

# 3-D MIMO-SAR IMAGING USING MULTI-CHIP CASCADED MMWAVE SENSORS

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# MOTIVATION

- 3-D holographic millimeter-wave (mmWave) imaging technology has a wide range of applications including security, packaging, automotive, medical, aerial imaging, etc.



## Problems:

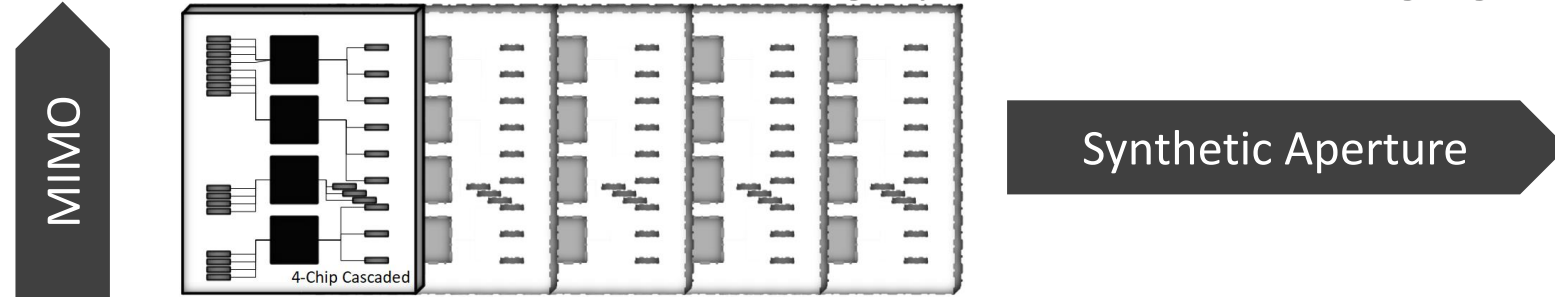
- Achieve high-resolution with as few antenna elements as possible
- Multiple-input multiple-output (MIMO) radars increase the degrees of freedom
- The complexity of extremely dense transceiver electronics limits the use of MIMO-only solutions

## Proposed Solution:

- Hybrid concepts combining synthetic aperture radar (SAR) techniques and MIMO arrays:
  - Present a good compromise to achieve short data acquisition time and low-complexity.

# RESEARCH OBJECTIVES

- Use 4-chip cascaded radar board in near-field 3-D holographic MIMO-SAR imaging



- Develop a novel and complete signal processing chain from data capture to image reconstruction



- Design a system-level imager prototype to demonstrate the proof-of-concept
  - Understand the challenges
  - Develop toolset and algorithms
  - Work towards real-world applications

# DATA CAPTURE

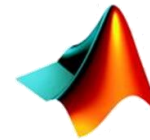
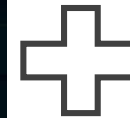
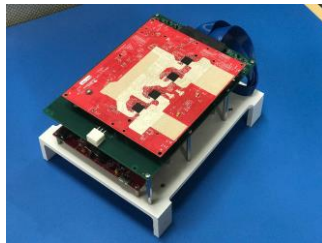
## Problem:

- Develop a system to capture real MIMO-SAR data for demonstration



## Tasks:

- Develop familiarity with 4-chip cascaded mmWave board and data collection toolset



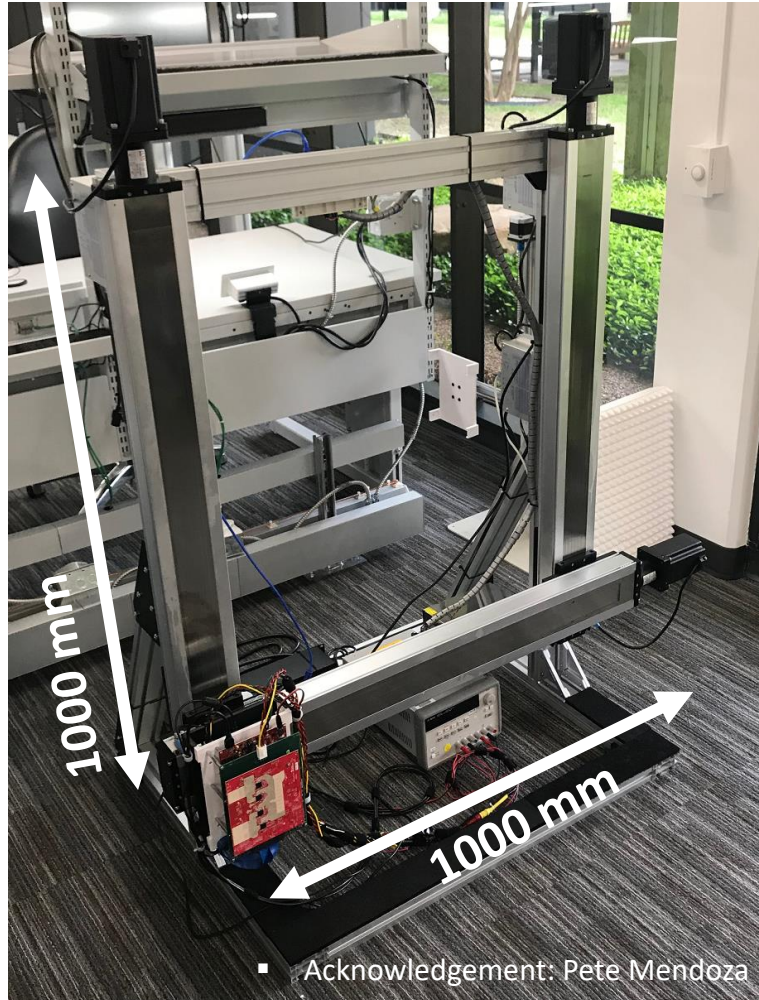
MATLAB

- Build a 2-D mechanical scanner to synthesize a larger aperture
- Integrate 4-chip cascaded board to the scanner
- Develop a complete software package in MATLAB to capture MIMO-SAR data

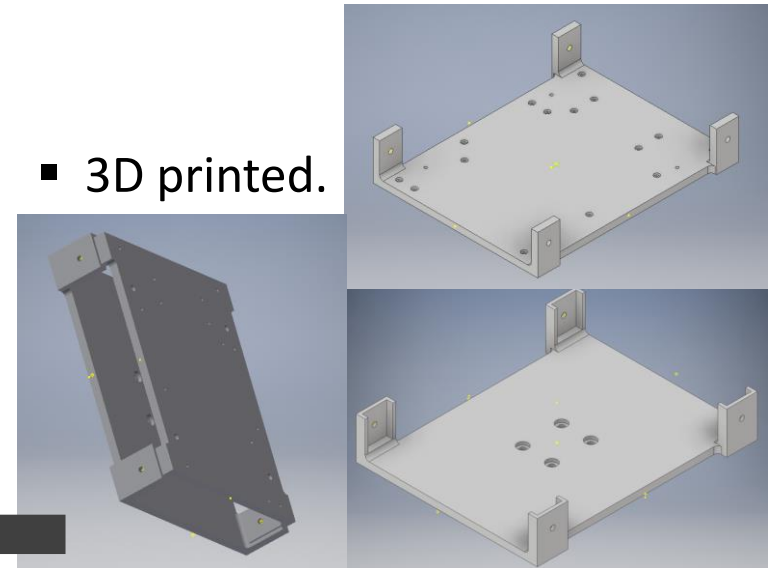
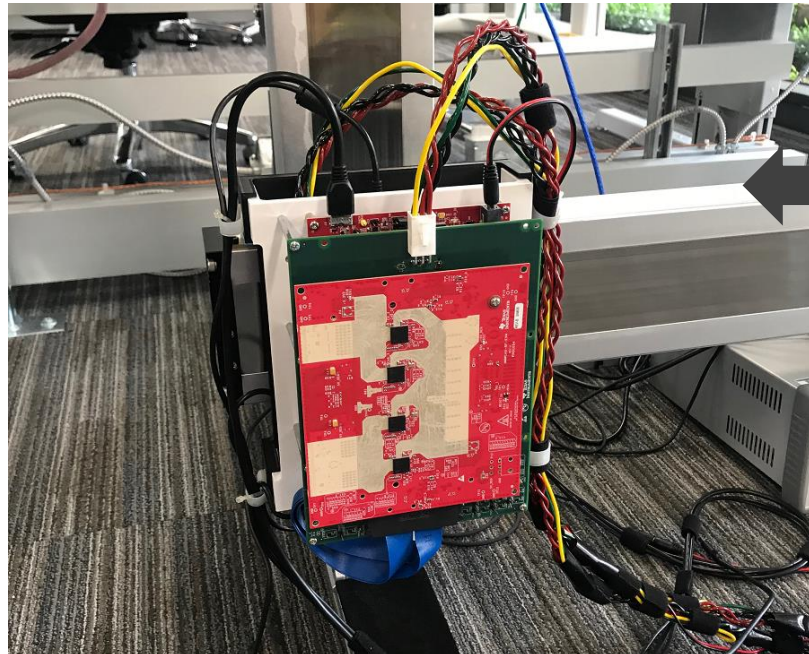


# DESIGNING A NEW IMAGER PROTOTYPE

- A mechanical scanner has been designed, multi-chip cascaded sensors has been integrated



- Scanning area:
  - **1000 mm by 1000 mm**
- Maximum speed:
  - **400 mm/s at both axes**

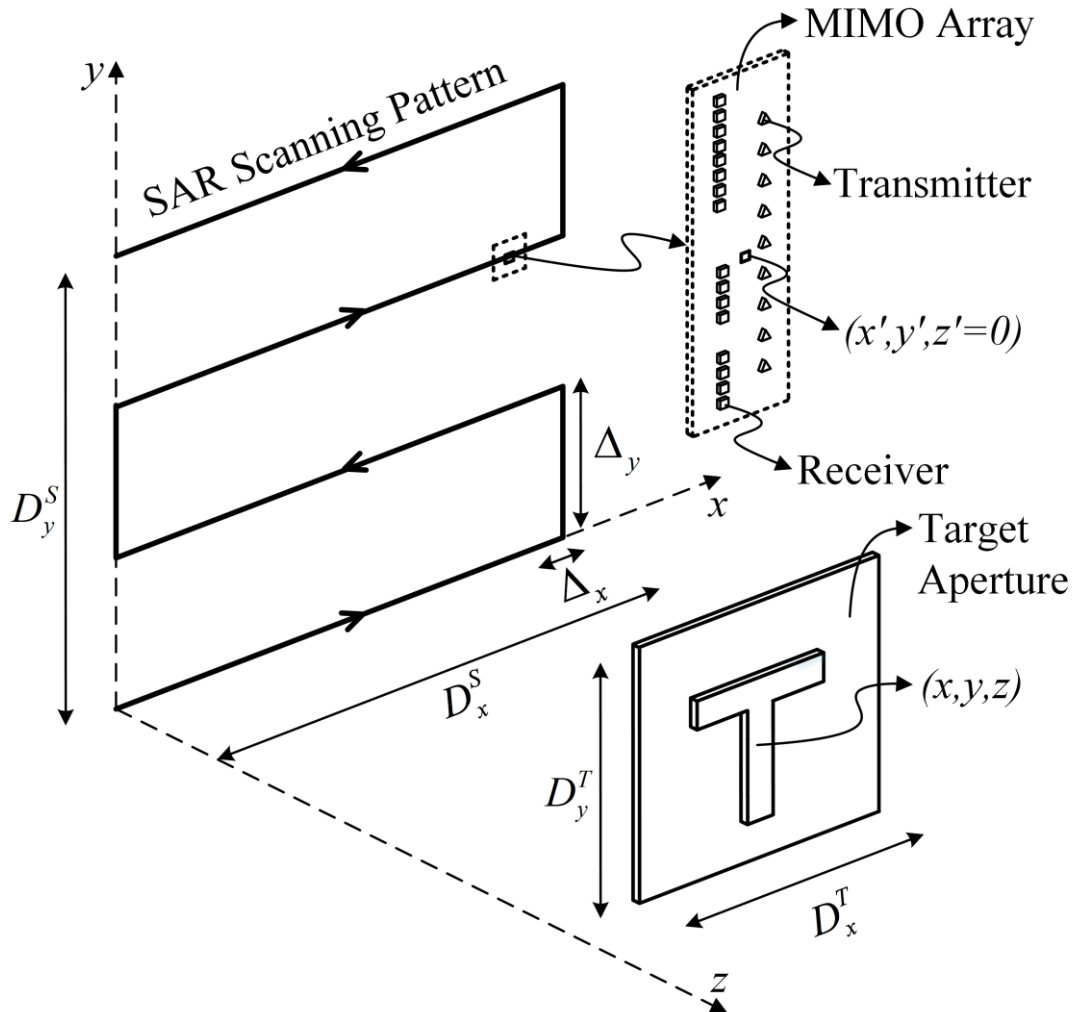


- 3D printed.

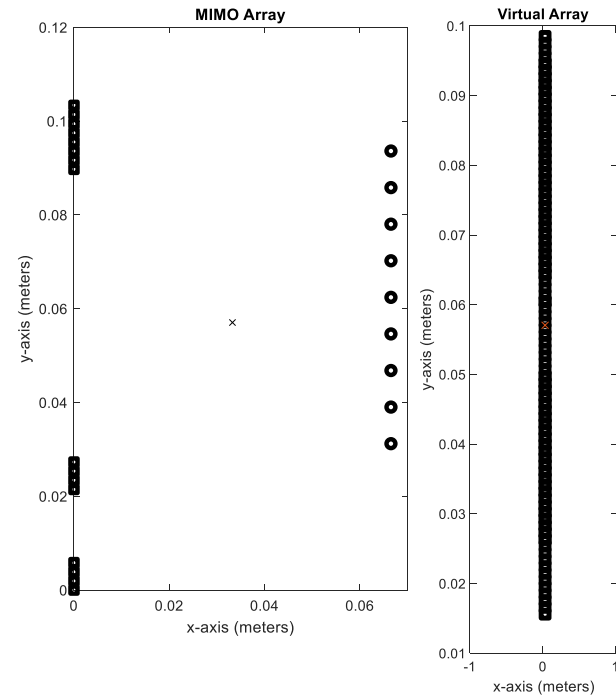
- The mmWave sensor hardware stack is integrated:
  - 1) 4-Chip cascaded board
  - 2) TSW14J56
  - 3) Mother Board + Adapter Board

# 4-CHIP CASCADED BASED MIMO-SAR SYSTEM

- Data collection is performed by moving the **4-chip cascaded MIMO radar** along a trajectory in  $x - y$  plane



- MIMO array topology of 4-chip cascaded (9Tx and 16Rx)
- 86 non-overlapped virtual channels

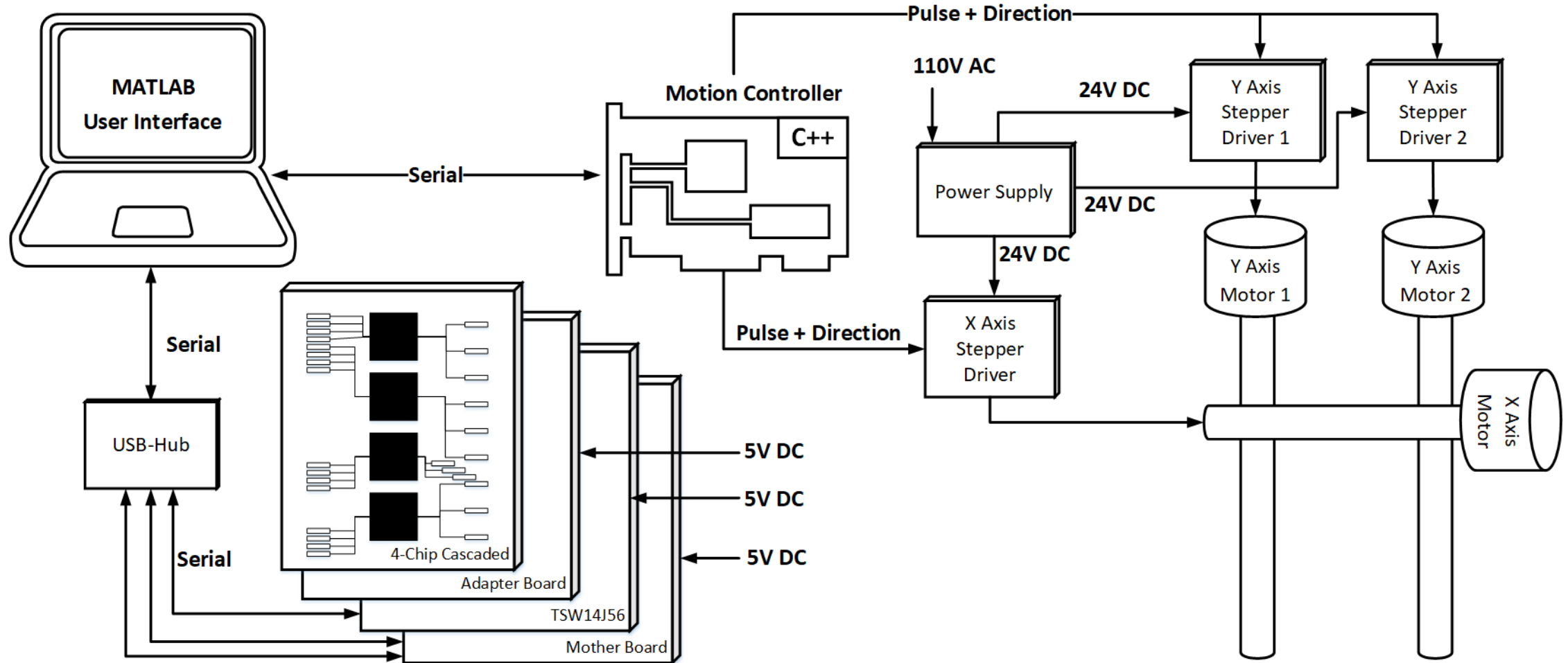


- Typical SAR parameters:  
 $D_x^S = D_y^S \approx 400$  mm  
 $\Delta_y \approx 83.86$  mm  
 # of vertical scans = 5

$$85\lambda / 4 = 82.88 \text{ mm}$$

# HIGH-LEVEL SYSTEM ARCHITECTURE

- MATLAB GUI is developed to control the platform and the radar

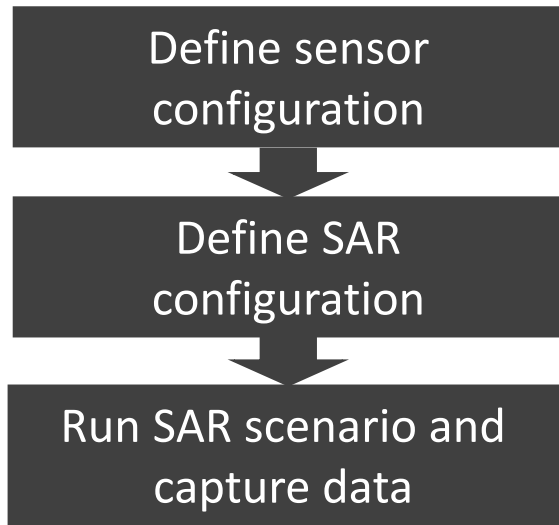


- Radar hardware is integrated into MATLAB GUI
- Two-axis rail system is integrated into MATLAB GUI

# DATA CAPTURE GUI – SAR SCENARIO GENERATION SCREEN

## SAR configuration page:

- Fully automated process



The screenshot displays the SAR Imaging Toolbox v2.0.1 interface. It features two main configuration panels: "SAR Configuration (Continuous Horizontal Scan)" and "SAR Configuration (Discrete Horizontal Scan)".

**SAR Configuration (Continuous Horizontal Scan):**

- Platform Speed (mm/s): 10
- Horizontal Step Size (mm): 0.0000
- # of Samples/Channel: 0
- Vertical Scan Size (mm): 0.0000
- Frame Periodicity (ms): 100
- Number of Frames: 1
- Time Before Capturing (s): -1 (Note: (-) if Radar Trigger First)
- Horizontal Scan Size (mm): 0
- Number of Steps at Vertical Scan: 1
- Vertical Step Size (mm): 83.859
- Blank between values. Ex: 0.9 1.9
- Buttons: Reconfigure Radar, Start Capturing, Stop Capturing
- Fields: Total Movement, SAR Status

**SAR Configuration (Discrete Horizontal Scan):**

- # of Samples/Channel: 0
- Number of Frames: 1
- Horizontal Scan Size (mm): 0.0000
- Vertical Scan Size (mm): 0.0000
- Number of Steps at Horizontal Scan: 1
- Horizontal Step Size (mm): 0
- Number of Steps at Vertical Scan: 1
- Vertical Step Size (mm): 0
- Blank between values. Ex: 0.9 1.9
- Wait Time Between Steps (s): 1
- Buttons: Reconfigure Radar, Start Capturing, Stop Capturing
- Fields: Total Movement, SAR Status

Emergency Stop Scanner



# NEAR-FIELD MIMO ARRAY CALIBRATION

## Problem:

- In a practical system, measurement errors in the MIMO array arise due to antenna gain and phase mismatches (because of imperfections in antenna layouts on the board: **RF delays**, etc.)
- Uncorrected phase error leads to unacceptable defocused blur and range shift in images



## Tasks:

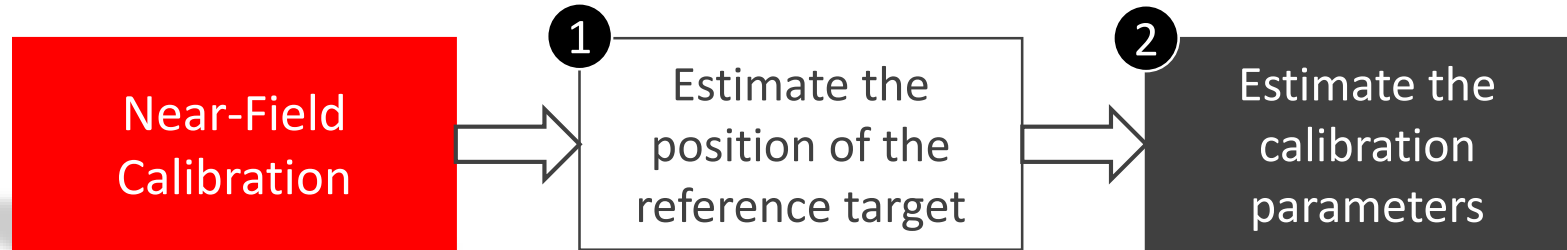
- Propose a calibration method based on the ideal backscattered signal model from a reference point target

## Solution:

- The uncalibrated measured beat signal:  $\tilde{s}_\ell(t) = a_\ell e^{j2\pi(f_0 + Kt)(\tau_i + \tau_\ell)}$
- Rewrite:  $\tilde{s}_\ell(t) = \underbrace{a_\ell e^{j\psi_i}}_{\eta_\ell} \underbrace{e^{j2\pi f_i t}}_{\text{Reference beat signal}} s_\ell(t)$  The total round-trip delay
- Estimate:  $f_i = K\tau_i$  and  $\eta_\ell$

# NEAR-FIELD MIMO ARRAY CALIBRATION

- The accuracy of the presented approach depends on the reference beat signal
- The target needs to be precisely positioned in calibrating process!



2 Given the measurements  $\tilde{s}_\ell(t)$ , the calibration error signal can be computed by:

$$w_\ell(t) = \tilde{s}_\ell(t)s_\ell^*(t) = \underbrace{\eta_\ell e^{j2\pi f_i t}}_{\text{Simple demodulation process}}$$

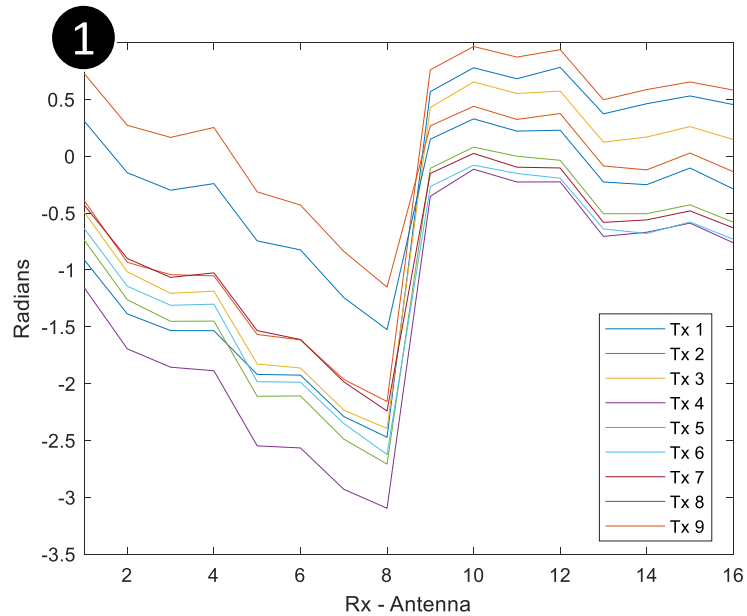
- Parameter estimation problem of a single-frequency complex tone

- Estimate:  $\hat{f}_i = \arg \max_{\langle \ell \rangle} \sum |W_\ell(f)|^2$       $W_\ell(f) = \int_0^T w_\ell(t)e^{-j2\pi ft} dt$

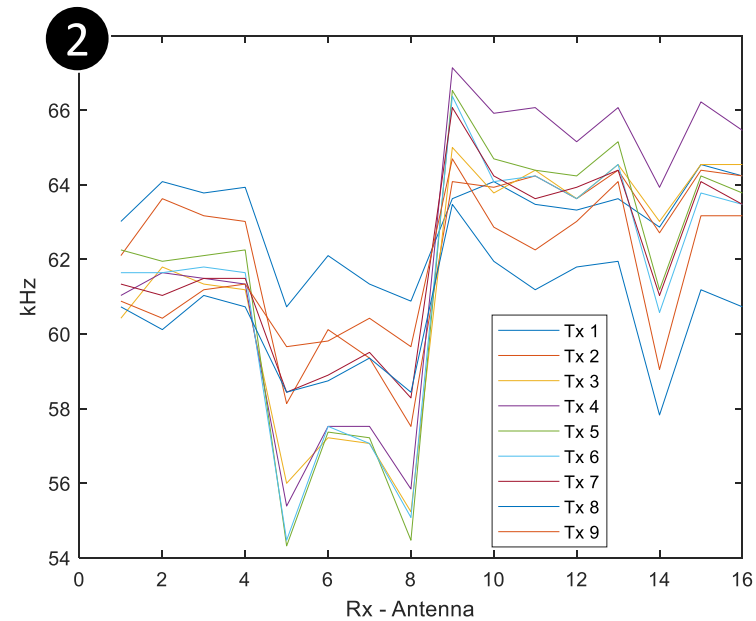
- Estimate  $\eta_\ell$  by plugging the estimate  $\hat{f}_i$  into  $w_\ell(t)$

# NEAR-FIELD MIMO ARRAY CALIBRATION

- Simulate the backscattered signal for each channel based on the exact target location
- Calculate complex calibration data  $\eta_\ell$  and range (beat frequency) offset  $K\tau_i$



Complex calibration data



Beat frequency offset

# 3-D MIMO SAR IMAGE RECONSTRUCTION IN NEAR-FIELD

## Problems:

- Near-field: the plane-wave assumption is invalid and the spherical wave model has to be used
- MIMO sampling: different trajectories of the incident and reflected electric fields has to be considered
- Proposed algorithm has to be computationally efficient



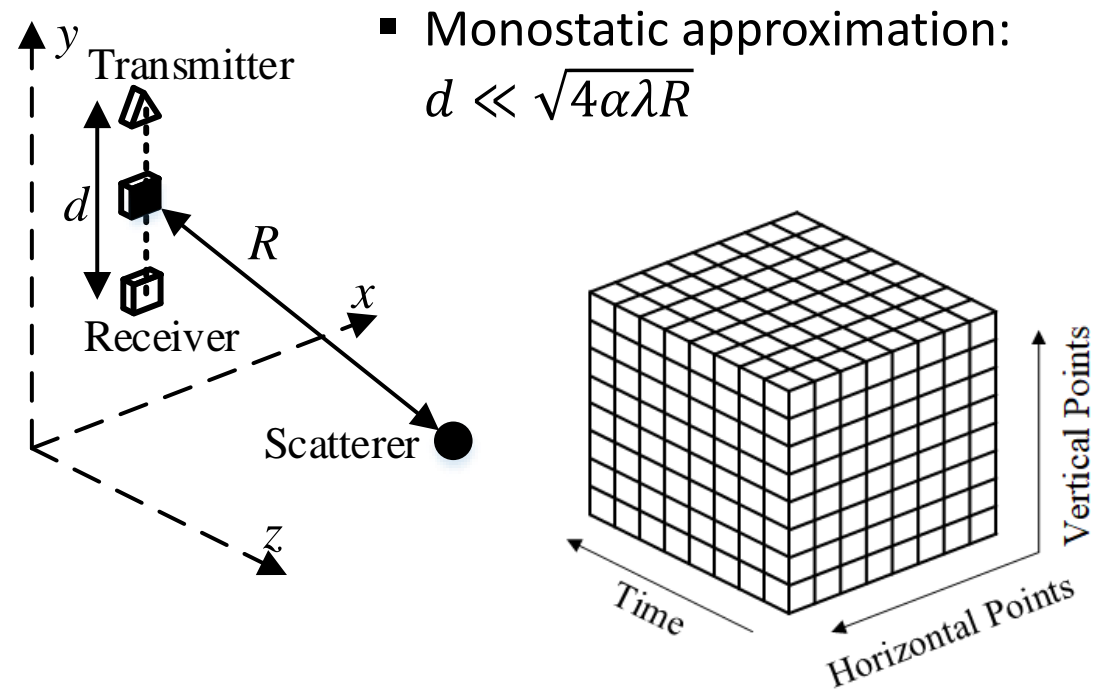
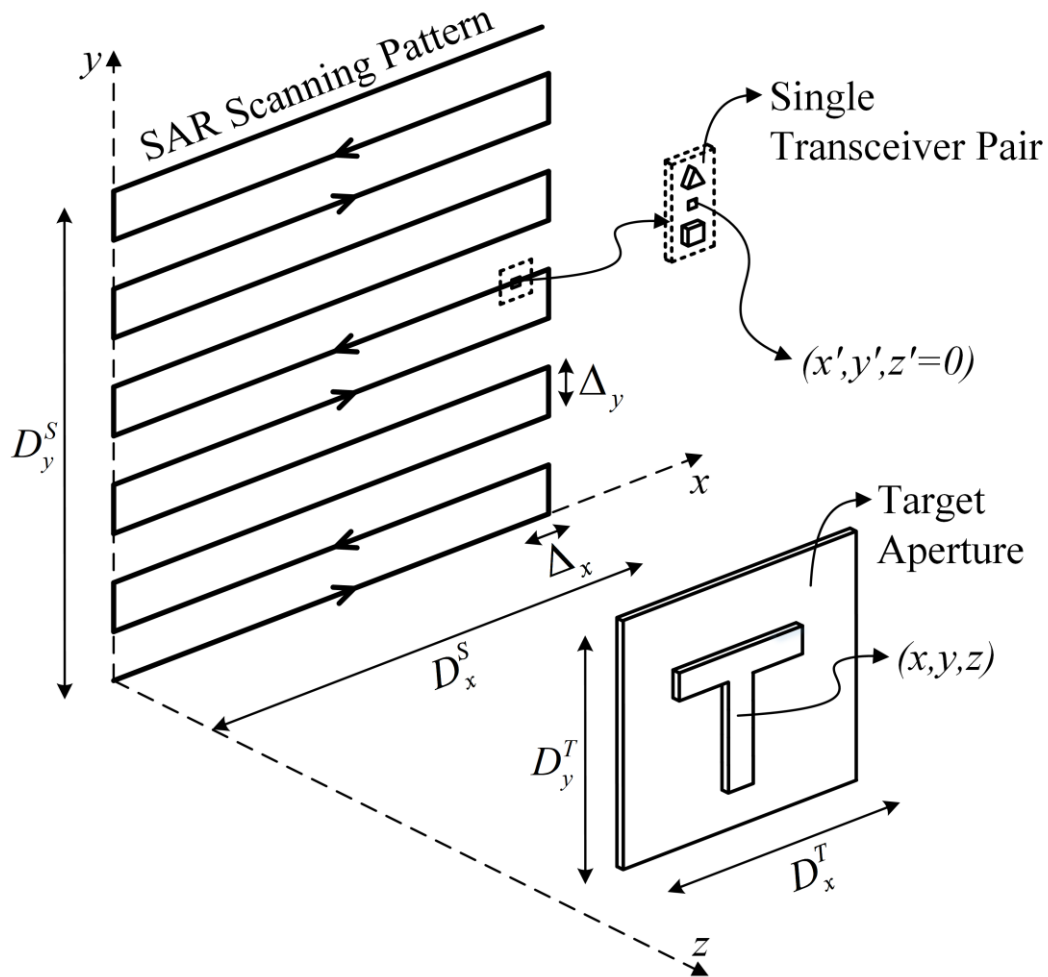
## Tasks:

- Develop low-complexity and novel image reconstruction algorithms for MIMO-SAR configuration
- Validate the algorithms using simulation environment
- Demonstrate the real high-resolution 3-D imaging results using prototyped imager



# CONVENTIONAL SAR SYSTEM CONFIGURATION

- The complex “beat” signal:  $s(t) = \sigma \exp(j2\pi(f_0\tau + K\tau t - 0.5K\tau^2))$  Delay:  $\tau = 2R/c$  Gain:  $\sigma = p/R^2$

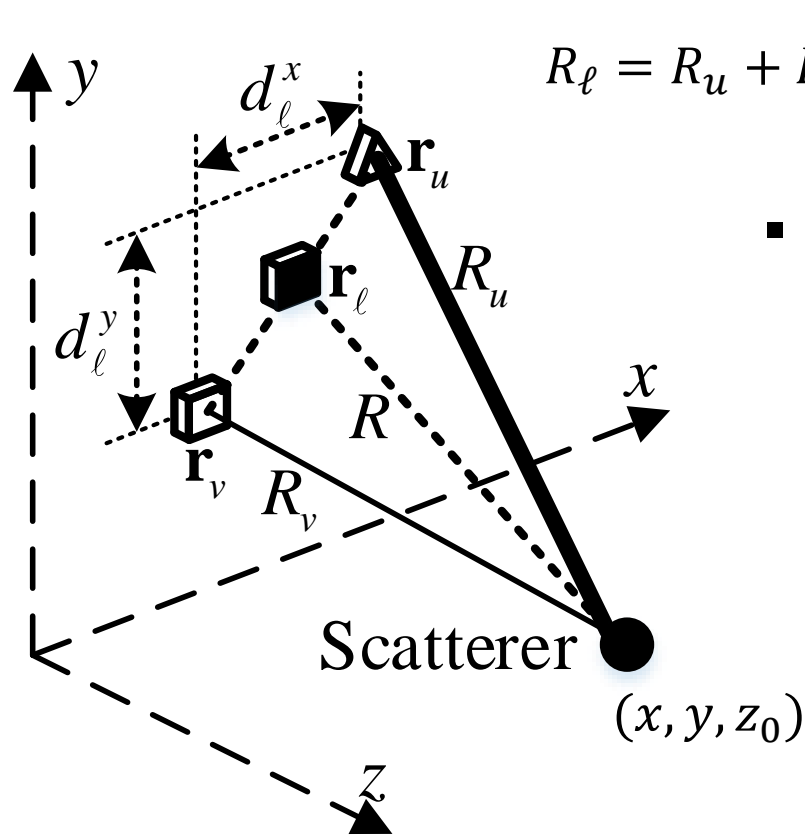


- Monostatic approximation:  
 $d \ll \sqrt{4\alpha\lambda R}$

- 3-D radar cube is captured as  $s(x', y', t)$
- The target image is characterized by:
  - 3-D reflectivity function  $p(x, y, z)$
- Goal:** Estimate  $p(x, y, z)$  from  $s(x', y', t)$  **efficiently**

# MULTISTATIC EFFECT IN NEAR-FIELD

- Midpoint approximation:  $|\mathbf{r}_u - \mathbf{r}_v| \leq \sqrt{4\alpha\lambda R}$  for a small  $\alpha$  doesn't hold in near field
- The total round-trip distance for the  $\ell$ -th virtual channel



$$R_\ell = R_u + R_v = \sqrt{(x_u - x)^2 + (y_u - y)^2 + z_0^2} + \sqrt{(x_v - x)^2 + (y_v - y)^2 + z_0^2}$$

- Complex solution:  $s_\ell(x', y', k) = \iiint p(x, y, z) \frac{e^{jk(R_u + R_v)}}{R_u R_v} dx dy dz$

- Taylor expansion

$$R_\ell \approx 2R + \frac{(d_\ell^x)^2 + (d_\ell^y)^2}{4R} - \frac{((x - x')d_\ell^x + (y - y')d_\ell^y)^2}{4R^3}$$

- Multistatic to monostatic phase correction is proposed
- The received signal by the  $\ell$ th hypothetical monostatic element:

$$s_\ell(k) \approx p \frac{\exp(jkR_\ell)}{R^2} \approx s(k) e^{j\phi_\ell(k)} \quad \phi_\ell(k) \approx k \frac{(d_\ell^x)^2 + (d_\ell^y)^2}{4z_0}$$

# 3-D MONOSTATIC IMAGE RECONSTRUCTION

- Recall the beat signal:  $s(t) = \sigma \exp(j2\pi(f_0 t + K t \tau - 0.5 K \tau^2))$  → Residual video phase (RVP) is negligible

- Rewrite in the wavenumber domain as:

$$s(k) = p \frac{\exp(j2kR)}{R^2} \quad R = \sqrt{(x' - x)^2 + (y' - y)^2 + z^2}$$

- The received monostatic backscattered data from a 3-D target

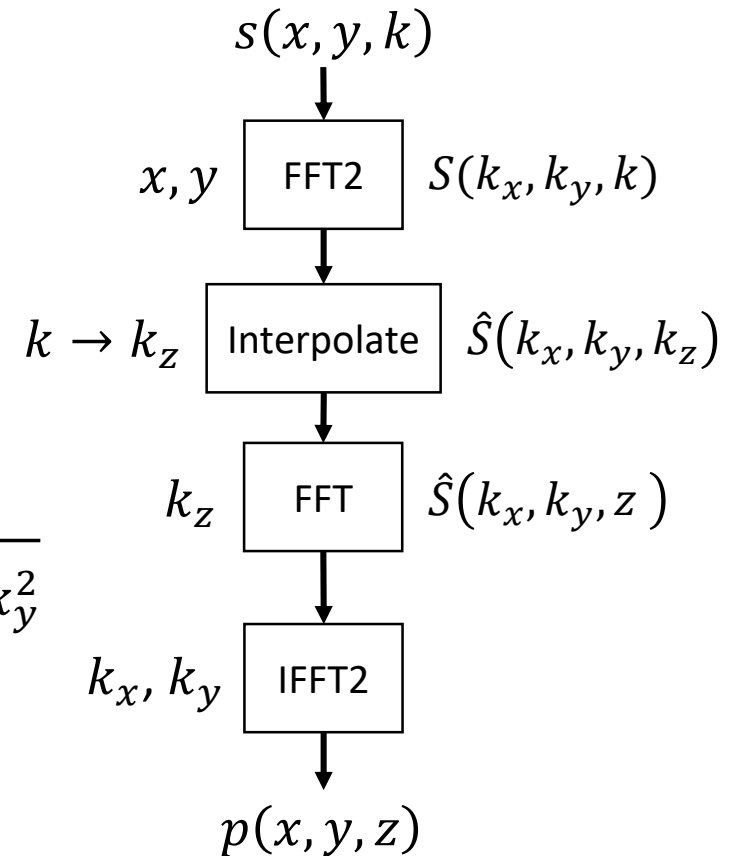
$$s(x', y', k) = \iiint p(x, y, z) \frac{e^{j2kR}}{R} dx dy dz \quad R^{-2} \approx (z_0 R)^{-1}$$

- Representation of a spherical wave as a superposition of plane waves

$$\frac{e^{j2kR}}{R} = \frac{j}{2\pi} \iint \frac{e^{j(k_x(x'-x) + k_y(y'-y) + k_z z)}}{k_z} dk_x dk_y \quad k_z = \sqrt{4k^2 - k_x^2 - k_y^2}$$

- The final 3-D image in spectral domain:  $P(k_x, k_y, k_z) = \hat{S}(k_x, k_y, k_z)$

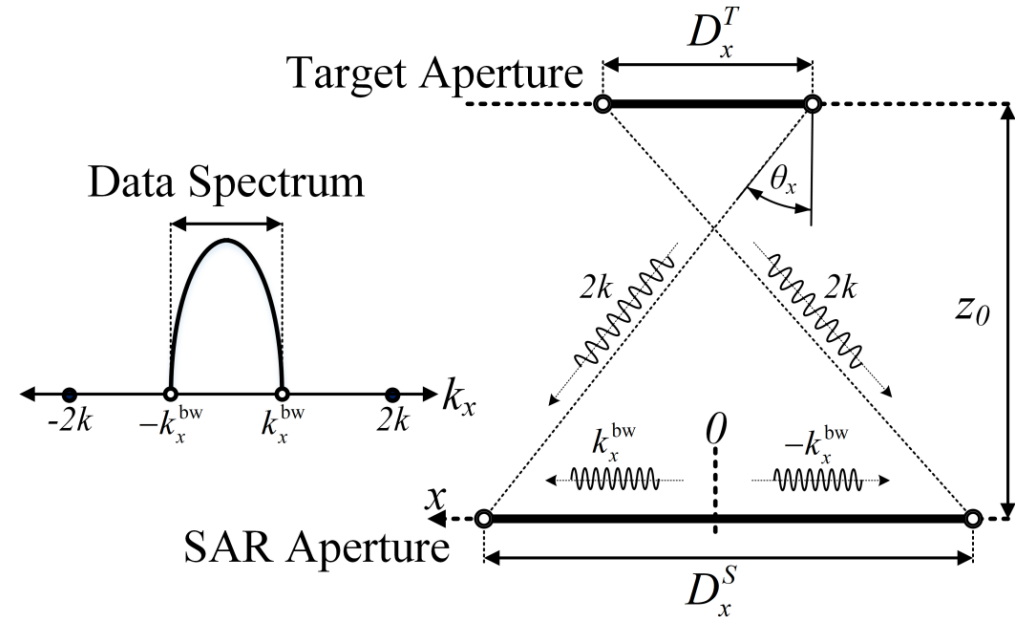
- Interpolation step with  $k_z$ :  $k_z S(k_x, k_y, k) \rightarrow \hat{S}(k_x, k_y, k_z)$



- 3-D image formation

# PERFORMANCE PARAMETERS – MONOSTATIC ANALYSIS

- Data bandwidth depends on:
  - Wavelength ( $\lambda$ )
  - Size of the radar aperture ( $D_x^S, D_y^S$ )
  - Size of the target aperture ( $D_x^T, D_y^T$ )
  - Distance between the target and the radar apertures ( $z_0$ )



- The total bandwidth:

$$\Delta k_x \approx 2k_x^{\text{bw}} \approx 4k \sin \theta_x$$

- The cross range resolution:

$$\delta_x \approx \frac{2\pi}{\Delta k_x} \approx \frac{\lambda z_0}{2D_x^S}$$

- Nyquist rate:  $k_x^S \geq 2k_x^{\text{bw}} = \frac{4\pi(D_x^S + D_x^T)}{\lambda \sqrt{(D_x^S + D_x^T)^2/4 + z_0^2}}$
- Sampling interval:

- Phase center concept:  $\frac{\mathbf{r}_u + \mathbf{r}_v}{2} \longleftarrow \Delta_x \leq \frac{2\pi}{k_x^S} = \frac{\lambda \sqrt{(D_x^S + D_x^T)^2/4 + z_0^2}}{2(D_x^S + D_x^T)}$
- For  $D_x^S \gg z_0$   
 $\Delta_x \leq \frac{\lambda}{4}$  Virtual elements!



# MIMO-SAR SIMULATIONS – MULTISTATIC EFFECT

- Simulated uniform array with 86 non-overlapped virtual elements, **two captures** in vertical axis

- Multistatic** data capture
- Monostatic image reconstruction

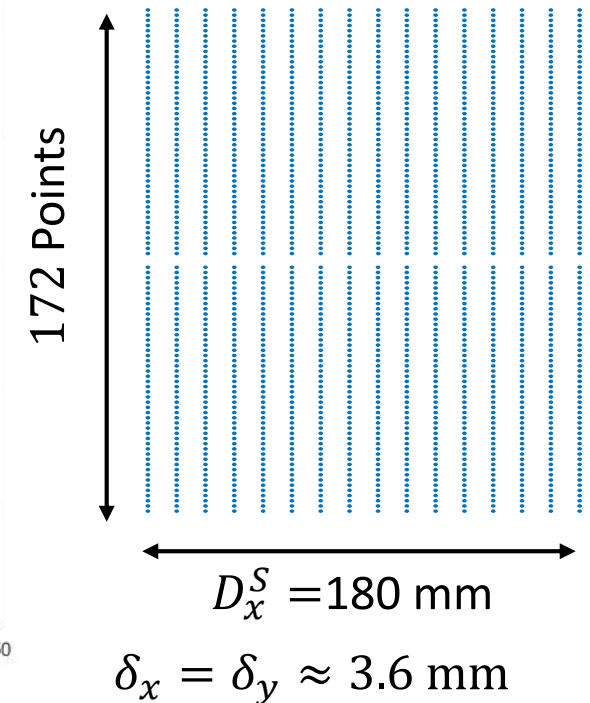
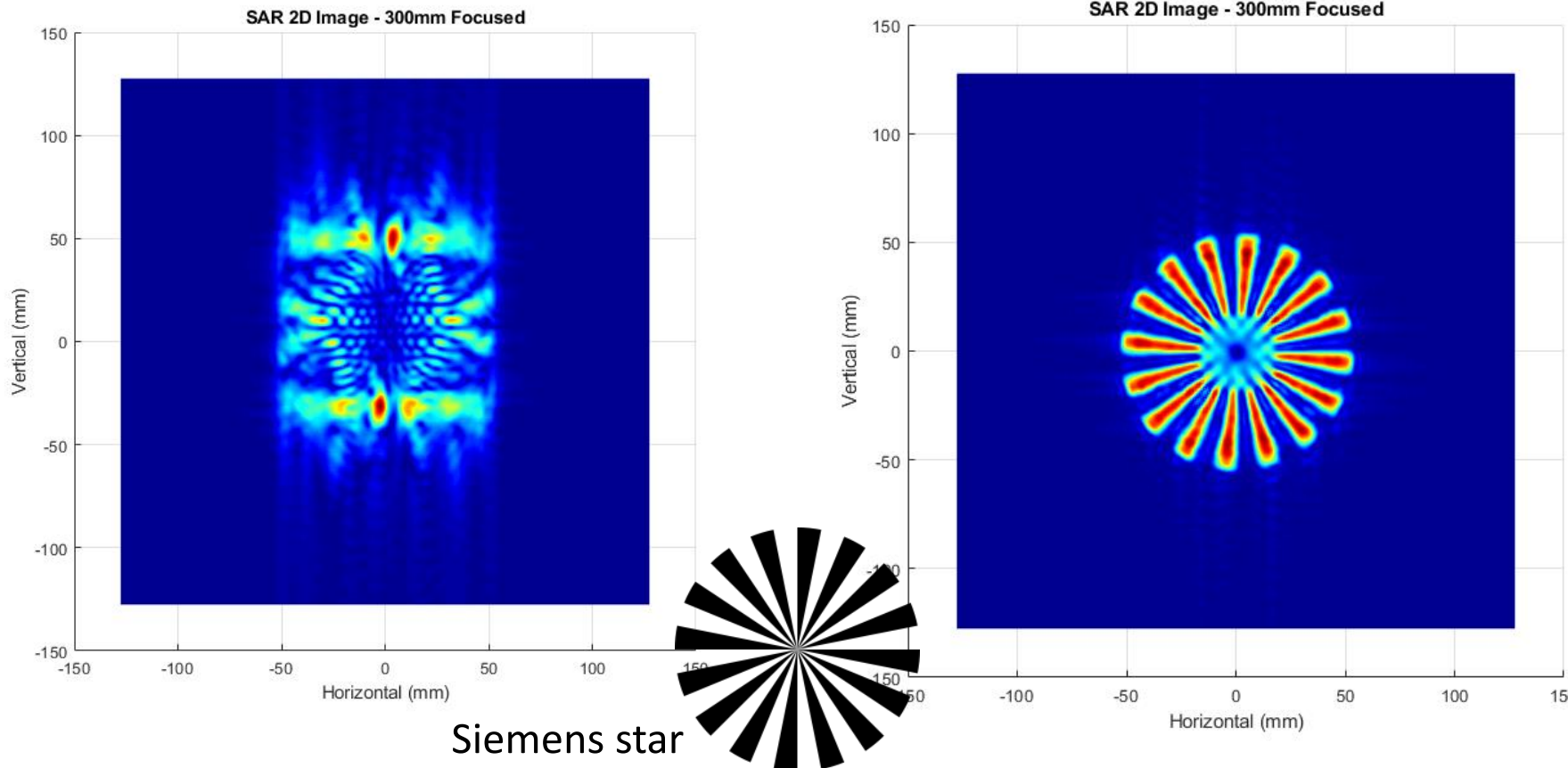
- After multistatic to monostatic phase correction**
- Monostatic image reconstruction

$$\Delta_x = \lambda/4 \quad D_x^S \approx 180 \text{ mm}$$

$$\Delta_y = \lambda/4 \quad D_y^S \approx 170 \text{ mm}$$

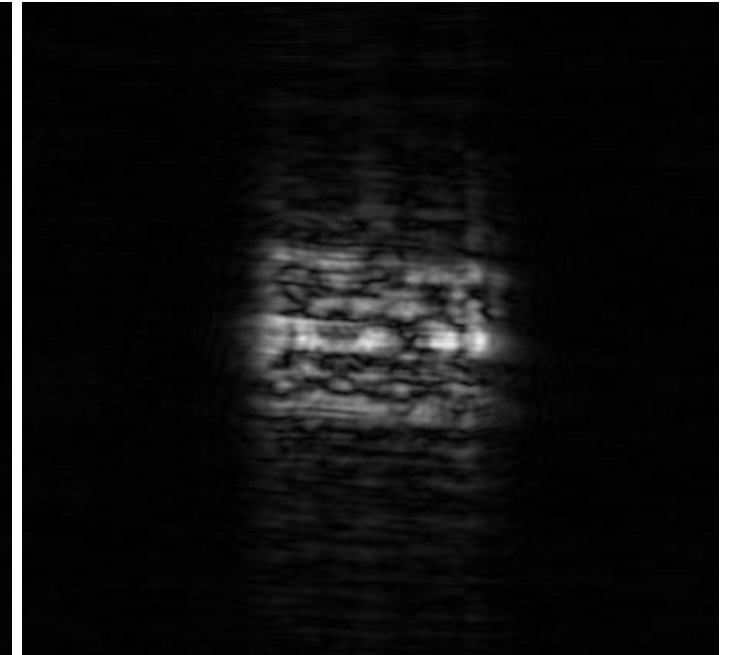
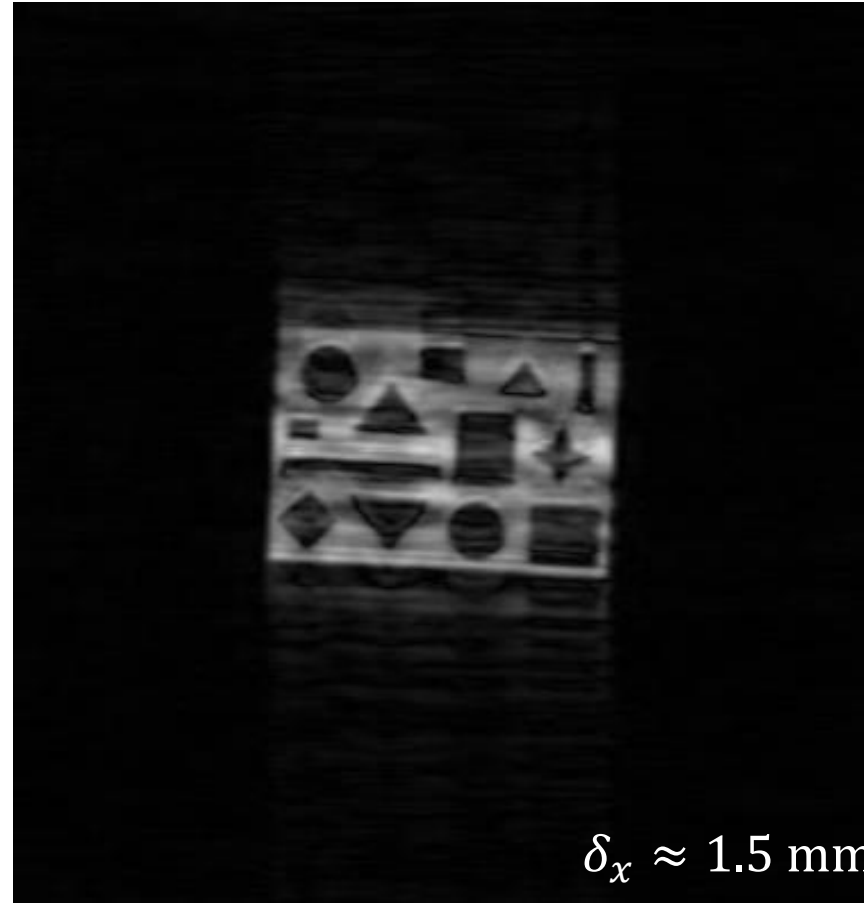
$$f_0 = 77 \text{ GHz (Single tone)}$$

$$z_0 = 300 \text{ mm}$$



# MIMO-SAR EXPERIMENTS

- Image reconstruction using 4-Chip Cascaded Radar (86 virtual channels)

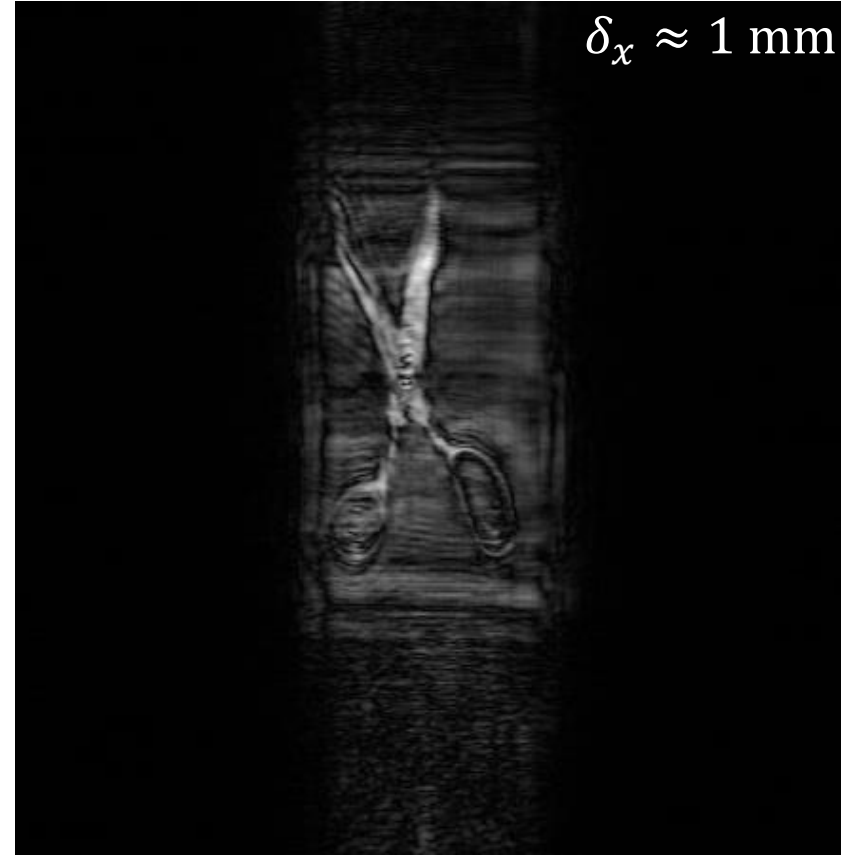
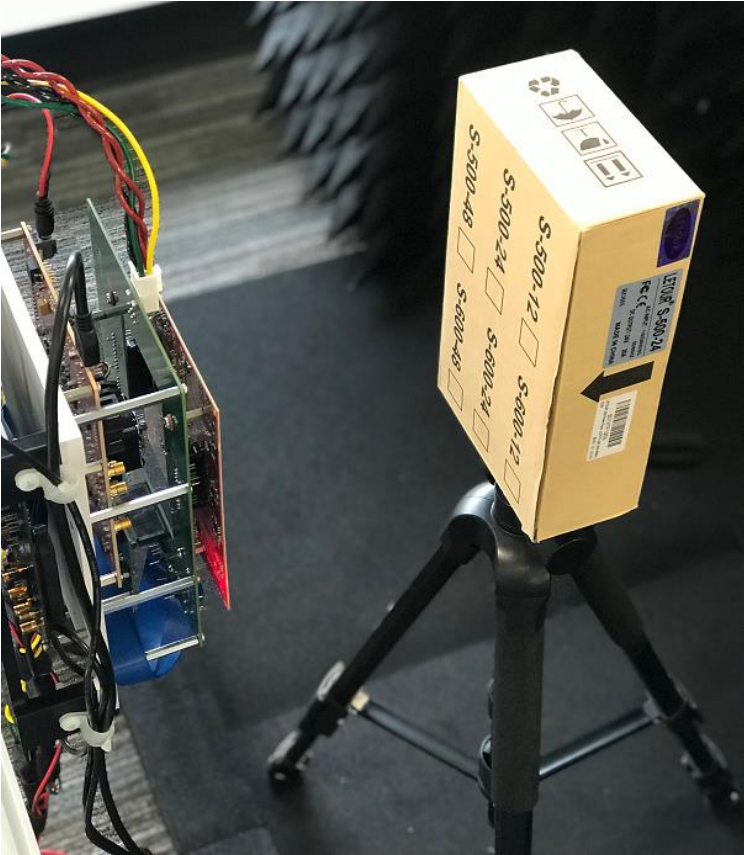


- Image result without calibration!!

$$D_x^S \approx D_y^S \approx 500 \text{ mm} \quad \Delta_x = 1 \text{ mm} \approx \lambda/4 \quad \Delta_y = 83.859 \text{ mm} = 86\lambda/4 \quad z_0 \approx 400 \text{ mm}$$

# IMAGING OF CONCEALED PHYSICAL OBJECTS

- Experiment with scissors concealed in a cardboard box
- Image reconstruction using 4-Chip Cascaded Radar (86 virtual channels)



$$D_x^S \approx D_y^S \approx 500 \text{ mm} \quad \Delta_x = 1 \text{ mm} \approx \lambda/4 \quad \Delta_y = 83.859 \text{ mm} = 86\lambda/4 \quad z_0 \approx 250 \text{ mm}$$

# SUMMARY

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- Developed a near-field mmWave imaging prototype utilizing 4-chip cascaded board in SAR configuration
- Proposed a complete signal processing toolset from data capture to image formation
  - Developed a fully automated data capture software
  - Presented a calibration method for MIMO arrays
  - Proposed an efficient image reconstruction method based on monostatic reconstruction framework
- Investigated the design considerations including the spatial sampling criteria, and image resolution.
- Demonstrated the real imaging results using prototyped imager (1<sup>st</sup> image of the 4-chip cascaded board )
- Investigated the future improvements and challenges to work towards real-world applications



**THE END**

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**THANK YOU  
QUESTIONS?**