$\left| \begin{array}{c} 1 \\ 2 \\ 2 \\ 0 \\ 1 \\ 9 \\ \end{array} \right|$ 

### Introduction •

• Hazy Image Generation Process

 $\mathbf{I}(\mathbf{x}) = \mathbf{J}(\mathbf{x})t(\mathbf{x}) + (1 - t(\mathbf{x}))\mathbf{A}$ 

#### Physically Grounded Priors

Dark channel prior (DCP, PAMI, 2011); Color lines prior (TOG, 2014); Color attenuation prior (*TIP*, 2015); Non-local prior (*CVPR*, 2016); Color ellipsoid prior (*TIP*, 2018).

• Deep Learning Methods Dehaze-Net (TIP, 2016); Multi-scale CNN (ECCV, 2016); AOD-Net (ICCV, 2017); FEED-Net (ICME, 2018); Flexible cascaded CNN (Access, 2018); Proximal Dehaze-Net (ECCV, 2018).

#### Motivations

- DCP-based methods easily fail since DCP assumption is based on statistical analysis in non-sky regions.
- > Learning-based dehazing performance is dependent upon the diversity and volume of training datasets.

# **Two-Step Framework**



Step 1: Coarse transmission via DCP and luminance fusion Step 2: Fine transmission via variational regularized model

# Variational Regularized Transmission Refinement For Image Dehazing Qiaoling Shu<sup>1</sup>, Chuansheng Wu<sup>1</sup>, Zhe Xiao<sup>2</sup>, Wen Liu<sup>1</sup> <sup>1</sup>Wuhan University of Technology, China; <sup>2</sup>A\*STAR, Singapore

## **Coarse Transmission**

### DCP-Based Transmission

#### • Luminance-Based Transmission

$$\overline{t}_{l}(\mathbf{x}) = e^{-\frac{\beta\tau}{L^{*}}L(\mathbf{x})}$$

$$\beta = \begin{cases} 0.3324 \text{ Red channel} \\ 0.3433 \text{ Green channel} \\ 0.3502 \text{ Blue channel} \end{cases}$$

$$\bar{t}(\mathbf{x}) = \chi(\mathbf{x})\bar{t}_{\mathrm{d}}(\mathbf{x}) + \mathbf{x}_{\mathrm{d}}(\mathbf{x}) + \mathbf{x}$$

with transmission weight

 $\chi(\mathbf{x}) = \frac{1}{1 + e^{-\theta_1 \overline{t}_d(\mathbf{x}) - \theta_2}}$ 

### Fine Transmission

Image Degradation Model

 $\overline{I}(x) = \overline{J}(x)t(x)$  with  $\overline{I} = A - I$  and  $\overline{J} = A - J$ 

 Variational Regularized Model (Solver: ADMM)  $\min_{\bar{I},t} \frac{\lambda_1}{2} \|\bar{I} - \bar{J}t\|_2^2 + \frac{\lambda_2}{2} \|t - \bar{t}\|_2^2$  $+\lambda_3 \|W \circ (\nabla t - \nabla I)\|_1 + \lambda_4 \|\nabla \overline{J}\|_1 + \lambda_4 \|\nabla V \overline{J}\|_1$ where  $I = \mathbf{I}_{c}, \, \overline{I} = \overline{\mathbf{I}}_{c}$  and

(h) Dehazing with (g)



d 
$$\overline{J} = \overline{\mathbf{J}}_c$$
 for  $c \in \{r, g, b\}$ .





# Conclusions

He-13: IEEE TPAMI, 2013, 35(6): 1397-1409; Ren-16: ECCV, 2016, 154-169; Chen-16: ECCV, 2016, 576-591; Berman-16: IEEE CVPR, 2016, 1674-1682; Liu-17: CVIU, 2017, 162: 23-33.

 A joint variational regularized model with hybrid constraints was proposed to implement transmission map refinement and haze-free image estimation.

The resulting nonsmooth optimization problem was effectively solved via an ADMM-based numerical method.