

1. Introduction

Depth imaging using single-photon Lidar

- Active imaging using pulsed-lasers
- Accurate depth/range resolution (< centimeters at several hundreds of meters in air)

⇒ 3D image reconstruction

- Long range imaging (defence)
- Building monitoring (heritage conservation)
- Environmental sciences: forest monitoring
- Underwater imaging

Single-surface observation model

- observed Lidar waveform $\mathbf{y}_{i,j} = [y_{i,j,1}, \dots, y_{i,j,T}]^T$

$$y_{i,j,t} | r_{i,j}, t_{i,j}, b_{i,j} \sim \mathcal{P}(r_{i,j} g_0(t - t_{i,j}) + b_{i,j})$$

- $y_{i,j,t}$: photon count within the t th bin of the pixel (i, j)
- $b_{i,j} > 0$: background and dark photon level
- $t_{i,j}$: position of an object (if present) at a given range from the sensor
- $r_{i,j}$: object reflectivity
- $g_0(\cdot) > 0$: instrumental impulse response

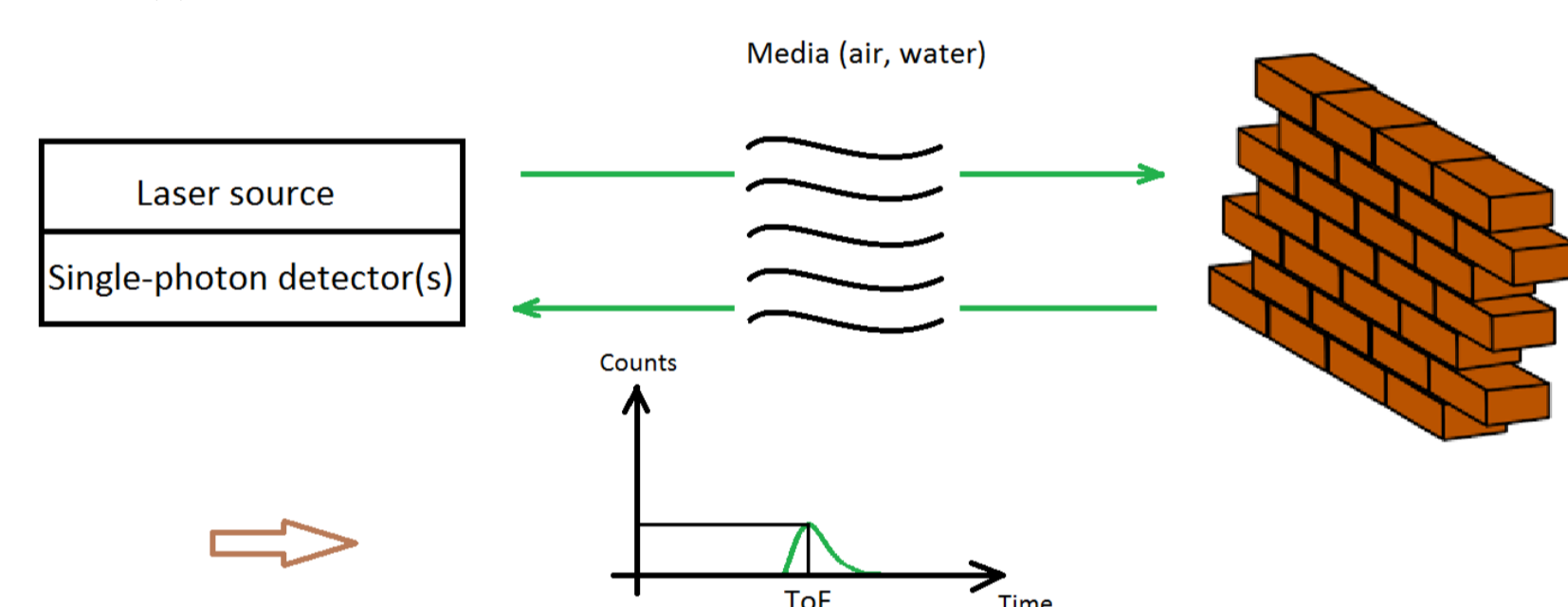


Fig. 1: Single-photon Lidar principle.

3. Reversible-Jump Markov chain Monte Carlo algorithm

- Bayesian estimation in union of subspaces
 - Pixel-wise model selection but...
 - Dependencies between pixels (spatial correlation)
- ⇒ MCMC method for global Bayesian inference

Moves within a subspace

- Updating $b_{i,j}$ and $r_{i,j}$: standard Gibbs step (conditional distr. → mixtures of gamma distributions)
- Updating $t_{i,j}$: Sampling from a discrete distribution (finite support)

Moves between subspaces

- Move from $z_{i,j} = 0$ to $z_{i,j} = 1$: Proposal distribution designed to generate candidates in **regions of high prob.** → **High acceptance rate** (good mixing properties)

Other parameters

- Updating β : standard Gibbs step (conditional distr. → inverse-gamma)
- Updating α : Metropolis-Hastings step (non-standard conditional distr.)
- Updating c : stochastic gradient (during burn-in) [3]

4. Results

Data acquisition

- Detection of a life-sized polystyrene head at 325m
- 3 acquisitions : noon, 3p.m., and 8p.m
- Different acquisition times per pixel

Target detection problem

- Usually performed during post-processing (reflectivity thresholding)
- Estimation and detection performance highly dependent on the background levels
- Severe performance degradation in the limit of low “useful” detections

Model selection problem

- observed pixel spectrum

$$y_{i,j,t} | z_{i,j} = 0, \theta_{i,j}^0 \sim \mathcal{P}(b_{i,j}) \quad (1)$$

$$y_{i,j,t} | z_{i,j} = 1, \theta_{i,j}^1 \sim \mathcal{P}(r_{i,j} g_0(t - t_{i,j}) + b_{i,j}) \quad (2)$$

- $z_{i,j}$: binary label for target detection
- $\theta_{i,j}^0 = r_{i,j} \in \mathbb{R}^+$
- $\theta_{i,j}^1 = [r_{i,j}, t_{i,j}, b_{i,j}] \in \mathbb{R}^+ \times \mathbb{T} \times \mathbb{R}^+$
- \mathbb{T} : admissible set of target ranges

Proposed method: Joint target detection and depth/reflectivity estimation using Bayesian inference

2. Proposed Bayesian model

Likelihoods

- Defined by (2) and (3)

Parameter prior distributions

- Background levels: **Gamma Markov random** [1, 2] to capture spatial dependencies affecting the ambient illumination
- Improves the parameter estimation in the limit of few detected counts.

- Depth/range parameters:

Uniform prior distributions $p(t_{i,j} = t | z_{i,j} = 1)$ to reflect the lack of knowledge about the 3D structure of the scene

- Reflectivity coefficients:

Hierarchical prior model using conjugate gamma/inverse-gamma priors

$$r_{i,j} | \alpha, \beta \sim \mathcal{G}(\alpha, \beta), \quad \forall (i, j)$$

$$\alpha | \alpha_1, \alpha_2 \sim \mathcal{G}(\alpha_1, \alpha_2)$$

$$\beta | \beta_1, \beta_2 \sim \mathcal{IG}(\beta_1, \beta_2)$$

- Detection/model selection labels:

Ising model

$$f(\mathbf{Z} | c) \propto \exp[c\phi(\mathbf{Z})]$$

$$-\phi(\mathbf{Z}) = \sum_{i,j} \sum_{(i',j') \in \mathcal{V}_{i,j}} \delta(z_{i,j} - z_{i',j'})$$

– $\delta(\cdot)$: Kronecker delta function

– $\mathcal{V}_{i,j}$: set of neighbours of pixel (i, j)

– c : spatial granularity parameters

Joint posterior distribution

$$f(\mathbf{Z}, \Theta, \alpha, \beta | \mathbf{Y}, c) \propto \prod_{i,j} f(y_{i,j} | z_{i,j}, \theta_{i,j}) f(\theta_{i,j} | \mathbf{Z}, \alpha, \beta) \times f(\mathbf{Z} | c) f(\alpha) f(\beta).$$

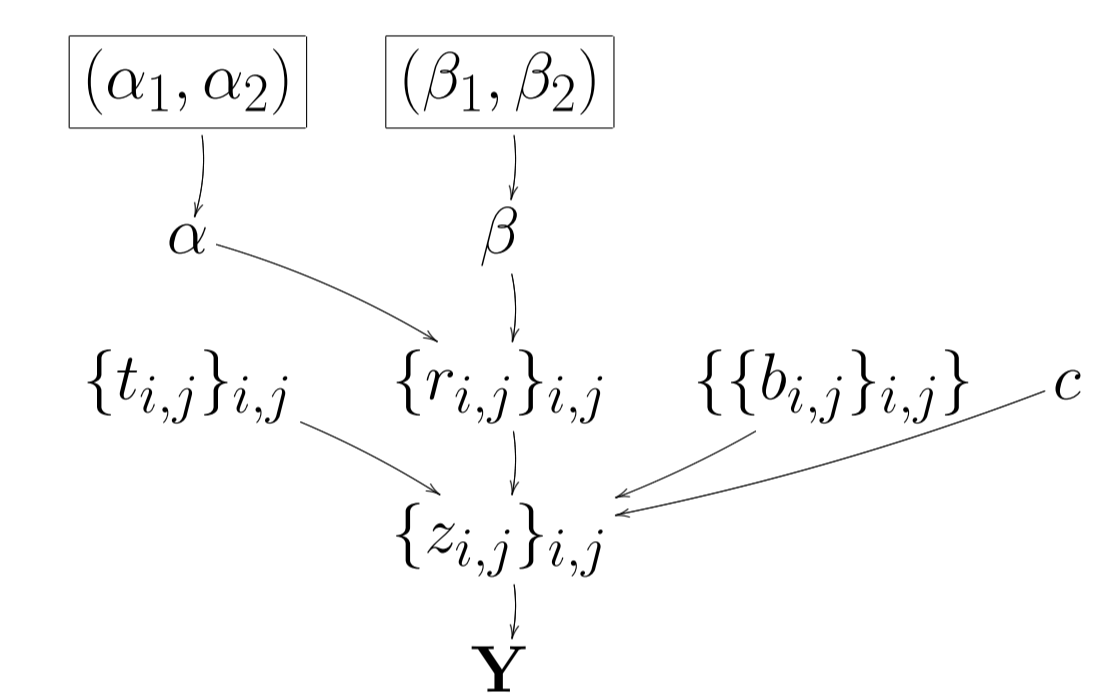


Fig. 2: Directed acyclic graph (DAG) representing the proposed hierarchical Bayesian model.

Estimation performance

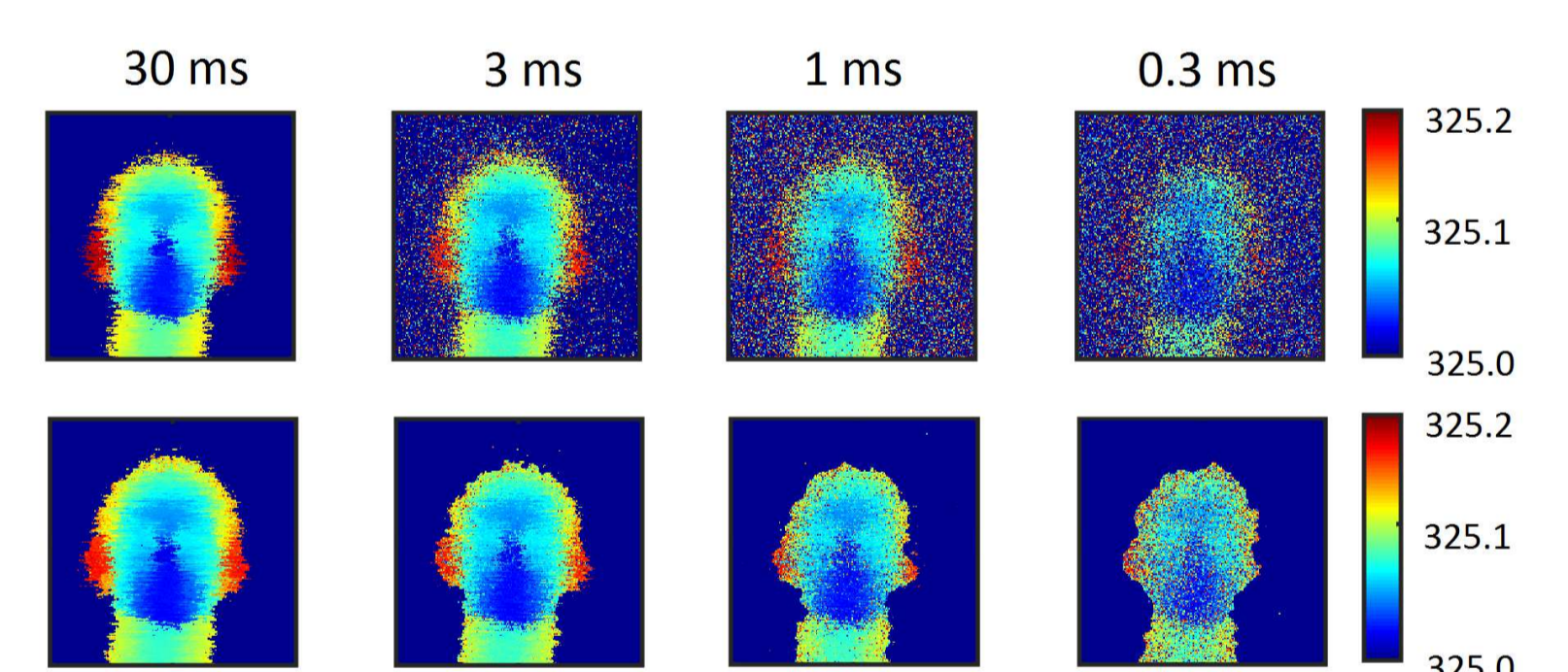


Fig. 4: Target ranges estimated by the standard (top) and proposed (bottom) method.

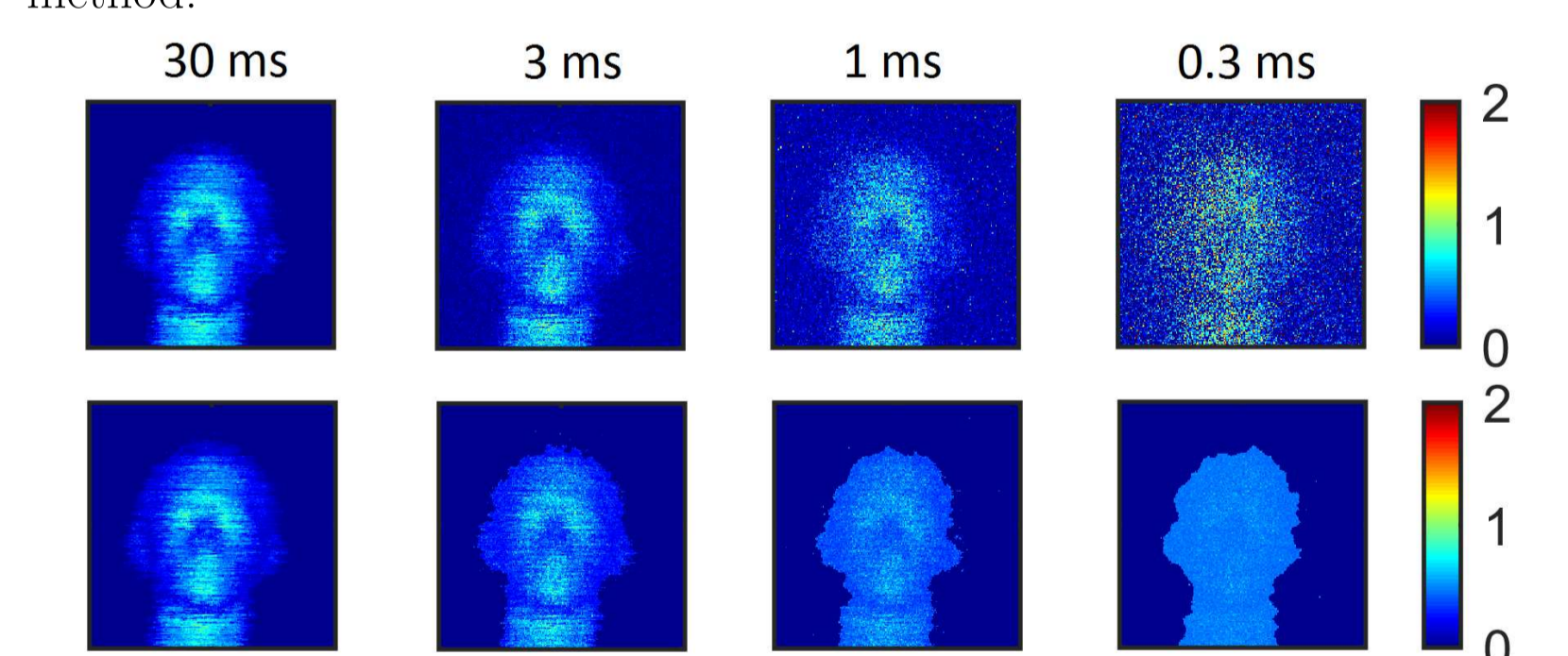


Fig. 5: Target reflectivity (noon) estimated by the standard (top) and proposed (bottom) method.

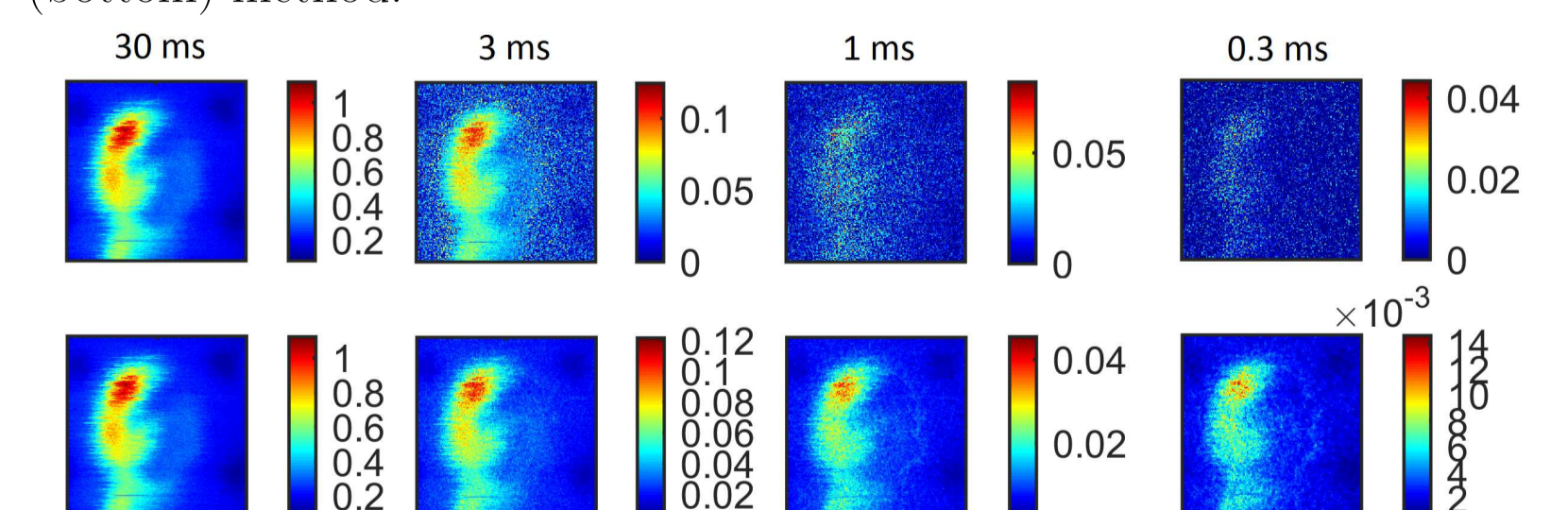


Fig. 6: Background levels (noon) estimated by the standard (top) and proposed (bottom) method.

References

- [1] O. Dikmen and A. Cemgil, “Gamma markov random fields for audio source modeling,” IEEE Trans. Audio, Speech, Language Processing, vol. 18, no. 3, pp. 589-601, March 2010.
- [2] Y. Altmann, X. Ren, A. McCarthy, G. S. Buller, and S. McLaughlin, “Lidar waveform based analysis of depth images constructed using sparse single-photon data,” IEEE Trans. Image Processing, 2016, to appear.
- [3] M. Pereyra, N. Whiteley, C. Andrieu, and J.-Y. Tourneret, “Maximum marginal likelihood estimation of the granularity coefficient of a Potts-Markov random field within an mcmc algorithm,” in Proc. IEEE-SP Workshop Stat. and Signal Processing, Gold Coast, Australia, July 2014.

		Acquisition Time			
		300μs	1ms	3ms	30ms
Av. photon counts	noon	5.6	18.5	55.5	554.6
	3 p.m.	4.1	13.7	41.0	408.9
	8 p.m.	1.2	4.9	11.6	116.0
Empty pixels (%)	noon	2.79	< 0.01	0	0
	3 p.m.	4.2	0.02	0	0
	8 p.m.	61.8	52.2	40.4	2.2

Table 1: Average number of detected photons per pixel and proportion of empty pixels for the different acquisitions.

Detection performance



		Acquisition Time				
		300μs	1ms	3ms	30ms	
noon	3ms	X-corr	79.9	20.1	8.9	91.1
		Prop. algo.	99.9	0.01	10.8	89.2
	1ms	X-corr	57.4	42.6	16.9	83.1
Prop. algo.		99.9	0.01	18.6	81.4	
0.3ms	X-corr	59.6	40.4	39.1	60.9	
	Prop. algo.	99.9	0.01	20.4	79.6	

Table 2: Detection performance (prob. in %)

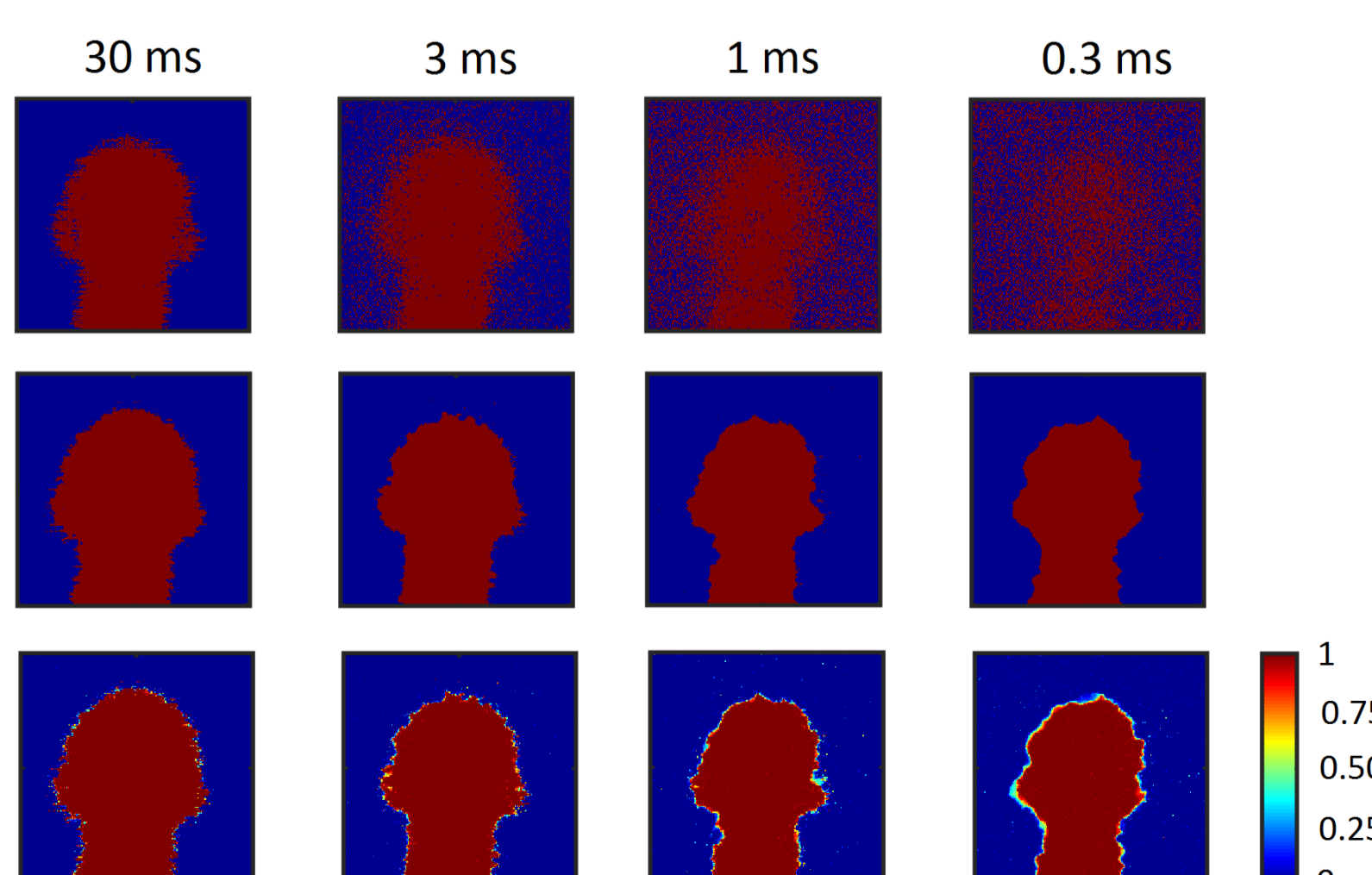


Fig. 3: Example of detection (noon) results obtained by the standard (top) and proposed (bottom) method.