, about (7dB better than with a LMS)
- ii) convergence considered @  $-30$ dB
- iii) a log-normal pmf is observed

# How loopback interference impacts on SINR

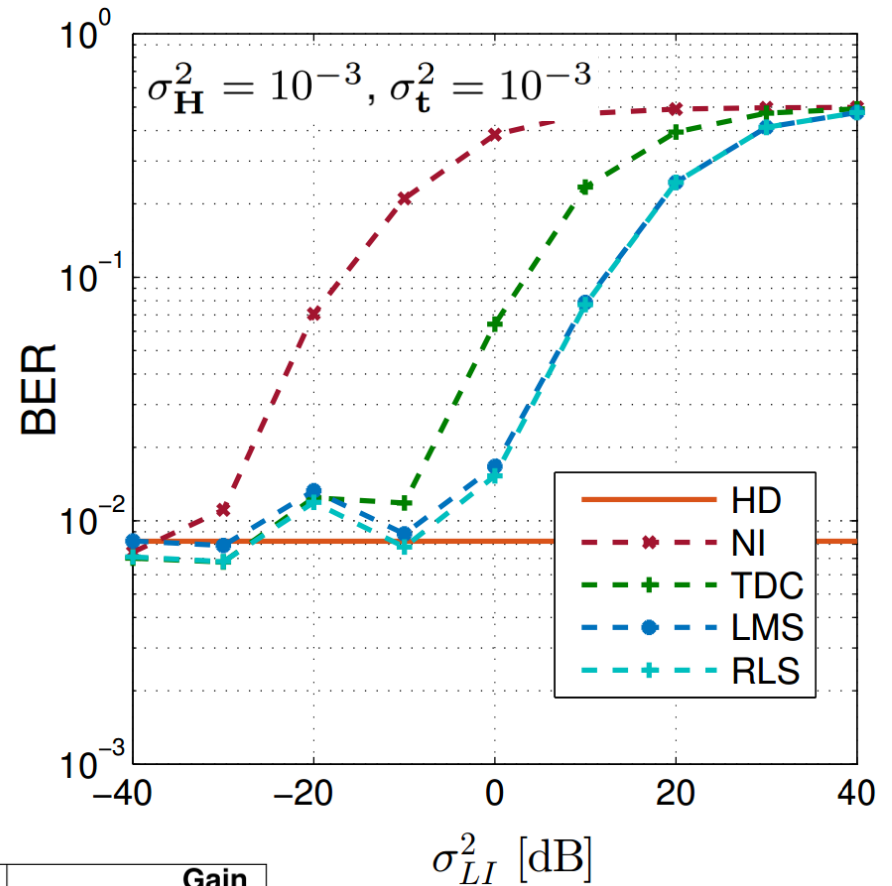
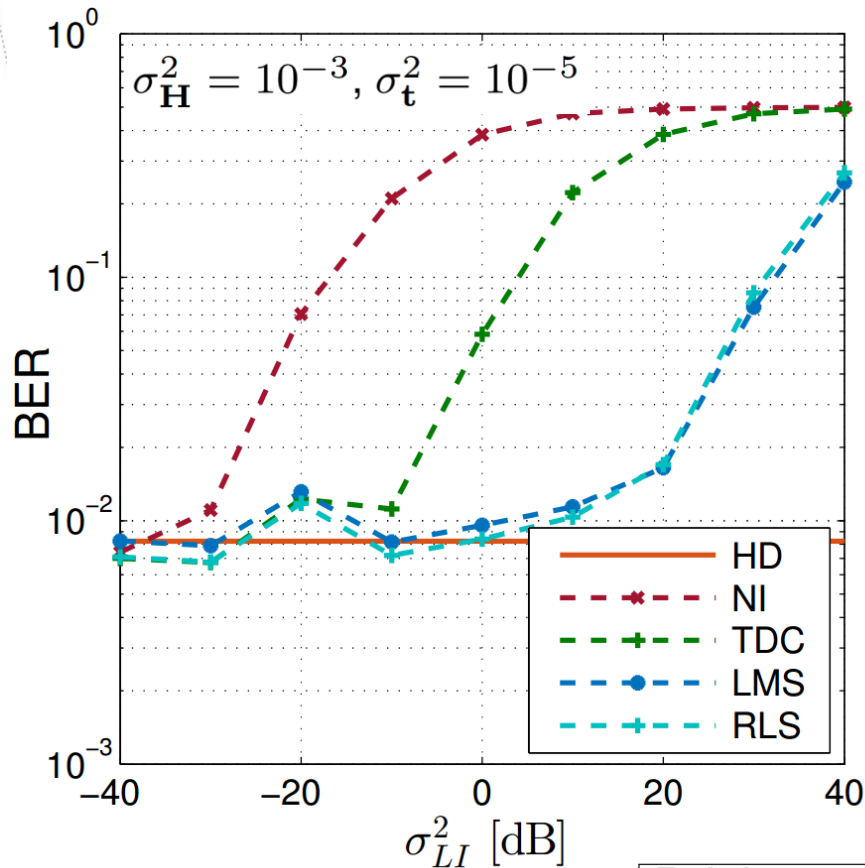


(a)  $\sigma_H^2 = 10^{-3}$ ,  $\sigma_t^2 = 10^{-5}$ .



(b)  $\sigma_H^2 = 10^{-3}$ ,  $\sigma_t^2 = 10^{-3}$ .

# Protection to self-interference as a BER “resilience gain”



Technique	Gain
Natural Isolation	Reference (0 dB)
NSP	-20 dB
MMSE	-25 dB
LMS	-30 to -40 dB
RLS	-30 to -40 dB
Perfect Cancellation	$-\infty$ dB

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# Conclusions

- Loopback self-interference cancelation is possible with Recursive Least Squares;
- RLS was derived for MIMO-OFDM  
*(we were not able to find this in the literature);*
- An update rule was derived;
- Convergence was proved and was always observed. Convergence time is negligible in comparison to the OFDM symbol length.

# Acknowledgements

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Francisco Monteiro (assistant prof.)

Ivo Sousa (post-doc)

António Rodrigues (group leader)



**Thank you**



**Back up slides**



# MIMO Processing for 4G and Beyond

Fundamentals  
and Evolution

Edited by  
Mário Marques da Silva  
Francisco A. Monteiro



Includes an introduction to  
*MIMO detection techniques*

*(CRC Press - Taylor and Francis, June 2014)*