

Ghost-free HDR Imaging via Unrolling Low-Rank Matrix Completion

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High Dynamic Range Imaging

- Multi-exposure fusion algorithms merge multiple input low dynamic range (LDR) images to produce a single high dynamic range (HDR) image. However, they suffer from ghosting artifacts caused by camera and object motions.



Figure 1: Ghosting artifacts.

Low-rank Model

- We construct the observed irradiance matrix

$$\mathbf{D} = [\text{vec}(\mathbf{H}_1), \dots, \text{vec}(\mathbf{H}_n)] \quad (1)$$

where \mathbf{H}_i is the irradiance computed from the i -th warped LDR image.

- The irradiance matrix \mathbf{D} can be decomposed into two matrices,
 - \mathbf{X} : static background which has a rank-1 structure.
 - \mathbf{E} : moving objects in the foreground which resembles a sparse matrix
- Exploiting these properties, we employ the truncated nuclear norm [1] to formulate the fusion task as a rank minimization problem as

$$\begin{aligned} & \underset{\mathbf{X}, \mathbf{E}, \mathbf{S}}{\text{minimize}} \quad \|\mathbf{X}\|_{r=1} + \lambda \|\mathbf{E}\|_1 + f(\mathbf{X}) + g(\mathbf{E}) \\ & \text{subject to} \quad \mathbf{X} + \mathbf{E} + \mathbf{S} = \mathcal{P}_\Omega(\mathbf{D}), \|\mathcal{P}_\Omega(\mathbf{S})\|_F \leq \delta, \end{aligned} \quad (2)$$

where λ is the trade-off parameter, $f(\cdot)$ and $g(\cdot)$ are adaptive priors.

The Network

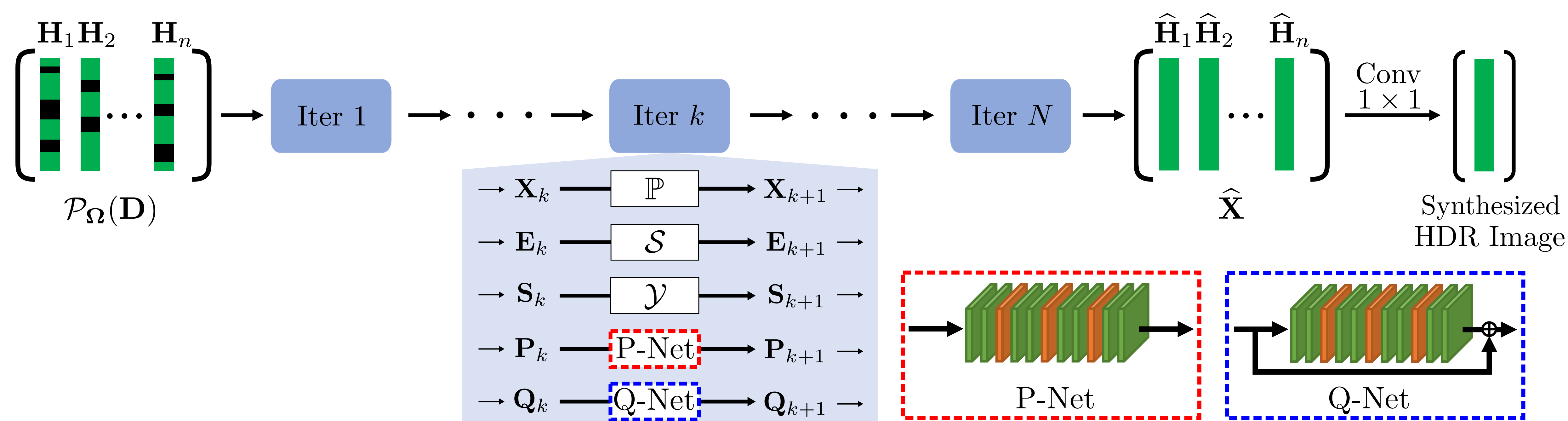


Figure 2: The network takes \mathbf{D} in (1) as input. For initialization, $\mathbf{X}_1 = \mathcal{P}_\Omega(\mathbf{D})$ and others are zero matrices. Operations in each iteration correspond to solutions in (4) and (5). The green and orange blocks in P-Net and Q-Net indicate the convolutional layers and ReLU layers, respectively. The network process image channels separately and the weights are shared.

Solutions

- Variable separation for (2)

$$\begin{aligned} & \underset{\mathbf{X}, \mathbf{E}, \mathbf{S}, \mathbf{P}, \mathbf{Q}}{\text{minimize}} \quad \|\mathbf{X}\|_{r=1} + \lambda \|\mathbf{E}\|_1 + f(\mathbf{P}) + g(\mathbf{Q}) \\ & \text{subject to} \quad \mathbf{P} = \mathbf{X}, \mathbf{Q} = \mathbf{E}, \\ & \quad \quad \quad \mathbf{X} + \mathbf{E} + \mathbf{S} = \mathcal{P}_\Omega(\mathbf{D}), \|\mathcal{P}_\Omega(\mathbf{S})\|_F \leq \delta. \end{aligned} \quad (3)$$

- Closed-form solutions by an iterative technique

$$\begin{aligned} \mathbf{X}_{k+1} &= \arg \min_{\mathbf{X}} \mathcal{L}(\mathbf{X}, \mathbf{E}_k, \mathbf{S}_k, \mathbf{P}_k, \mathbf{Q}_k, \Lambda_k, \Gamma_k, \Phi_k) \\ \mathbf{E}_{k+1} &= \arg \min_{\mathbf{E}} \mathcal{L}(\mathbf{X}_{k+1}, \mathbf{E}, \mathbf{S}_k, \mathbf{P}_k, \mathbf{Q}_k, \Lambda_k, \Gamma_k, \Phi_k) \\ \mathbf{S}_{k+1} &= \arg \min_{\mathbf{S}} \mathcal{L}(\mathbf{X}_{k+1}, \mathbf{E}_{k+1}, \mathbf{S}, \mathbf{P}_k, \mathbf{Q}_k, \Lambda_k, \Gamma_k, \Phi_k) \end{aligned} \quad (4)$$

where \mathcal{L} is the augmented Lagrangian function derived from (3).

- We learn prior information from the data via CNNs

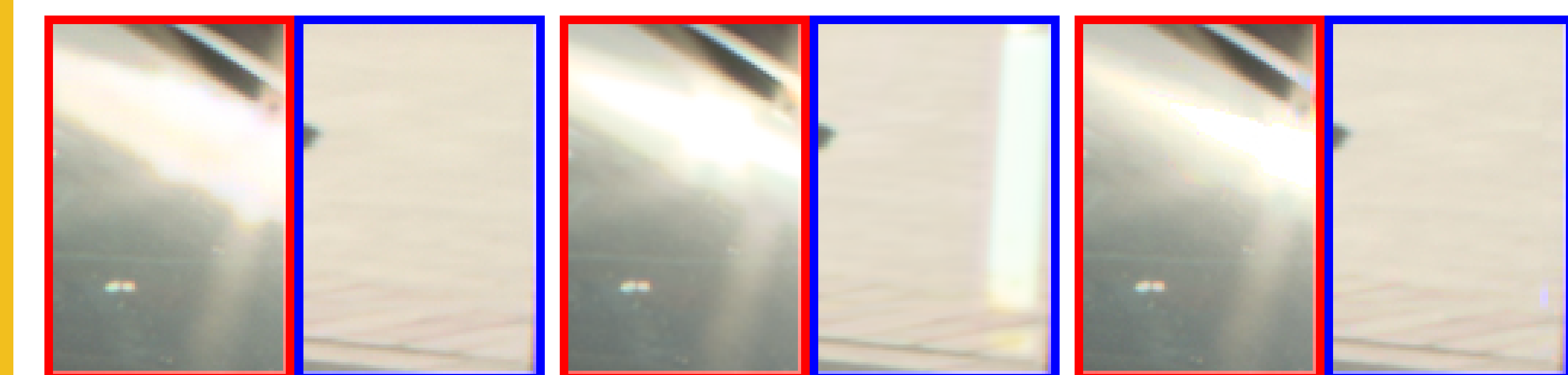
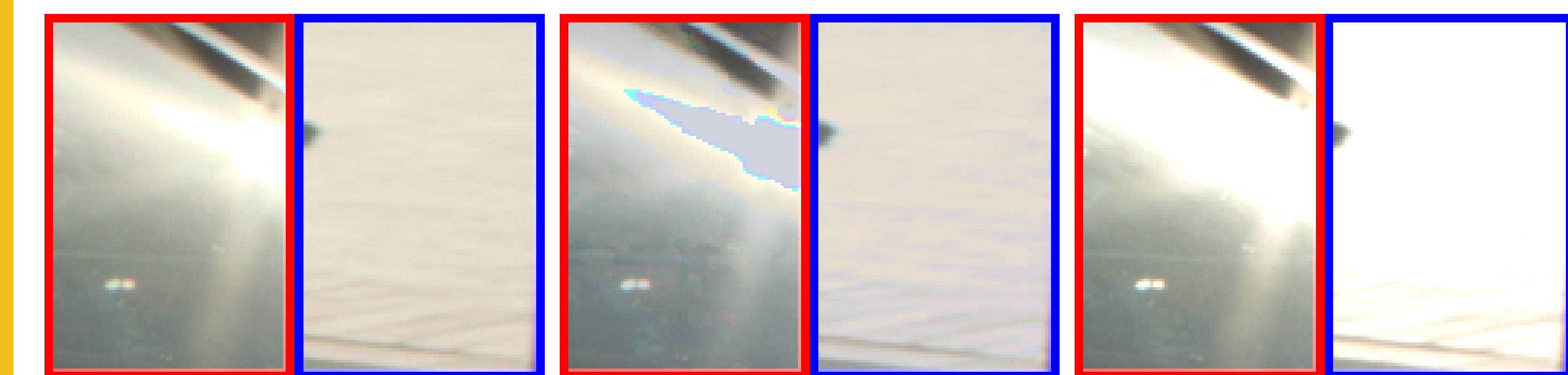
$$\begin{aligned} \mathbf{P}_{k+1} &= \arg \min_{\mathbf{P}} \mathcal{L}(\mathbf{X}_{k+1}, \mathbf{E}_{k+1}, \mathbf{S}_{k+1}, \mathbf{P}, \mathbf{Q}_k, \Lambda_k, \Gamma_k, \Phi_k) \\ &= \text{P-Net}_k(\mathbf{X}_{k+1} + \alpha_k^{-1} \Gamma_k), \\ \mathbf{Q}_{k+1} &= \arg \min_{\mathbf{Q}} \mathcal{L}(\mathbf{X}_{k+1}, \mathbf{E}_{k+1}, \mathbf{S}_{k+1}, \mathbf{P}_{k+1}, \mathbf{Q}, \Lambda_k, \Gamma_k, \Phi_k) \\ &= \text{Q-Net}_k(\mathbf{E}_{k+1} + \beta_k^{-1} \Phi_k) \end{aligned} \quad (5)$$

- The HDR image is computed by weighted average of columns in $\hat{\mathbf{X}}$

$$\mathbf{R} = \frac{1}{n} \sum_{i=1}^n \omega_i \hat{\mathbf{X}}_i$$

Experimental Results

- Conventional algorithms produce unfaithful textures since end-to-end learning algorithms infer them from learned features, which may be different from those in the ground-truth.
- In contrast, the proposed algorithm faithfully synthesizes HDR images without texture losses and color artifacts by strictly constraining low-rank priors with learned regularizers.



(a) Ground-truth (b) TNNM-ALM [1] (c) Kalantari et al. [2]

(d) Wu et al. [3] (e) Yan et al. [4] (f) The proposed algorithm

Figure 3: Comparison of the HDR synthesis results.

References

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