

# Single Image Interpolation Exploiting Semi-Local Similarity

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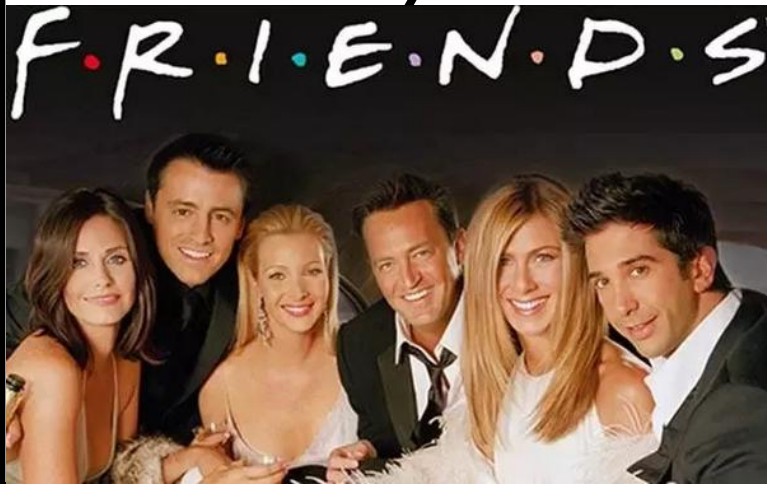
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Rice University



# Ubiquitous Need

iMac (Late 2013) :  $1920 \times 1080$

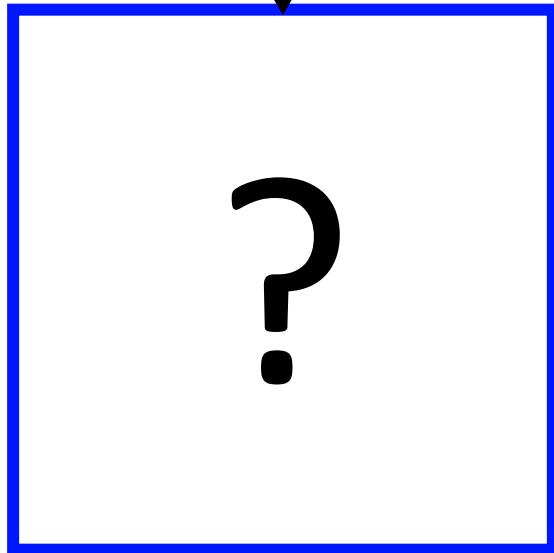
*Friends* (debut 1994) :  $720 \times 480$



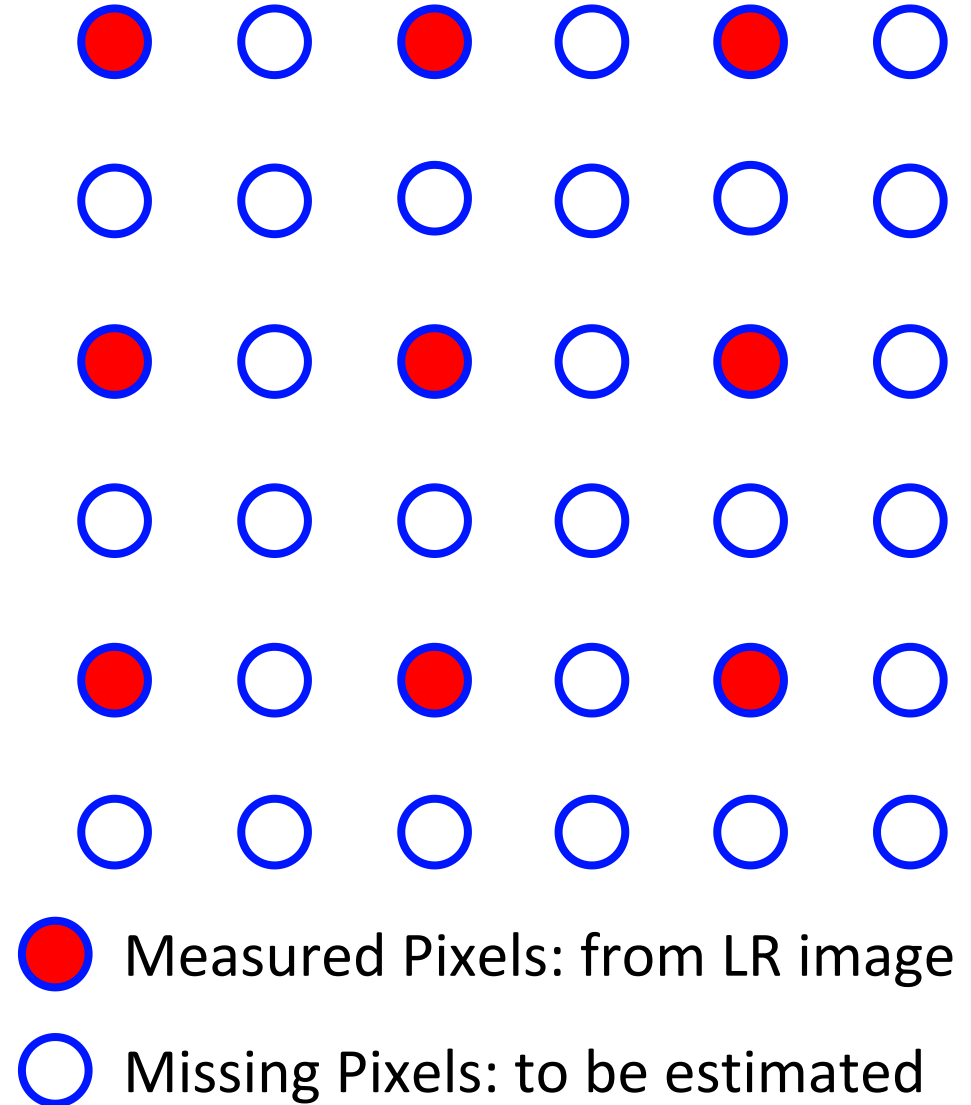
# The Interpolation Problem



Low-Resolution  
(LR) image

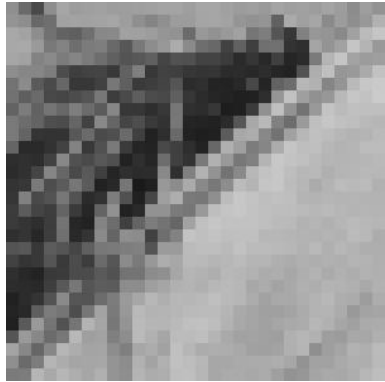


High-Resolution  
(HR) image

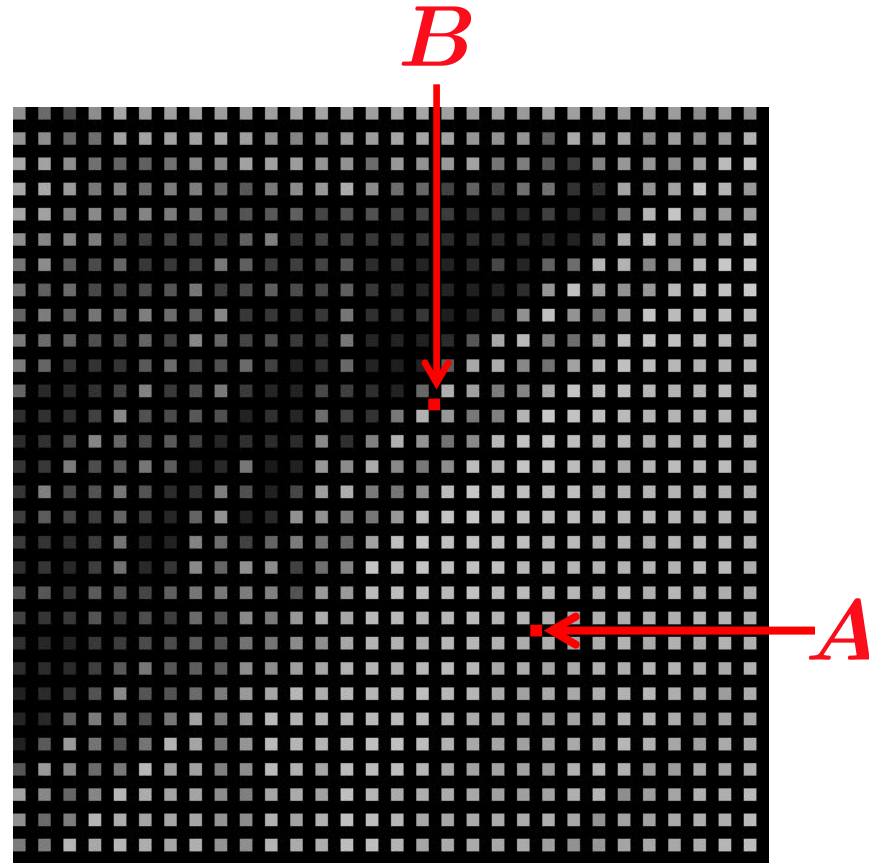


# Challenge

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LR image



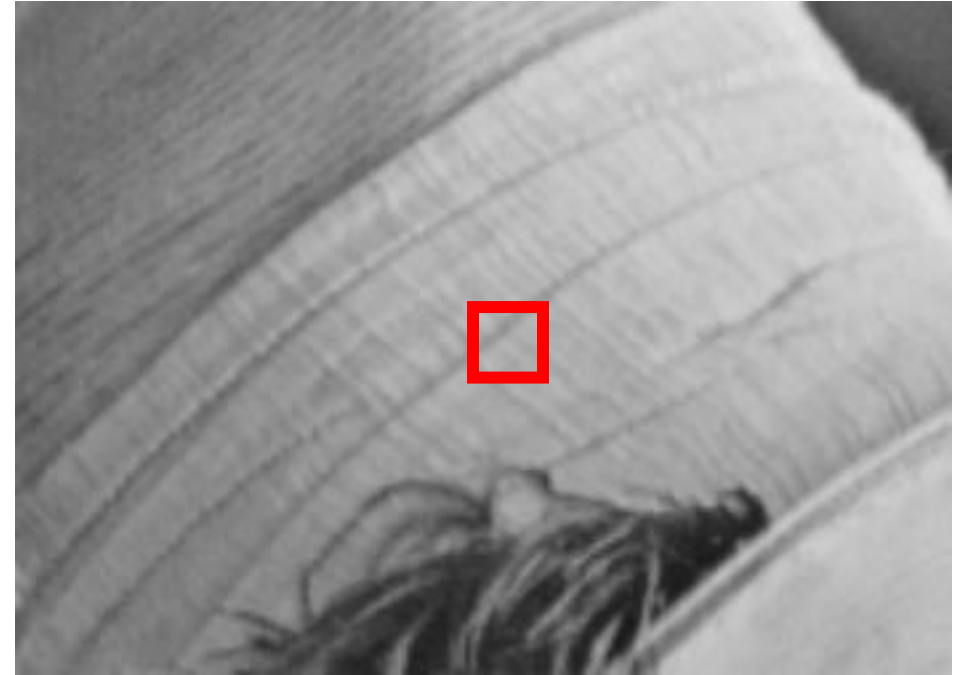
Upsampled-by-2  
LR image



HR Image

# Semi-Local Similarity

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A Patch (the red block of pixels)  
and its Neighboring Similar Patches  
(the green blocks of pixels) in *Lena*.

# Semi-Local Similarity

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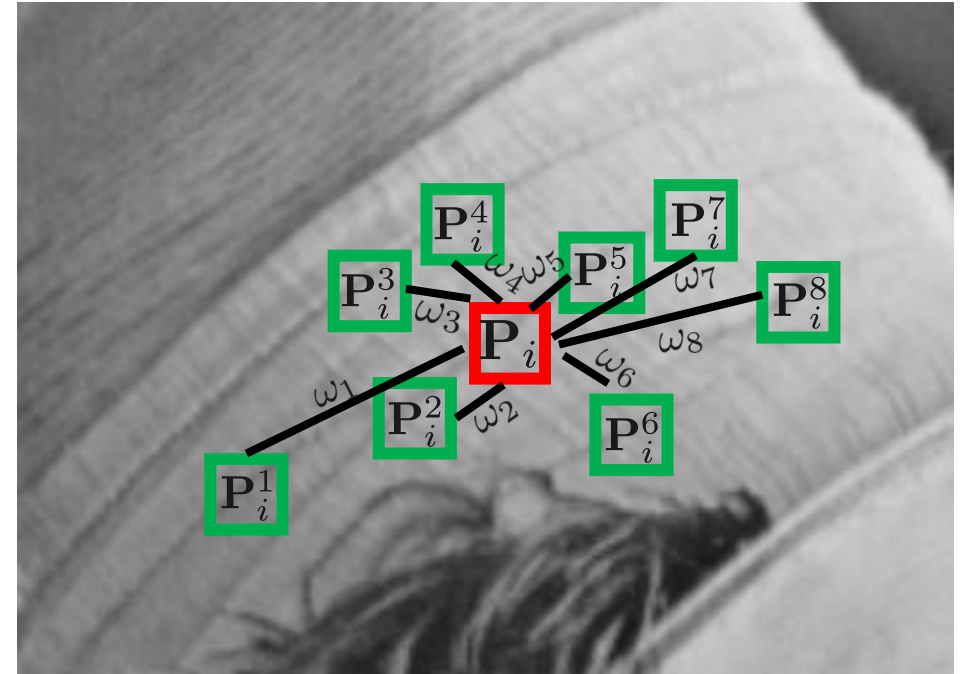
A Patch (the red block of pixels) and its Neighboring Similar Patches (the green blocks of pixels) in *Lena*.

# Semi-Local Similarity

$$\mathbf{P}_i \approx \sum_j \omega_j \mathbf{P}_i^j$$

An individual patch in a natural image

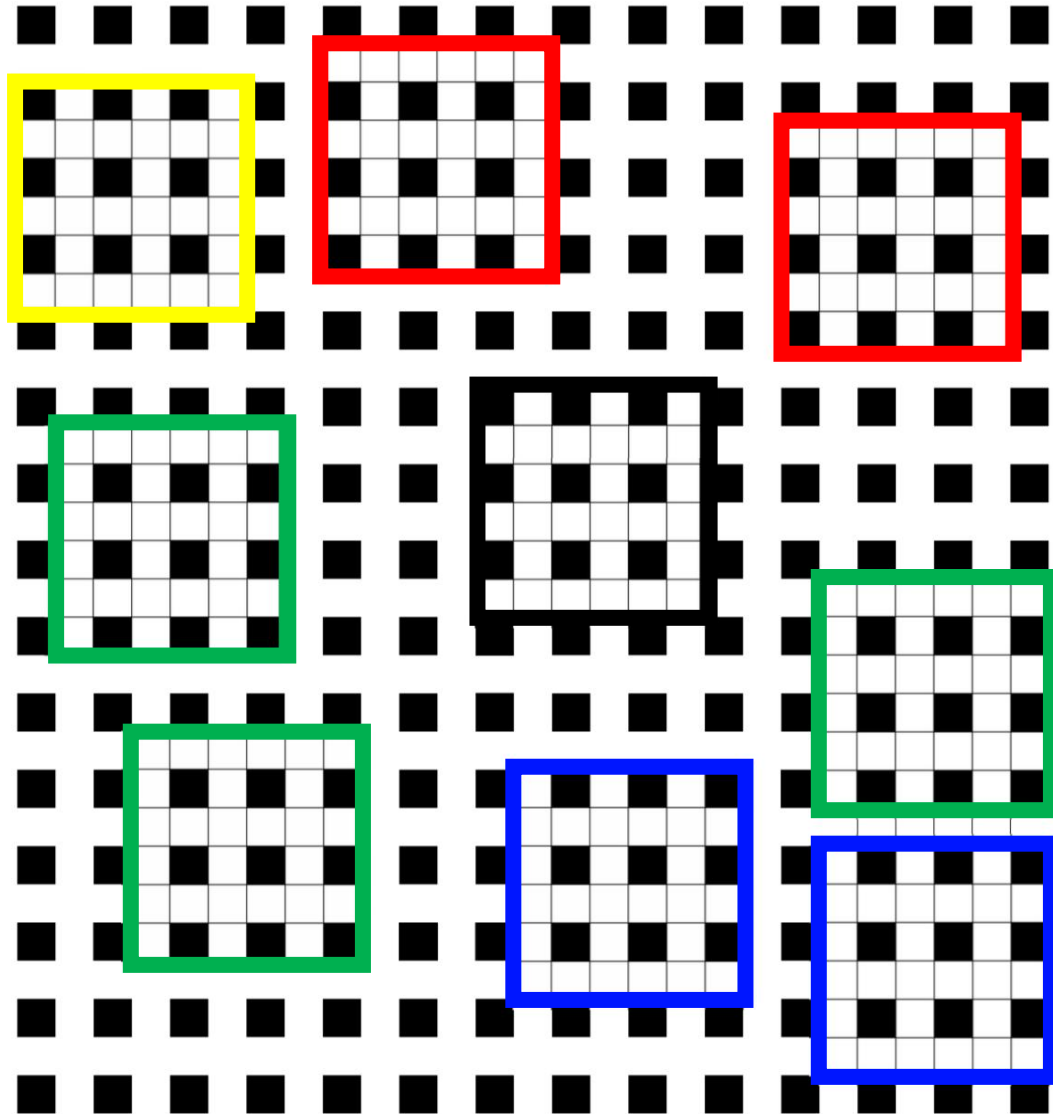
Similar patches searched in  $\mathbf{P}_i$ 's spatial neighborhood



A Patch (the red block of pixels) and its Neighboring Similar Patches (the green blocks of pixels) in *Lena*.

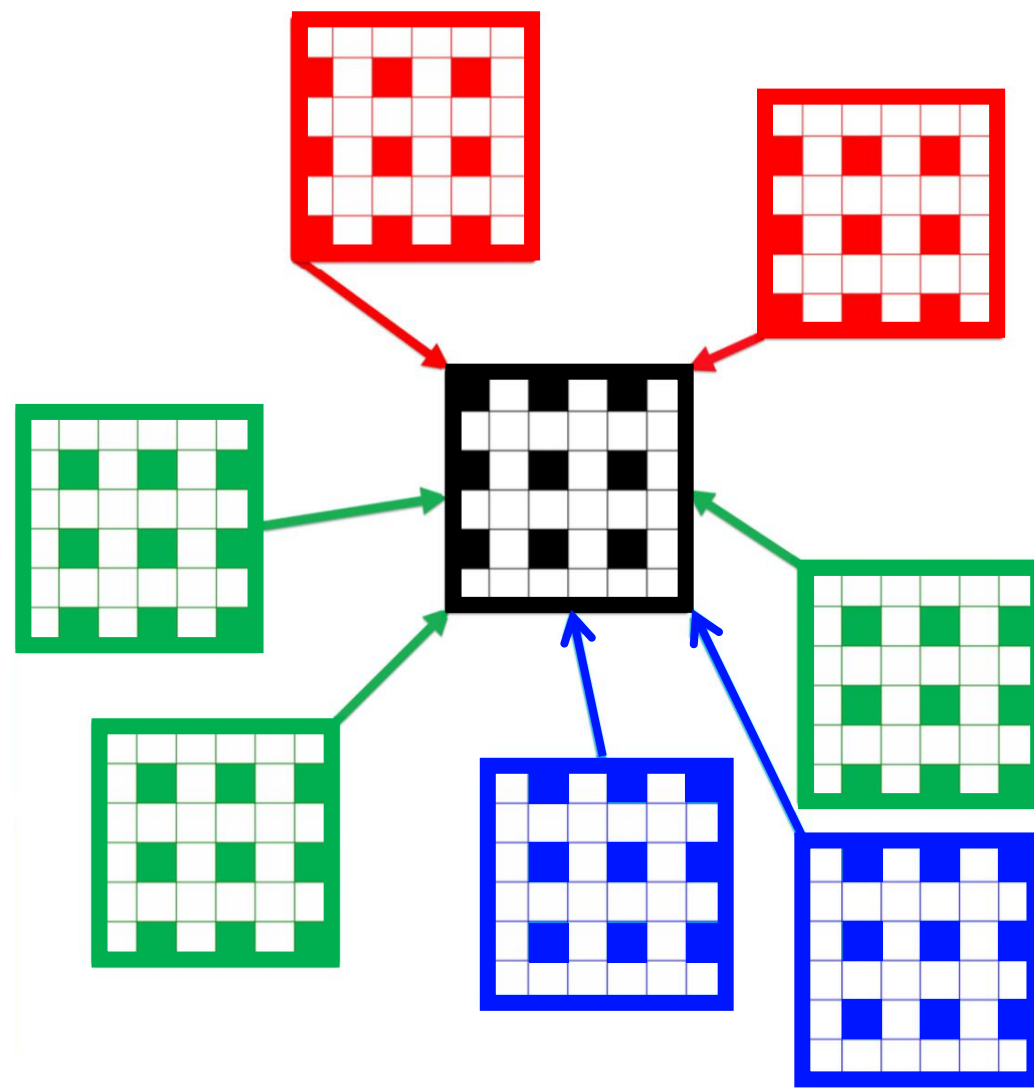
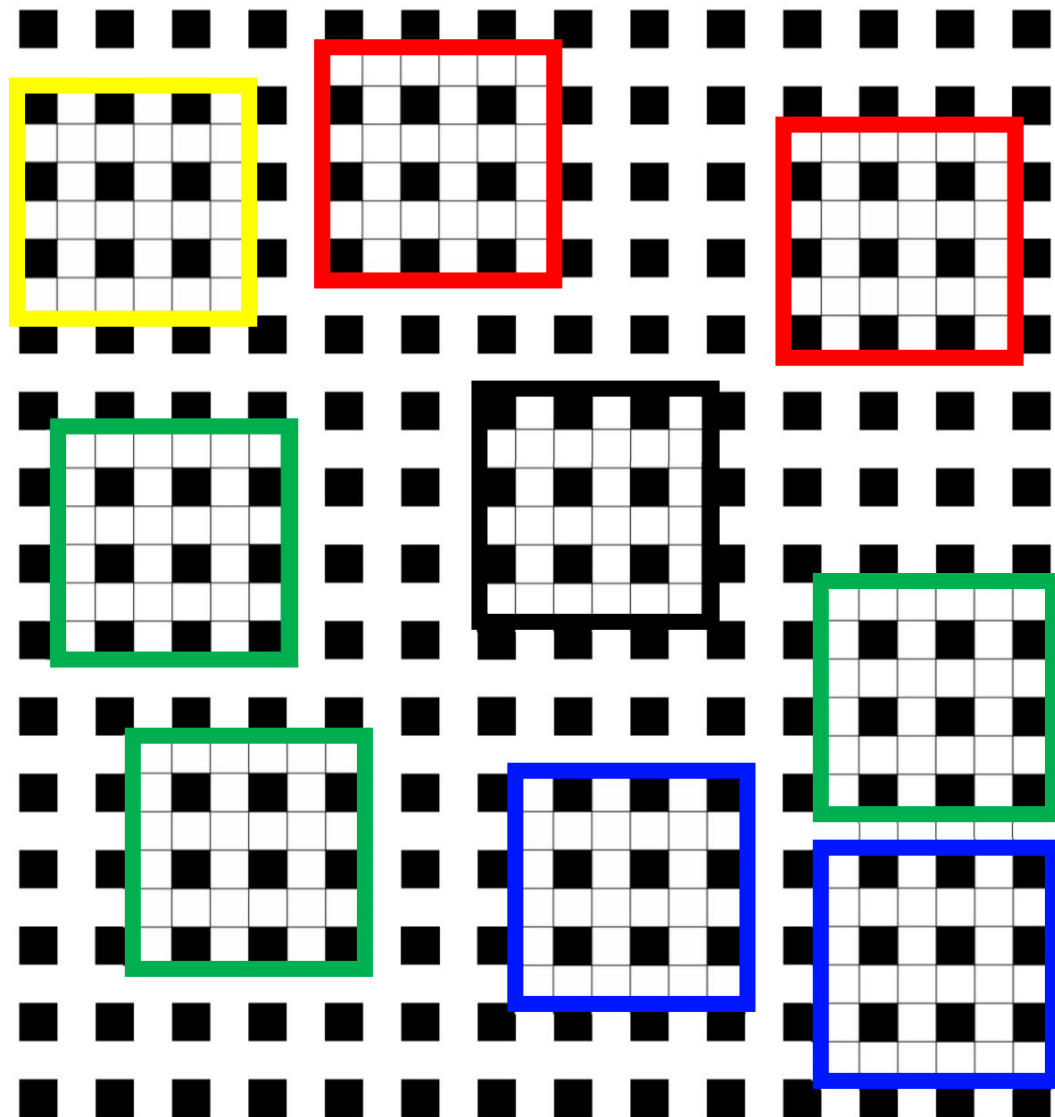
# Exploit Semi-Local Similarity

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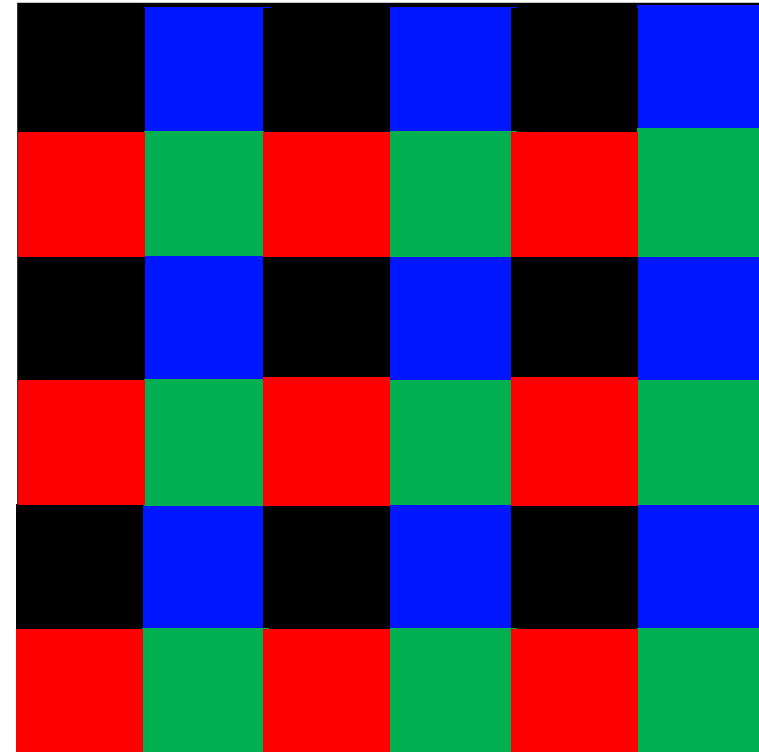
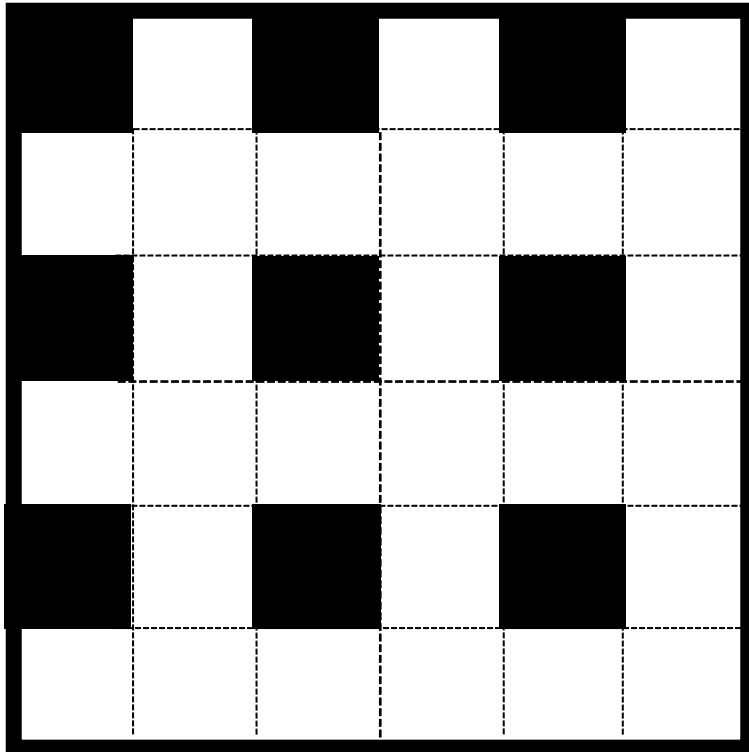


# Exploit Semi-Local Similarity



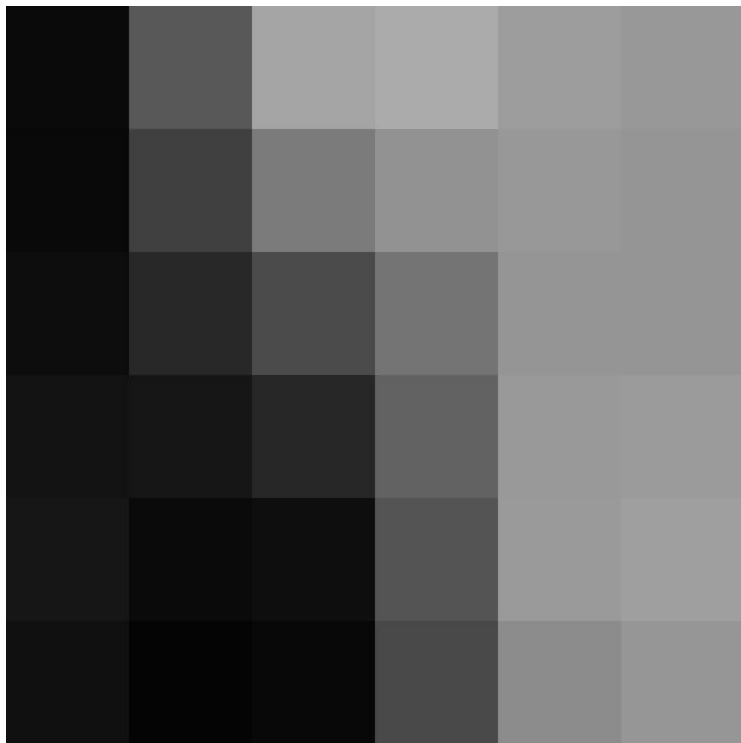
# Exploit Semi-Local Similarity

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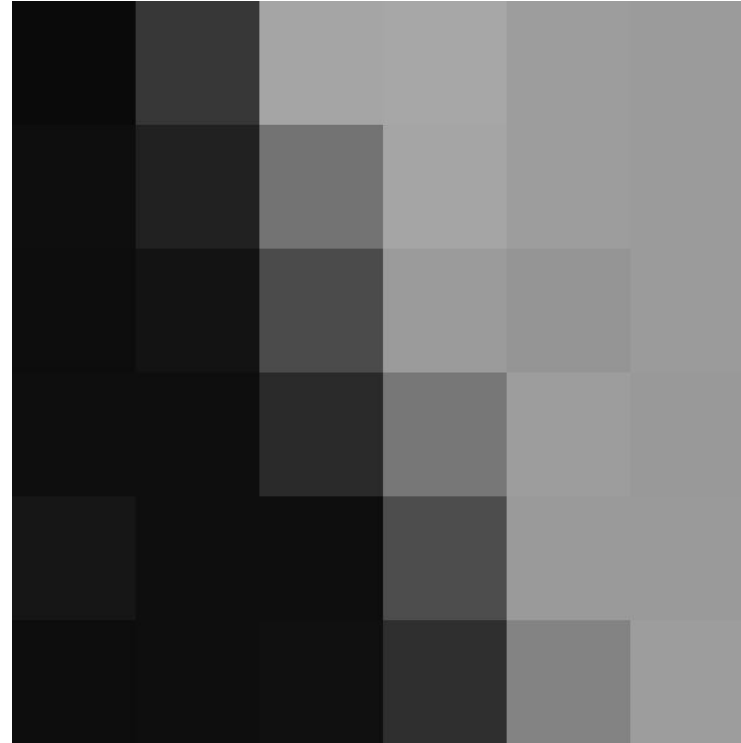


# Exploit Semi-Local Similarity

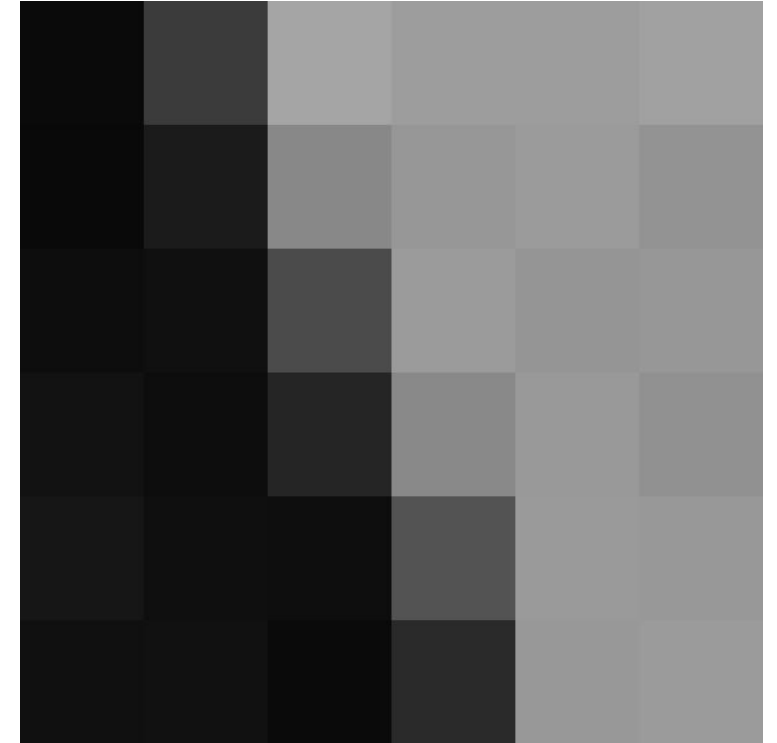
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(a) initial estimate



(b) after first iteration



(c) ground-truth

# Scheme of Each Iteration

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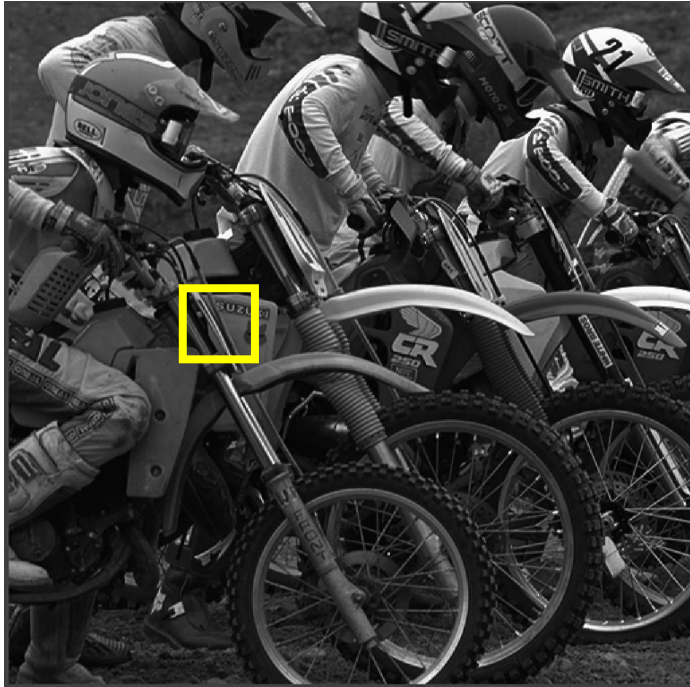
- Decompose an image into overlapping patches
- Update each patch:
  - ❖ Identify the positions of similar patches
  - ❖ Compute the weights of similar patches
- Average the contribution of overlapping patches to each missing pixel

# Unique Features

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- Robust initialization of the positions of similar patches
- Regularization of the weights of similar patches

# Robust Position Initialization



HR Image and a window of interest

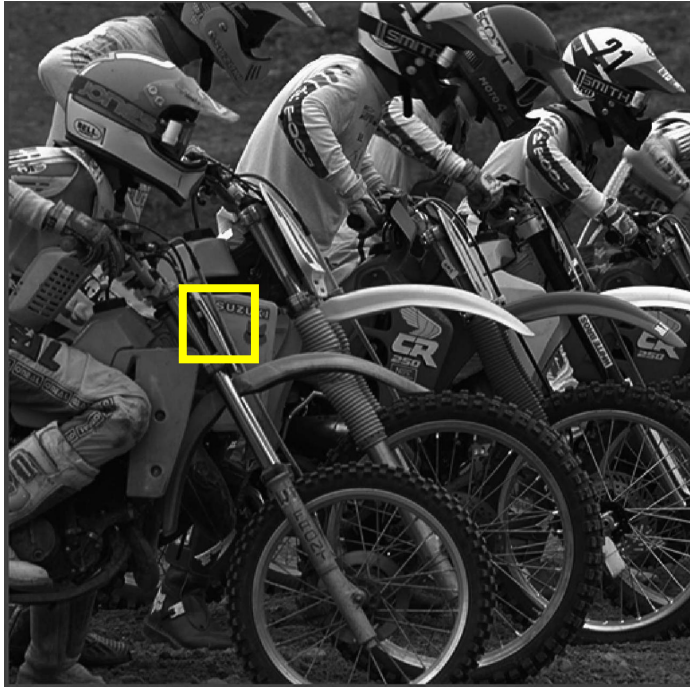


Bicubic Initial Estimate

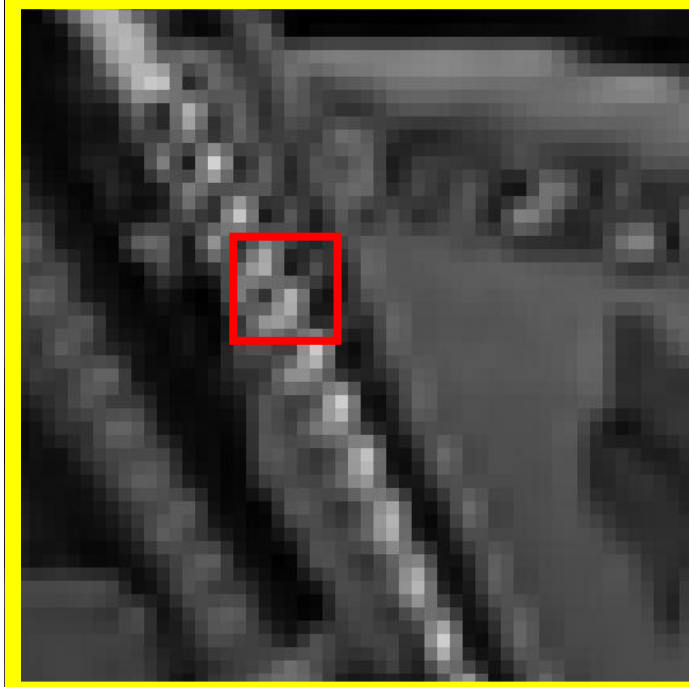


HR image

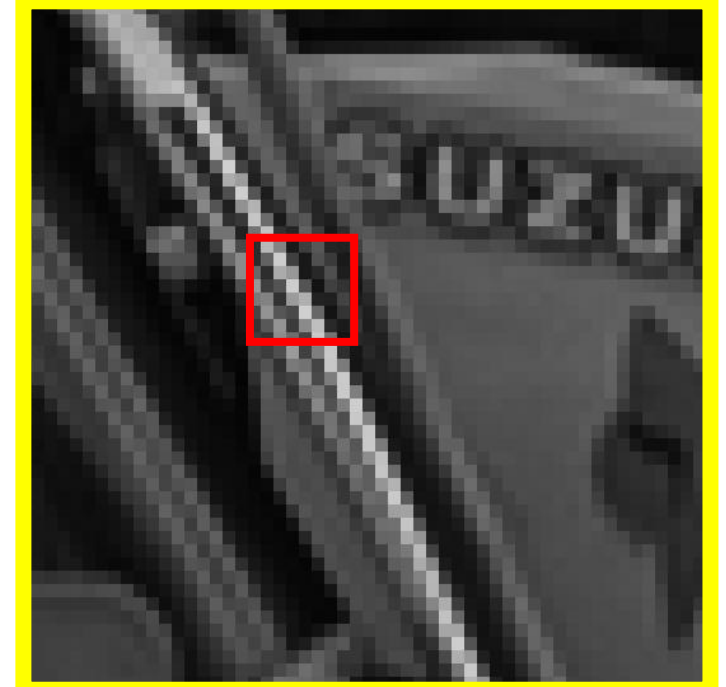
# Robust Position Initialization



HR Image and a  
window of interest

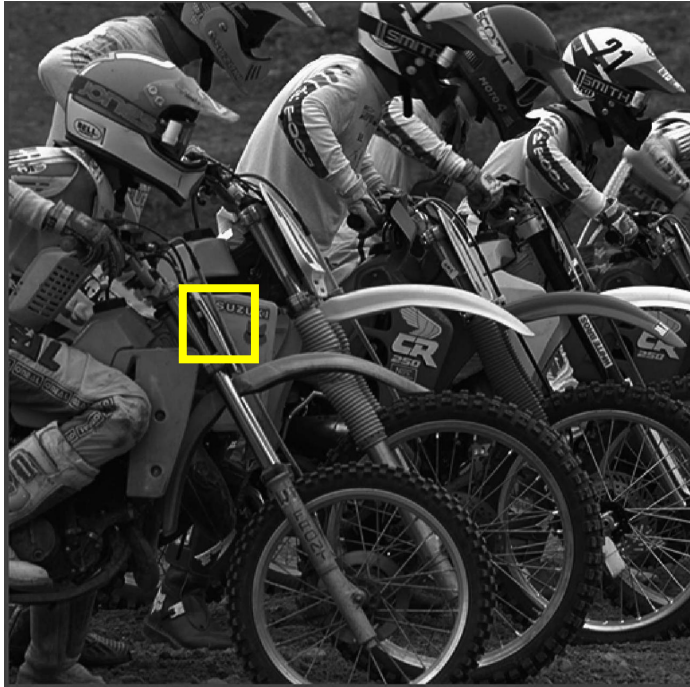


Bicubic Initial Estimate  
target patch

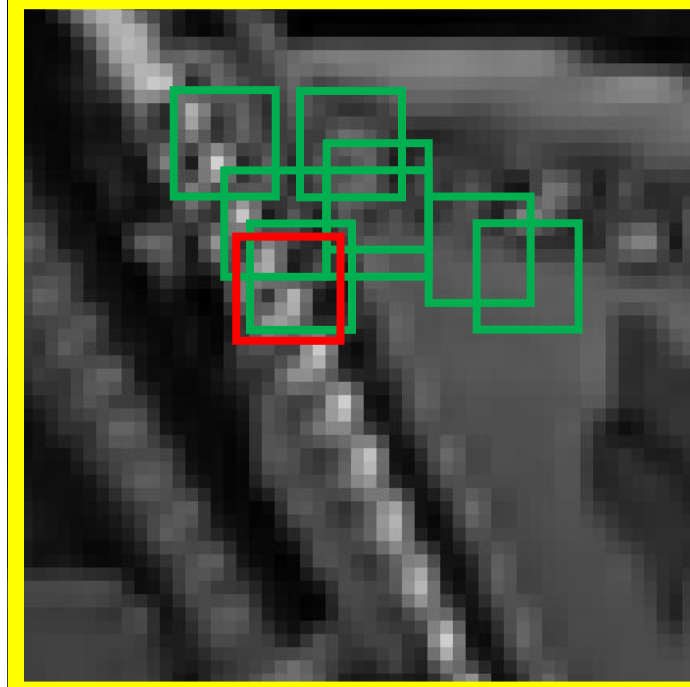


HR image  
target patch

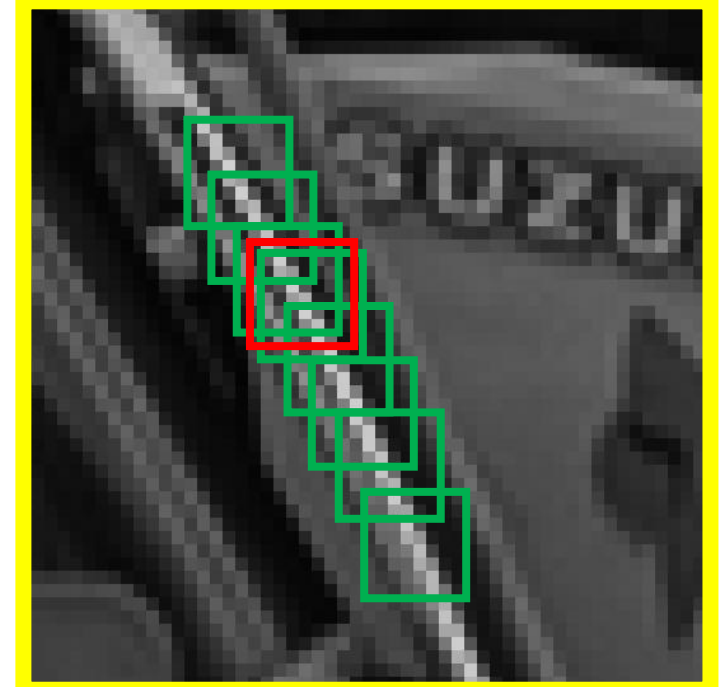
# Robust Position Initialization



HR Image and a window of interest



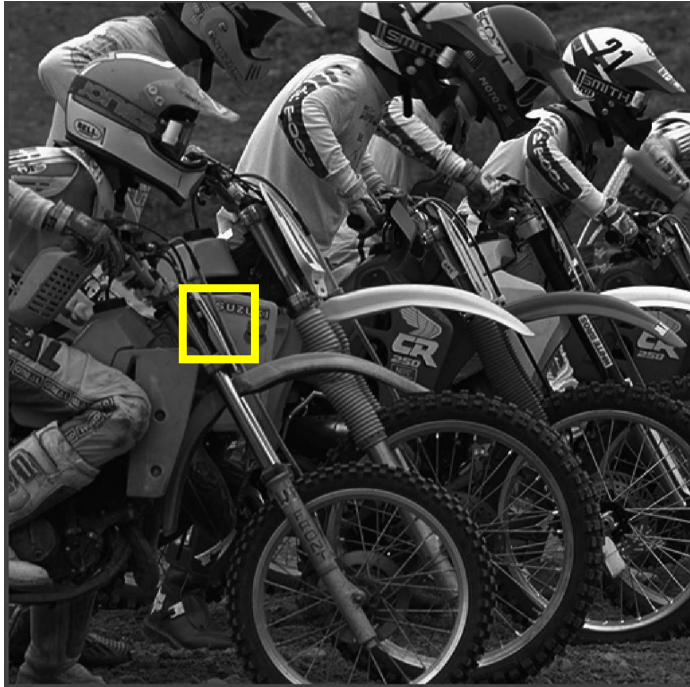
Bicubic Initial Estimate  
target patch and  
similar patches



HR image  
target patch and  
similar patches



# Robust Position Initialization



HR Image and a window of interest

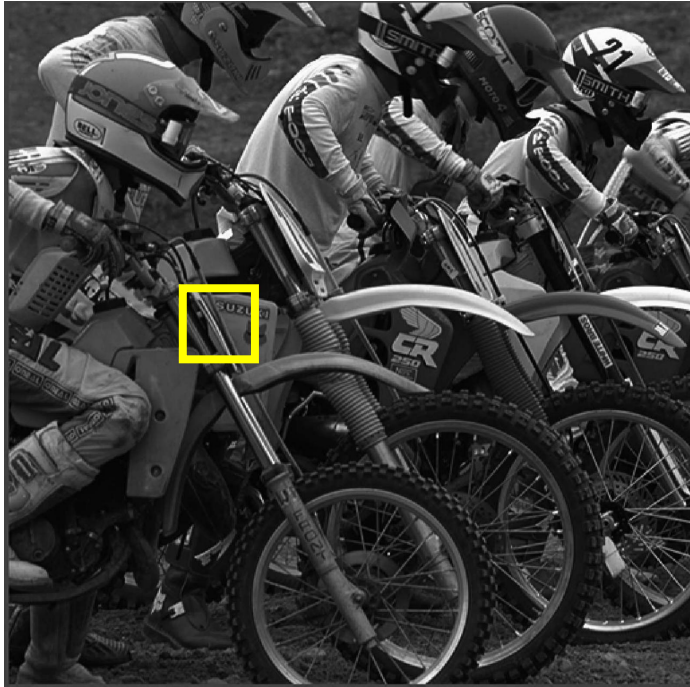


Guide Image

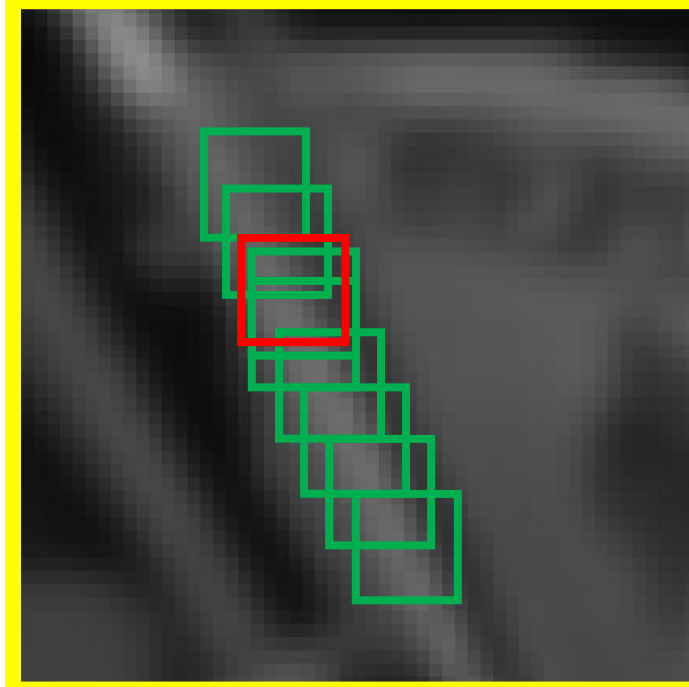


HR image

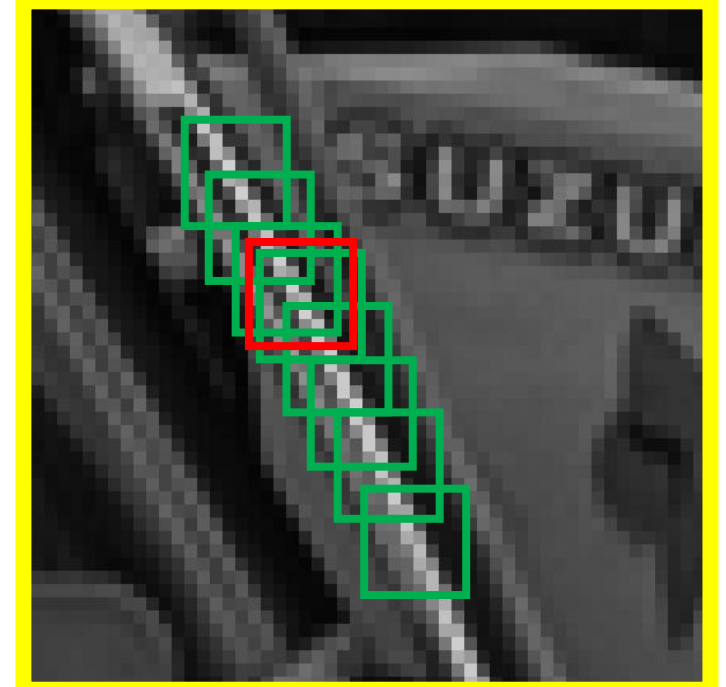
# Robust Position Initialization



HR Image and a window of interest

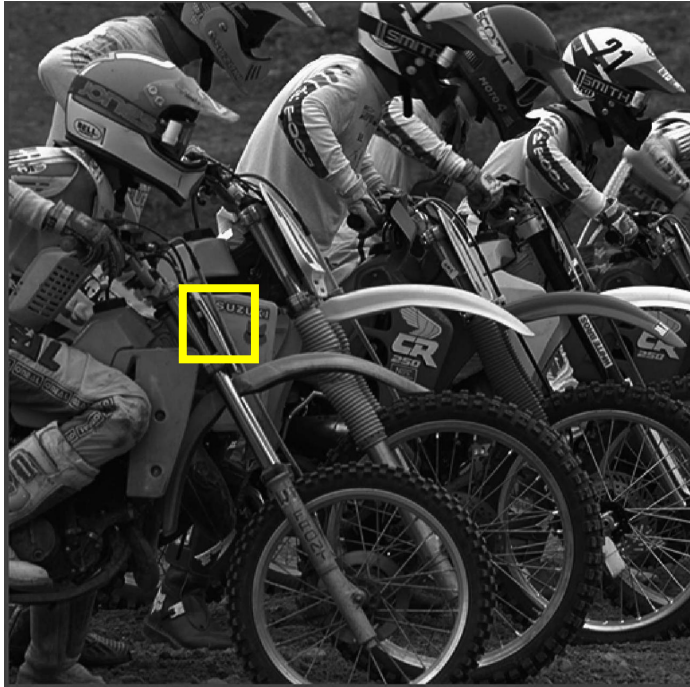


Guide Image  
target patch and  
similar patches

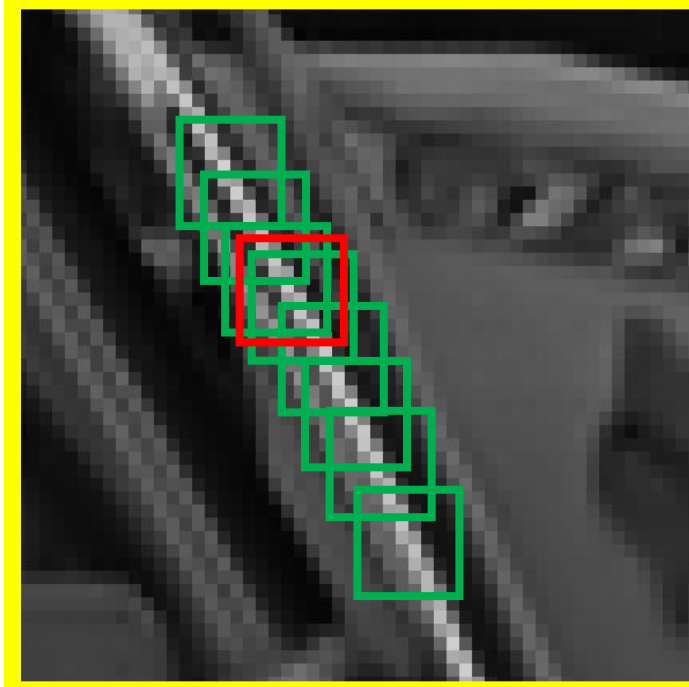


HR image  
target patch and  
similar patches

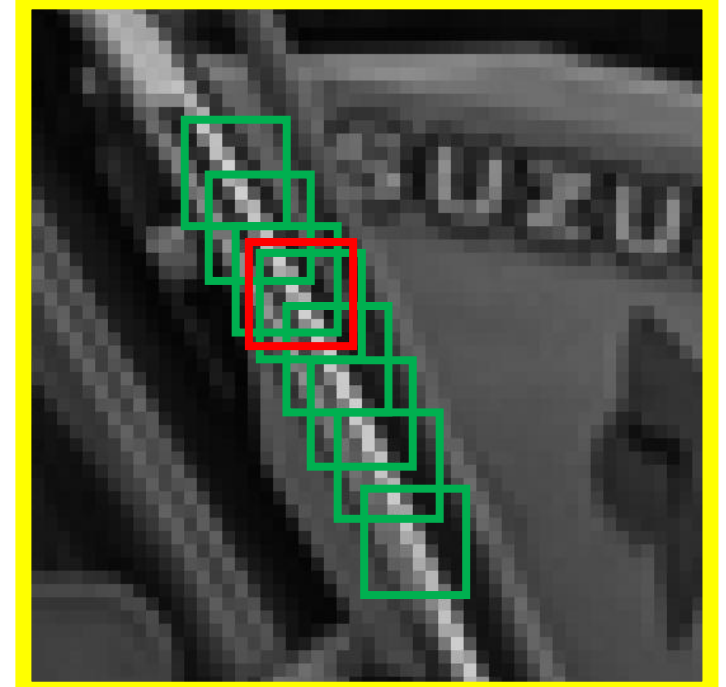
# Robust Position Initialization



HR Image and a window of interest



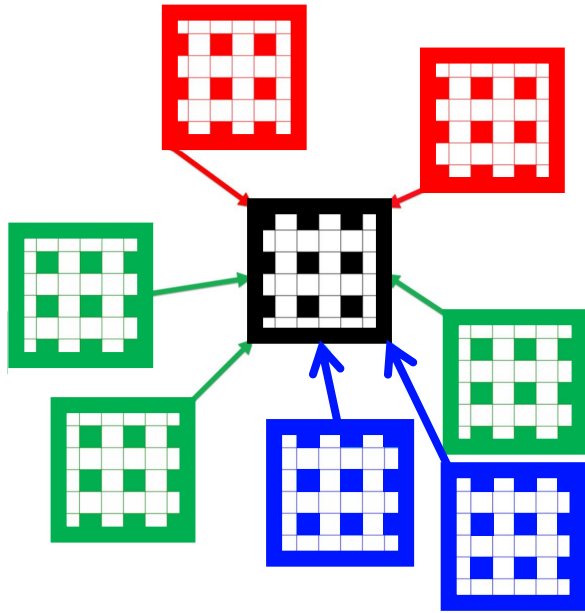
Input Image in Last Iter  
target patch and  
similar patches



HR image  
target patch and  
similar patches

# Regularized Weights

$$\omega = \arg \min \left[ \underbrace{\|Q_i \omega - p_i\|_2^2}_{\text{Data Fidelity Term}} + \underbrace{\lambda \omega^T \Sigma \omega}_{\text{Penalty Term}} \right]$$



Data Fidelity Term

Penalty Term

# Testset



USC-SIPI Database  
Berkeley Segmentation Database

# Quantitative Comparison

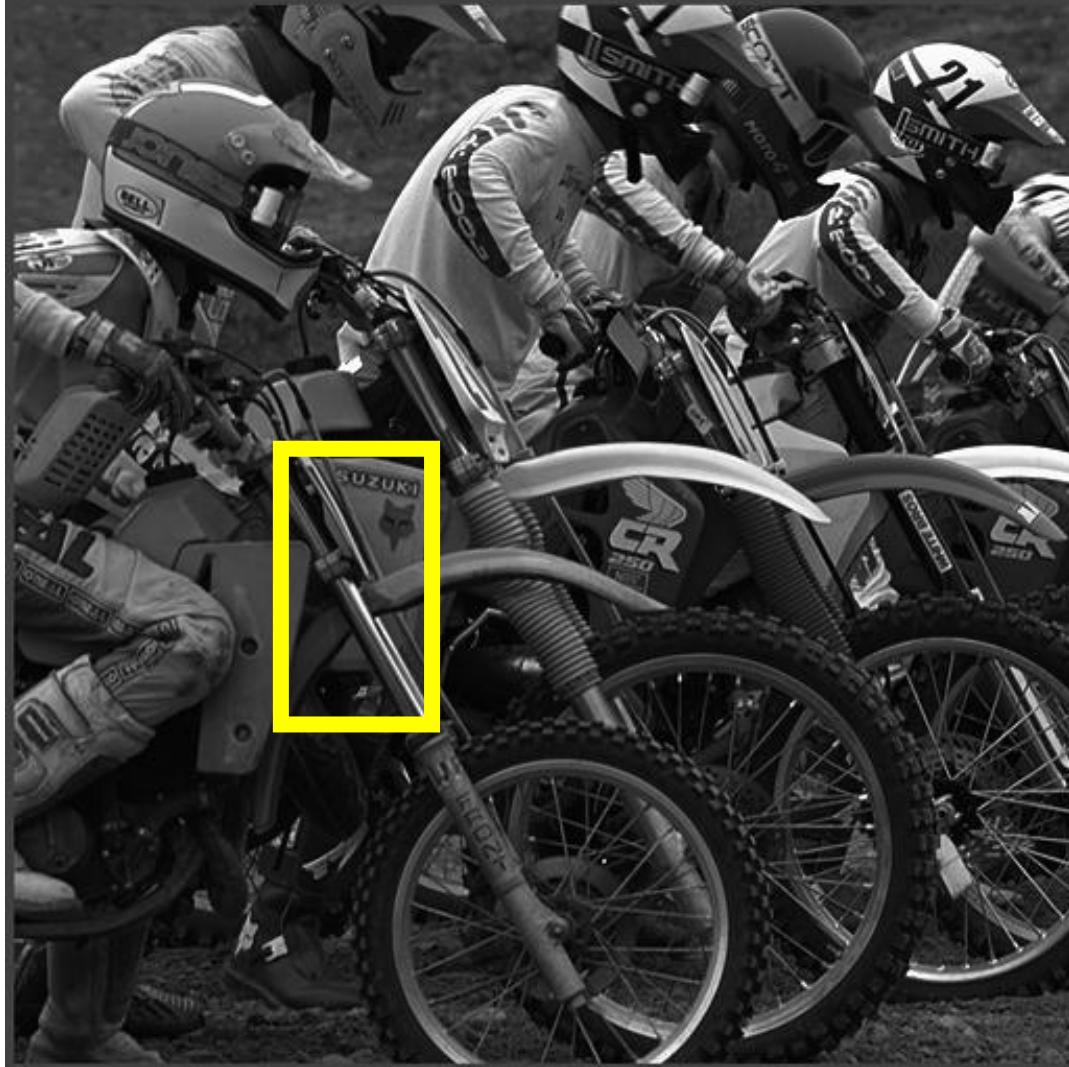
Table 1: Comparison of Average PSNR (in decibels) of interpolated images.

Method	X2	X3
NEDI [Li & Orchard, 2001]	30.25	/
SAI [Zhang & Wu, 2008]	30.80	/
SME [Mallat & Yu, 2010]	30.74	/
RLLR [Liu et al., 2011]	30.80	/
NARM [Dong et al., 2013]	31.20	27.29
ANSM [Romano et al., 2014]	31.32	27.54
NLPC [Sun et al., 2015]	31.31	27.64
NGSDG [Zhu et al., 2016]	30.76	/
<b>Proposed</b>	<b>31.64</b>	<b>27.86</b>

$$*\text{PSNR} = 20 \log_{10} \left( \frac{255}{\sqrt{\text{MSE}}} \right)$$

# Visual Comparison (X2)

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# Visual Comparison (X2)

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Original



Bicubic



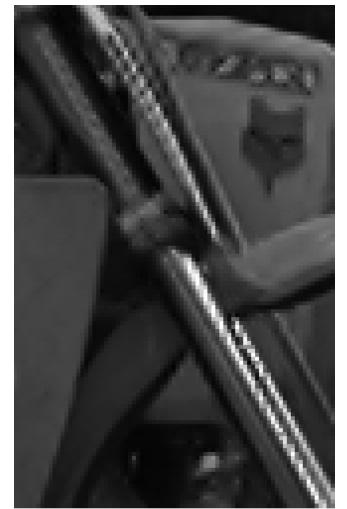
NEDI



SME



SAI



RLLR



NGSDG



NARM



ANSM



NLPC



Proposed



# Runtime Comparison (X2)

Table 2: Comparison of runtimes (in seconds) of interpolating a 128X128 LR image to a 256X256 HR image. Platform: Intel 2.6G Hz 18-Core Intel i9 processor, Matlab R2018b, C++ (GCC 7.3.0), Eigen 3, OpenMP.

Method	Programming Details	Runtime/second
NARM [Dong et al., 2013]	Matlab, Non-Parallel	43.4 ~ 138.9
ANSM [Romano et al., 2014]	Matlab, C/C++ MEX	1265.0
<b>Proposed</b>	Matlab, Non-Parallel	<b>155.6</b>
	Matlab, Parallel	<b>13.3</b>
	C++, Parallel	<b>3.6</b>

# Conclusion

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- Novel Way to Improve Exploitation of Semi-Local Similarity
- State-of-the-art PSNR
- Simple, Parallerizable Algorithm