# Energy Detection in ISI Channels Using Large-Scale Receiver Arrays

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### Motivation: Systems with a Large Number of Antennas

### Non-coherent Detection in Wideband Systems with Massive Receiver Arrays

Conclusions

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# Outline

## Motivation: Systems with a Large Number of Antennas

### Non-coherent Detection in Wideband Systems with Massive Receiver Arrays

Conclusions

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 $\ensuremath{\text{Massive MIMO}}\xspace$  : Base stations/ Back-hauls have the capacity to nest a large number of antennas.

In mmWave frequencies, small size terminals can host a large number of antennas.

# Why Hosting More Antennas?

### Drastic improvement of system capacity and reliability becomes possible.

More antennas, more DoF and multiplexing gain.

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- ▶ Beamforming gain: Pencil-beams direct power to desired user.

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#### Simple linear processing techniques lead to close-to-optimal performance.

- Uplink: when  $M \gg K$ , MF, ZF, MMSE nearly optimal.
- Downlink: simple precoders, e.g. MRT, ZF, MMSE, are promising.

Key assumption: **Perfect** or **nearly-perfect** channel state information (CSI) is required.

# **Channel Estimation Challenges**

### Downlink training becomes not "economical":

To provide optimal performance, orthogonal training is required:

- ▶ No. of downlink pilots scales with the number of BS antenna *M*: A large portion of time-frequency resource is needed.
- No. of unknown channel coefficients scales with M:
  - Resources demanded to feedback the CSI from user terminal to base station escalates.

Uplink Training Solution: TDD operation exploiting channel reciprocity.

▶ Training resources scale with K instead of M.

However,

- Channel reciprocity does not always hold: hardware constraints and fast fading channels.
- Large channel estimation error in medium and low SNR scenarios.
- Pilot contamination.

# Our Proposal: Low Complexity Non-coherent Energy Detection



Figure: Single stream transmission with a large-scale receiver array.

#### Advantages:

- Low hardware complexity: No phase shifter and amplifiers at RF chains.
- Noise hardening: Deterministic noise.
- ▶ Central limit theorem: Gaussian approximations for related variables.
- Simple decoding method: Detection based on the statistics of the channel energy instead of instantaneous CSI.
- ▶ No capacity loss compared to coherent detection when *M* is large.

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# Non-coherent Energy Detection in Wideband (mmWave) Systems



Consider additive white Gaussian noise, the received signal at time j reads

$$\mathbf{y}(j) = \sum_{l=0}^{L-1} \mathbf{h}_l x(j-l) + \mathbf{n}(j),$$
(1)

▶ *I*th path channel coeff.:  $\mathbf{h}_{l} = [h_{1,l}, \dots, h_{M,l}]^{T}$ . **Objective**: Detect unknown data x(j) based on

$$z(j) = \frac{||\mathbf{y}(j)||_2^2}{M}.$$
 (2)

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# Asymptotical Analysis

The output of the ED is written as:

$$z(j) = \frac{1}{M} ||\mathbf{h}_{0}||_{2}^{2} |x(j)|^{2} + \underbrace{\frac{1}{M} \sum_{l=1}^{L-1} ||\mathbf{h}_{l}||_{2}^{2} |x(j-l)|^{2}}_{\text{ISI}_{1}} + \underbrace{\frac{1}{M} \sum_{l \neq l'} x^{*}(j-l)x(j-l')\mathbf{h}_{l}^{H}\mathbf{h}_{l'}}_{\text{ISI}_{2}} + \underbrace{\frac{2}{M} \Re\left(\sum_{l=0}^{L-1} \mathbf{h}_{l}^{H}\mathbf{n}x(j-l)\right)}_{\text{ISI}_{3}} + \frac{1}{M} \mathbf{n}^{H}(j)\mathbf{n}(j).$$
(3)

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# Asymptotical Analysis

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(3)

Employing uncorrelated scattering assumption, asymptotically, we obtain

$$\frac{\mathbf{h}_{l}^{H}\mathbf{h}_{l'}}{M} \xrightarrow{M \to +\infty} \sigma_{h,l}^{2} \delta_{l,l'}, \quad \frac{\mathbf{h}_{l}^{H}\mathbf{n}(j)}{M} \xrightarrow{M \to +\infty} \mathbf{0}, \quad \frac{\mathbf{n}^{H}(j)\mathbf{n}(j)}{M} \xrightarrow{M \to +\infty} \sigma_{n}^{2}.$$

Thus,

$$z(j) \xrightarrow{M \to +\infty} \sum_{l=0}^{L-1} \sigma_{h,l}^2 |x(j-l)|^2 + \sigma_n^2.$$
(4)

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## Asymptotical Analysis

A standard equalization problem is obtained:

$$z(j) \xrightarrow{M \to +\infty} \sum_{l=0}^{L-1} \sigma_{h,l}^2 |x(j-l)|^2 + \sigma_n^2.$$
(5)

- Noise contribution becomes deterministic.
- Instantaneous CSI becomes irrelevant: only average channel energy of each tap is required (long term statistics).
- Simple equalization techniques may work well.

Proposed solution: Employing Zero Forcing equalizer and use average channel energy to compute its coefficients.

## Performance Evaluation

Uncoded system: channel with exponential power decay PDP and L = 4.



- ZF produces a SER performance scales with the number of antennas and SNR.
- Promising results at low and medium SNR regimes.
- More antennas leads to significantly lower SER.
- Reach extension is granted with equipping more antennas.

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## Performance Evaluation

Uncoded system: channel with exponential power decay and L = 4.



As SNR increases, the performance gap widens a bit due to the noise enhancement when applying the ZF equalizer.

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## Conclusions: Coherent or Non-coherent Detection

Coherent detection is optimal, but channel estimation is the bottleneck.

With a large number of receiver antennas, **non-coherent detection performs close-to-optimal:** 

- Second order statistics of the channel coefficients are required instead of instantaneous CSI.
  - Long term and more robust statistics can be estimated over a longer horizon.
  - ► A simplified channel estimation problem and robust to mobility.
- Noise hardening: reach extension is guaranteed and noise may not be the limiting factor for system performance.
- Low complexity hardware: no phase shifters and gain controller at each RF chain.
- Low complexity decoding algorithms thanks to the law of large numbers and central limit theorem.