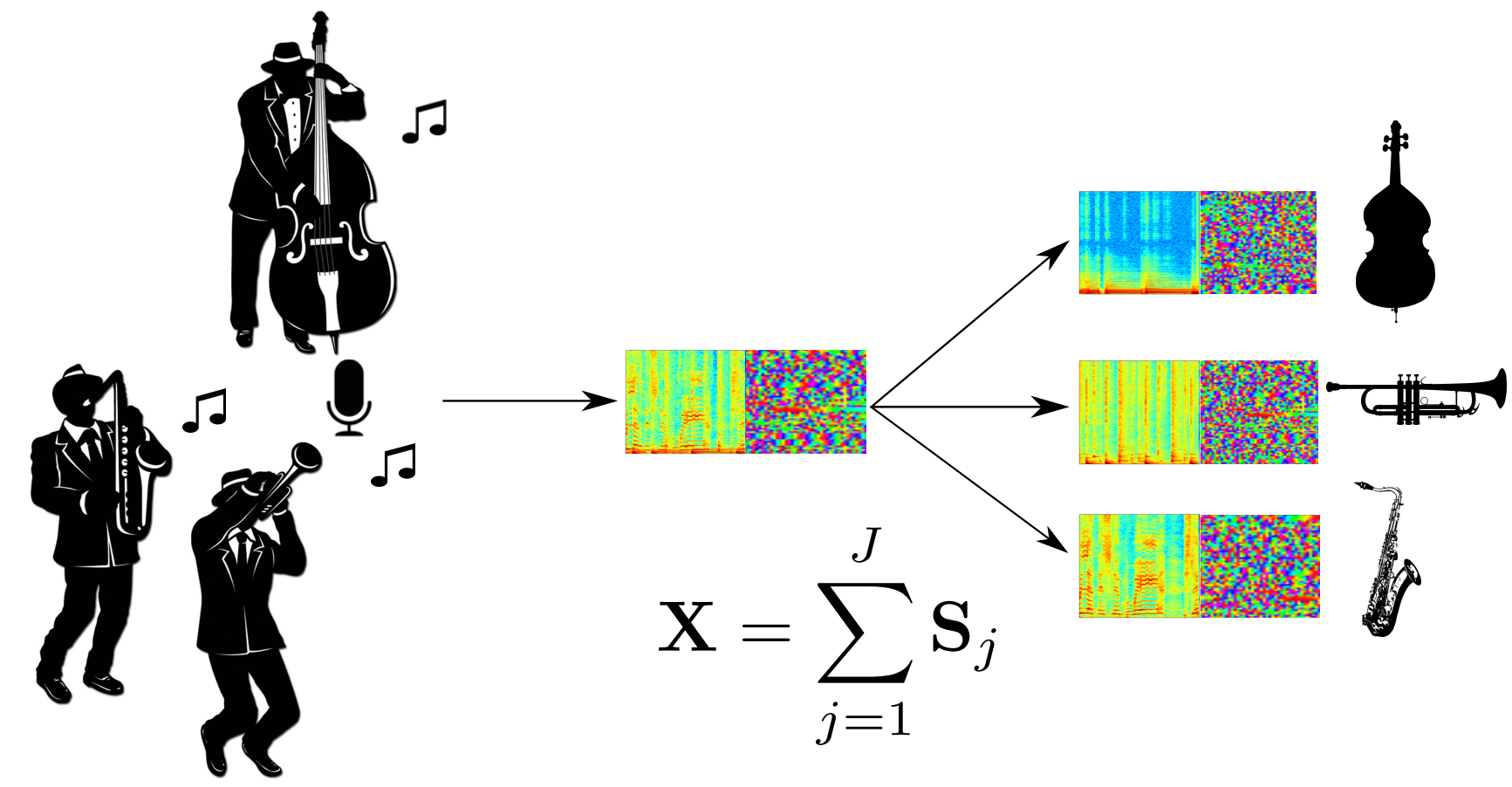
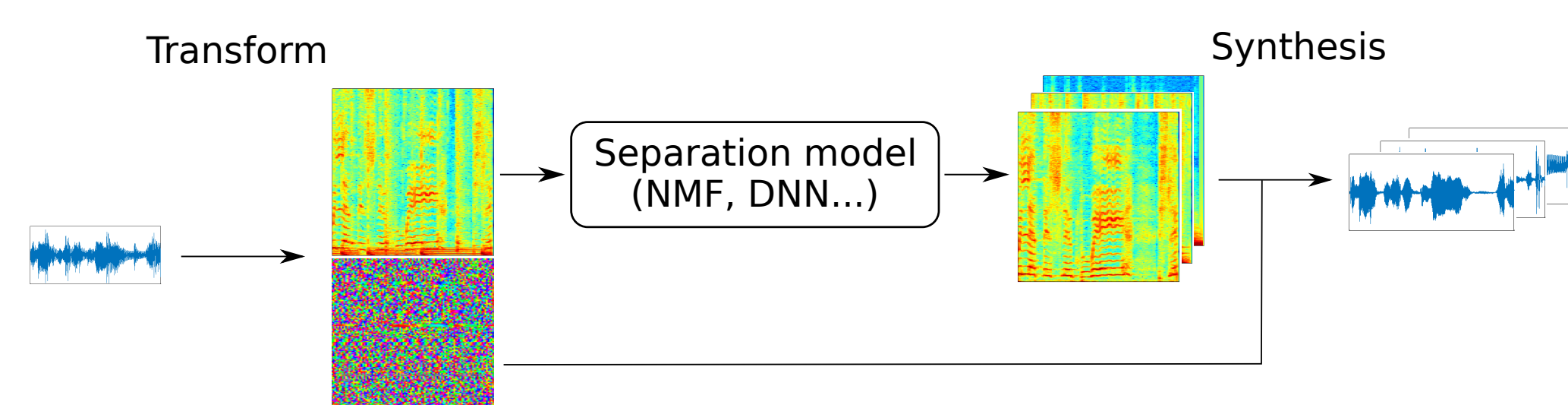


### Source separation



- Isolate individual sources from their mixture.
- Here: operate in the short-time Fourier transform (STFT) domain.

### General framework



- Extract a nonnegative representation (magnitude/power spectrogram).
- Fit a structured model (nonnegative matrix factorization, deep neural network).
- Mask the mixture to retrieve isolated sources  $\hat{\mathbf{S}}_j$ .
- Synthesize time-domain signals through inverse STFT.

### Phase recovery

Nonnegative masking  $\rightarrow \angle \mathbf{S}_j = \angle \mathbf{X}$ .

- The phase of the mixture is assigned to each source.
- Issues in sound quality when the sources overlap in the STFT domain.

### Multiple Input Spectrogram Inversion (MISI) [1]

- Extends the Griffin-Lim algorithm to multiple signals in mixture models.
- Find time-domain sources  $\mathbf{s}_j$  whose magnitude is close to the target value  $\mathbf{V}_j$  by solving:

$$\min_{\mathbf{s}_j} \sum_{j=1}^J \|\mathbf{V}_j - |\text{STFT}(\mathbf{s}_j)|\|^2 \text{ s.t. } \sum_{j=1}^J \mathbf{s}_j = \mathbf{x}.$$

### Problem

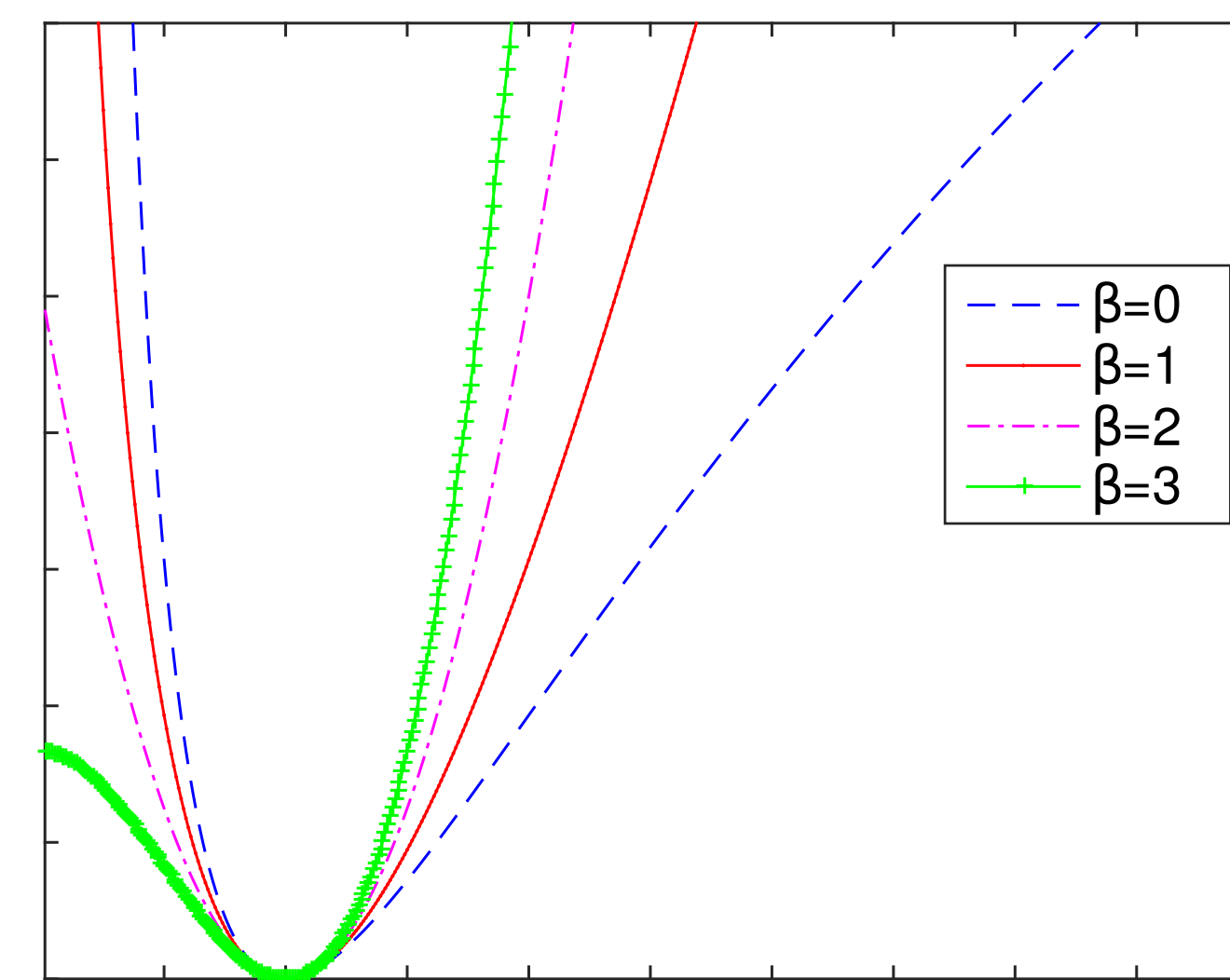
The Euclidean distance is not the most appropriate measure for audio spectrograms.

### Proposed approach

#### Bregman divergences

$$\mathcal{D}_\psi(\mathbf{P} | \mathbf{Q}) = \sum_{f,t} \psi(p_{f,t}) - \psi(q_{f,t}) - \psi'(q_{f,t})(p_{f,t} - q_{f,t})$$

- $\psi$  is a strictly-convex, continuously-differentiable generating function.
- Encompass the  $\beta$ -divergences [2] and its particular cases:
  - Euclidean ( $\beta = 2$ )
  - Kullback-Leibler ( $\beta = 1$ )
  - Itakura-Saito ( $\beta = 0$ )



#### Problem setting

$$\min_{\mathbf{s}_j} \underbrace{\sum_{j=1}^J \mathcal{C}_j(\mathbf{s}_j)}_{\text{Data fitting}} \text{ s.t. } \underbrace{\sum_{j=1}^J \mathbf{s}_j = \mathbf{x}}_{\text{Mixing constraint}}$$

Accounting for the non-symmetry of Bregman divergences:

$$\mathcal{C}_j(\mathbf{s}_j) = \begin{cases} \mathcal{D}_\psi(\mathbf{V}_j | |\text{STFT}(\mathbf{s}_j)|^d) & \text{“right”} \\ \mathcal{D}_\psi(|\text{STFT}(\mathbf{s}_j)|^d | \mathbf{V}_j) & \text{“left”} \end{cases}$$

Accounting for variable nonnegative measurements:

$$d = \begin{cases} 1 & \text{if } \mathbf{V}_j \text{ are magnitudes} \\ 2 & \text{if } \mathbf{V}_j \text{ are power spectrograms} \end{cases}$$

#### Algorithm

- The set defined by the mixing constraint is convex.
- The gradients can be computed using the chain rule as in [3].

#### Projected gradient descent

$$\begin{aligned} \mathbf{y}_j &\leftarrow \mathbf{s}_j - \mu \nabla \mathcal{C}_j(\mathbf{s}_j) \\ \mathbf{s}_j &\leftarrow \mathbf{y}_j + \frac{1}{J} \left( \mathbf{x} - \sum_{i=1}^J \mathbf{y}_i \right) \end{aligned}$$

$\mu$  is the step size.

#### Update rules

Starting from initial estimates, alternate the following:

- Compute the STFT:
 
$$\mathbf{S}_j = \text{STFT}(\mathbf{s}_j)$$
- Compute the gradient:
 
$$\mathbf{G}_j = \begin{cases} \mathbf{G}_j = \psi''(|\mathbf{S}_j|^d) \odot (|\mathbf{S}_j|^d - \mathbf{V}_j) & \text{“right”} \\ \psi'(|\mathbf{S}_j|^d) - \psi'(\mathbf{V}_j) & \text{“left”} \end{cases}$$

- Gradient descent:

$$\mathbf{Y}_j = \mathbf{S}_j - \mu d \times \mathbf{S}_j \odot |\mathbf{S}_j|^{d-2} \odot \mathbf{G}_j$$

- Inverse STFT:

$$\mathbf{y}_j = \text{STFT}^{-1}(\mathbf{Y}_j)$$

- Mixing:

$$\mathbf{s}_j = \mathbf{y}_j + \frac{1}{J} \left( \mathbf{x} - \sum_{i=1}^J \mathbf{y}_i \right)$$

*Remark:* MISI is a particular case (quadratic loss,  $d = 1$ , and  $\mu = 1$ ).

#### References

- [1] Gunawan and Sen, “Iterative phase estimation for the synthesis of separated sources from single-channel mixtures”, *IEEE Signal Processing Letters*, vol. 17, no. 5, pp. 421–424, May 2010.
- [2] Hennequin et al., “Beta-divergence as a subclass of Bregman divergence”, *IEEE Signal Processing Letters*, vol. 18, no. 2, pp. 83–86, Feb. 2011.
- [3] Vial et al., “Phase retrieval with Bregman divergences and application to audio signal recovery”, *IEEE Journal of Selected Topics in Signal Processing*, vol. 15, no. 1, pp. 51–64, Jan. 2021.

### Experimental protocol

#### Speech enhancement ( $J = 2$ )

- Clean speech from the VoiceBank dataset.
- Real-life noises from the DEMAND dataset (living room, bus, and public square noises).
- Mixtures at various input SNR ( $-10, 0$ , and  $10$  dB).

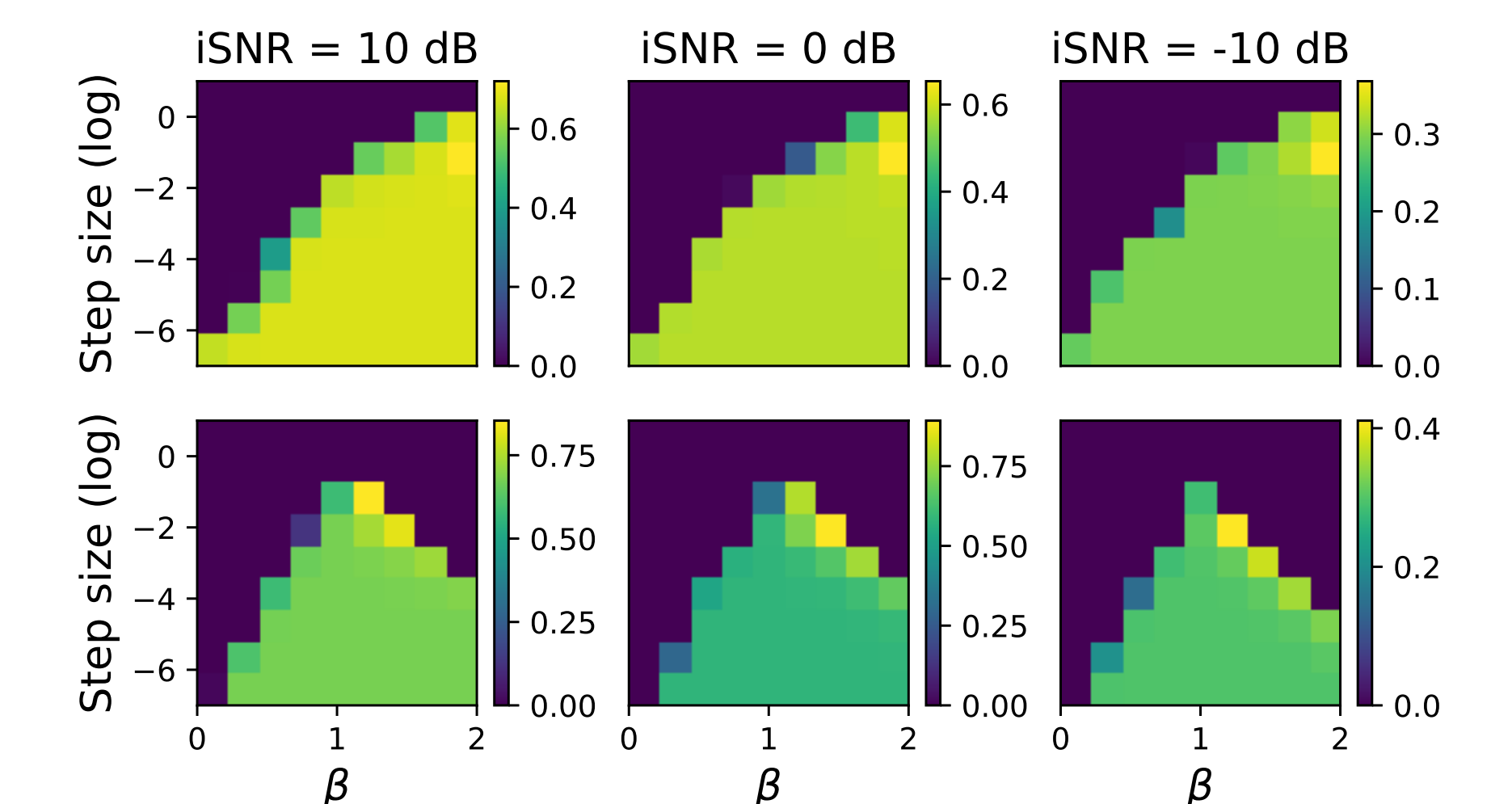
#### Magnitude estimation with Open-Unmix.

- A freely available Bi-LSTM network.
- Pretraining on different speakers and noises.

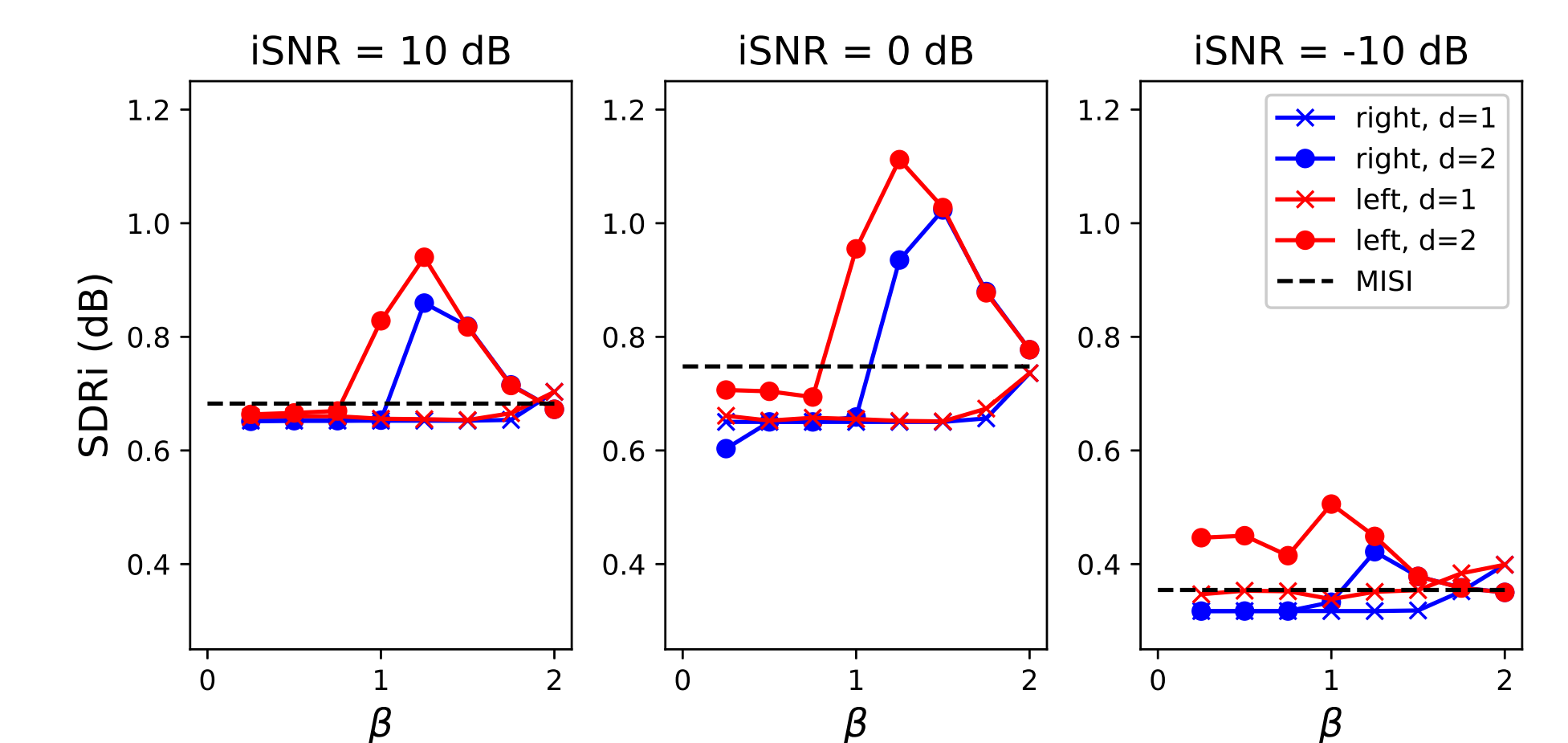
**Metric:** Signal-to-distortion ratio improvement over the baseline amplitude mask (SDRi).

### Results

#### Step size tuning (top: $d = 1$ ; bottom: $d = 2$ )



#### Separation performance:



- Our method outperforms MISI when  $d = 2$ :
  - At high/moderate input SNR when  $\beta > 1$ .
  - At low input SNR for all  $\beta$  and the “left” problem.
- Performance peak around  $\beta = 1.25$ , close to Kullback-Leibler ( $\beta = 1$ ).
- Results depend on the type of noise.

### Summary

- MISI is extended to Bregman divergences.
- Projected gradient descent algorithm.
- Alternative divergences are interesting when spectrogram are highly degraded.