

# Information-Bottleneck-Based Behavior Representation Learning for Multi-agent Reinforcement Learning

Yue Jin<sup>1</sup> Shuangqing Wei<sup>2</sup> Jian Yuan<sup>1</sup> Xudong Zhang<sup>1</sup>

<sup>1</sup> Department of Electronic Engineering, Tsinghua University

<sup>2</sup> School of Electrical Engineering and Computer Science, Louisiana State University

# Outline

1. Background
2. Method
3. Experiments
4. Conclusion

# Outline

1. Background
2. Method
3. Experiments
4. Conclusion

# I. BACKGROUND

- Representation learning in DRL
  - Why representation learning
    - Learn informative and effective features of a task
    - Efficiency, robustness, and scalability (Multi-agent DRL)
  - Early works combine deep auto-encoder with DRL (Lang et al. 2010)
  - Recent works involve
    - advanced unsupervised learning to extract **discriminative** features from observations (Laskin et al. 2020)
    - information estimation methods to learn **compact/ task-relevant** representation for DRL (Pacelli et al. 2020)
    - model-based DRL to learn abstract state representation/ **low-dimensional** representation of the environment (François-Lavet et al. 2019)

Lang et al. 2010. **Deep Auto-Encoder Neural Networks in Reinforcement Learning.**

Laskin et al. 2020. **CURL: Contrastive Unsupervised Representations for Reinforcement Learning.**

Pacelli et al. 2020. **Learning Task-Driven Control Policies via Information Bottlenecks.**

François-Lavet et al. 2019. **Combined Reinforcement Learning via Abstract Representations.**

# I. BACKGROUND

- Issues of representation learning in MADRL
  - Teammate/opponent-relevant
  - What to represent
  - Combination with MADRL
- Previous works
  - Design general frameworks to combine teammate/opponent representation with MADRL (He et al. 2016)
  - Represent other agents' behaviors **implicitly** using their positions at adjacent time steps (Jin et al. 2020, Jin et al. 2021)
- This work focuses on
  - **Explicit** and **interpretable** other agents' behavior representation learning based on our previous work (Jin et al. 2020)
  - **Information compression** and **retention** in the representation
  - More **efficient** and **scalable** algorithm

Jin et al. 2020. **Stabilizing Multi-Agent Deep Reinforcement Learning by Implicitly Estimating Other Agents' Behaviors.**

Jin et al. 2021. **Hierarchical and Stable Multiagent Reinforcement Learning for Cooperative Navigation Control.**

He et al. 2016. **Opponent Modeling in Deep Reinforcement Learning.**

# Outline

1. Background
2. Method
3. Experiments
4. Conclusion

## 2. METHOD

- From implicit learning to explicit learning of other agents' behavior representation

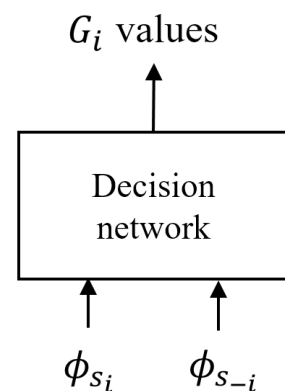
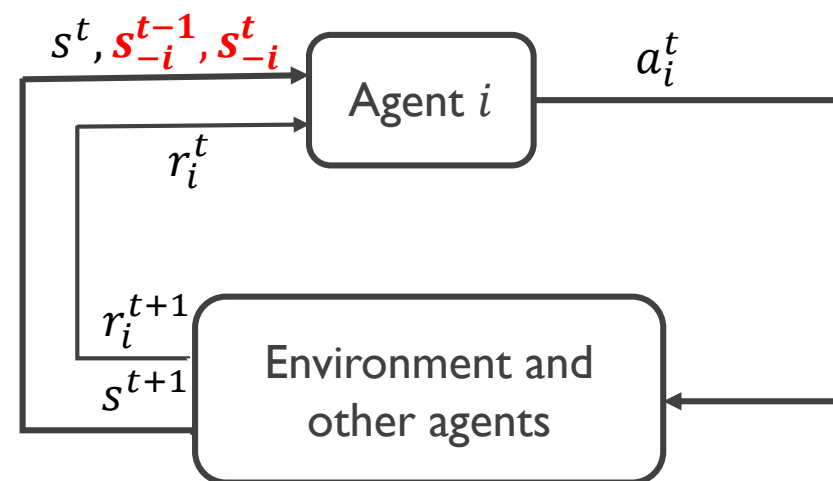
- Implicit action representation learning

SMADQN (Jin et al. 2020)

- Define an extended action-value function  $G$  for each agent
  - Incorporates the states of other agents at two adjacent time steps into its input
- Design a stabilized MADRL algorithm

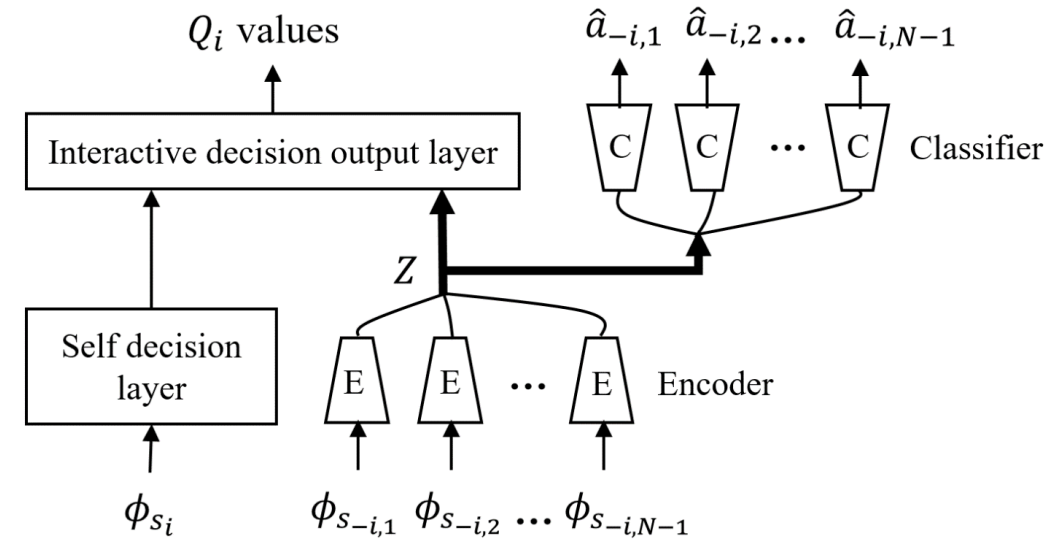
$$L = \mathbb{E}_{s^t, s^{t+1}, a_i^t} \left[ \left( r_i^{t+1} + \gamma \max_{a_i^{t+1}} G_i(s^{t+1}, s_{-i}^t, s_{-i}^{t+1}, a_i^{t+1}) - G_i(s^t, s_{-i}^t, s_{-i}^{t+1}, a_i^t) \right)^2 \right]$$

- Other agents' behavior representation is implicit



## 2. METHOD

- From implicit learning to explicit learning of other agents' behavior representation
  - Explicit action representation learning
    - An encoder to learn low-dimensional features of other agents' actions using their states at adjacent time steps as inputs
    - A classifier to predict the actions via supervised learning
    - Leverage cross entropy as part of the loss
- Information compression and retention
  - Relevant to the task
  - Relevant to other agents
  - Filtering out irrelevant information





## 2. METHOD

- IBORM: **I**nformation-**B**ottleneck-based **O**ther agents' behavior **R**epresentation learning for **M**ulti-agent reinforcement learning

- Information bottleneck principle (Tishby et al. 2015)

- Extracting an **optimal representation Z** of a random variable **X** about another correlated random variable **Y** while **minimizing the amount of irrelevant information**

- is formulated as minimizing

$$\mathcal{L}(p(z|x)) = I(X; Z) - \kappa I(Z; Y)$$

- $(Y, X, Z)$  forms a Markov chain,  $Y \rightarrow X \rightarrow Z$

## 2. METHOD

- **IBORM: Information-Bottleneck-based Other agents' behavior Representation learning for Multi-agent reinforcement learning**

- Based on IB principle, we constrain the representation learning (encoder) by minimizing

$$\mathcal{L}(\alpha) \triangleq I(\phi_{s-i,j}; ENC_i^\alpha(\phi_{s-i,j})) - \kappa I(ENC_i^\alpha(\phi_{s-i,j}); a_{-i,j})$$

- $a \rightarrow \phi_s \rightarrow z$
- $z = ENC(\phi_s)$
- Overall objective of IBORM
  - To minimize

$$L_i(\alpha, \beta, \theta) = J_i^{CE}(\alpha, \beta) + \lambda_1 J_i^{DRRL}(\alpha, \theta) + \lambda_2 I(\phi_{s-i,j}, ENC_i^\alpha(\phi_{s-i,j})) - \lambda_3 I(ENC_i^\alpha(\phi_{s-i,j}), a_{-i,j})$$

## 2. METHOD

- Mutual information estimation in IBORM

- Leverage Mutual Information Neural Estimator (MINE) (Belghazi et al. 2018)

- Estimate the mutual information between two variables  $X$  and  $Z$  as

$$I(\widehat{X}, \widehat{Z}) = \sup_{\omega \in \Omega} \mathbb{E}_{\mathbb{P}_{XZ}} [T_{\omega}(x, z)] - \log(\mathbb{E}_{\mathbb{P}_X \otimes \mathbb{P}_Z} [e^{T_{\omega}(x, z)}])$$

with a trainable neural network  $T_{\omega}$

- IBORM uses two MINE networks corresponding to

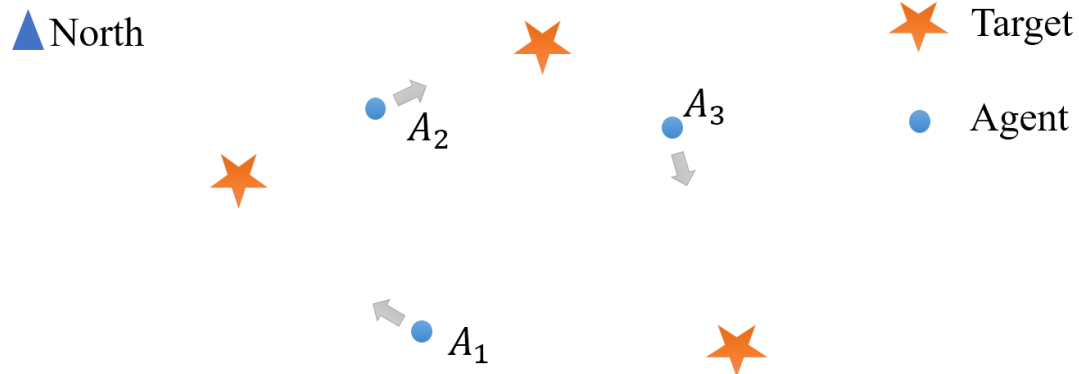
$$I(\phi_{s-i,j}; ENC_i^{\alpha}(\phi_{s-i,j})) \text{ and } I(ENC_i^{\alpha}(\phi_{s-i,j}); a_{-i,j}) .$$

# Outline

1. Background
2. Method
- 3. Experiments**
4. Conclusion

### 3. EXPERIMENTS

- Multi-agent cooperative navigation task with the same settings used in our previous work (Jin et al. 2020)
  - Agents need to cooperate through motions to reach a set of targets with the minimum time cost
  - Randomly generate positions of targets and agents in every episode
  - Different numbers of targets and agents ( $N = 3, 4, 5, 6, \text{ and } 7$ )



Observation: positions of targets and the current and last positions of other agents

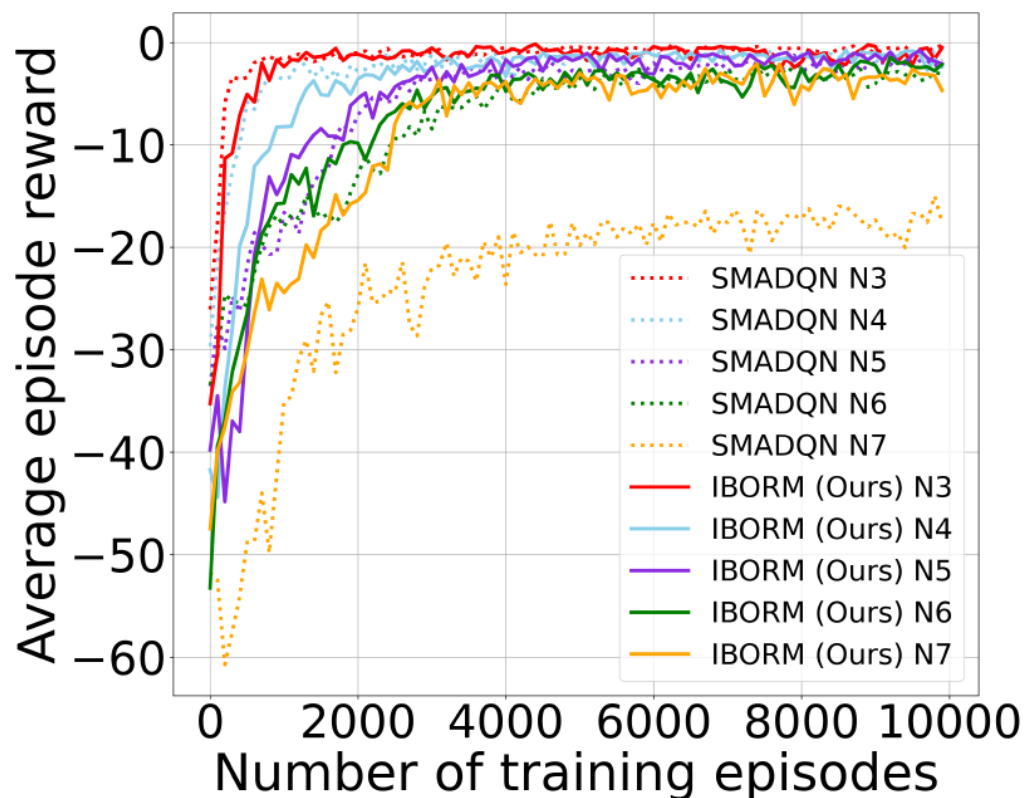
Action: select a target to head for  $a_i \in [1, N]$

Assuming a constant speed

# 3. EXPERIMENTS

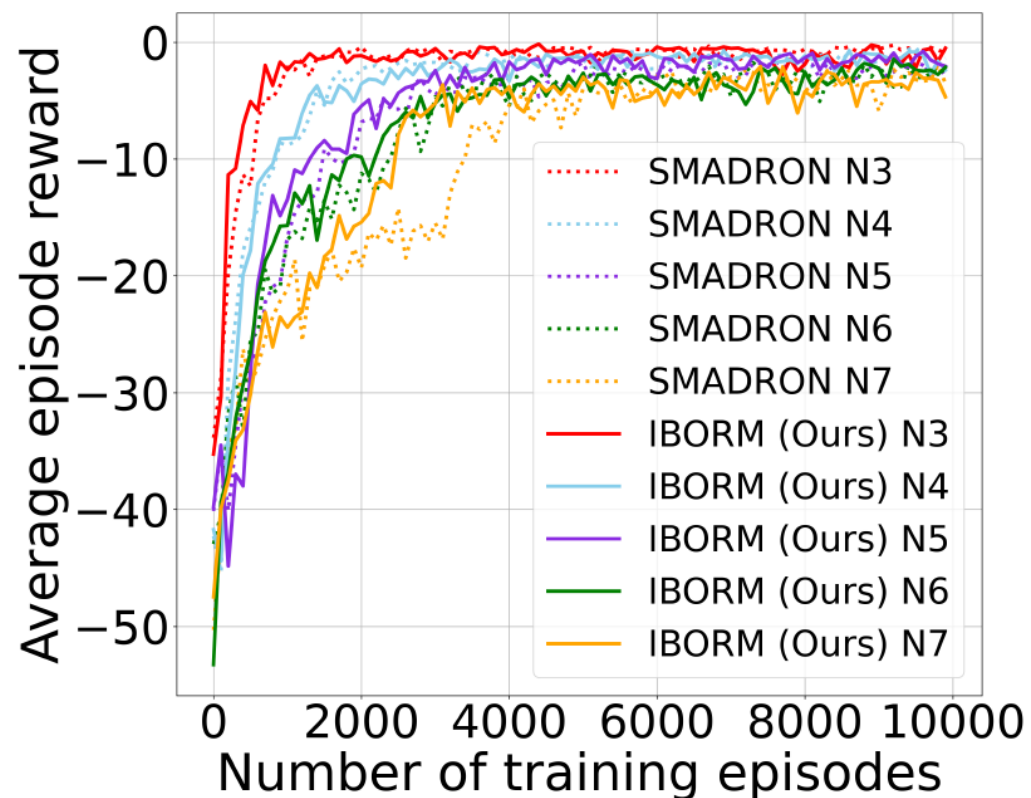
- Training performance

IBORM vs. SMADQN (implicit representation)



**IBORM learns faster than the other two methods**

IBORM vs. SMADRON (without information constraints)



## 3. EXPERIMENTS

- Testing performance
  - One thousand randomly generated tasks
  - Success: agents arrive at different targets without conflicts

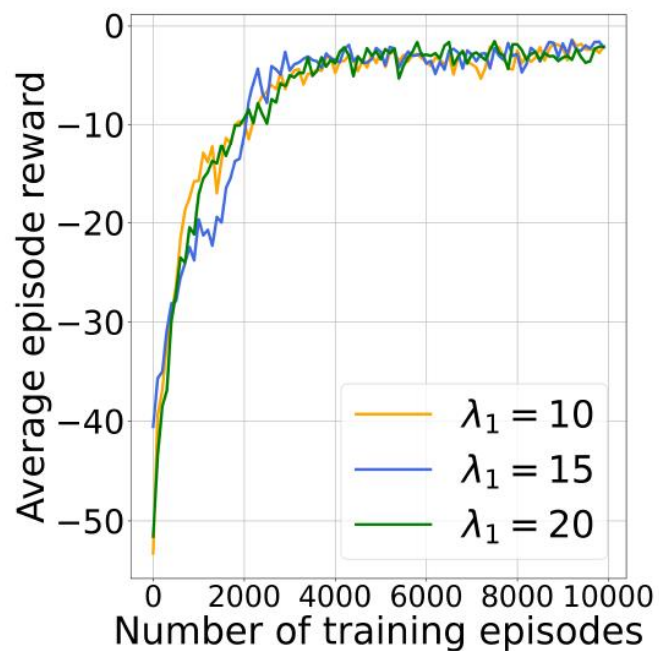
**Table 1:** Test results of different methods.

Method	Success rate				
	N=3	N=4	N=5	N=6	N=7
SMADQN	98.2%	97.8%	96.1%	91.2%	0.0%
SMADRON	98.9%	96.9%	92.9%	93.5%	82.5%
IBORM	<b>99.3%</b>	<b>98.1%</b>	<b>97.1%</b>	<b>93.5%</b>	<b>87.8%</b>

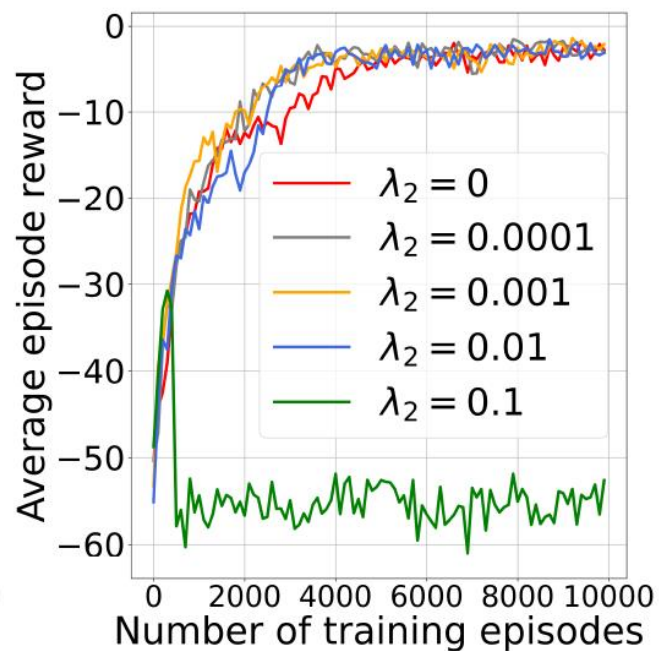
### 3. EXPERIMENTS

- Further study
  - Effect of different terms in IBORM's objective function

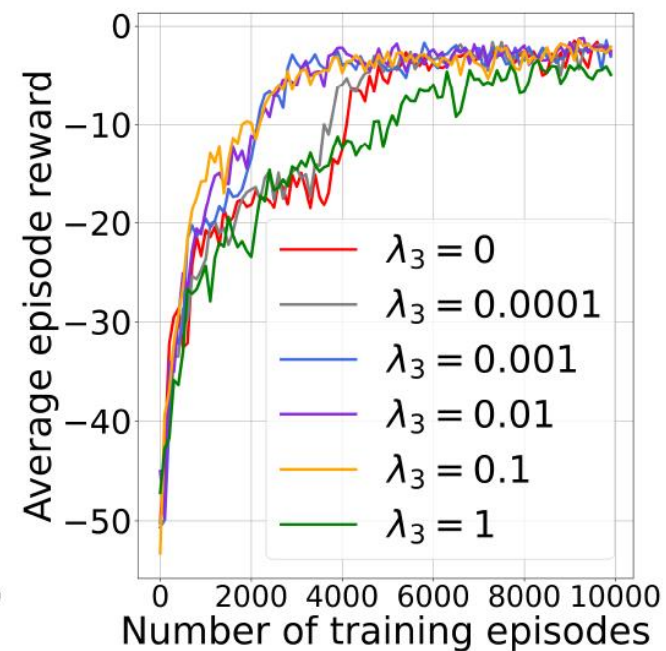
$$L_i(\alpha, \beta, \theta) = J_i^{CE}(\alpha, \beta) + \lambda_1 J_i^{DRL}(\alpha, \theta) + \lambda_2 I(\phi_{s-i,j}, ENC_i^\alpha(\phi_{s-i,j})) - \lambda_3 I(ENC_i^\alpha(\phi_{s-i,j}), a_{-i,j})$$



(a)



(b)



(c)



# Outline

1. Background
2. Method
3. Experiments
4. Conclusion

## 4. CONCLUSION

We propose IBORM to facilitate MADRL by learning representation regarding other agents' behaviors in an **explicit and more interpretable** manner compared with our previous work.

We leverage information bottleneck principle to push the representation to be **compact and relevant to both the task and other agents' behaviors**.

Experimental results demonstrate that IBORM **learns faster** and the resulting policies can **achieve higher success rate** consistently, as compared with implicit behavior representation learning (SMADQN) and explicit behavior representation learning (SMADRON) without considering information compression and utility.

# Thanks!

e-mail:

[jiny23@126.com](mailto:jiny23@126.com)