

# **SIMPLE COOPERATIVE TRANSMISSION SCHEMES FOR UNDERLAY SPECTRUM SHARING USING SYMBOL-LEVEL PRECODING AND LOAD-CONTROLLED ARRAYS**

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# Outline

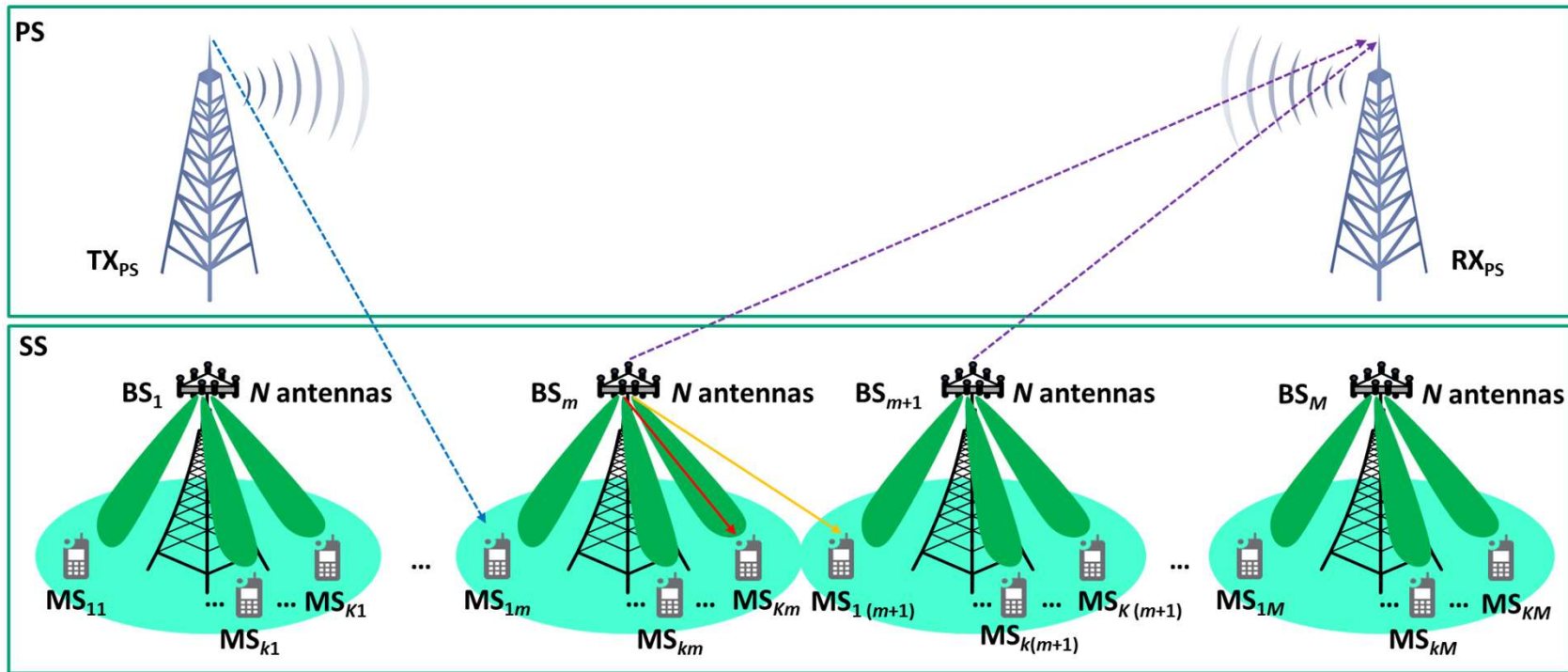
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## Introduction

- **Sub-6 GHz spectrum** will be an important part of the 5G landscape.
- The **scarcity of spectral resources** and the **stringent capacity requirements of 5G services**, though, necessitate the use of **spectral efficiency (SE) enhancement technologies**.
- Examples include **coordinated multi-point (CoMP)** and **spectrum sharing**.
- The combination of CoMP and underlay spectrum sharing promises substantial SE gains.
- **However, this concept has been largely overlooked in the literature.**
- The use of **load-controlled antenna arrays (LC-AA)** and **symbol-level (SL) precoding** can further enhance the performance of CoMP cellular networks.
- **Nevertheless, the corresponding research works do not consider a spectrum sharing setup.**
- **In this paper, we fill this gap in the literature.**
- **We focus on the use of standard precoding schemes and simple yet novel power allocation methods that can be applied in commercial setups.**

K. Ntougias, D. Ntaikos, C. B. Papadias, G. K. Papageorgiou, "Simple Cooperative Transmission Schemes for Underlay Spectrum Sharing Using Symbol-Level Precoding and Load-Controlled Arrays," *ICASSP*, Brighton, UK, May 12-17, 2019.

# System Setup



- Intra-System Intra-cell CCI
  - Intra-System Inter-cell CCI
  - Forward Inter-System CCI
  - Reverse Inter-System CCI
- PS: Primary System. SS: Secondary System.  
BS: Base Station. MS: Mobile Station.  
TX: Transmitter. RX: Receiver.  
CCI: Co-Channel Interference.

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## Signal and Channel Models

- The received signal at MS<sub>km</sub> is given by:

$$\begin{aligned}
 y_{km} = & (\mathbf{h}_{km}^m)^\dagger \mathbf{w}_{mk}^m \sqrt{P_{mk}^m} S_{mk}^m \\
 & + \sum_{\substack{i=1 \\ i \neq k}}^K (\mathbf{h}_{km}^m)^\dagger \mathbf{w}_{mi}^m \sqrt{P_{mi}^m} S_{mi}^m \\
 & + \sum_{\substack{j=1 \\ j \neq m}}^M \sum_{l=1}^K (\mathbf{h}_{km}^j)^\dagger \mathbf{w}_{jl}^j \sqrt{P_{jl}^j} S_{jl}^j \\
 & + h_{km} \sqrt{P} d + n_{km}
 \end{aligned}$$

Data

Intra-Cell CCI

Inter-Cell CCI

Reverse Inter-System CCI + Noise

- In matrix form:

$$\mathbf{y} = \mathbf{HWP}^{1/2} \mathbf{s} + \sqrt{P} \mathbf{h} d + \mathbf{n}$$

## Signal and Channel Models

- The received signal at  $RX_{ps}$  is given by:

$$y = \underbrace{g\sqrt{P}d}_{\text{Data}} + \sum_{m=1}^M \sum_{k=1}^K \underbrace{\mathbf{g}_m^\dagger \mathbf{w}_{mk}^m}_{\text{Forward Inter-System CCI}} \sqrt{P_{mk}^m} s_{mk}^m + \underbrace{z}_{\text{Noise}}$$

- Let us apply **Zero-Forcing (ZF) precoding** in a **spectrum-sharing agnostic manner**:

$$\mathbf{W}^{(\text{ZF})} = \mathbf{H}^\# = \mathbf{H}^\dagger (\mathbf{H}\mathbf{H}^\dagger)^{-1}$$

- Then both **the intra-cell and inter-cell CCI are eliminated** and the SINR at  $MS_{km}$  is given by:

$$\gamma_{km} = \frac{|(\mathbf{h}_{km}^m)^\dagger (\mathbf{w}_{mk}^m)^{(\text{ZF})}|^2 P_{mk}^m}{|h_{km}|^2 P + 1}$$

# Problem Formulation

$$\max_{P_{mk}^m} R = \sum_{m=1}^M \sum_{k=1}^K \log_2(1 + \gamma_{km})$$

**Sum-SE**

$$P_{mk}^m \geq 0$$

**Nonnegative Power Constraints**

$$\text{s.t.} \quad \sum_{k=1}^K P_{mk}^m \leq P_T$$

**Sum-Power Constraints**

$$\sum_{m=1}^M \sum_{k=1}^K \left| \mathbf{g}_m^\dagger(\mathbf{w}_{mk}^m)^{(\text{ZF})} \right|^2 P_{mk}^m \leq P_I$$

**Interference Power Constraint**

**Convex problem (thus having a unique solution), since ZF precoding eliminates the inter-user coupling through the interference components.**

## Solution

- **Interference-Constrained Power Allocation (ICPA):**

$$P_{mk}^m = \left( \frac{1}{\ln 2 (v_m + \mu \alpha_{mk}^m)} - \frac{1}{\lambda_{mk}^m} \right)^+ \quad (1)$$

$$\lambda_{mk}^m = \frac{|(\mathbf{h}_{km}^m)^\dagger (\mathbf{w}_{mk}^m)(ZF)|^2}{|h_{km}|^2 P + 1}$$

$$\alpha_{mk}^m = |\mathbf{g}_m^\dagger (\mathbf{w}_{mk}^m)(ZF)|^2$$

- **This power-allocation method can be applied heuristically for other linear precoding or even symbol-level precoding schemes as well.**



# Algorithm

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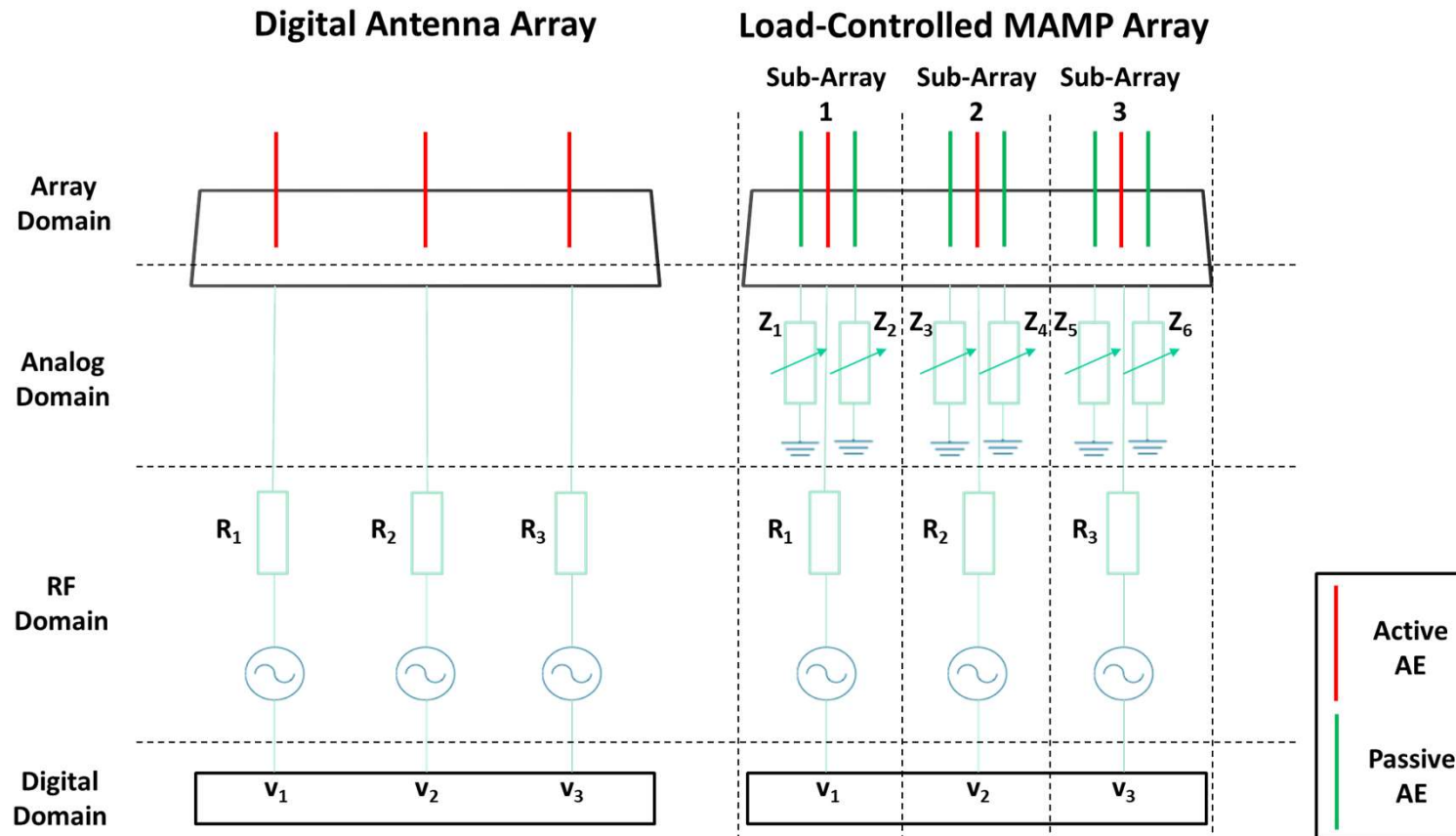
## Algorithm 1 ICPA Algorithm

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1: procedure ICPA( $\lambda_{mk}^m, \alpha_{mk}^m, P_T, P_I$ )
2:   Initialize:  $\mu_{\min}, \mu_{\max}$ 
3:   while  $|\mu_{\max} - \mu_{\min}| > \delta_\mu$  do
4:      $\mu = (\mu_{\min} + \mu_{\max}) / 2$ 
5:     for  $m = 1$  to  $M$  do
6:       Find min ( $\nu_m$ ),  $\nu_m \geq 0$  :
          $\sum_{k=1}^K (P_{mk}^m)^+ \leq P_T$ 
7:       Compute  $P_{mk}^m$  according to Eq. (1)
8:       if  $\sum_{m=1}^M \sum_{k=1}^K a_{mk}^m P_{mk}^m \geq P_I$  then
9:          $\mu_{\min} = \mu$ 
10:      else
11:         $\mu_{\max} = \mu$ 
12:   Output:  $P_{mk}^m, m = 1, \dots, M; k = 1, \dots, K$ 
```

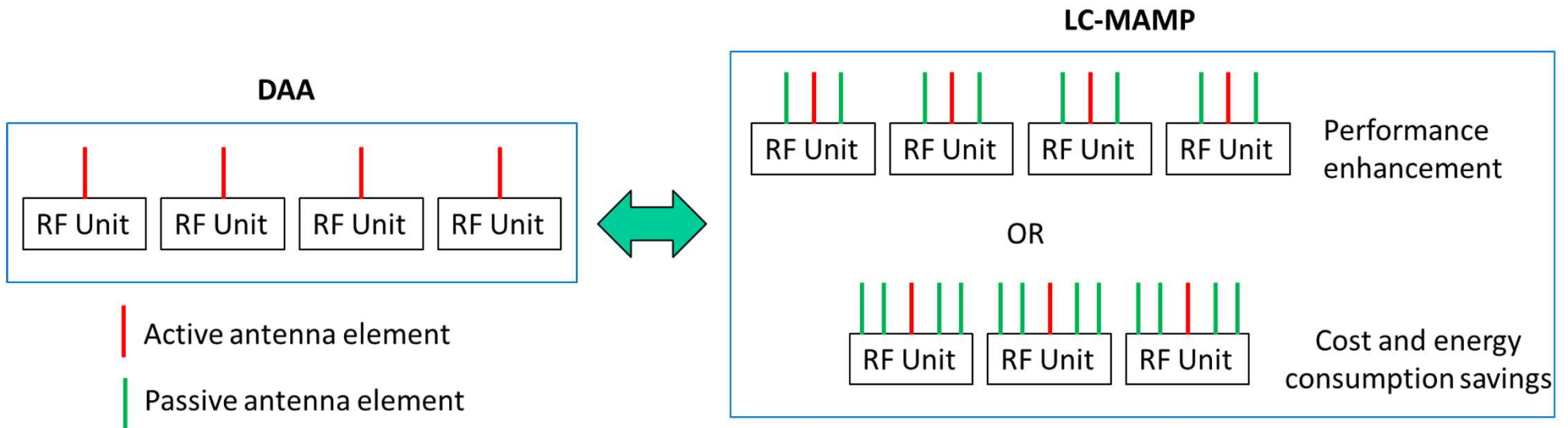
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# Load-Controlled Antenna Arrays (1/3)



K. Ntougias, D. Ntaikos, C. B. Papadias, G. K. Papageorgiou, "Simple Cooperative Transmission Schemes for Underlay Spectrum Sharing Using Symbol-Level Precoding and Load-Controlled Arrays," *ICASSP*, Brighton, UK, May 12-17, 2019.

# Load-Controlled Antenna Arrays (2/3)



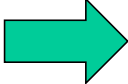
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## Load-Controlled Antenna Arrays (3/3)

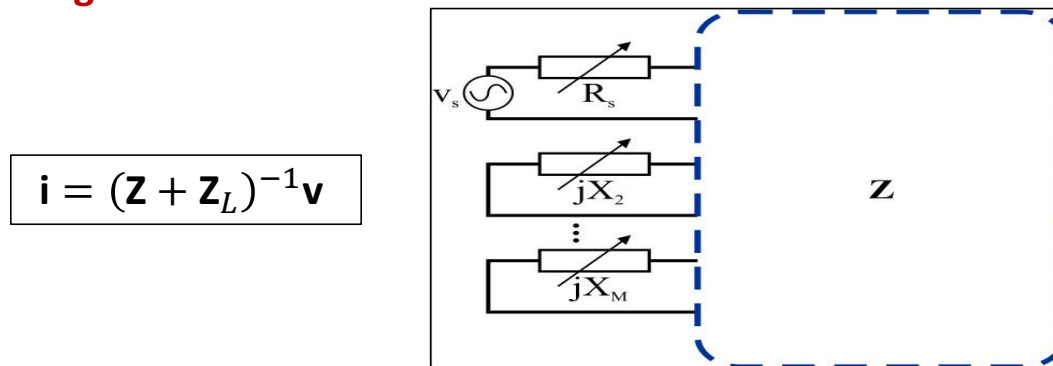
- We can perform channel-aware precoding with LC-AAs by **mapping the precoded signals onto the antenna currents:**

System model:  $\mathbf{y} = \mathbf{H}\mathbf{i} + \mathbf{n}$

Precoding:  $\mathbf{y} = \mathbf{H}\mathbf{W}\mathbf{s} + \mathbf{n}$


 $\mathbf{i} = \mathbf{W}\mathbf{s}$

- Then, we have to **calculate the corresponding loading values that will generate these currents through the generalized Ohm's law:**



- However, we should ensure that the real part of the input impedance (which depends on the loads and, therefore, on the precoded signal) is positive to achieve high radiation efficiency.

# Joint Beam Selection and Precoding (JBSP)

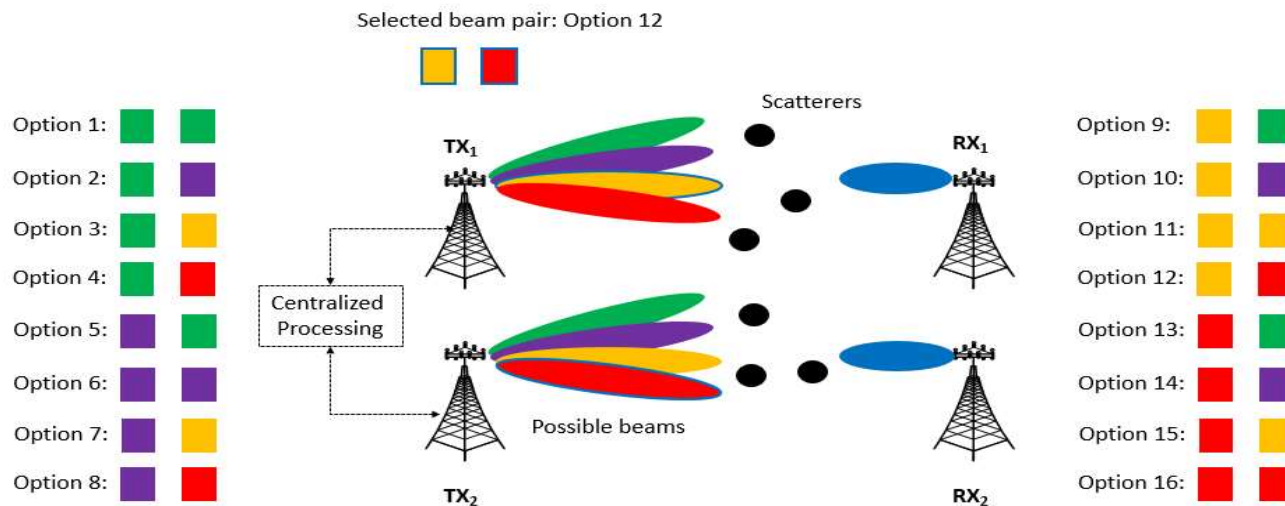
1. **Learning:** The MSs report the channel estimates or the SINR for each beam combination.
2. **Beam Selection:** The best beam combination (in terms of sum-SE) is selected.
3. **Transmission:** Precoded signals are transmitted over the selected beams.

### Beamforming: Analog domain (loads).

- Admits any input signal.
- Beam selection to improve performance.

### Precoding: Digital domain (baseband).

- Full control.
- Inter-BS cooperation to improve performance.



## Symbol-Level ZF Precoding

- This precoding scheme “zero-forces” only the destructive interference (at **symbol level**) and leaves unaffected the **constructive interference**.
- **It improves the performance in the low-SNR regime.**
- **Calculation of the precoding matrix symbol-by-symbol** (Binary Phase Shift Keying (BSPK) input assumed, i.e.,  $s_i = \pm 1$ ):

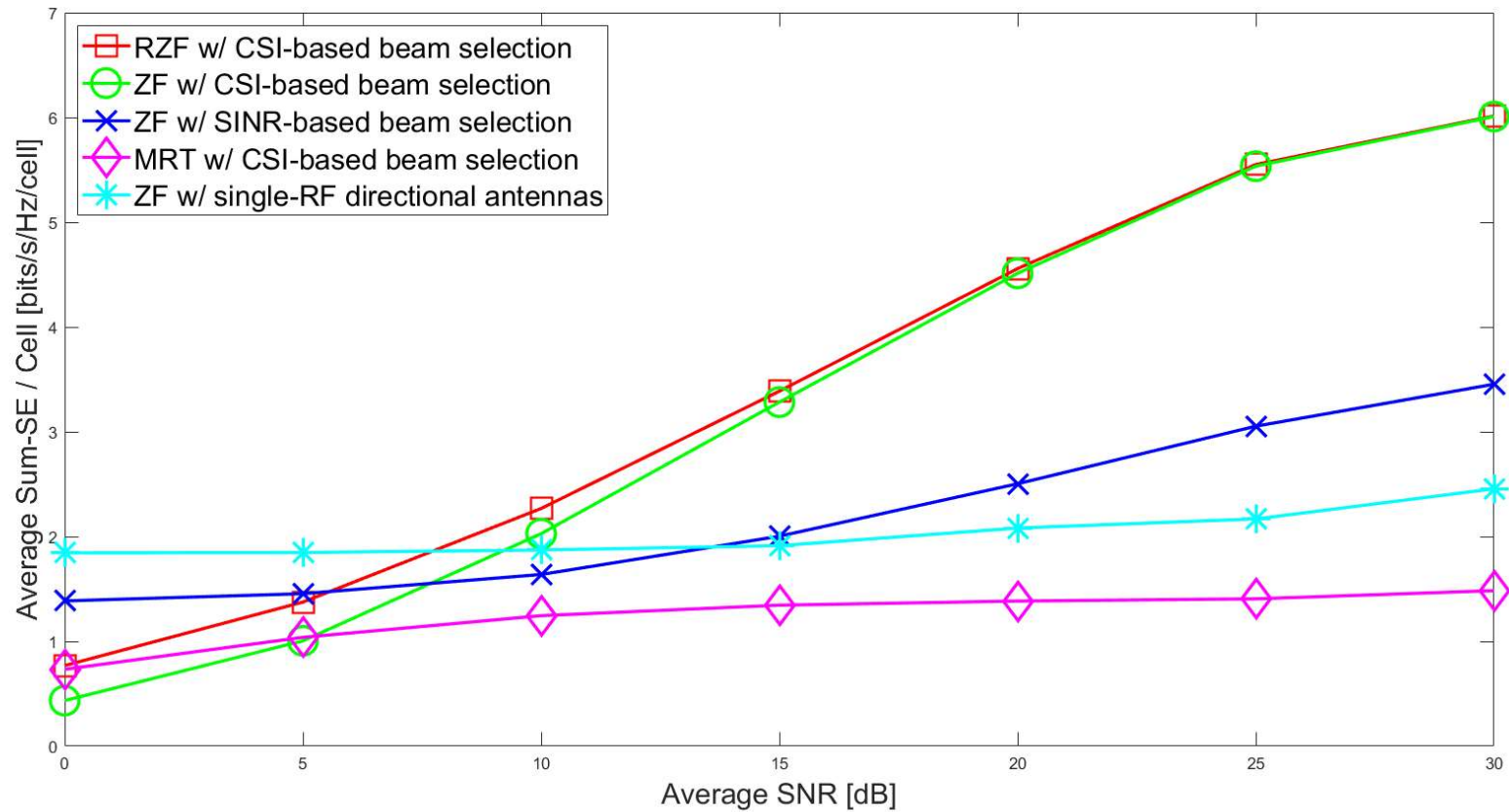
$$\mathbf{W}^{(\text{CIZF})} = \mathbf{W}^{(\text{ZF})} \mathbf{T} = \mathbf{H}^\dagger \mathbf{R}^{-1} \mathbf{T}$$

$$\mathbf{R} = \mathbf{H} \mathbf{H}^\dagger$$

$$\mathbf{G} = \text{diag}(\mathbf{s}) \text{Re}(\mathbf{R}) \text{diag}(\mathbf{s})$$

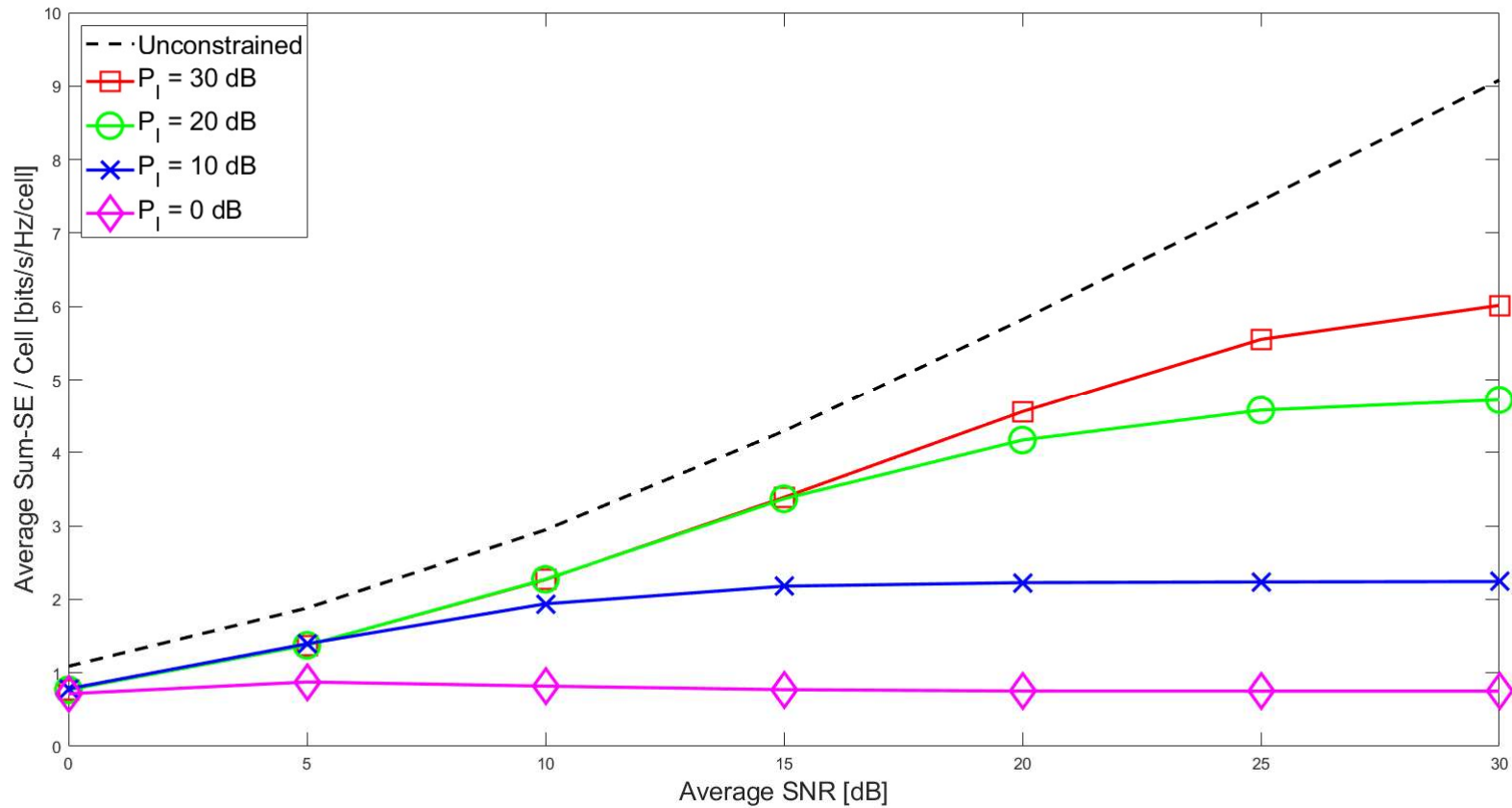
$$\begin{cases} \tau_{kk} = \rho_{kk} \\ \tau_{km} = 0 & \text{if } g_{km} < 0 \\ \tau_{km} = \rho_{km} & \text{otherwise} \end{cases}$$

# Performance Evaluation via Numerical Simulations (1/3)



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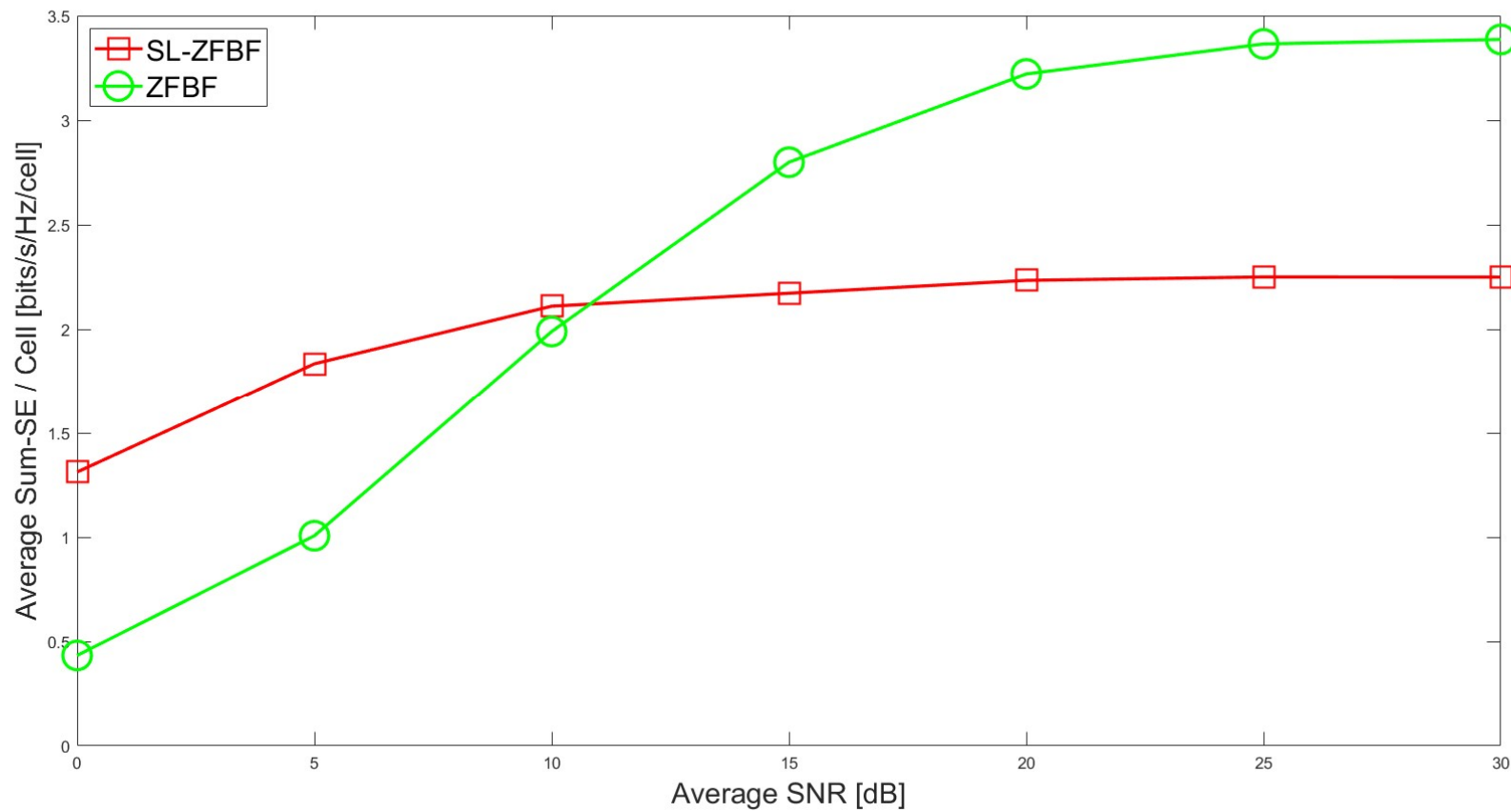
# Performance Evaluation via Numerical Simulations (2/3)



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# Performance Evaluation via Numerical Simulations (3/3)



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## Summary and Conclusions

- A **coordinated beamforming (CBF)** and **interference-constrained power allocation (ICPA)** strategy that **maximizes the sum-SE** of cellular networks in **underlay spectrum sharing** setups has been derived in this work.
- The application of **standard linear precoding schemes** has been considered (**MRT, ZF, RZF**).
- Also, the use of **SL ZF precoding** which **exploits the constructive symbol-level interference to improve the performance at the low SNR regime** has been studied.
- Furthermore, a **joint beam selection and precoding (JBSP)** method that enables us to perform **arbitrary channel-dependent precoding with LC-AAs** is presented.
- This method performs beamforming in the analog domain followed by beam selection (switching) and digital precoding to **overcome the load computation difficulties**.
- Load-controlled antenna arrays **improve the performance** for a target cost and energy consumption (# of RF chains) thanks to their **higher array gain / narrower beams**.
- **Numerical simulations** indicate that this technique performs significantly well for **small-to-moderate IPT values** and highlight the **performance gains of LC-AAs and SL precoding**.

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