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### Motivation of research

**Observation.** Given modern computational capabilities, it is possible to obtain new intra prediction modes as outcome of a training experiment; *Pfaff et al. 2018.* 

A question to ask. Given the computational burden of the conventional intra prediction modes as upper bound, are these predictors optimal among all?





**Fig.** 1 Generation of an intra prediction signal.

**Our goal.** Train affine-linear predictors which use one line of reconstructed boundary samples as input and require at most four multiplications per sample to predict.

### **Description of the trained predictors**

**Overview.** We propose to train N = 35 intra prediction modes on a large set of high resolution images as training data. The prediction consists of the following three steps:



Fig. 2 Flow chart of the trained intra prediction.

## An Affine-Linear Intra Prediction With Complexity Constraints

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Low pass analysis. The low-pass-filtered boundary  $bdry_{red}$  consists of two samples along each axis in the case of (4,4)-blocks and four samples else. Given the width  $W = 4 \cdot 2^n, n \ge 0$ , one computes

$$\mathrm{bdry}_{red}^{top}[i] = \begin{cases} \frac{1}{2^n} \sum_{j=0}^{2^n - 1} \mathrm{bdry}^{top}[2^n i + j], & \text{if } n > 0, \\ \\ \frac{1}{2} \left( \mathrm{bdry}^{top}[2i] + \mathrm{bdry}^{top}[2i + 1] \right), & \text{else.} \end{cases}$$
(1)

The low subband of the left boundary  $bdry_{red}^{left}$  is obtained analogously.

Matrix-Vector-Multiplication. Given the prediction mode k, the low subband of the prediction signal  $\operatorname{pred}_{red}$  is computed as

 $\operatorname{pred}_{red} = A_k \cdot \operatorname{bdry}_{red}$ 

The dimension  $(W_{red}, H_{red})$  of the low-pass signal pred<sub>red</sub> equals (4, 4)if  $\max(W, H) \leq 8$ . In any other case holds

> $(W_{red}, H_{red}) = (\min(W, 8), \min(H, 8)).$ (3)

The expression (2) requires not more than 4WH multiplications.

**Linear interpolation.** Assume  $W \geq H$ . The vertically interpolated signal pred<sup>*up*</sup><sub>*red*</sub> is given for  $y = 0, ..., H_{red} - 1, x = 0, ..., W_{red} - 1$  as

$$\operatorname{pred}_{red}^{up}[x][2y+1] = \operatorname{pred}_{red}[x][y],$$

$$\operatorname{pred}_{red}^{up}[x][2y] = \frac{1}{2}(\operatorname{pred}_{red}[x][y-1] + \operatorname{pred}_{red}[x][y]). \tag{4}$$
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The step (4)

### Training design.

- We train a single joint layer and N different linear output layers.
- Simplify after training by multiplying the weights from both layers.
- The predictors for shapes (4, 4), (8, 8) and (16, 16) are trained jointly in one run using a recursive quad-tree.

### Memory assessment.

Shape $(W, H)$	Input dim	Output dim	Nr. of $(A_k, b_k)$	Bits per entry	Memory in kB
W = H = 4	4	16	18	10	1.8
$\min(W,H) \le 8$	8	16	18	10	3.24
else	8	64	18	10	12.96

$$_{ed} + b_k. \tag{2}$$

### Loss function

$$L(\text{org}, k) = \sum_{i=1}^{WH} (|(c_k)_i| + \alpha g(\beta | (c_k)_i | - \gamma)) = \sum_{i=1}^{WH} l((c_k)_i), \quad (5)$$



### Experimental results and conclusion

All Intra	Y	Enc Time	Dec Time
Class A1	-1.38%	152%	104%
Class A2	-0.75%	151%	103%
Class B	-0.79%	155%	101%
Class C	-0.86%	154%	100%
Class E	-1.11%	151%	98%
Overall	-0.95%	153%	101%

- The predictors employ subband decomposition



Given the DCT-transformed residuals of prediction mode k by  $c_k = T(\text{org} - \text{pred}_k)$ , we approximate the bit-rate of the residuals as

where  $\alpha, \beta, \gamma$  are hand-tuned parameters. The total loss of a block is modelled as the sum of L and the signalling cost for the mode index k.

> Fig. 3 Profile of the function lin (5).

It penalizes nonzero coefficients. For large coefficients, the curve flattens.

**Table 1** BD-rate savings over VTM-3.0 (CTC; *JVET-L1010*).

• Novel data-driven training of affine-linear intra prediction modes

• Good trade-off between memory, complexity and bit-rate savings