

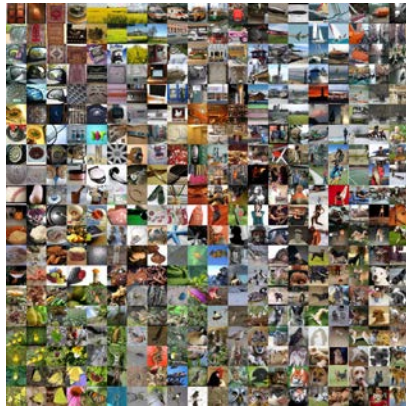
# Enhancing External learning with Internal Training Paradigm

**Methodical Design and Trimming of Deep Learning Networks: Enhancing External BP learning with Internal Omnipresent-Supervision Training Paradigm**

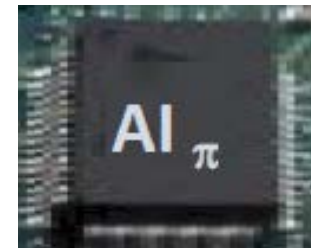
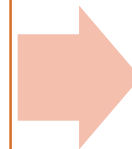
S. Y. Kung

Zejiang Hou  
Princeton

Yuchen Liu



Automatic Bigdata Deep  
Compiler (ABDC)



**Dedication: In fond memory of Jan Larsen (1965-2018).**

# Four (DONA) Gaps Differentiating Generalization from Optimization:

- **D: Data/Model Gap:  $x'$** 
  - *Data Augmentation*
  - *Image/Speech Variations*
- **O: Optimization Metric Gap:  $J'$** 
  - *External Optimization Metric (EOM)*
  - *Internal Optimization Metric (IOM)*
- **N: Net Capacity Gap:  $\theta' \Rightarrow (N, P)$** 
  - *Growing*
  - *Cherry Picking*
  - *Pruning Oversized Net*

• **A: Algorithmic Gap ( $P$ : parameter sub-optimization)**

- *Regularization: Explicit and our Implicit methods*

$\text{SubMax}_{\theta'} J'(\theta'; x')$

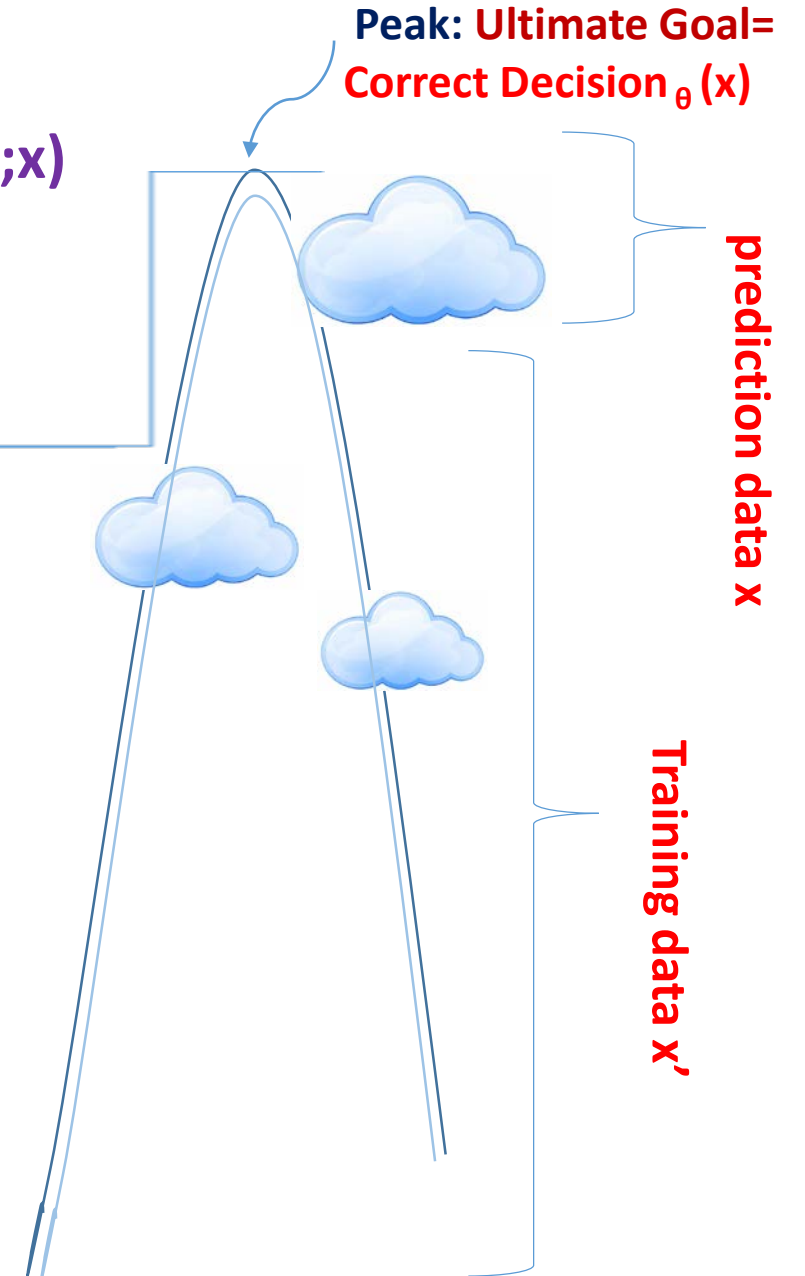
$\text{Max}_{\theta'} J'(\theta'; x')$

$\text{Max}_{\theta} J'(\theta; x')$

$\text{Max}_{\theta} J(\theta; x')$

$\text{Max}_{\theta} J(\theta; x)$

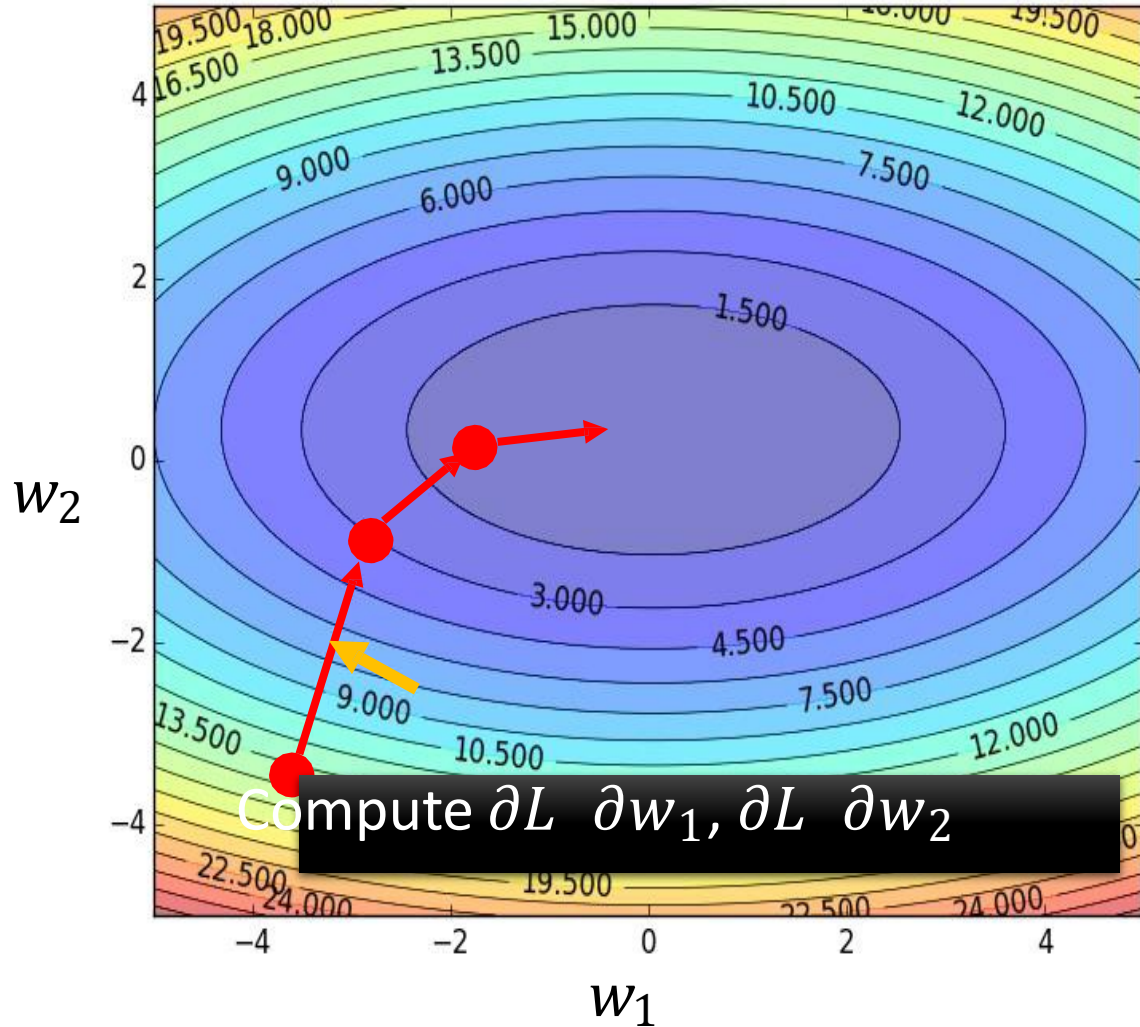
Peak: Ultimate Goal=  
Correct Decision  $\theta(x)$



- Current: Parameter Learning Only (**External BP**)
- Ours: Both Parameter/Structure Learning

Parameter Learning:

**EOM Gradient Descent**

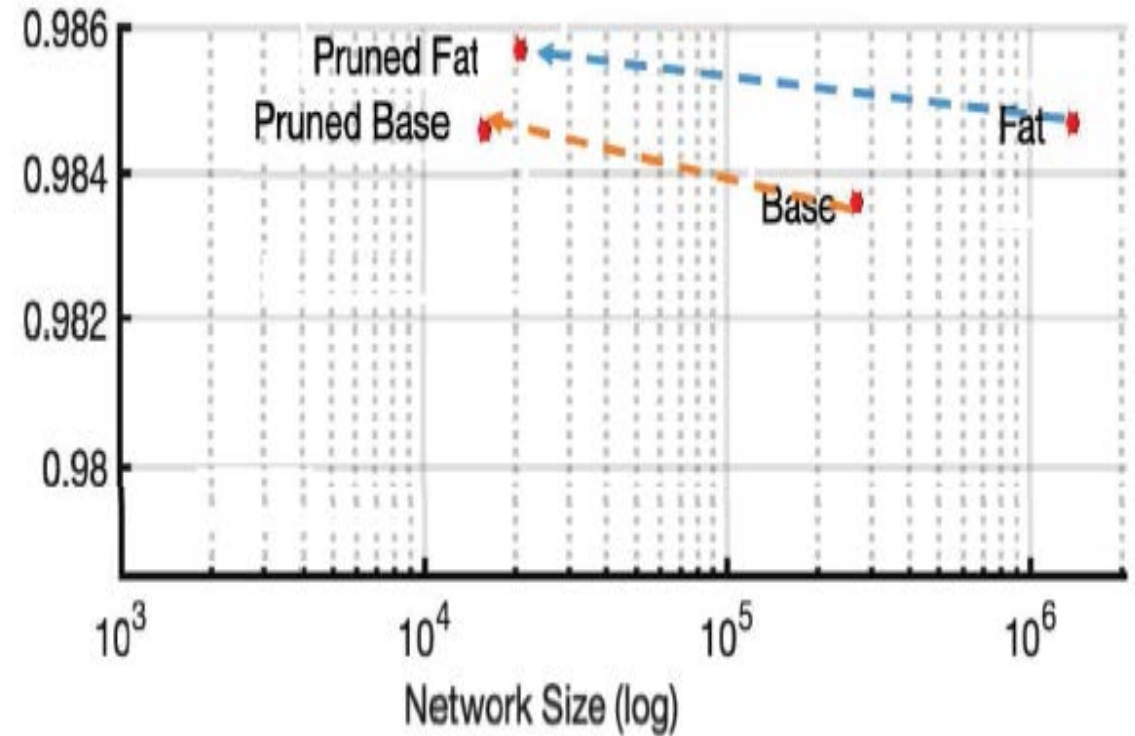


+

Structural Learning:

**IOM Guided Adaptation**

Lenet300 on MNIST

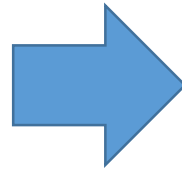
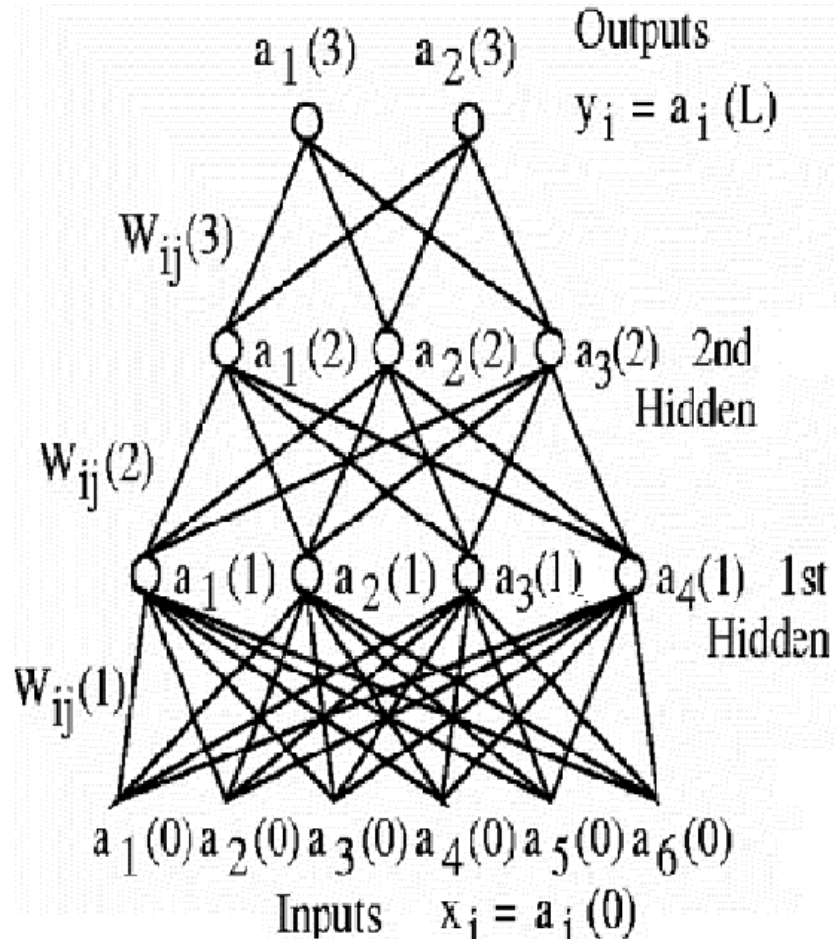


Structural characterization:

- The number of layers in the model.
- The number of nodes in each layer.

# Internal Node Evaluation/Ranking (INER)

*Nodes/Layers Treated Equally!*

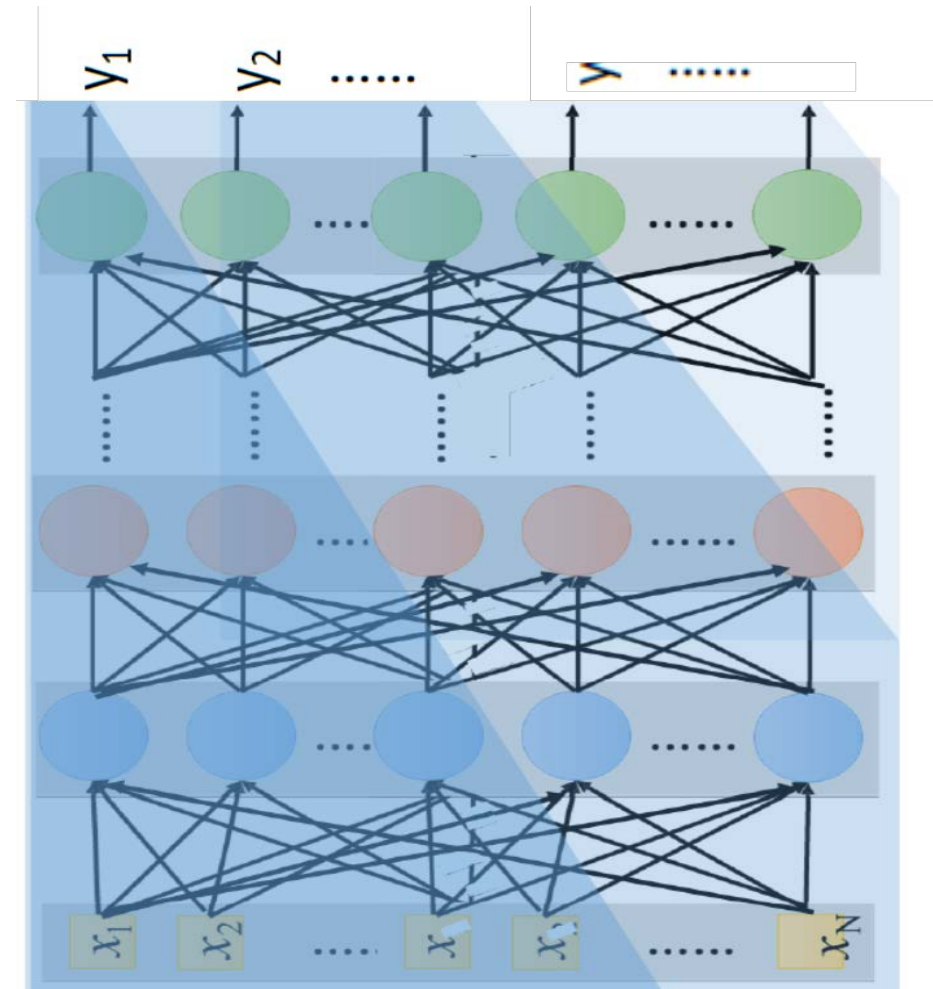


*Ranking of Layers:*

*Vertical Structural Training*

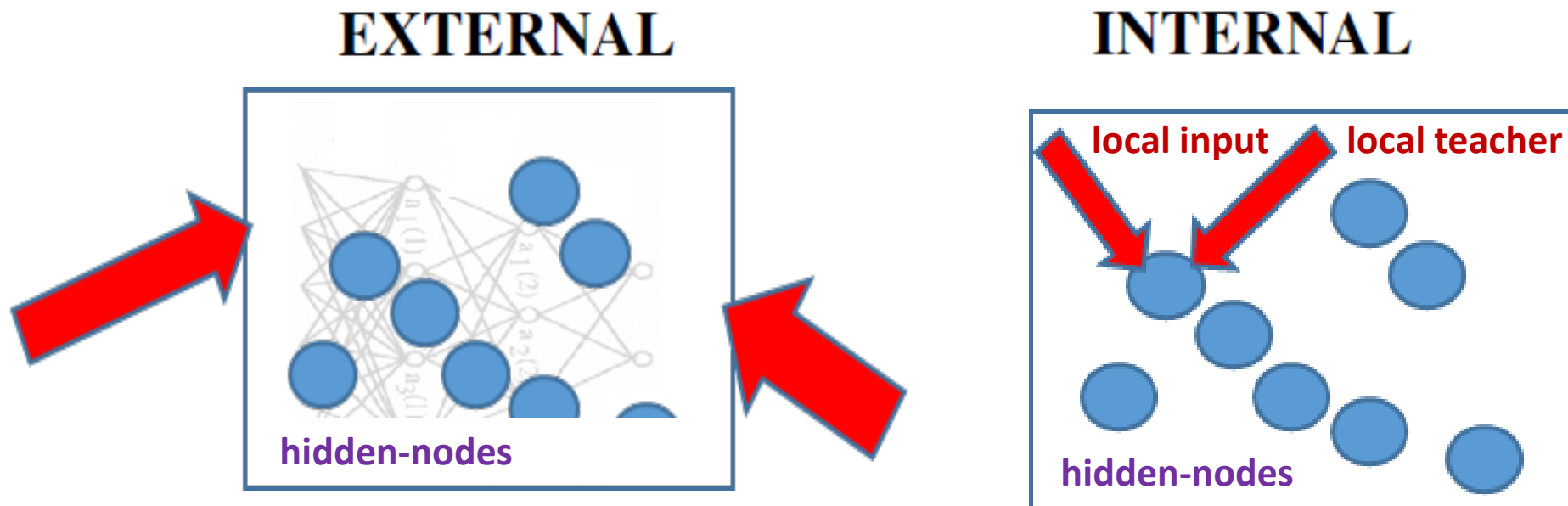
*Ranking of Nodes:*

*Horizontal Structural Training*



The internal learning paradigm allows us to evaluate/train hidden layers/nodes for directly.

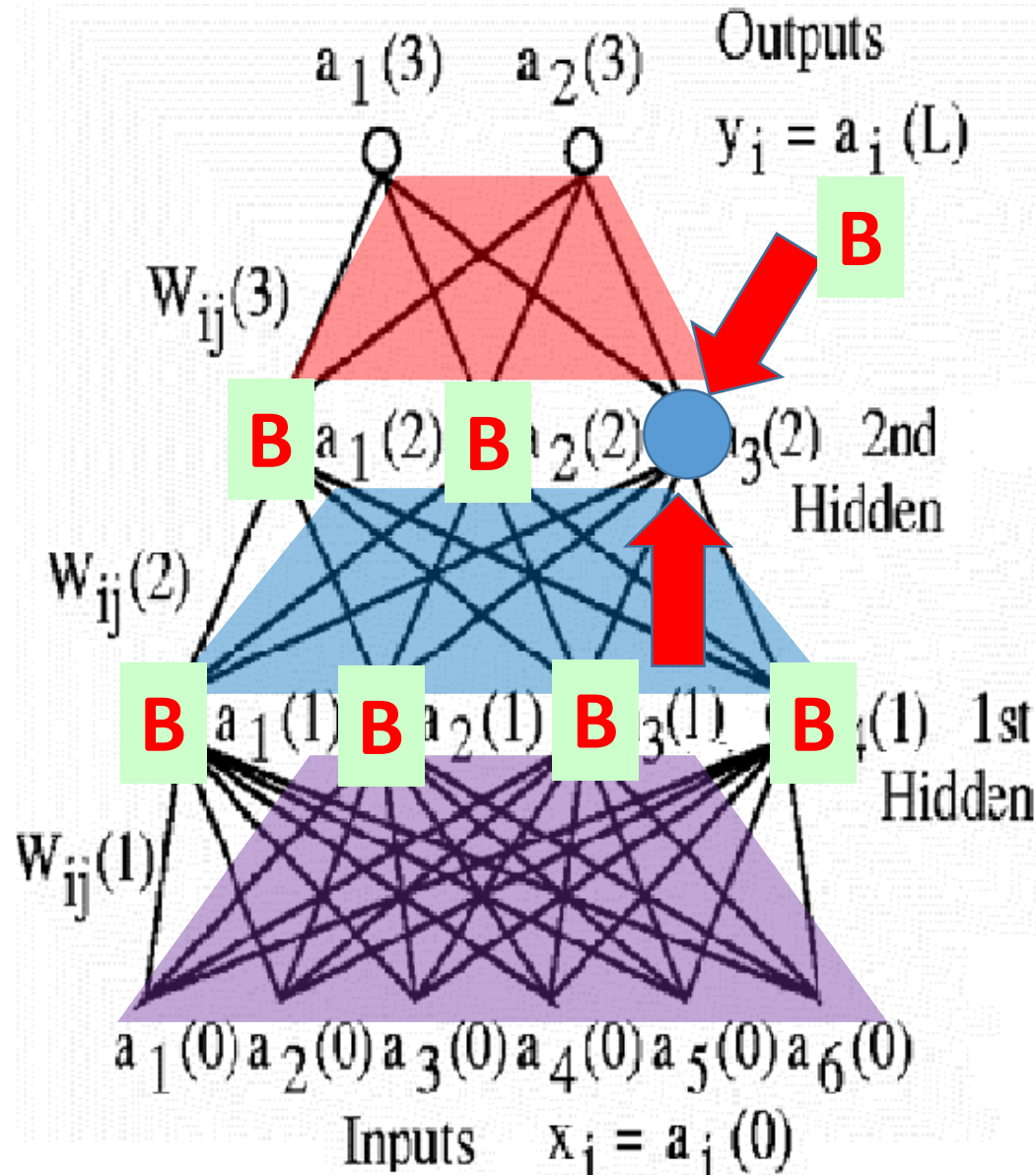
## (1) Internal Teacher Labels (ITL)



## (2) Internal Optimization Metrics (IOM)

Local Metrics for Internal Training must be of **classification-type** because one-hot encoding won't work!!

ITL may be adaptive w.r.t. layer, hierarchical, or end-user.



$$\{ a_i(3), \mathbf{B} \} \quad i=1, \dots, N$$

$$\{ a_i(2), \mathbf{B} \} \quad i=1, \dots, N$$

$$\{ a_i(1), \mathbf{B} \} \quad i=1, \dots, N$$

$$\{ a_i(0), \mathbf{B} \} \quad i=1, \dots, N$$

$$\{ x_i, \mathbf{B} \} \quad i=1, \dots, N$$



IOM must be of Classification-type:

## DI (Discriminant Information)

$$DI = DI(\mathbf{I}) = \text{tr} \left( [\bar{\mathbf{S}} + \rho \mathbf{I}]^{-1} \mathbf{S}_B \right) \quad \rho: \text{variance of additive noise}$$

### Three Scatter Matrices

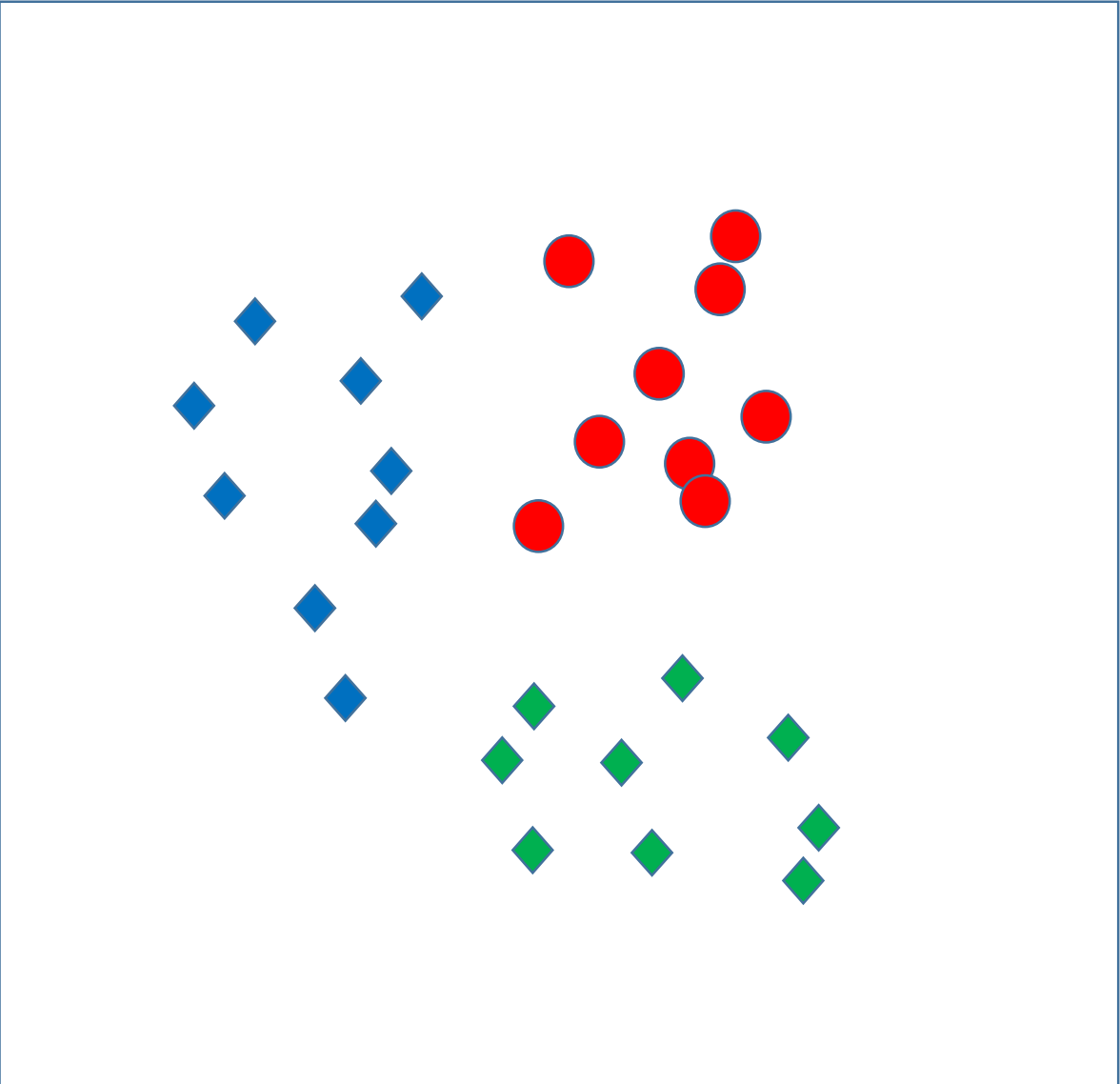
Scatter Matrix  $\bar{\mathbf{S}} = \bar{\mathbf{X}}\bar{\mathbf{X}}^T = \sum_{i=1}^N [\mathbf{x}_i - \bar{\boldsymbol{\mu}}][\mathbf{x}_i - \bar{\boldsymbol{\mu}}]^T$

Between Class Scatter Matrix  $\mathbf{S}_B = \sum_{\ell=1}^L N_{\ell} [\bar{\boldsymbol{\mu}}_{\ell} - \bar{\boldsymbol{\mu}}][\bar{\boldsymbol{\mu}}_{\ell} - \bar{\boldsymbol{\mu}}]^T = \Delta \mathbf{\Xi} \Delta^T$

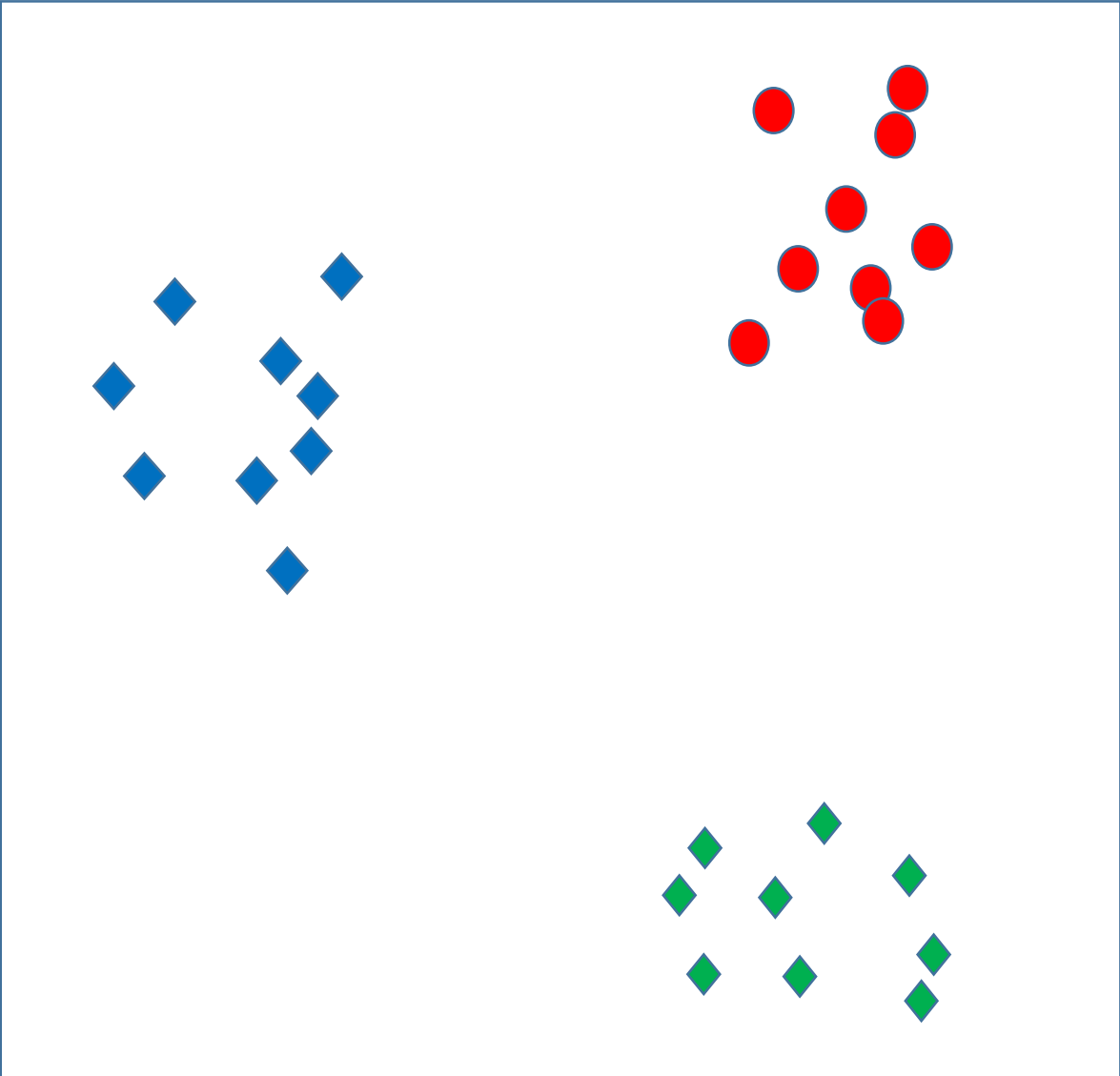
Within Class Scatter Matrix  $\mathbf{S}_W = \sum_{\ell=1}^L \sum_{j=1}^{N_{\ell}} [\mathbf{x}_j^{(\ell)} - \bar{\boldsymbol{\mu}}_{\ell}][\mathbf{x}_j^{(\ell)} - \bar{\boldsymbol{\mu}}_{\ell}]^T$

Suppose a hidden layer has 2 nodes (or more):

# Low-DI Space (2 nodes)



# High-DI Space (2 nodes)

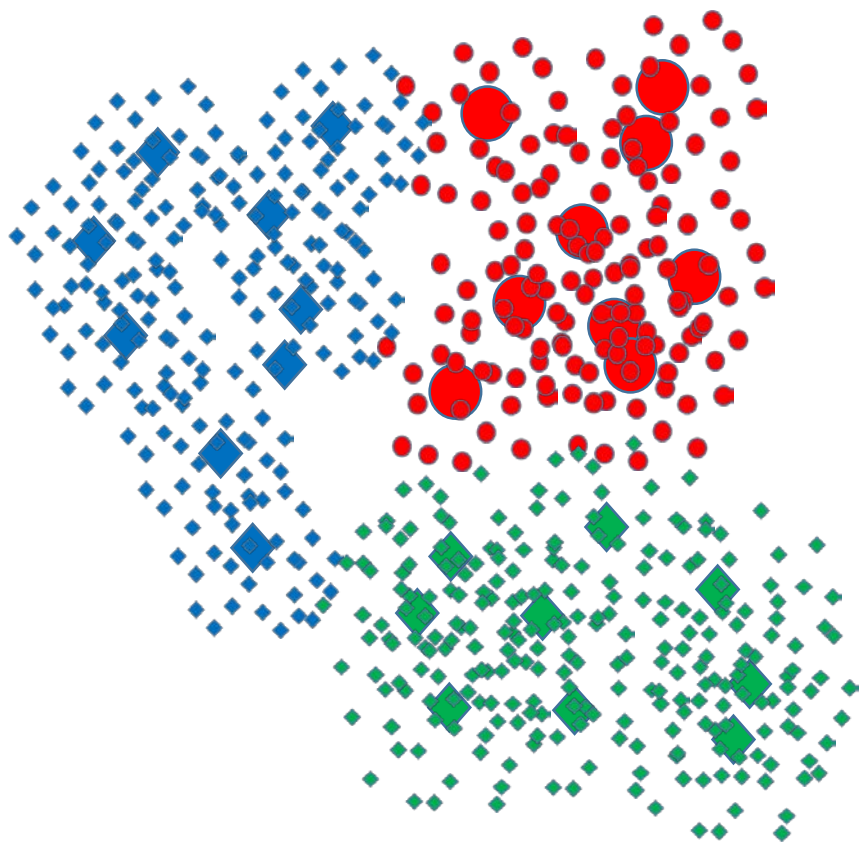




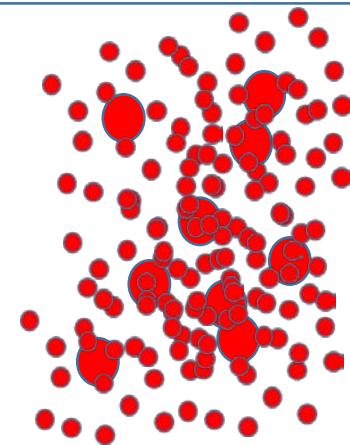
$$DI = DI(\mathbf{I}) = \text{tr}([\bar{\mathbf{S}} + \rho\mathbf{I}]^{-1}\mathbf{S}_B)$$

$\rho$ : variance of additive noise

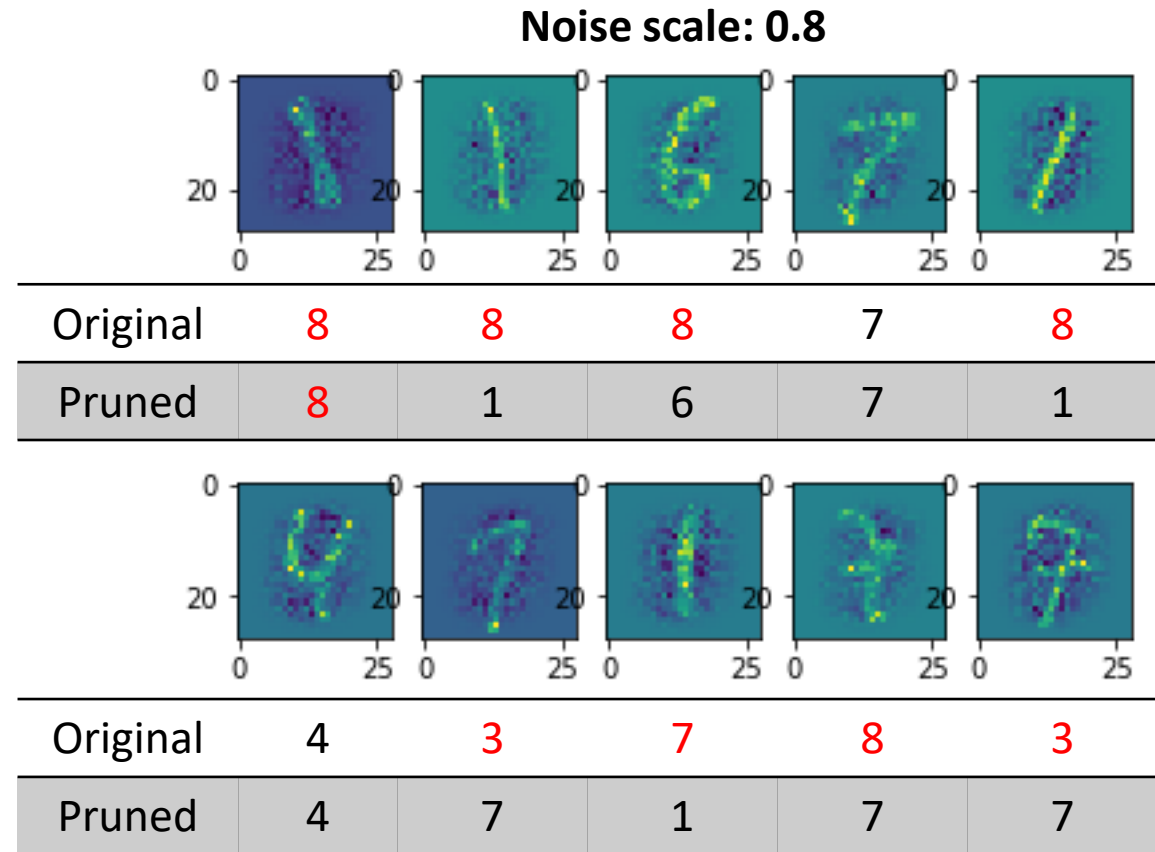
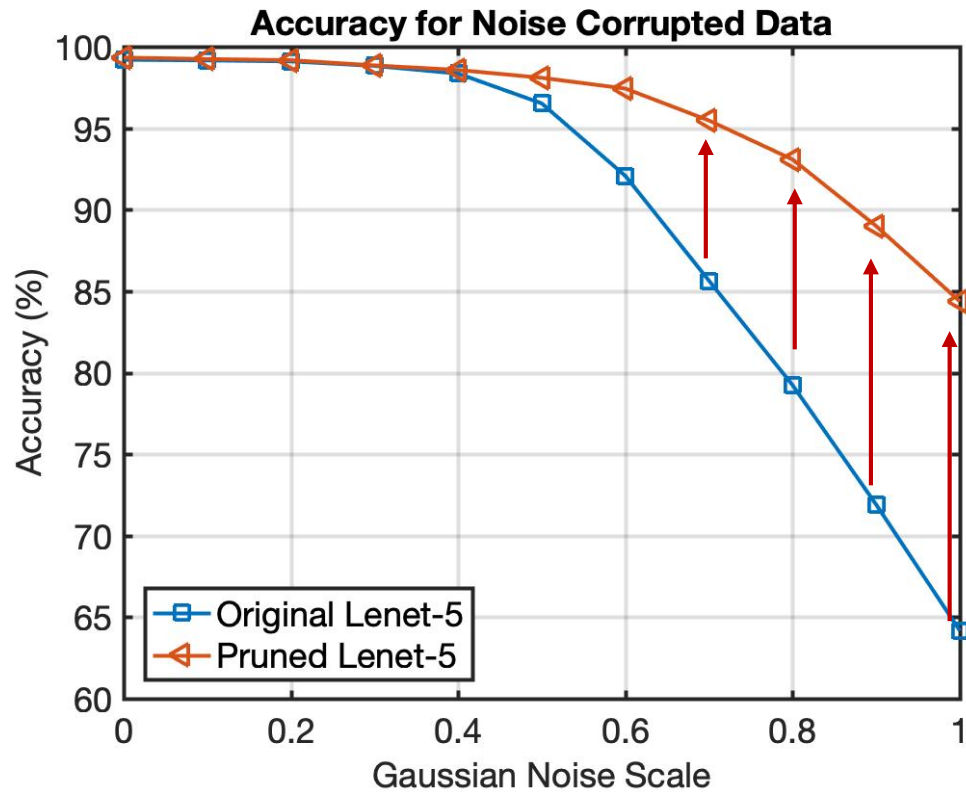
Low-DI Space (2 nodes)



High-DI Space (2 nodes)

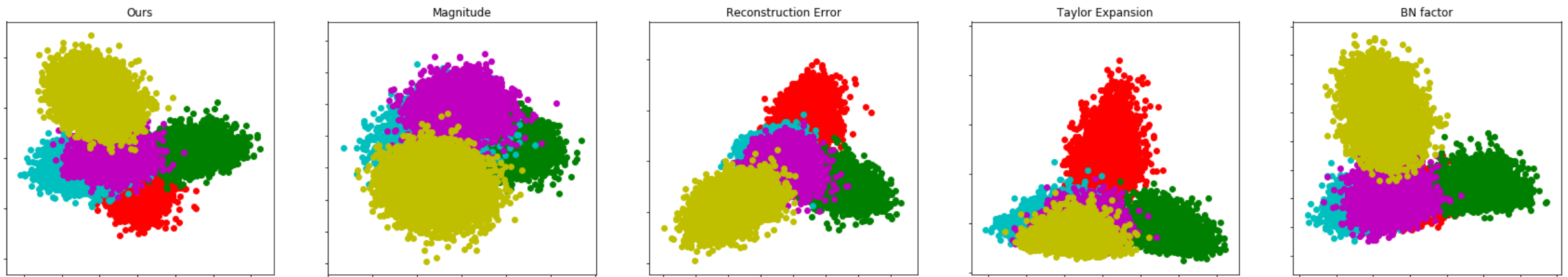


# DI enhances robustness to noise: Lenet on MNIST



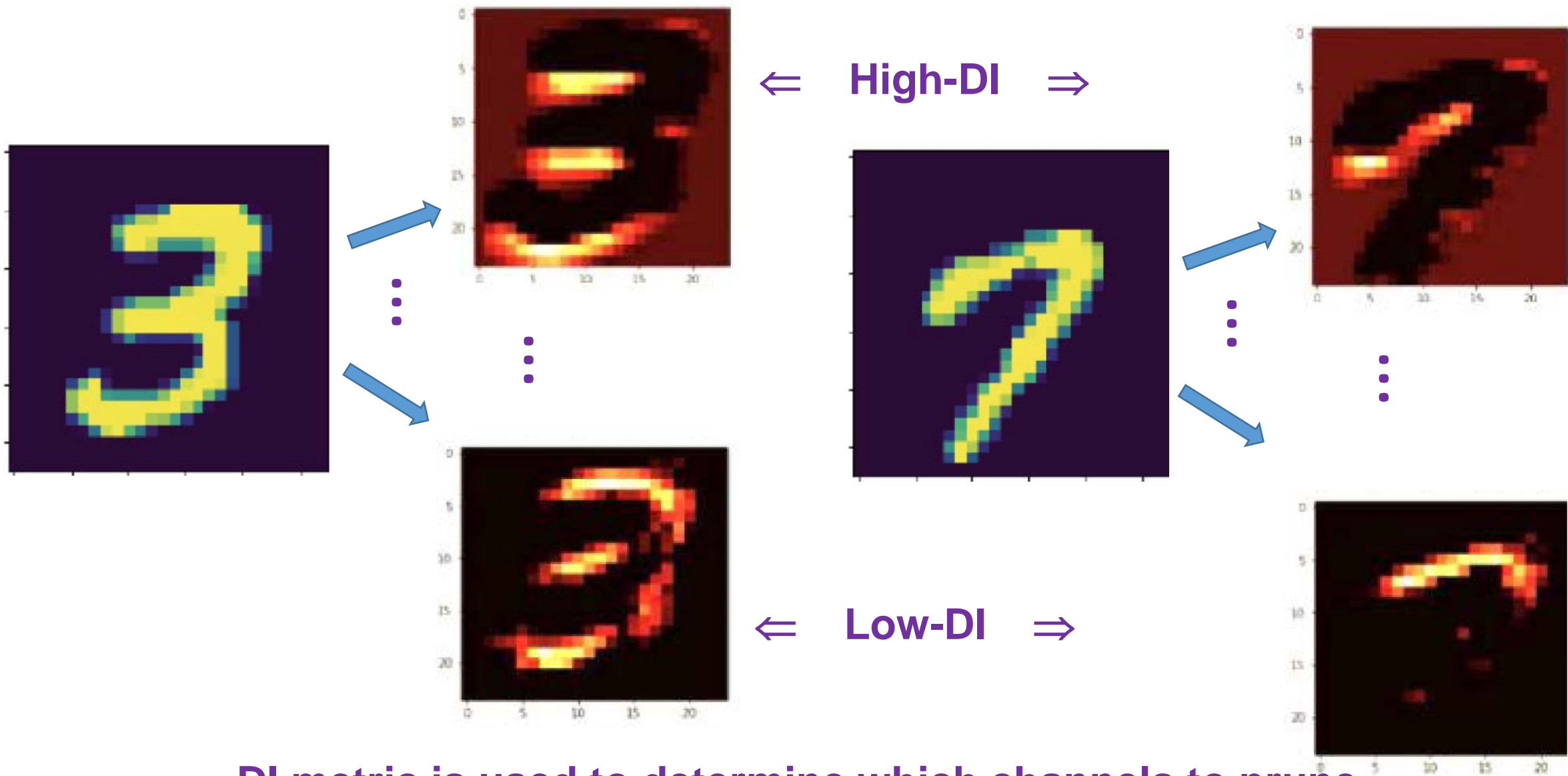
# Effectiveness of DI criterion: ResNet on CIFAR

- Compressed ResNet-56 by different criterion from the same pre-trained network
- 2D projected feature maps of the last residual layer
- CIFAR-10 samples from 5 classes for visualization
- Our method maximally preserves the feature separability, thus testing accuracy

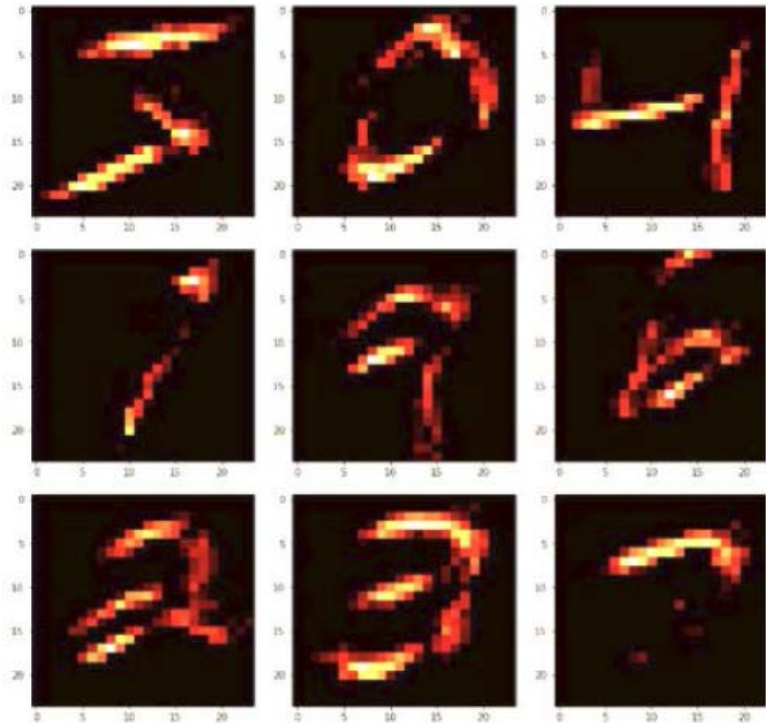
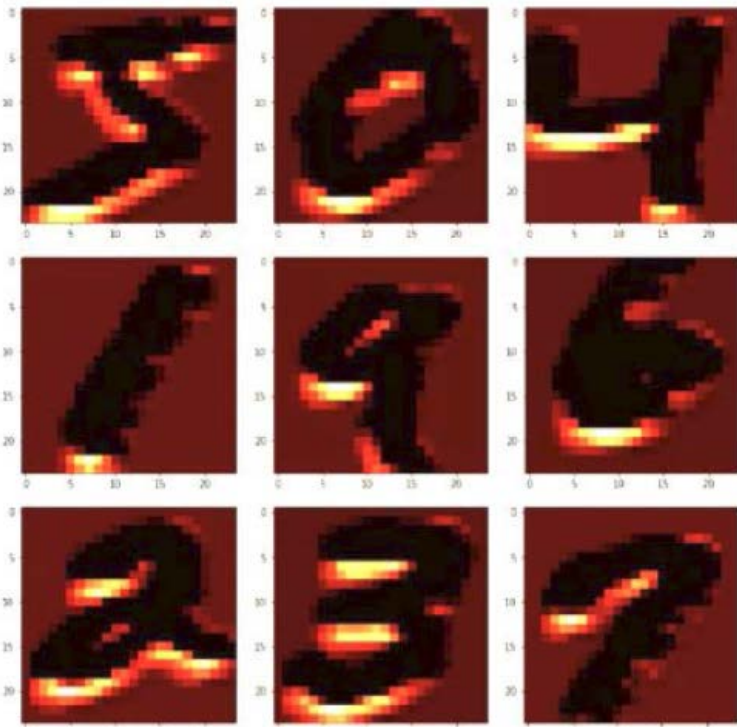


Criteria	Ours	Magnitude	Reconstruction error	Taylor Expansion	BN factor
Accuracy ↓	<b>1.75%</b>	2.17%	6.57%	2.69%	4.66%

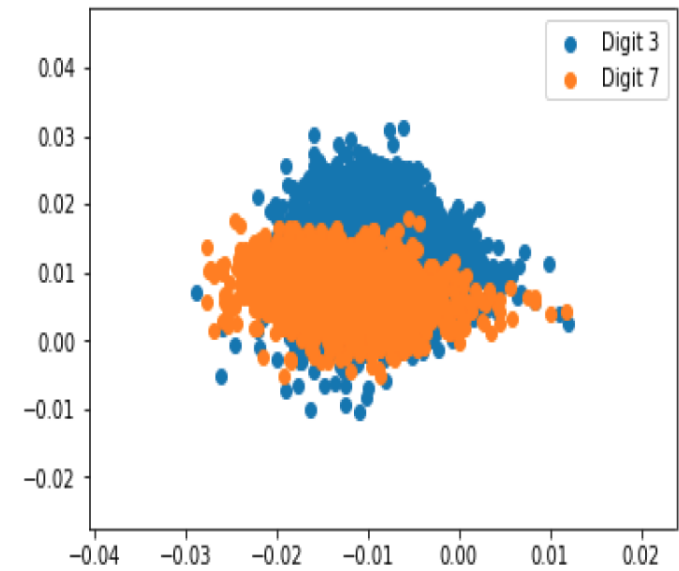
# Visualization via Chanel Images [KHL19]



# DI metric can determine which channels to prune/select



Low-DI Channel



High-DI Channel

For node evaluation:

# Subspace DI

$$DI = \text{tr}((\mathbf{W}^T \bar{\mathbf{S}} \mathbf{W} + \rho \mathbf{I})^{-1} \mathbf{W}^T \mathbf{S}_B \mathbf{W})$$

To assess the IOM of the full space of a layer, we set  $\mathbf{W} = \mathbf{I}$ :

For (supervised) deep compression, we adopt

$\mathbf{W}_{i\text{-keep}} / \mathbf{W}_{i\text{-drop}}$  to keep/drop only the  $i$ -th node/channel:

$$\mathbf{W}_{i_{keep}} = \begin{bmatrix} 0 & 0 & \dots & 0 & 0 \\ 0 & \ddots & \dots & \dots & 0 \\ \vdots & \dots & 0 & \dots & \vdots \\ 0 & \dots & \mathbf{1} & \dots & \vdots \\ 0 & 0 & \dots & 0 & 0 \end{bmatrix}$$

$$\mathbf{W}_{i_{drop}} = \begin{bmatrix} 1 & 0 & \dots & 0 & 0 \\ 0 & \ddots & \dots & \dots & 0 \\ \vdots & \dots & \mathbf{0} & \dots & \vdots \\ 0 & \dots & \dots & \mathbf{1} & \dots \\ 0 & 0 & \dots & 0 & 1 \end{bmatrix}$$

For pruning nodes/channels in MLP/ConvNet, we adopt:

- Fisher Discriminant Ratio (FDR):

$$\text{FDR} = DI(\mathbf{W}_{i_{keep}})$$

$$\mathbf{W}_{i_{keep}} = \begin{bmatrix} 0 & 0 & \dots & 0 & 0 \\ 0 & \ddots & \dots & \dots & 0 \\ \vdots & \dots & 0 & 1 & \dots \\ 0 & \dots & \dots & 0 & \ddots \\ 0 & 0 & \dots & 0 & 0 \end{bmatrix}$$

is the value of the  $i$ -th node/channel.

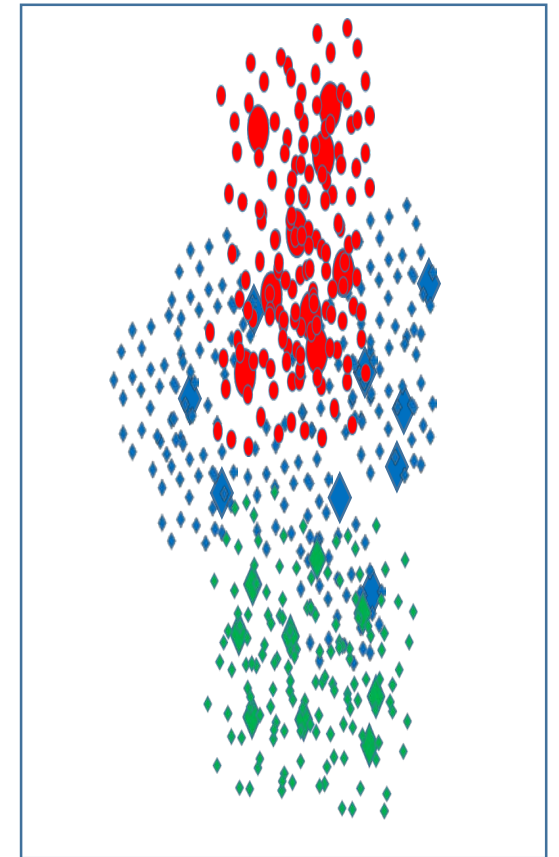
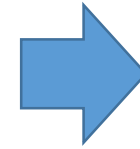
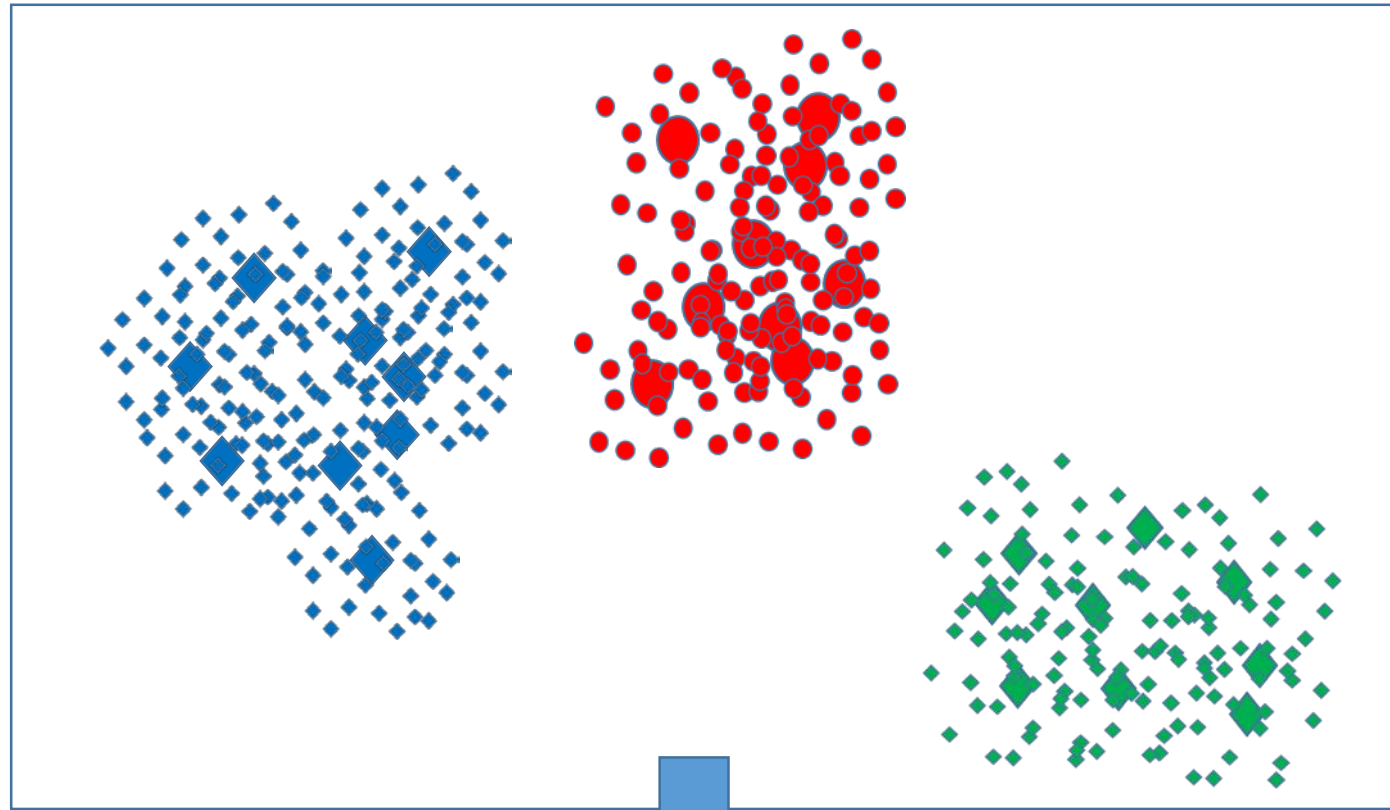
- Dispensability of a node/channel: DI-Loss:

$$\text{DILoss} \equiv DI(\mathbf{I}) - DI(\mathbf{W}_{i_{drop}})$$

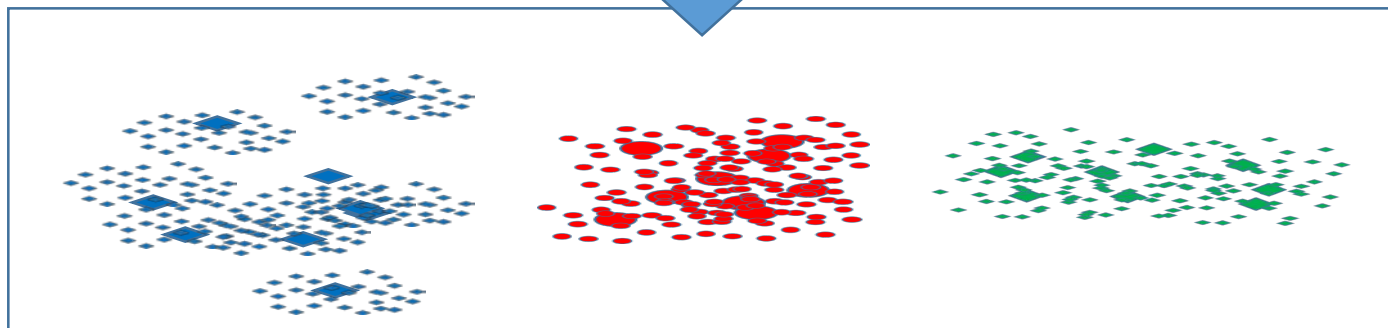
$$\mathbf{W}_{i_{drop}} = \begin{bmatrix} 1 & 0 & \dots & 0 & 0 \\ 0 & \ddots & \dots & \dots & 0 \\ \vdots & \dots & 1 & 0 & \dots \\ 0 & \dots & \dots & 0 & \ddots \\ 0 & 0 & \dots & 0 & 1 \end{bmatrix}$$

is the remaining value of the layer after removing the  $i$ -th node/channel.  
This reflects the dispensability of the  $i$ -th node/channel.

# Differential-DI Subspace (2 nodes: left-vs-right, top-down-neuron)



Low-DI: top-down neuron



High-DI: left-vs-right neuron



The internal teachers facilitate two structural training strategies:

**(1) DI-based Cherry Picking Method**

**(2) DI-based Pruning Method**

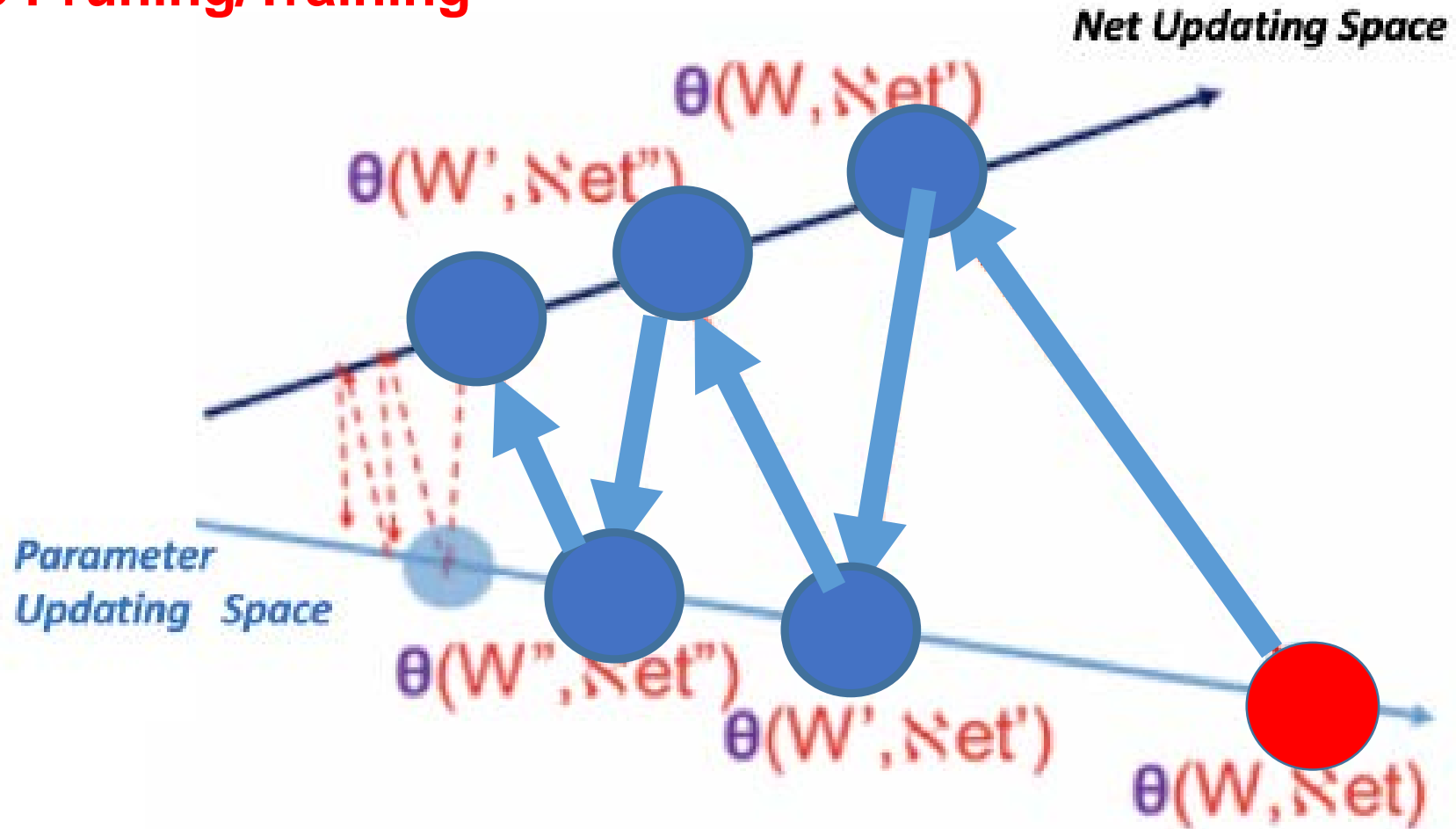
## DI-based Cherry Picking Offers Rapid Deep Compression/Quantization

LeNet-300 on MNIST	Accuracy	Storage Size	Compression	Quantized
Original	98.36%	840 KB	-	16-bit
DI pruning	98.42%	71.4 KB	12x	16-bit
Cherry-Picking	94.42%	8.7 KB	97x	16-bit
Quantization*	94.22%	5.8 KB	145x	64.8% 8-bit

VGG19 on CIFAR-100	Accuracy	Storage Size	Compression	Quantized
Original	73.26%	60 MB	-	16-bit
DI pruning	73.67%	9.8 MB	6x	16-bit
Cherry-Picking	71.01%	2.4 MB	25x	16-bit
Quantization*	70.36%	1.8 MB	33x	60.9% 10-bit

# DI-based Pruning Method Offers Win-Win Deep Compression/Quantization

## NP-Iterative Pruning/Training



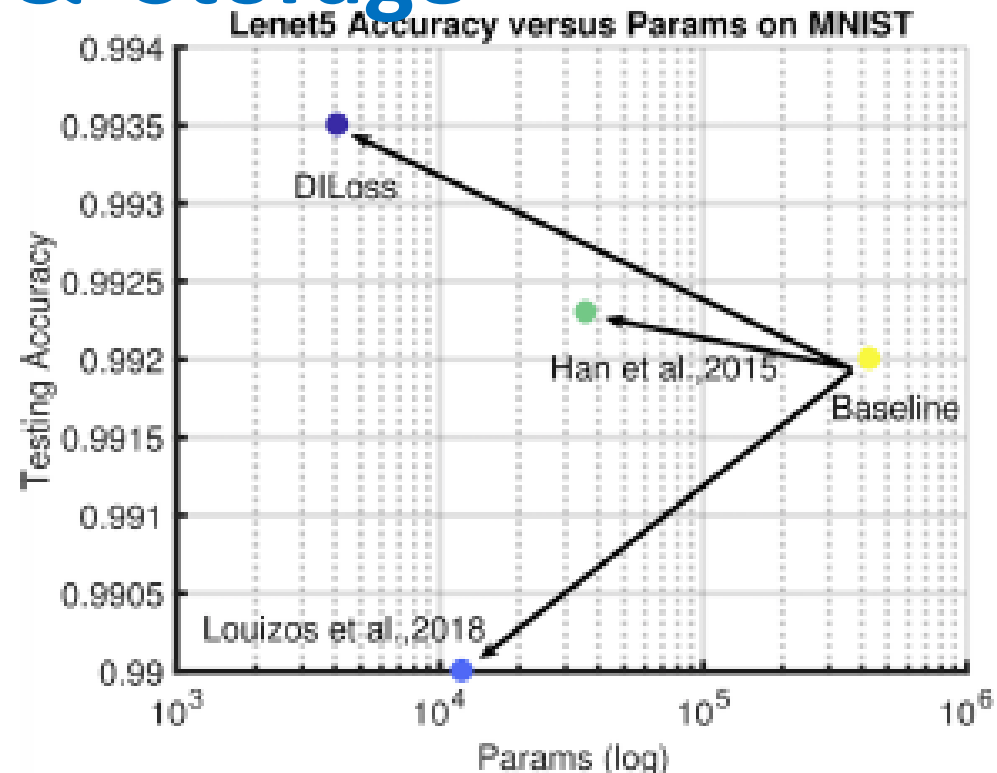
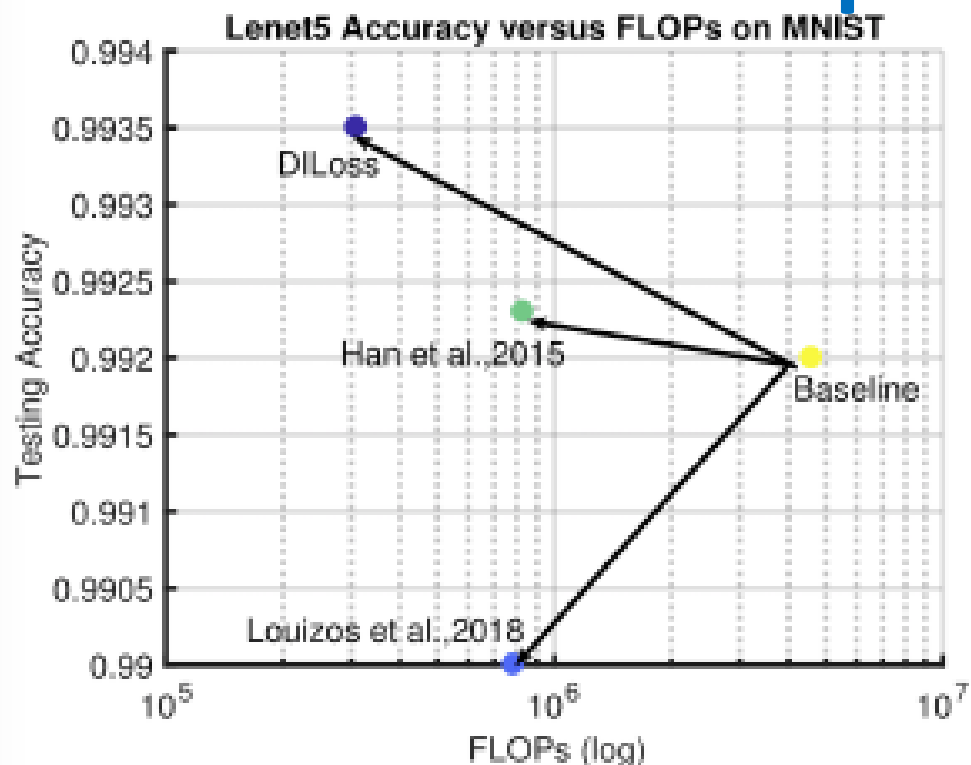
1. Biological Justification of Internal Learning
2. Pruning Efficacy
3. Performance Improvements: Experimental Results

# **BPOS:** Bridging GAP between regression-type and classification-type metrics

Definition: by balanced dataset we mean that the training samples for all the class labels are of the same size.

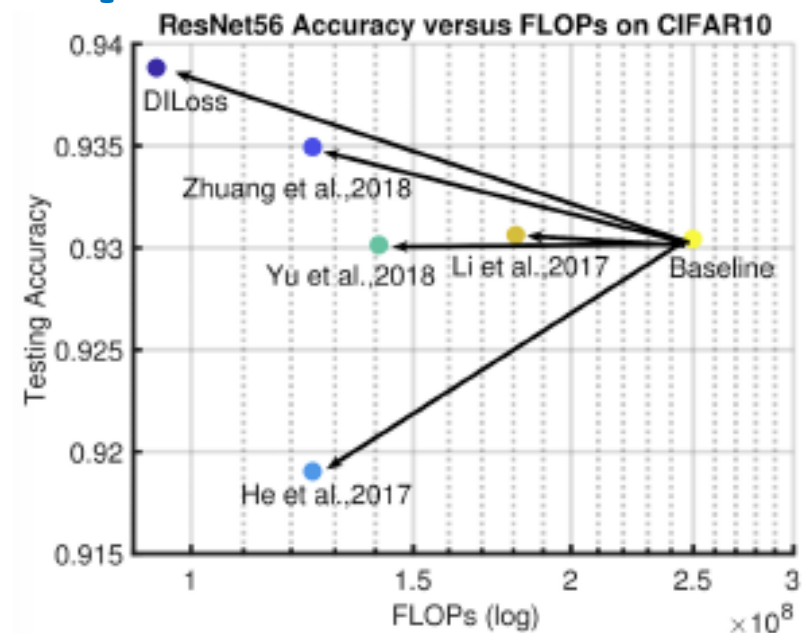
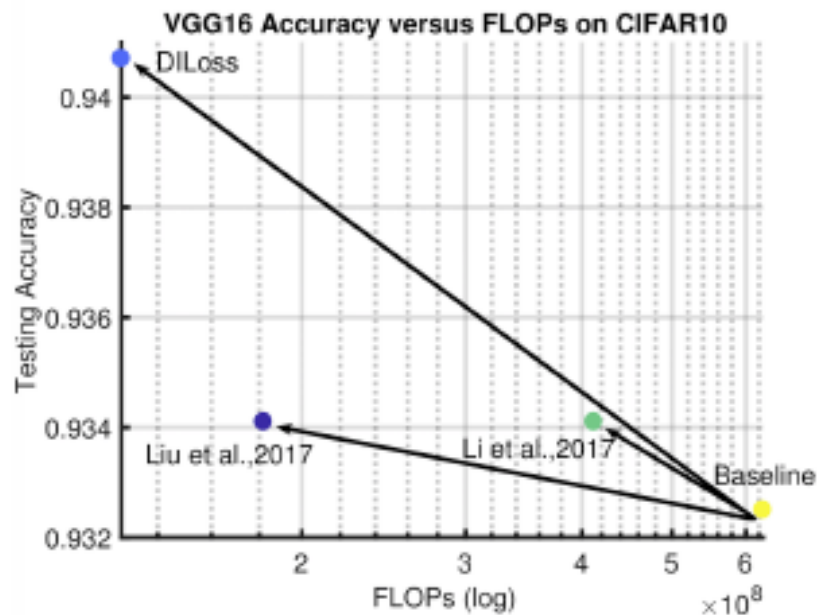
For balanced case, it can be shown that all of them are mathematically **equivalent optimization metrics** if one-hot encoding is used for LSE teacher values. (Next Page)

# MINIST: Speedup & Storage



Task	Models	Accuracy %	FLOPs	Params
MNIST	<i>Lenet-5 (baseline)</i>	99.2	$4.59 \times 10^6$	$4.3 \times 10^5$
	<i>Lenet-5 (Han et al., 2015)</i>	99.23	$8.3 \times 10^5$ (18.1%)	$3.6 \times 10^4$ (8.4%)
	<i>Lenet-5 (Louzois et al., 2018)</i>	99	$7.85 \times 10^5$ (17.1%)	$1.22 \times 10^4$ (2.83%)
	<i>Lenet-5 (FDR)</i>	99.33	$2.6 \times 10^5$ (5.74%)	$4.9 \times 10^3$ (1.1%)
	<i>Lenet-5 (DILoss)</i>	<b>99.35</b>	<b><math>2.46 \times 10^5</math> (5.36%)</b>	<b><math>3.86 \times 10^3</math> (0.89%)</b>
	<i>Lenet-300 (baseline)</i>	98.36	-	$2.7 \times 10^5$
	<i>Lenet-300 (Han et al., 2015)</i>	98.41	-	$2.24 \times 10^4$ (8.3%)
	<i>Lenet-300 (Louzois et al., 2018)</i>	98.2	-	$2.7 \times 10^4$ (10%)
	<i>Lenet-300-100 (FDR)</i>	98.42	-	$2.3 \times 10^4$ (8.5%)
	<i>Lenet-300 (DILoss)</i>	<b>98.46</b>	-	<b><math>1.63 \times 10^4</math> (6.04%)</b>

# CIFAR-10: Speedup

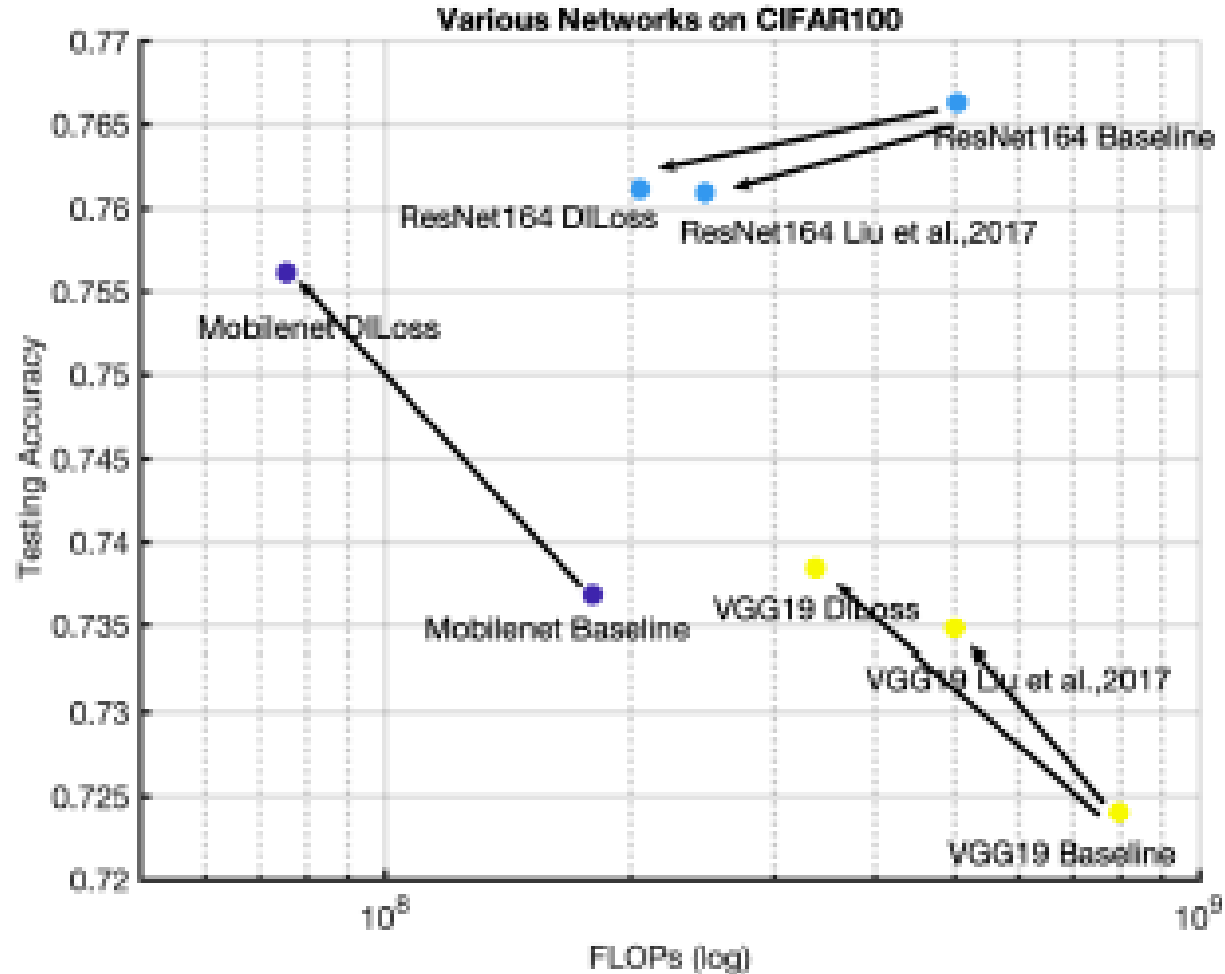


(c) CIFAR10: VGG16 speedup

(d) CIFAR10: Resnet56 speedup

Task	Models	Accuracy %	FLOPs	Params
CIFAR-10	<i>VGG-16 (baseline)</i>	93.25	$6.26 \times 10^8$	$1.5 \times 10^7$
	<i>VGG-16 (Li et al., 2017)</i>	93.41	$4.12 \times 10^8$ (65.81%)	$5.4 \times 10^6$ (36%)
	<i>VGG-16 (FDR)</i>	93.61	$1.35 \times 10^8$ (21.4%)	$7.1 \times 10^5$ (4.7%)
	<i>VGG-16 (DILoss)</i>	<b>94.07</b>	<b><math>1.28 \times 10^8</math> (20.45%)</b>	<b><math>5.32 \times 10^5</math> (3.55%)</b>
	<i>ResNet-56 (baseline)</i>	93.04	$2.5 \times 10^8$	$8.5 \times 10^5$
	<i>ResNet-56 (Li et al., 2017)</i>	93.06	$1.81 \times 10^8$ (72.4%)	$7.3 \times 10^5$ (85.88%)
	<i>ResNet-56 (Yu et al., 2018)</i>	93.01	$1.41 \times 10^8$ (56.4%)	$4.94 \times 10^5$ (58.12%)
	<i>ResNet-56 (He et al., 2017)</i>	91.9	$1.25 \times 10^8$ (50%)	-
	<i>ResNet-56 (Zhuang et al., 2018)</i>	93.49	$1.25 \times 10^8$ (50.25%)	$4.3 \times 10^5$ (50.76%)
	<i>ResNet-56 (DILoss)</i>	<b>93.84</b>	<b><math>8.38 \times 10^7</math> (33.52%)</b>	<b><math>3.12 \times 10^5</math> (35.52%)</b>
<i>ResNet-56 (bootstrap:DILoss+Zhuang)</i>	<b>93.84</b>	<b><math>7.58 \times 10^7</math> (30.32%)</b>	<b><math>2.81 \times 10^5</math> (33.05%)</b>	

# CIFAR-100: Speedup



Task	Models	Accuracy %	FLOPs	Params
CIFAR100	<i>Mobilenet-v2 (baseline)</i>	73.68	$1.8 \times 10^8$	$2.4 \times 10^6$
	<i>Mobilenet-v2 (DILoss)</i>	<b>75.61</b>	<b><math>7.57 \times 10^7</math> (42.06%)</b>	<b><math>1.07 \times 10^6</math> (44.58%)</b>

# ImageNet Classification

LPIRC  
2018  
Winners

Neural network architecture	Input image resolution	Data type	Accuracy (%)	Google Pixel-2 inference time (ms)	Accuracy/inference time (%/ms)
mobilenet v1	224x224	float32	70.2	81.5	0.86
mobilenet v1	224x224	uint8	65.5	68.0	0.96
<b>mobilenet v1</b>	<b>128x128</b>	<b>uint8</b>	<b>64.1</b>	<b>28.0</b>	<b>2.28</b>
mobilenet v2	150x150	uint8	64.4	36.6	1.75
mobilenet v2	132x132	uint8	62.7	31.8	1.97
mobilenet v2	130x130	uint8	59.9	31.2	1.91

For LPIRC 2019:

DI-Reduced Mobilenet V1:

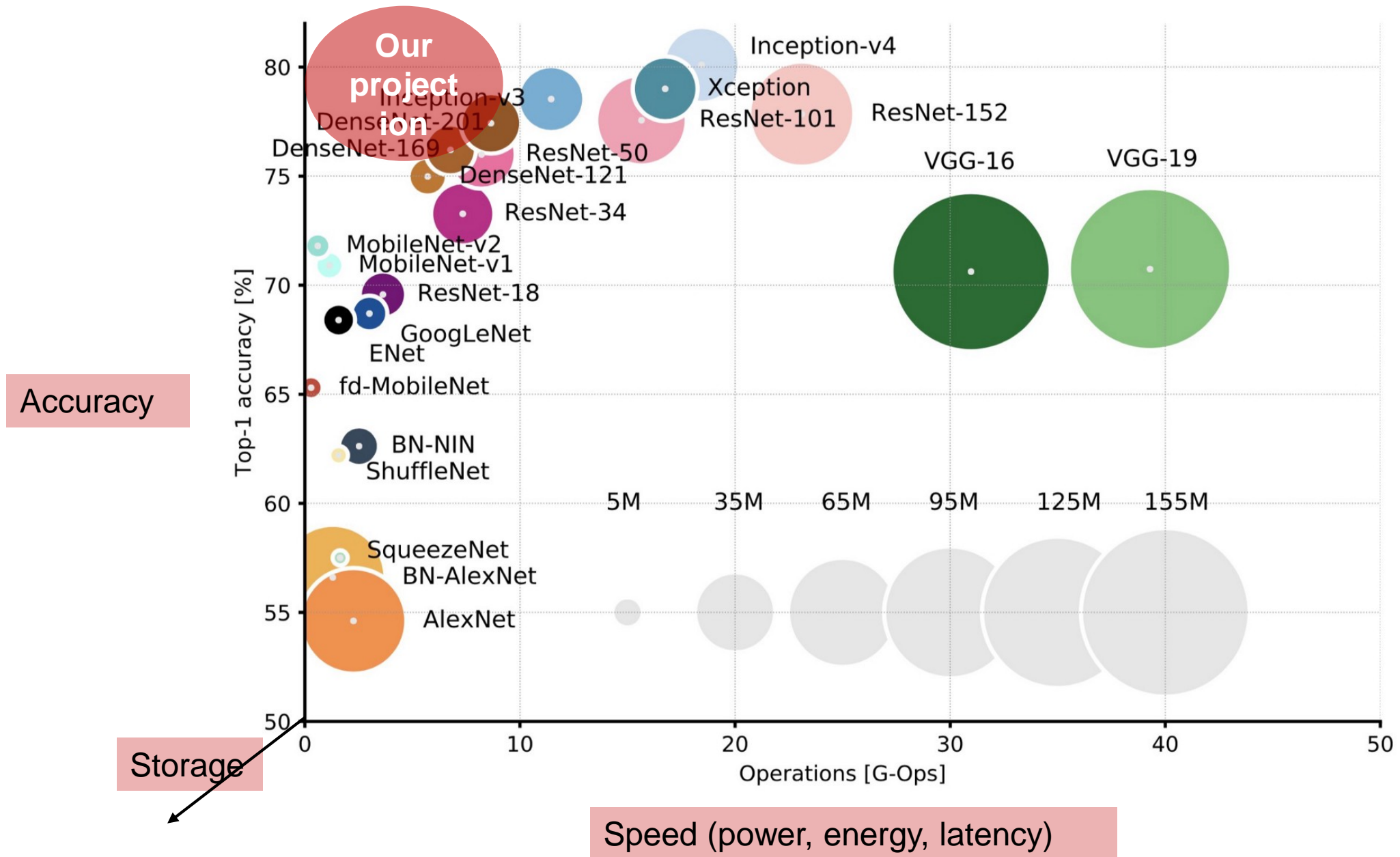
Model	Acc %	FLOPs ( $10^6$ )	Params. ( $10^6$ )	GPU (ms)	Google Pixel-2 (ms)
MobileNet V1	70.2	574	4.24	29.1	81.5
MobileNet V1 (ours)	70.2	277	2.28	12.7	-
MobileNet V1 (8-bit)	67.26	-	-	12.2	-
MobileNet V2	71.8	300	3.41	8.3	-
MobileNet V2 (ours)	70.85	210	2.33	-	-

DI-Reduced ResNet-50:

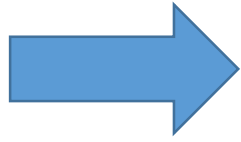
FLOPs	Parameters	Accuracy
4.08 B	25.50 M	76.112%



# ImageNet Classification

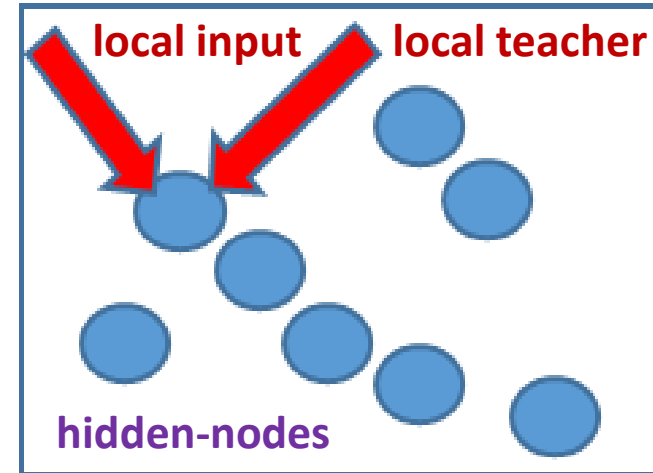


# Internal Teacher Labels (ITL)



## Internal Optimization Metrics (IOM)

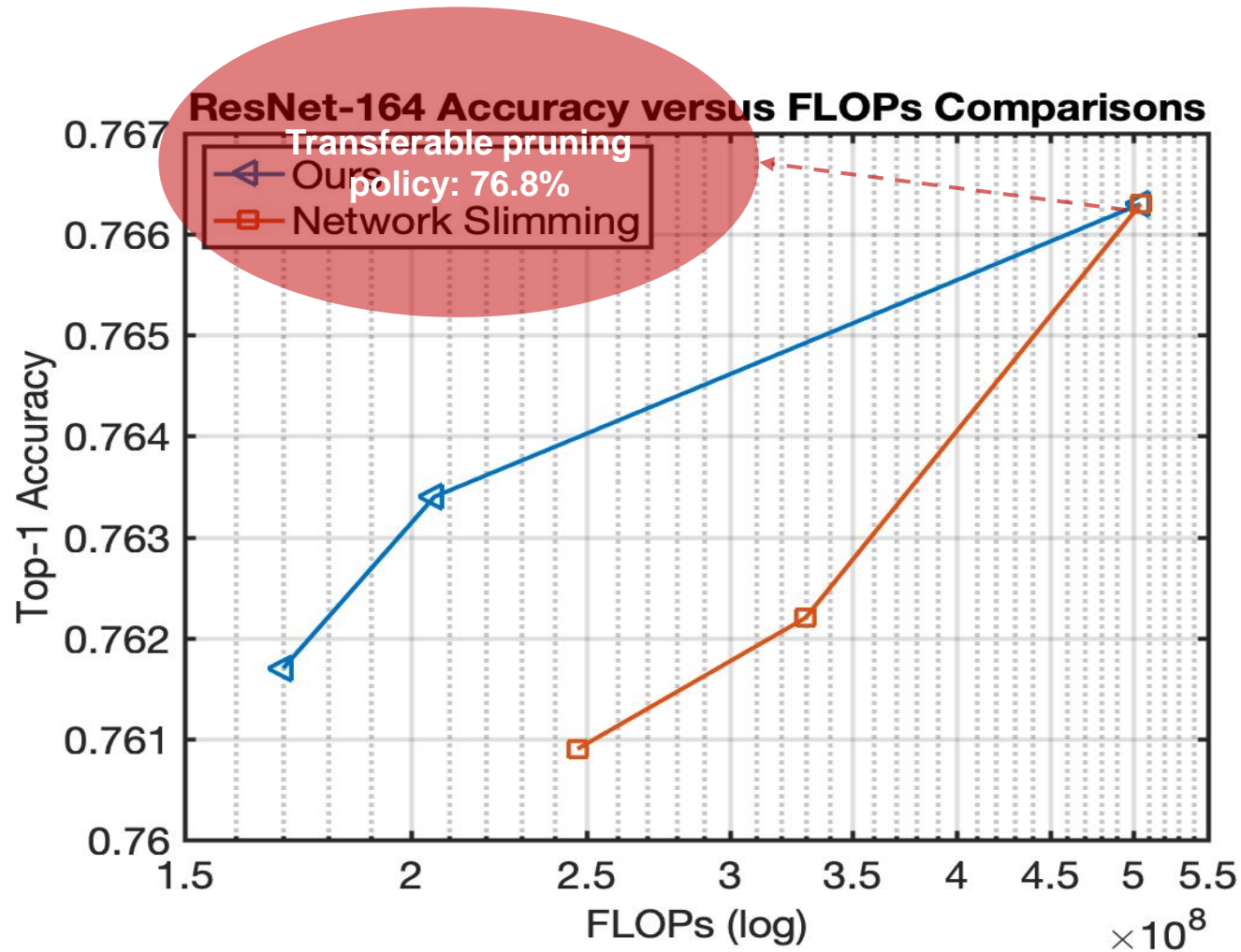
Local Metrics for Internal Training must be of **classification-type** because one-hot encoding won't work!!



For classification problem, the teacher labels can be metaphorically hidden in “Trojan-horses” and transported (along with the data) from the input layer to all hidden nodes.

- The original label, say B, is being sent to all hidden nodes; (discussed above)
- **Possible internal teacher labels ITLs are: granularity-adaptive (class or super-class), layer adaptive, or end-user-adaptive to facilitate INEX in XAI. (NEXT)**

# Applying Transfer Learning to ResNet on CIFAR



## A Major Focus of Explainable AI (XAI) is Explainable Learner (vs. Classifiable Learner)

XAI: Internal Neuron's Explainability, championed by DARPA's XAI (or AI3.0).

### Broad Agency Announcement

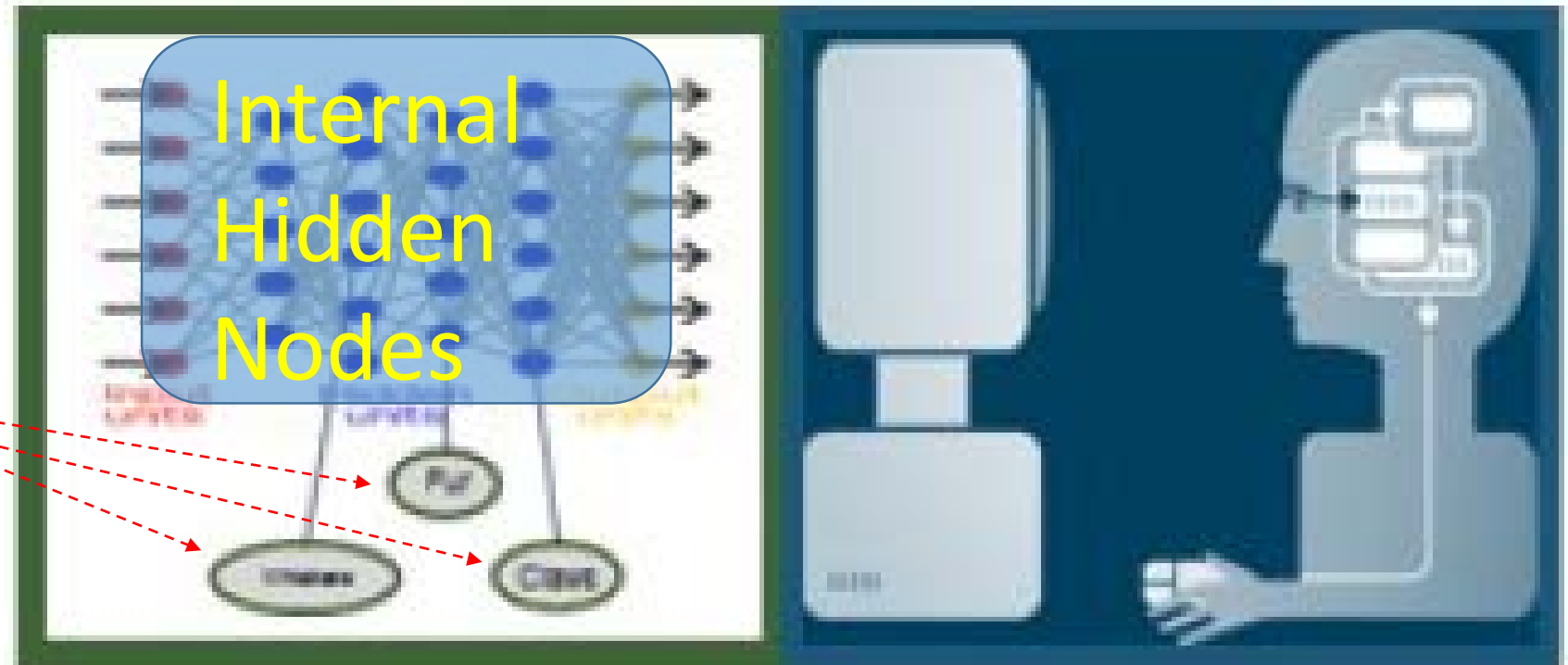
Explainable Artificial Intelligence (XAI)

DARPA-BAA-16-53

August 10, 2016

### XAI TA1: Deep Learning

**Internal Node EXplainability (INEX):** BAA ``XAI is most interested in explanations of higher-level decisions that would be relevant to the end user and the missions he/she needs to manage.



# NN/AI: dónde quieres ir?

1950



2000



2020

**NN1.0**

**model: MLP**

M. Minsky,, first neural network simulator, Princeton Ph. D. 1951, Paul Werbos, Ph. D. Harvard, 1974. Rumelhart, Hinton, and Williams, "Learning internal representations by error propagation," 1985.



**NN 2.0**

⇒ **model: CNN**

⇒ **Deep Learning**  
(深度学习)



**new NN**

⇒ **Enhanced CNN: e.g. highways**

⇒ **Internal Learning**  
(深入学习)

**INER**  
(Internal Node Evaluation/Ranking)

**AI 1.0**

MIT AI Lab (1958, M. Minsky)  
Knowledge Systems Laboratory,  
(1970 Feigenbaum)



**AI 2.0**

⇒ **Big-Data-Driven**

⇒ **Deep BP Learning**



**XAI**

**INEX**  
(Internal Node Explainability)