

Introduction

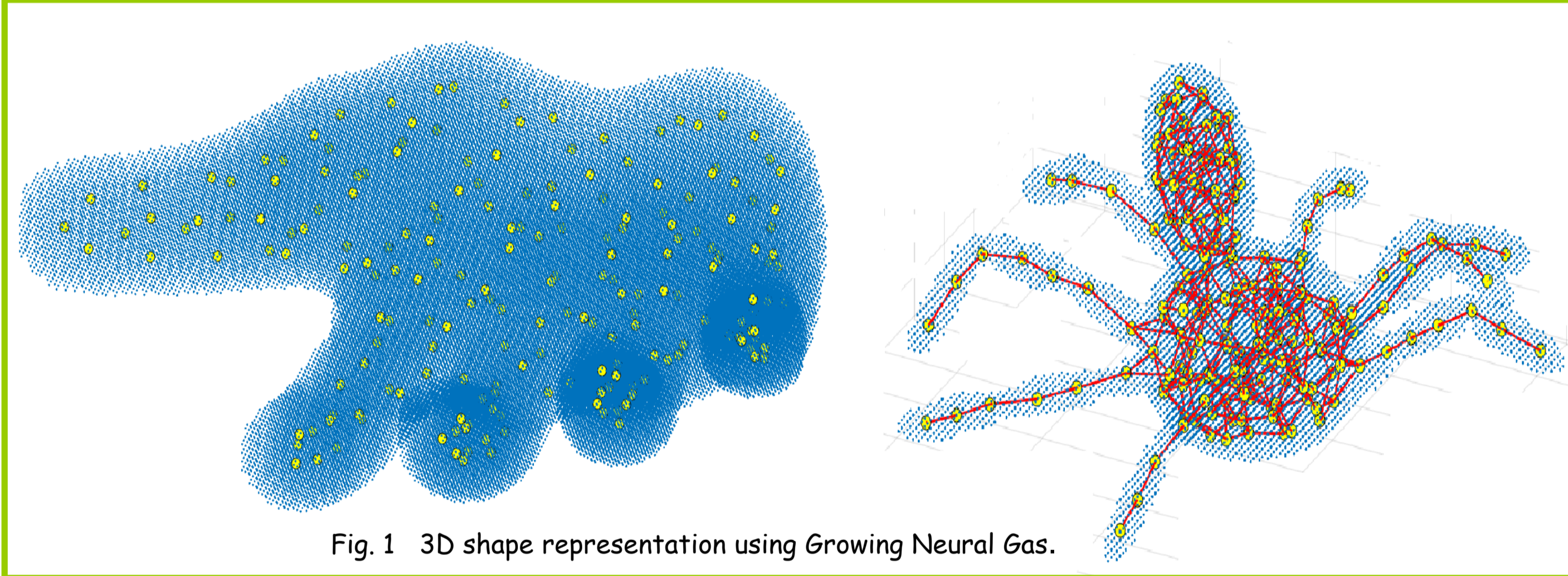
- This work aims to develop an optimal model for 3D shape recognition with high level of accuracy, real-time operation and invariant to the angle-of-view changes.
- The current works on 3D shapes recognition, such as, deep learning, model-based, feature-based, shows good improvements in the recognition level. However, high similarities and different angles of view remain a challenge to these recognition methods.
- Graphs and complex networks display useful topological features based on the types of connection between their elements. Such features include degree distribution, clustering coefficient, and hierarchical structure.
- This paper proposes a new method to represent the 3D shapes by capturing local variations into the feature representation.
- The main contributions from this work are:
 - A new method for graph formulation with adaptive connectivity to represent 3D shapes preserving both local and global characteristics of the shape.
 - The proposal of a new set of graph spectral features based on the node distribution of the adaptive graph for 3D shape representation.

The proposed method

The proposed method consists of four stages: 1) shape representation, 2) adaptive graph connectivity modification, 3) feature extraction and 4) the classification process.

1- Shape representation

- A 3D shape consists of a point cloud contain a large number of points on the 3D Cartesian plane.
- Therefore, we use Growing Neural Gas (GNG) to reduce the complexity and to get the same number of pixels for each shape.
- At the end of the training process, the GNG should satisfactory cover the shape regions as can be seen in Fig. 1



2- Graph decomposition

We can represent the nodes on the surface as an undirected graph, $G = \{V, \epsilon, A\}$, where V is the set of N vertices, ϵ is the set of edges and A is the adjacency matrix with edge weights. We consider ϵ as the Euclidean distance between nodes because it is invariable to rotation and translational operations. We define the weight, $A_{i,j}$ corresponding to $\epsilon_{i,j}$ connecting between vertices i and j as follows:

$$A_{i,j} = \begin{cases} \epsilon_{i,j} & \text{If nodes } i \text{ and } j \text{ are connected} \\ 0 & \text{Otherwise} \end{cases}$$

We also define the signal $r: \nu \rightarrow \mathbb{R}$, where i^{th} component represents the Euclidean distance from the centre $(0,0,0)$ to the vertex i in ν .

$$r_i = \sqrt{x_i + y_i + z_i}$$

The degree matrix $D_{i,j}$ is calculated as shown.

$$D_{i,j} = \sum_{j=0}^{N-1} A_{i,j}$$

The graph Laplacian matrix is then calculated, as follows:

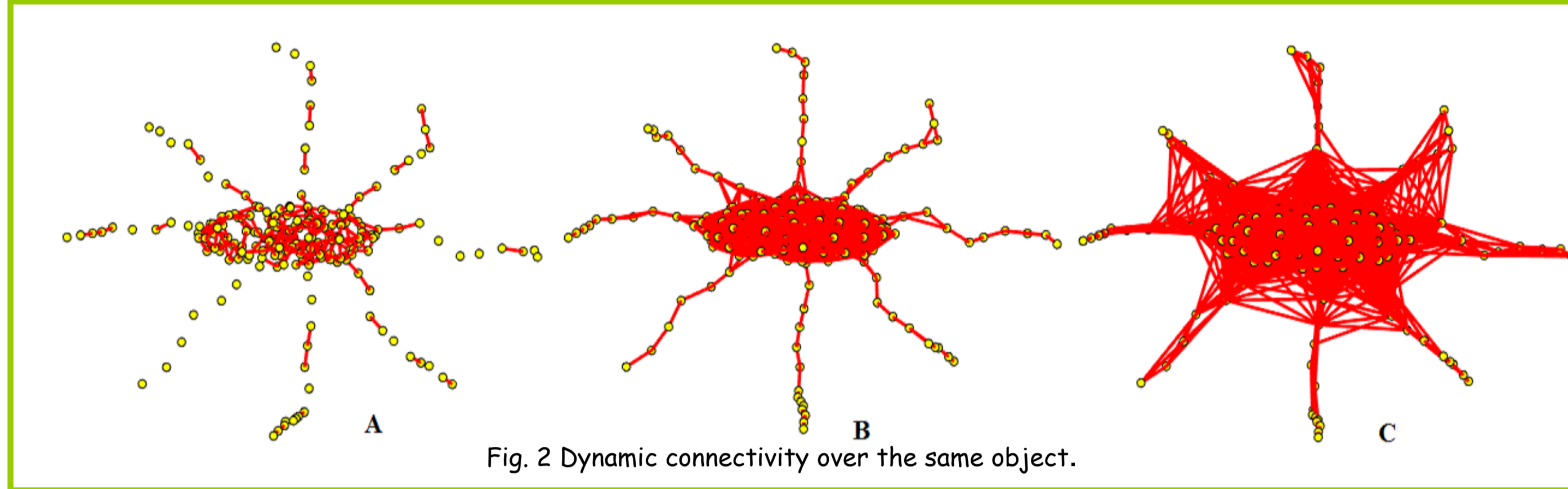
$$L = D - A$$

Since, L is symmetrically positive, there exists a real unitary matrix, U , that diagonalizes L , such that $U^t L U = \Lambda = \text{diag} \{ \lambda_j \}$ is a non-negative diagonal matrix, leading to an eigenvalue decomposition of L matrix as follows:

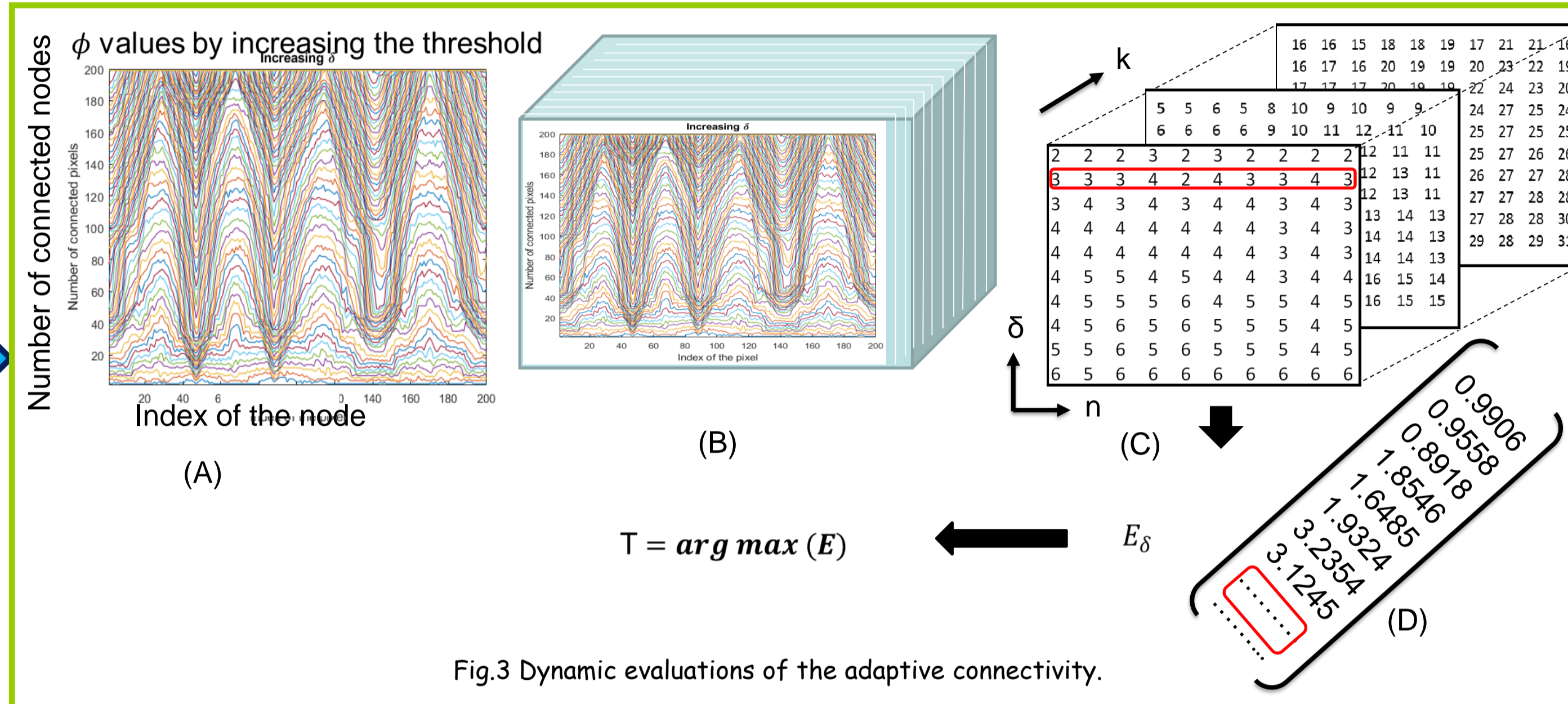
$$L = U^t L U = \sum_{i=0}^{N-1} \lambda_i u_i u_i^t$$

u_i is the column vectors of U , and λ_i are a set of orthonormal eigenvectors of L with corresponding eigenvalues, as follows: $0 = \lambda_0 < \lambda_1 < \lambda_2 \dots < \lambda_{N-1} = \lambda_{max}$

- Initially, a graph is generated over the candidate nodes using GNG.
- We begin with the minimum fully connectivity. Then, we continue increase the links between the nodes as shown in Fig.2 .



- At each level, we compute the variance of the node distribution.
- At the end, we take into account the level, which provides the maximum variance as shown in fig. 3



Algorithm 1 also shows how to obtain the optimal connectivity level.

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1- For  $i = 0 : (m-1)$  do
2-    $P_i \leftarrow$  Shape representation as  $(x_i, y_i, z_i)$ .
3-    $t \leftarrow$  Minimum distance to link pixels as a one group.
4-   For  $\delta = 0 : (N-1)$  do
5-      $\Phi_\delta \leftarrow$  Compute the node distribution at  $\delta$ .
6-      $B \leftarrow \frac{\Phi_\delta}{\max(\Phi_\delta)}$ 
7-      $\sigma_\delta^2 \leftarrow$  Compute the variance of  $B$ .
8-   End
9-    $T_i \leftarrow \text{Max}(\sigma^2)$ 
10- End
    
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3- Feature extraction

We propose the following three features taking global and local details into account.

$$F_1 = \frac{\Phi_\delta}{\max(\Phi_\delta)} \quad F_2 = r_i \lambda_i$$

$$F_3 = \left\{ \underbrace{\frac{\sum_{i=0}^{N-1} B_i}{N}}_{\text{Mean}}, \underbrace{\frac{1}{N-1} \sum_{i=1}^N |B_i - \mu|}_{\text{Variance}}, \underbrace{\sum_{i=0}^{N-1} B_i \log_2 \frac{1}{B_i}}_{\text{Entropy}}, \underbrace{\sqrt{\sum_{i=0}^{N-1} B_i^2}}_{\text{L2-Norm}} \right\}$$

4- Classification

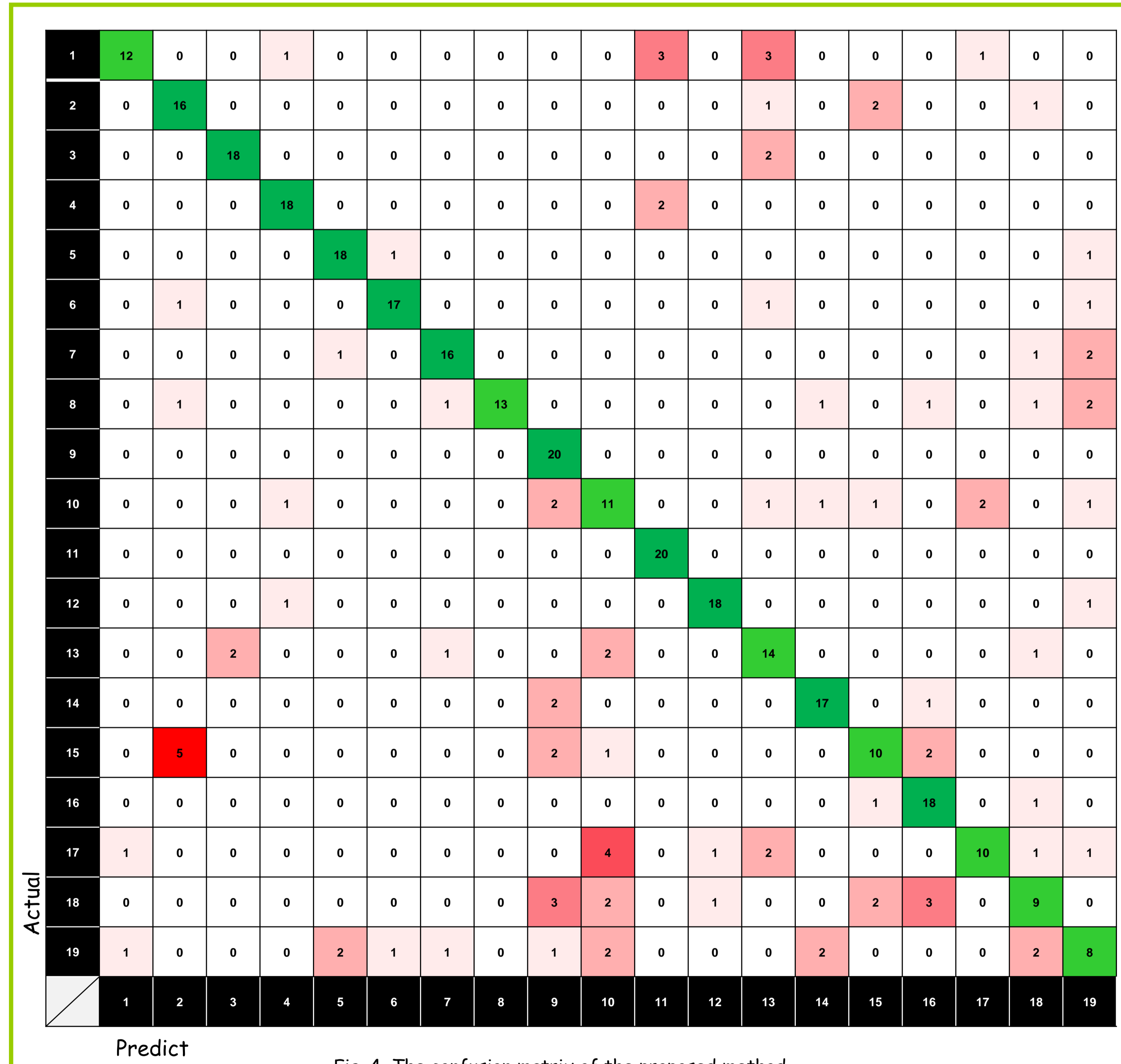
- The total length of the features is $(2N + 4)$.
- In the final step, these features are concatenated and categorised using k-Nearest Neighbour classifier (KNN).

Performance evaluation

- The proposed method was tested on a variety of shapes using artificial 3D shape dataset: A benchmark for 3D mesh segmentation (X. Chen et al (2009)). This dataset contains 19 classes with 20 samples per class giving 380 shapes in total.
- These classes include: Human, Cup, Glasses, Airplane, Ant, Chair, Octopus, Table, Teddy bear, Hand, Plier, Fish, Bird, Mech, Bust, Armadillo, Bearing, Vase, and Four Leg respectively.
- The experiment was implemented using MatLab R2018a Intel processor, CPU@3.6GHz and RAM 16GB.
- We reduce the number of pixels for all shapes into $N = 200$ using GNG.
- The average speed of the training and testing 380 samples was 6.3 seconds, which is fast for such a large amount of data and the average time for testing a new one sample is 12 milliseconds.
- Compared with the state-of-the-art methods, our algorithm demonstrates a high performance by recording the highest level of accuracy (74.47%) as shown in Table 1.
- Fig.4 shows the confusion matrix of our proposed method. For more details, please visit <http://tiny.cc/demo3d>

Table.1 Comparison with the state-of-the-art studies.

Method	Classification score (%)
M. Ankerst, et al (1999) (3D shape histogram)	43.42
R. Osada, et al (2002) Shape distribution	67.37
G. E. da Silva and A. R. Backes (2018) Complex network	70.79
The proposed method	74.47



Conclusions

- We have proposed a new 3D shape recognition method based on local details.
- Our approach includes a proposal of a new method for graph formulation with adaptive connectivity to represent 3D shapes preserving both local and global characteristics of the shape .
- This is followed by a new set of graph spectral and node domain features based on the node distribution of the adaptive graph for 3D shape representation.
- The performance evaluation based on one of the most challenging 3D dataset showed that the proposed method exceeded the existing node distribution methods by 4%.