



# Generalized Coherence-based Signal Enhancement

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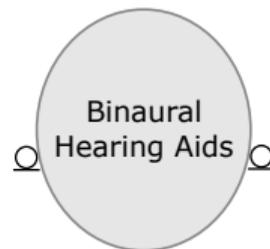
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# Introduction

## Signal enhancement based on the coherent-to-diffuse power ratio (CDR)

- ▶ Well-established concept for two-channel speech dereverberation and noise reduction, e.g., [Habets 2007, Jeub 2012, Schwarz 2015]
- ▶ Beneficial for signal enhancement in hearing aids or mobile phones
- ▶ Algorithms for such applications have to cope with
  - heterogeneous signal quality at each microphone
  - erroneous or missing TDOA information about the desired speaker

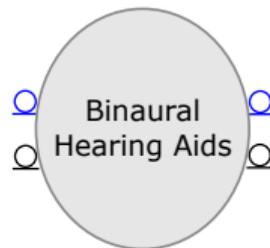


→ New multichannel CDR-based signal enhancement approach for such a scenario will be presented

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→ **New multichannel CDR-based signal enhancement approach for such a scenario will be presented**

# Overview

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- ▶ Introduction
- ▶ CDR-based Speech Enhancement
- ▶ New  $N$ -channel CDR-based Speech Enhancement
- ▶ Evaluation
- ▶ Conclusions

# Signal Model

## Noisy reverberant speech at microphone $i$

$$\begin{aligned}x_i(k) &= \sum_{\kappa=0}^{L-1} s(\kappa) h_i(k - \kappa) + n_i^{(\text{diff})}(k) \\ &= \underbrace{\sum_{\kappa=0}^{K_{\text{early}}-1} s(\kappa) h_i(k - \kappa)}_{\text{desired speech } d_i(k)} + \underbrace{\sum_{\kappa=K_{\text{early}}}^{L-1} s(\kappa) h_i(k - \kappa) + n_i^{(\text{diff})}(k)}_{\text{reverberant speech + diffuse noise } n_i^{(\text{diff})}(k)}\end{aligned}$$

- $s(k)$  : speech signal  
 $h_i(k)$  : room impulse response (RIR)  
 $n_i^{(\text{diff})}(k)$  : diffuse noise  
 $i = 1, \dots, N$  : microphone index  
 $K_{\text{early}}$  : onset of late reverberation

## Coherent-to-diffuse power ratio (CDR)

$$\Lambda_i(l, f) = \frac{\Phi_{d_i, d_i}(l, f)}{\Phi_{n_i, n_i}(l, f)}$$

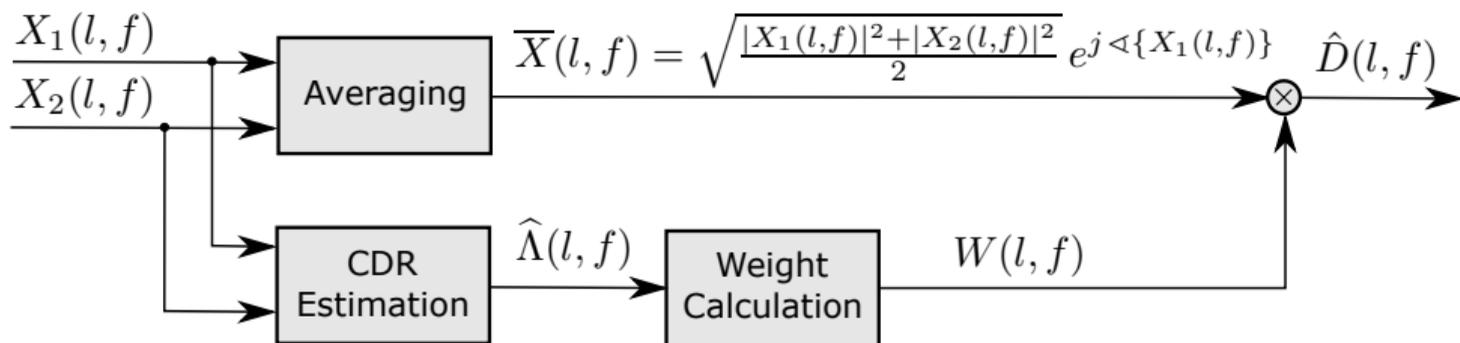
$\Phi_{d_i, d_i}(l, f)$  : short time power spectral density (PSD) of desired speech

$\Phi_{n_i, n_i}(l, f)$  : PSD of reverberant speech and diffuse noise

$l$  : frame index

$f$  : frequency

# CDR-based Speech Enhancement



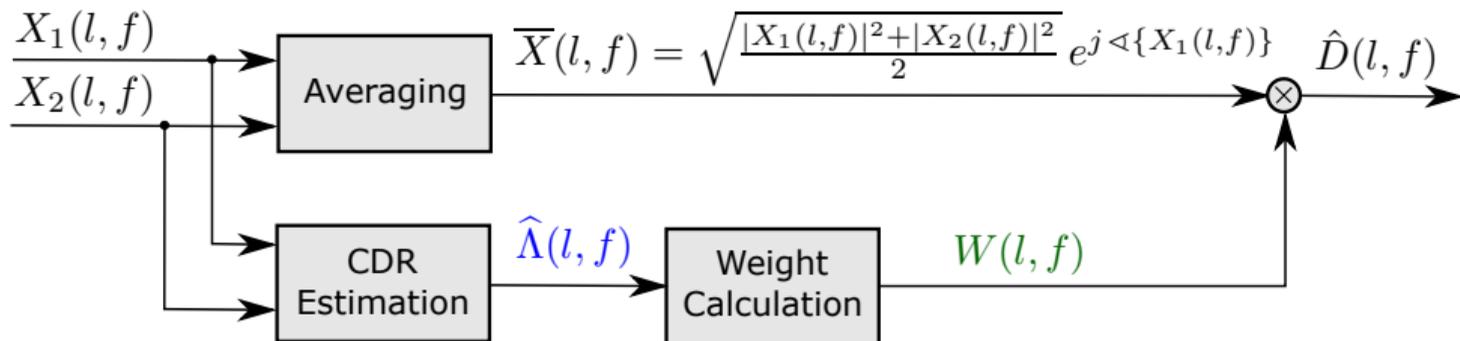
- ▶ Speech enhancement by common noise suppression schemes, e.g.,

$$W(l, f) = \max \left\{ W_{\min}, \left( 1 - \left( \frac{\mu}{\hat{\Lambda}(l, f) + 1} \right)^\beta \right)^\alpha \right\}$$

$W_{\min}$ : minimum weight,  $\mu$  oversubtraction factor,  $\alpha, \beta$ : determines weighting rule

- ▶ Implicit channel selection by choice of phase term  $\angle\{X_1(l, f)\}$  for averaging operation

# CDR-based Speech Enhancement



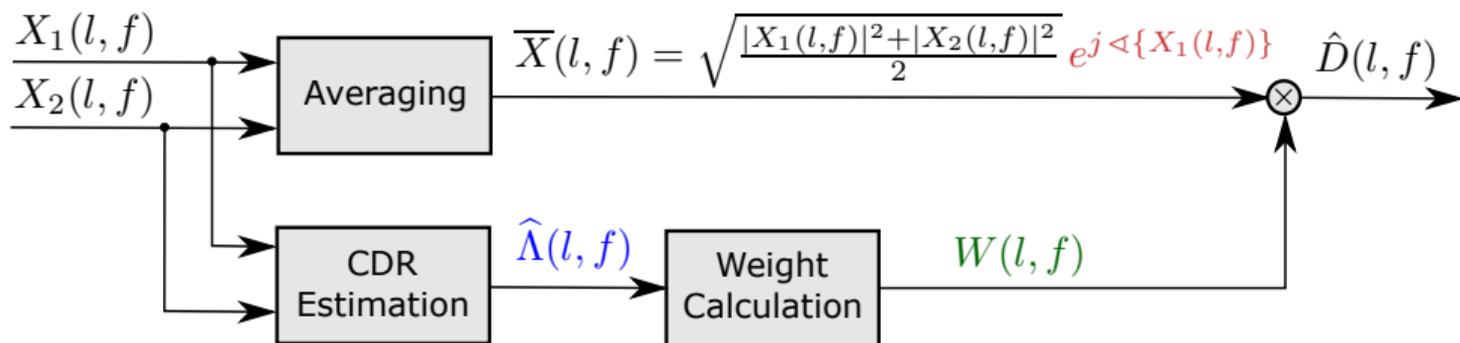
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# CDR Estimation

- ▶ Short time CDR for two microphone signals

$$\Lambda_{1,2}(l, f) = \frac{\Gamma_{n_1, n_2}(l, f) - \Gamma_{x_1, x_2}(l, f)}{\Gamma_{x_1, x_2}(l, f) - \Gamma_{d_1, d_2}(l, f)}$$

- Might become complex-valued due to model and/or estimation errors
- Solved by heuristic modifications, e.g., [Thiergart 2012]

$$\Lambda_{1,2}^{(\text{Th})}(l, f) = \text{Re} \left\{ \frac{\hat{\Gamma}_{n_1, n_2}(l, f) - \hat{\Gamma}_{x_1, x_2}(l, f)}{\hat{\Gamma}_{x_1, x_2}(l, f) - e^{j \angle \{\hat{\Gamma}_{x_1, x_2}(l, f)\}}} \right\}$$

**How to exploit  $N \geq 2$  microphone signals for CDR estimation?**

# New CDR Estimator

Based on the generalized magnitude-squared coherence (GMSC) [Ramirez 2008]

## Generalized Magnitude Coherence (GMC)

$$\gamma_x(l, f) = \frac{1}{N-1} \left( \lambda_x^{(\max)}(l, f) - 1 \right)$$

$\lambda_x^{(\max)}(l, f)$ : largest eigenvalue of the  $N \times N$  coherence matrix

$$\mathbf{C}_x(l, f) = \begin{bmatrix} 1 & \Gamma_{x_1, x_2}(l, f) & \dots & \Gamma_{x_1, x_N}(l, f) \\ \Gamma_{x_2, x_1}(l, f) & 1 & \dots & \Gamma_{x_2, x_N}(l, f) \\ \vdots & \vdots & \ddots & \vdots \\ \Gamma_{x_N, x_1}(l, f) & \Gamma_{x_N, x_2}(l, f) & \dots & 1 \end{bmatrix}$$

## *N*-channel CDR estimator

$$\Lambda_{\text{gen}}(l, f) = \frac{\gamma_n(l, f) - \gamma_x(l, f)}{\gamma_x(l, f) - 1}$$

$\gamma_x(l, f)$  : GMC of coherence matrix  $\mathbf{C}_x(l, f)$  estimated from input signals

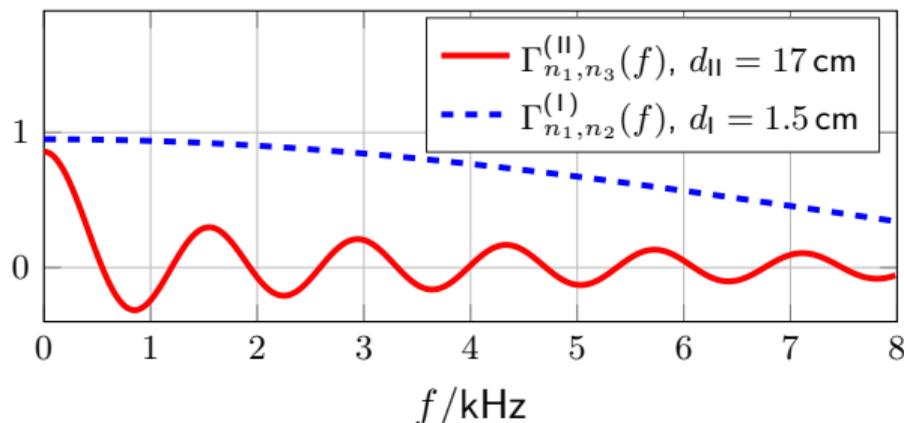
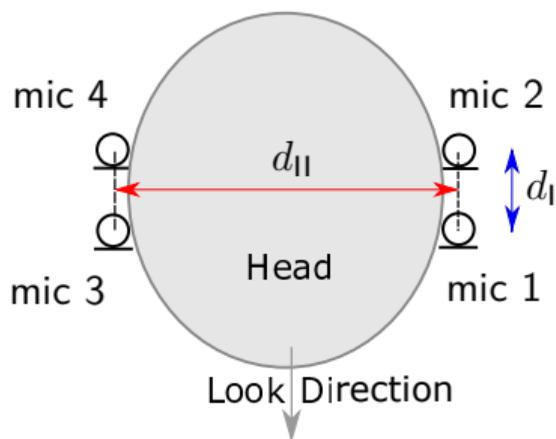
$\gamma_n(l, f)$  : GMC of coherence matrix  $\mathbf{C}_n(l, f)$  obtained by noise coherence models

## Properties

- ▶ Real-valued and positive
- ▶ No TDOA information of desired source  $d(k)$  needed
- ▶  $\Lambda_{\text{gen}}(l, f) = \frac{|\Gamma_n(l, f)| - |\Gamma_x(l, f)|}{|\Gamma_x(l, f)| - 1}$  for special case  $N = 2$

# GMC for Binaural Hearing Aids (HAs)

Coherence Functions



- ▶ Diffuse noise coherence model for one device:

$$\Gamma_{n_1, n_2}^{(I)}(f) = a_s \operatorname{sinc}\left(2\pi f \frac{d_{\perp}}{c}\right) \text{ with } 0 \ll a_s \leq 1$$

- ▶ Diffuse noise coherence model between both devices:

$\Gamma_{n_1, n_3}^{(II)}(f)$  can be determined, e.g., by semi-analytical expressions [Jeub 2012]

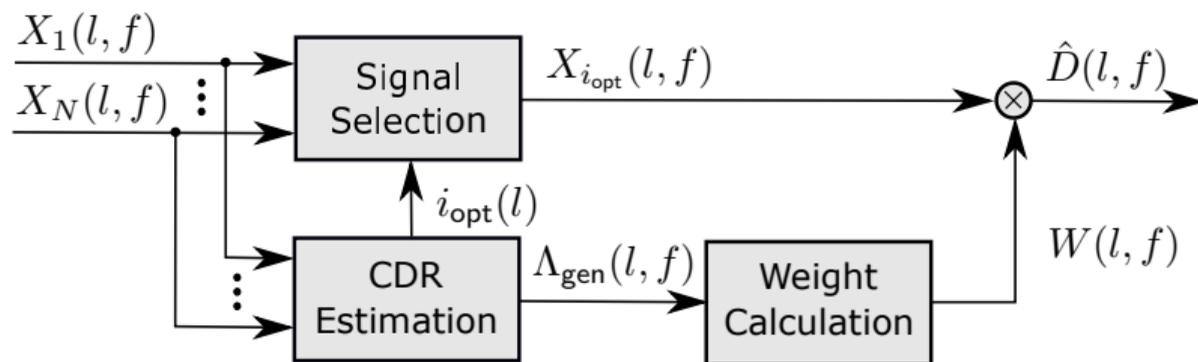
# GMC for Binaural Hearing Aids (HAs)

- ▶ GMC for diffuse noise  $\gamma_n(f)$  determined by noise coherence matrix

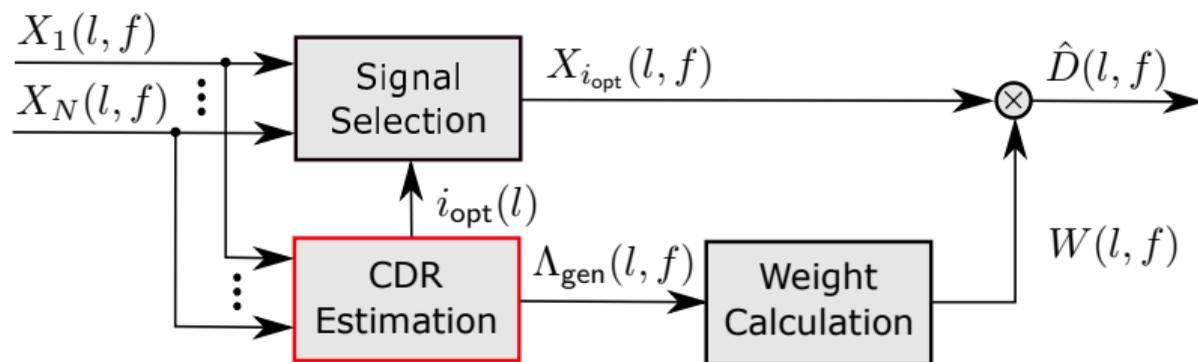
$$\mathbf{C}_n(f) = \begin{bmatrix} 1 & \Gamma_{n_1, n_2}^{(I)}(f) & \Gamma_{n_1, n_3}^{(II)}(f) & \Gamma_{n_1, n_4}^{(II)}(f) \\ \Gamma_{n_2, n_1}^{(I)}(f) & 1 & \Gamma_{n_2, n_3}^{(II)}(f) & \Gamma_{n_2, n_4}^{(II)}(f) \\ \Gamma_{n_3, n_1}^{(II)}(f) & \Gamma_{n_3, n_2}^{(II)}(f) & 1 & \Gamma_{n_3, n_4}^{(I)}(f) \\ \Gamma_{n_4, n_1}^{(II)}(f) & \Gamma_{n_4, n_2}^{(II)}(f) & \Gamma_{n_4, n_3}^{(I)}(f) & 1 \end{bmatrix}$$

- ▶ Assumed to be time-invariant
  - $\gamma_n(f)$  can be calculated in advance

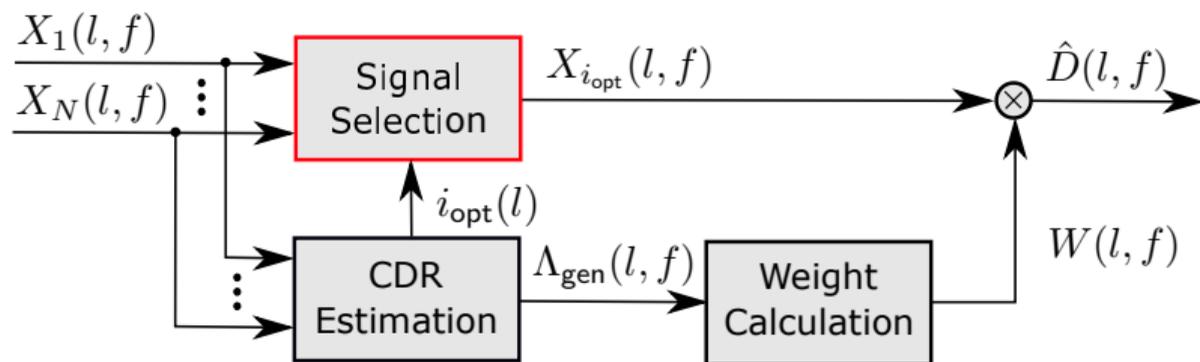
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- ▶ Largest coefficient  $v_x^{(\max)}(l, f_m, i)$  of principal eigenvector of  $\mathbf{C}_x(l, f)$  provides an indicator for signal contribution of microphone  $i$ , cf. [Ramirez 2008]
- ▶ Exploited for signal selection

$$i_{\text{opt}}(l) = \text{round} \{ \alpha i_{\text{opt}}(l-1) + (1 - \alpha) \bar{i}_{\text{opt}}(l) \}, \quad 0 < \alpha < 1$$

$$\bar{i}_{\text{opt}}(l) = \frac{1}{M} \sum_{m=0}^{M-1} \arg \max_i \left\{ |v_x^{(\max)}(l, f_m, i)| \right\}, \quad M: \text{no. of frequency bands}$$

## Setup

- ▶ Speech enhancement for binaural HAs with 4 microphones (2 per device)
- ▶ Speech signal convolved with head-related impulse responses (HRIRs) [Kayser 2009]:
  - cafeteria ( $T_{60} = 1.25$  s, 12 HRIR sets)
  - courtyard ( $T_{60} = 0.9$  s, 12 HRIR sets)
  - first office room ( $T_{60} = 0.4$  s, 37 HRIR sets)
  - second office room ( $T_{60} = 0.3$  s, 8 HRIR sets)
- ▶ Babble noise added to achieve **CDR of 5 dB** for microphone # 1 ( $f_s = 16$  kHz)

## CDR-based speech enhancement using

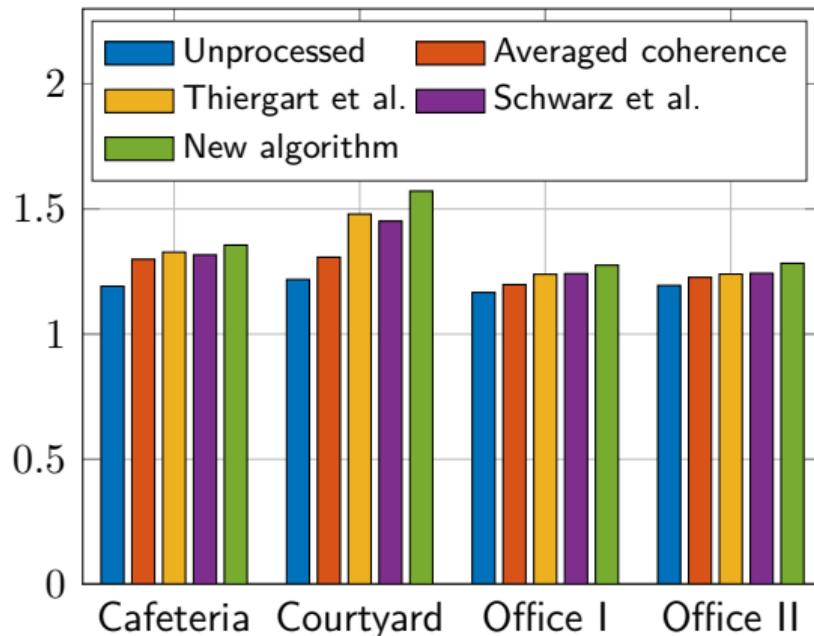
- ▶ biased DOA-independent CDR estimator of [Thiergart 2012]
- ▶ unbiased DOA-independent CDR estimator of [Schwarz 2012]
- ▶ unbiased DOA-independent CDR estimator of [Schwarz 2012] with averaged coherence estimates (see paper for details)
- ▶ new CDR estimator with signal selection

## Same weighting rule for all algorithms

- ▶ Spectral magnitude subtraction ( $\beta = 1/2$ ,  $\alpha = 1$ )
- ▶ Overlapp-add method (512 frequency bands)

# Evaluation

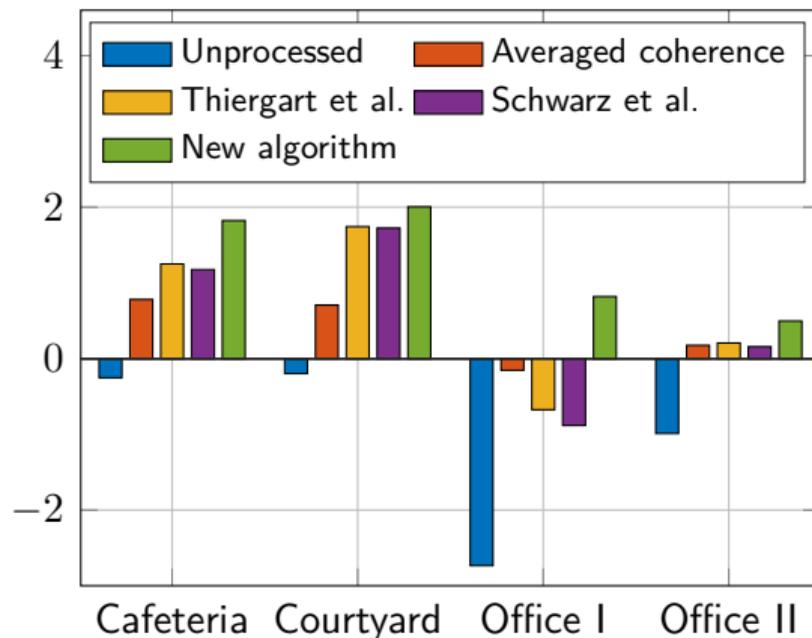
## Wideband PESQ



- ▶ Clean speech taken as reference signal
- ▶ Average results for each room
- ▶ Similar performance for all algorithms
- ▶ New algorithm shows best performance for all scenarios

# Evaluation

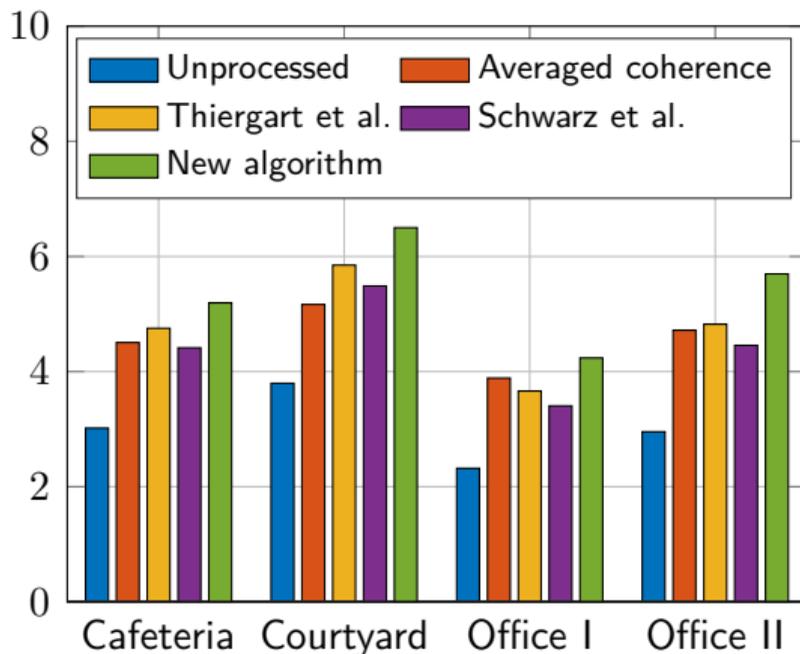
## Frequency-weighted segmental SNR in dB



- ▶ Clean speech taken as reference signal
- ▶ New algorithm shows best performance
- Outperforms averaging of coherence estimates

# Evaluation

## Speech-to-reverberation modulation energy ratio



- ▶ Non-intrusive measure
- ▶ Quality assessment for dereverberated speech [Falk 2010]
- ▶ New algorithm shows best performance

# Conclusions

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## Generalized CDR-based signal enhancement algorithm presented

- ▶ Adopts concept of generalized magnitude coherence (GMC)
- ▶ Exploits inherently an arbitrary number of microphone signals
- ▶ Most appropriate microphone for signal enhancement determined implicitly without requiring TDOA information
- ▶ Achieves a consistently better signal quality than related approaches for binaural speech enhancement
- ▶ Also of interest for speech enhancement in mobile phones or sensor networks
  - Subject for further investigations

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**Thank you for your attention!**

# References

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- [Habets 2007] E. A. P. Habets,  
*Single- and Multi-Microphone Speech Dereverberation using Spectral Enhancement*,  
Ph.D. thesis, Eindhoven University, Eindhoven, The Netherlands, 2007.
- [Schwarz 2015] A. Schwarz and W. Kellermann,  
"Coherent-to-Diffuse Power Ratio Estimation,"  
*IEEE/ACM Trans. on Audio, Speech, and Language Processing*, vol. 23, no. 6, pp. 1006–1018, 6 2015.
- [Ramirez 2008] D. Ramirez, J. Via, and I. Santamaria,  
"A Generalization of the Magnitude Squared Coherence Spectrum for More than Two Signals: Definition, Properties and Estimation,"  
in *Proc. of Intl. Conference on Acoustics, Speech, and Signal Processing (ICASSP)*, Las Vegas (Nevada), USA., Mar. 2008, pp. 3769–3772.
- [Jeub 2012] M. Jeub,  
*Joint Dereverberation and Noise Reduction for Binaural Hearing Aids and Mobile Phones*,  
Ph.D. thesis, RWTH Aachen University, Aachen, Germany, 2012.
- [Thiergart 2012] O. Thiergart, G. Del Galdo, and E. A. P. Habets,  
"Signal-to-Reverberant Ratio Estimation Based on the Complex Spatial Coherence Between Omnidirectional Microphones,"  
in *Proc. of Intl. Conference on Acoustics, Speech, and Signal Processing (ICASSP)*, Kyoto, Japan, Mar. 2012, pp. 309–312.
- [Kayser 2009] H. Kayser, S. D. Ewert, J. Anemüller, T. Rohdenburg, V. Hohmann, and B. Kollmeier,  
"Database of Multichannel In-Ear and Behind-the-Ear Head-Related and Binaural Room Impulse Responses,"  
*EURASIP Journal on Advances in Signal Processing*, vol. 2009, pp. 1–10, 2009.
- [Falk 2010] T. H. Falk, C. Zheng, and W. Chan,  
"A Non-Intrusive Quality and Intelligibility Measure of Reverberant and Dereverberated Speech,"  
*IEEE Trans. on Audio, Speech, and Language Processing*, vol. 18, no. 7, pp. 1766–1774, Sept. 2010.