

---

---

**SAR IMAGING TUTORIAL**

---

---



---

---

**SAR IMAGING TUTORIAL**

---

---

**PREPARED BY:  
MUHAMMET EMIN YANIK  
PROF. MURAT TORLAK**

---

---

## SAR IMAGING TUTORIAL

---

---

# CONTENTS

1. INTRODUCTION.....	2
2. SYSTEM CONFIGURATION AND RECORDED DATA FORMAT.....	2
2.1. System Configuration.....	2
2.2. Recorded Data Format.....	4
3. SIMPLIFIED 2-D IMAGING ALGORITHM.....	5
4. RECORDED DATA SCENARIOS .....	6
4.1. Flat 2-D Target .....	6
4.2. Two Flat 2-D Targets Concealed in Box.....	7
4.3. Cascaded Concealed Targets .....	8
5. PROCESSING SOFTWARE.....	9
6. 2-D IMAGING RESULTS .....	11

## SAR IMAGING TUTORIAL

### 1. INTRODUCTION

In scope of the project, a two-dimensional (2-D) near-field imaging system based on the combination of synthetic aperture radar (SAR) processing techniques and the low-cost system-on-chip millimeter-wave frequency-modulated continuous-wave (FMCW) radars is designed. To create a synthetic aperture over the target scene, a two-axis automatic rail system is built and integrated with Texas Instruments IWR1443 77-GHz millimeter-wave FMCW radar sensor.

In this tutorial, simplified signal processing techniques for near-field 2-D image formation is introduced and the specifications of recorded SAR data samples are detailed.

### 2. SYSTEM CONFIGURATION AND RECORDED DATA FORMAT

#### 2.1. System Configuration

To reconstruct the 2-D image of the scene, data collection is performed by moving the radar along a trajectory in  $x - y$  plane, which creates a rectangular grid of measurement points, as shown in Figure 1. It is assumed that transmitting and receiving antenna are located very close to each other, then they are represented by the mid-point between them. In the established  $(x, y, z)$  Cartesian coordinate system,  $x -$  axis,  $y -$  axis, and  $z -$  axis denote horizontal, vertical, and range directions, respectively.

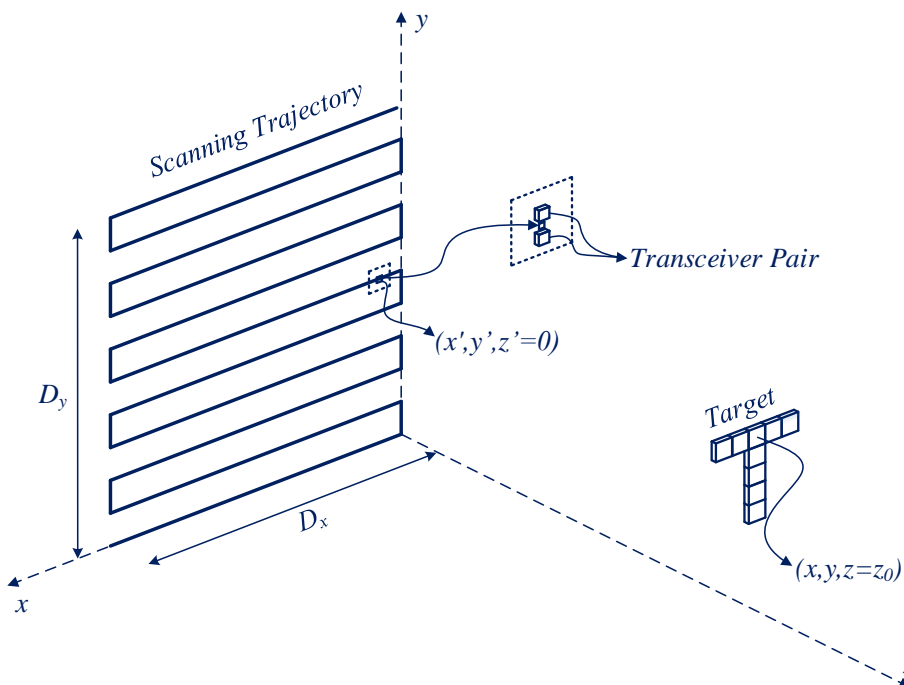


Figure 1 System Configuration

## SAR IMAGING TUTORIAL

As illustrated in the measurement configuration, transceiver is at position  $(x', y', 0)$  for a specific measurement instant and a general point on the target placed at the distance  $z_0$  from the imaging system is at position  $(x, y, z_0)$ . The detailed scanning aperture configuration is shown in Figure 2. Total scan size is  $D_x$  and  $D_y$  in  $x$  –axis and  $y$  – axis, respectively, and the corresponding sampling distance is  $d_x$  and  $d_y$ .

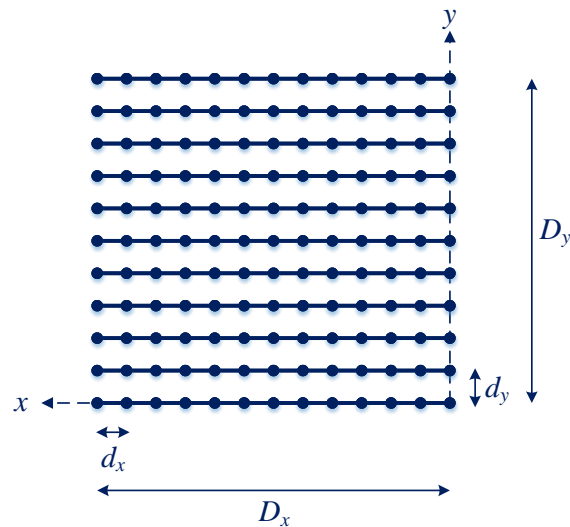


Figure 2 Aperture Configuration

Chirp parameters used at the experiments are shown in Figure 3.

Profile			
Profile Id	0	HPF1 Corner Freq	175K
Start Freq (GHz)	77.000000	HPF2 Corner Freq	350K
Frequency Slope (MHz/ $\mu$ s)	63.343	O/p Pwr Backoff TX0 (dB)	0
Idle Time ( $\mu$ s)	10.00	O/p Pwr Backoff TX1 (dB)	0
TX Start Time ( $\mu$ s)	1.00	O/p Pwr Backoff TX2 (dB)	0
ADC Start Time ( $\mu$ s)	6.00	Phase Shifter TX0 (deg)	0.0
ADC Samples	512	Phase Shifter TX1 (deg)	0.0
Sample Rate (ksps)	9121	Phase Shifter TX2 (deg)	0.0
Ramp End Time ( $\mu$ s)	63.14	Bandwidth(MHz)	3999.48
RX Gain (dB)	30	<input type="button" value="Set"/> <input type="button" value="Manage Profile"/>	
RF Gain Target	30dB		
VCO Select	VCO1	<input type="checkbox"/> Force VCO Select	
Calib LUT Update	<input type="checkbox"/> RetainTxCallUT <input type="checkbox"/> RetainRxCallUT		

Figure 3 Chirp Parameters

---

## SAR IMAGING TUTORIAL

---

### 2.2. Recorded Data Format

The 3-D recorded data cube is shown in Figure 4 and properties are detailed below.

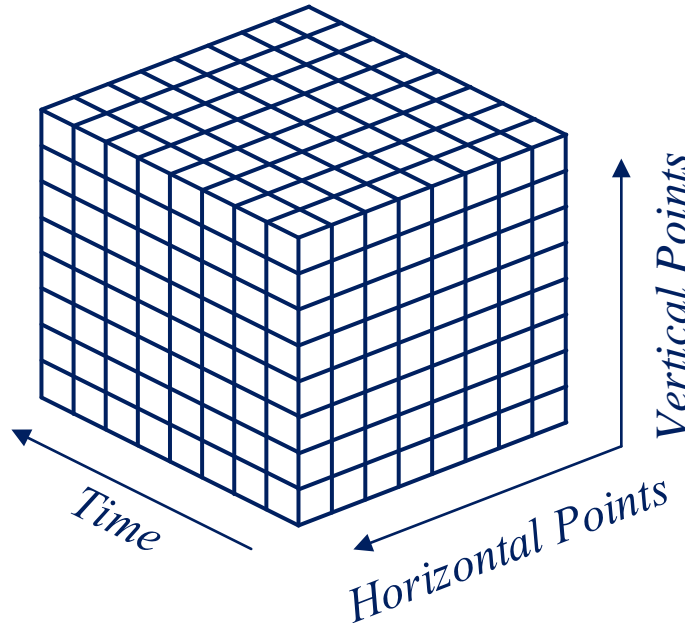


Figure 4 Recorded Data Cube

#### Data

---

**rawData3D** is an  $n_{\text{Sample}} \times n_{\text{Vertical}} \times n_{\text{Horizontal}}$  3-D data matrix. Details of parameters are given below.

#### Dimensions

---

<b>nSample:</b>	Number of samples in time domain.
<b>nVertical:</b>	Number of sample points in vertical ( $y$ ) axis.
<b>nHorizontal:</b>	Number of sample points in horizontal ( $x$ ) axis.
<b>D<sub>x</sub>:</b>	Aperture size of horizontal ( $x$ ) axis.
<b>D<sub>y</sub>:</b>	Aperture size of vertical ( $y$ ) axis.
<b>d<sub>x</sub>:</b>	Sampling distance of horizontal ( $x$ ) axis.
<b>d<sub>y</sub>:</b>	Sampling distance of vertical ( $y$ ) axis.
<b>z<sub>0</sub>:</b>	Target distance.

---

## SAR IMAGING TUTORIAL

---

### 3. SIMPLIFIED 2-D IMAGING ALGORITHM

After coinciding the target and aperture coordinates, the 2-D reflectivity image can be formulated as

$$f(x, y) = \text{FT}_{2D}^{-1}[\text{FT}_{2D}[s(x, y)]\text{FT}_{2D}[h(x, y)]]$$

where  $\text{FT}_{2D}$  and  $\text{FT}_{2D}^{-1}$  denote 2-D Fourier and inverse Fourier transform operations over the  $x - y$  plane,  $f(x, y)$  is 2-D target reflectivity function,  $s(x, y)$  is the measured radar signals, and  $h(x, y)$  is the impulse response or the point spread function of the imaging system calculated for each  $(x, y)$  measurement point as

$$h(x, y) = e^{-j2k\sqrt{x^2+y^2+z_0^2}}$$

The reconstruction algorithm summarized in Figure 5 does not consider any visibility condition. Thus, built-in MATLAB 2-D FFT function can be used directly.

---

**Algorithm** Image reconstruction using matched filter approach

---

- 1: gather uniformly sampled complex FMCW data cube,  $r(x, y, t)$  from transceiver over a 2-D planar aperture
  - 2: perform range focusing to  $z_0$  distance and gather uniformly sampled complex data,  $s(x, y)$
  - 3: perform the 2-D FFT of  $s(x, y)$  to obtain sampled version of  $S(k_x, k_y) = \text{FT}_{2D}[s(x, y)]$
  - 4: create matched filter,  $h(x, y) = e^{-j2k\sqrt{x^2+y^2+z_0^2}}$
  - 5: perform the 2-D FFT of  $h(x, y)$  to obtain sampled version of  $H(k_x, k_y) = \text{FT}_{2D}[h(x, y)]$
  - 6: multiply  $S(k_x, k_y)$  and  $H(k_x, k_y)$
  - 7: perform the 2-D IFFT
  - 8: compute the magnitude and display the data
- 

Figure 5 Simplified Image Reconstruction Algorithm

---

## SAR IMAGING TUTORIAL

---

### 4. RECORDED DATA SCENARIOS

#### 4.1. Flat 2-D Target

The scenario is shown in Figure 6 and properties are detailed below.



Figure 6 Flat 2-D Target Scenario

#### Data Name

---

rawData3D\_simple2D

#### Parameters

---

<b>nSample:</b>	512
<b>nVertical:</b>	100
<b>nHorizontal:</b>	407
<b>D<sub>x</sub>:</b>	200 mm ( <b>d<sub>x</sub></b> : 200/406 mm)
<b>D<sub>y</sub>:</b>	198 mm ( <b>d<sub>y</sub></b> : 2 mm)
<b>z<sub>0</sub>:</b>	280 mm



---

## SAR IMAGING TUTORIAL

---

### 4.2. Two Flat 2-D Targets Concealed in Box

The scenario is shown in Figure 7 and properties are detailed below.



Figure 7 Two Flat 2-D Targets Concealed in Box Scenario

#### Data Name

---

rawData3D\_twoConcealed2D

#### Parameters

---

<b>nSample:</b>	512
<b>nVertical:</b>	101
<b>nHorizontal:</b>	407
<b>D<sub>x</sub>:</b>	200 mm ( <b>d<sub>x</sub></b> : 200/406 mm)
<b>D<sub>y</sub>:</b>	200 mm ( <b>d<sub>y</sub></b> : 2 mm)
<b>z<sub>0</sub>:</b>	260 mm (front side of the box), 320 mm (back side of the box)



---

## SAR IMAGING TUTORIAL

---

### 4.3. Cascaded Concealed Targets

The scenario is shown in Figure 8 and properties are detailed below.



Figure 8 Cascaded Concealed Targets Scenario

#### Data Name

---

rawData3D\_cascadedConcealed

#### Parameters

---

<b>nSample:</b>	512
<b>nVertical:</b>	101
<b>nHorizontal:</b>	407
<b>D<sub>x</sub>:</b>	200 mm ( <b>d<sub>x</sub></b> : 200/406 mm)
<b>D<sub>y</sub>:</b>	200 mm ( <b>d<sub>y</sub></b> : 2 mm)
<b>z<sub>0</sub>:</b>	250 mm (first target), 340 mm (second target)

## SAR IMAGING TUTORIAL

### 5. PROCESSING SOFTWARE

Main scripts of the processing software are identified in Table 1.

No	Script Name	Called Script
1	mainSAR.m <b>Definition:</b> Main script that preprocess the data for 2-D imaging and calls the related sub-scripts for SAR imaging.	2, 3
2	createMatchedFilterSimplified.m <b>Definition:</b> Script that creates matched filter.	-
3	reconstructSARimageMatchedFilterSimplified.m <b>Definition:</b> Script that creates the 2-D SAR image	-

Table 1 Software Scripts

#### Main Code

This code block preprocess the rawData3D for 2-D imaging and calls other SAR imaging functions.

Following parameters should be updated based on the scenario.

```
%% Load rawData3D
dataName = 'rawData3D_simple2D'; % Change only this line
rawData = load(dataName);
rawData = rawData.(dataName);

%% Define parameters, update based on the scenario
nFFTtime = 1024; % Number of FFT points for Range-FFT
z0 = 280e-3; % Range of target (range of corresponding image slice)
dx = 200/406; % Sampling distance at x (horizontal) axis in mm
dy = 2; % Sampling distance at y (vertical) axis in mm
nFFTspace = 1024; % Number of FFT points for Spatial-FFT
```

Following line calls matched filter creation function.

```
%% Create Matched Filter
matchedFilter =
createMatchedFilterSimplified(nFFTspace, dx, nFFTspace, dy, z0*1e3);
```

Following line calls image reconstruction function. **imSize** parameter can be changed.

```
%% Create SAR Image
imSize = 200; % Size of image area in mm
sarImage =
reconstructSARimageMatchedFilterSimplified(sarData, matchedFilter, dx, dy, imSize
);
```

---

## SAR IMAGING TUTORIAL

---

### Matched Filter Function

---

**matchedFilter =  
createMatchedFilterSimplified(xPointM,xStepM,yPointM,yStepM,zTarget)**

This function creates 2-D matched filter. Input parameters and output are detailed below:

#### Inputs

---

<b>xPointM:</b>	number of measurement points at x (horizontal) axis, should be greater than nHorizontal
<b>xStepM:</b>	Sampling distance at x (horizontal) axis in mm
<b>yPointM:</b>	number of measurement points at y (vertical) axis, should be greater than nVertical
<b>yStepM:</b>	Sampling distance at y (vertical) axis in mm
<b>zTarget:</b>	z distance of target in mm

#### Output

---

**matchedFilter:** 2-D yPointM × xPointM matched filter

### SAR Imaging Function

---

**sarImage =  
reconstructSARImageMatchedFilterSimplified(sarData,matchedFilter,xStepM,yStepM,xySizeT)**

This function creates 2-D SAR image. Input parameters and output are detailed below:

#### Inputs

---

<b>sarData:</b>	nVertical x nHorizontal 2-D SAR Data
<b>matchedFilter:</b>	yPointM × xPointM 2-D matched filter
<b>xStepM:</b>	Sampling distance at x (horizontal) axis in mm
<b>yStepM:</b>	Sampling distance at y (vertical) axis in mm
<b>xySizeT:</b>	z distance of target in mm

#### Output

---

**sarImage:** 2-D SAR Image

---

## SAR IMAGING TUTORIAL

---

### 6. 2-D IMAGING RESULTS

2-D imaging result of Flat 2-D Target Scenario is given in Figure 9.

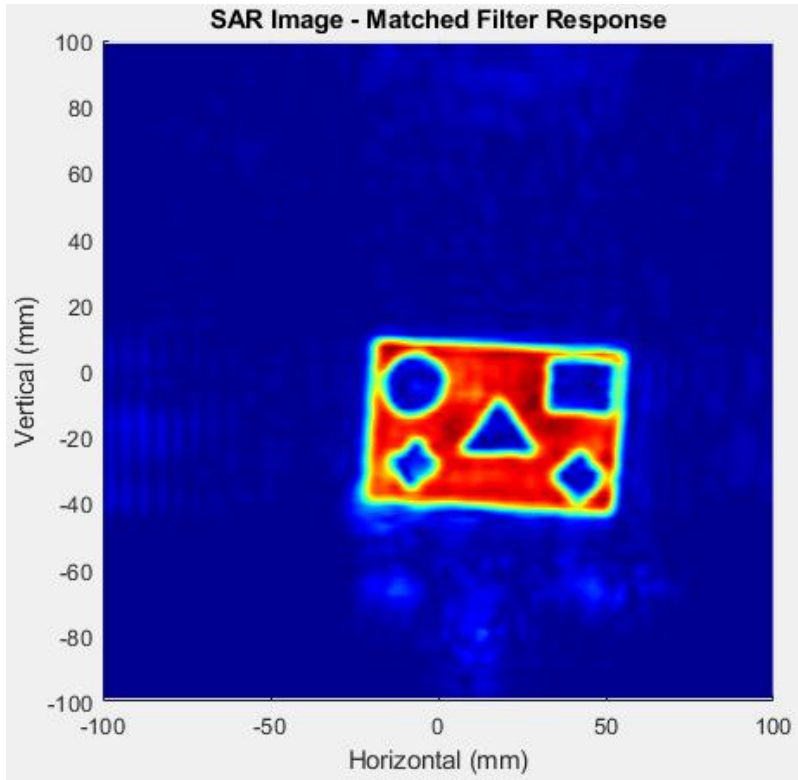


Figure 9 Flat 2-D Target Scenario Image Result

## SAR IMAGING TUTORIAL

2-D imaging results of Two Flat 2-D Targets Concealed in Box Scenario are given in Figure 10. Two different slices are obtained by using two different range bins.

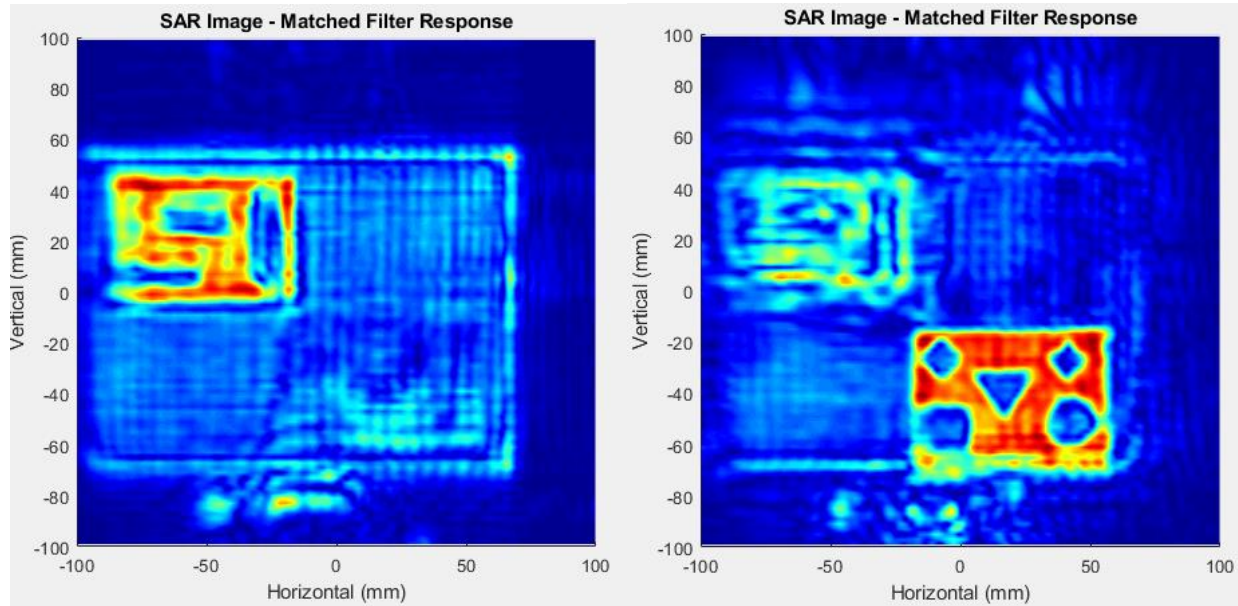


Figure 10 Two Flat 2-D Targets Concealed in Box Scenario Image Results (Note: These are initial results, will be tuned after 3-D imaging)

## SAR IMAGING TUTORIAL

2-D imaging results of Cascaded Concealed Targets Scenario are given in Figure 11. Two different slices are obtained by using two different range bins.

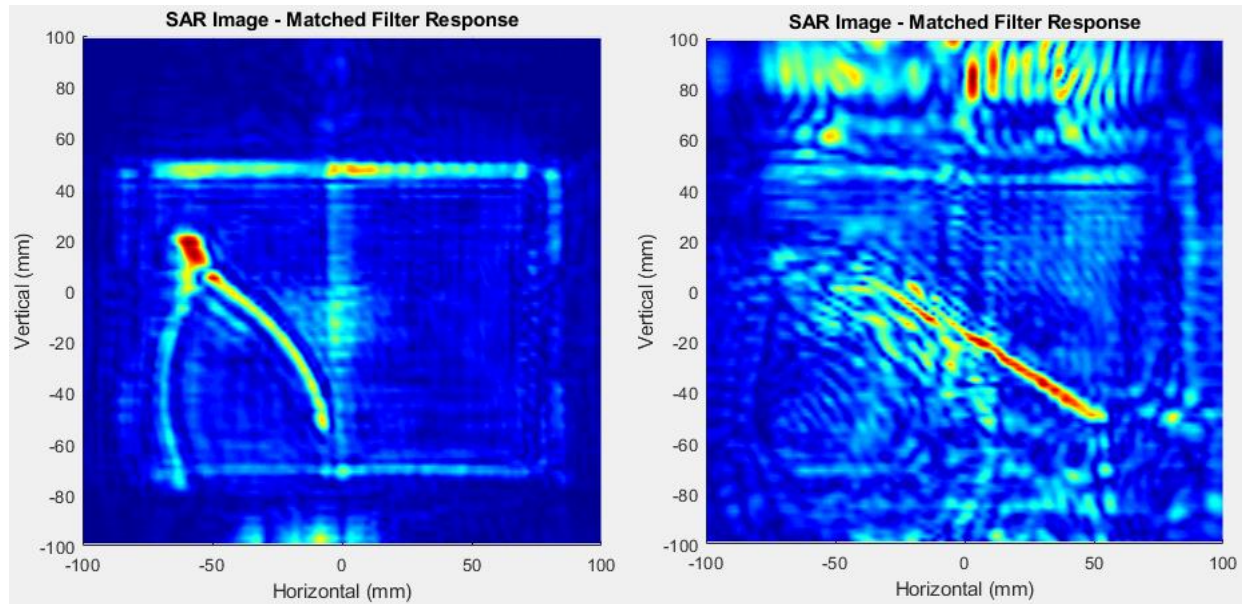


Figure 11 Cascaded Concealed Targets Scenario Image Results (Note: These are initial results, will be tuned after 3-D imaging)