

# Efficient Near Optimal Joint Modulation Classification and Detection for MU-MIMO Systems

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## Introduction

A joint maximum likelihood (ML) modulation classification (MC) of the co-scheduled user and data detection receiver is developed

### Reference MU-MIMO Detection Schemes:

- Interference Ignoring
- Interference Rejection Combining (IRC) and MMSE  
Only make use of the channel estimate of the interferer
- Interference Assuming  
Say 16-QAM for example
- Interference Estimation  
Add a MC routine  
Feed estimate to a regular Interference Aware (IA) receiver

### Modulation Classification Schemes:

- Likelihood-based
- Feature-based

## System Model

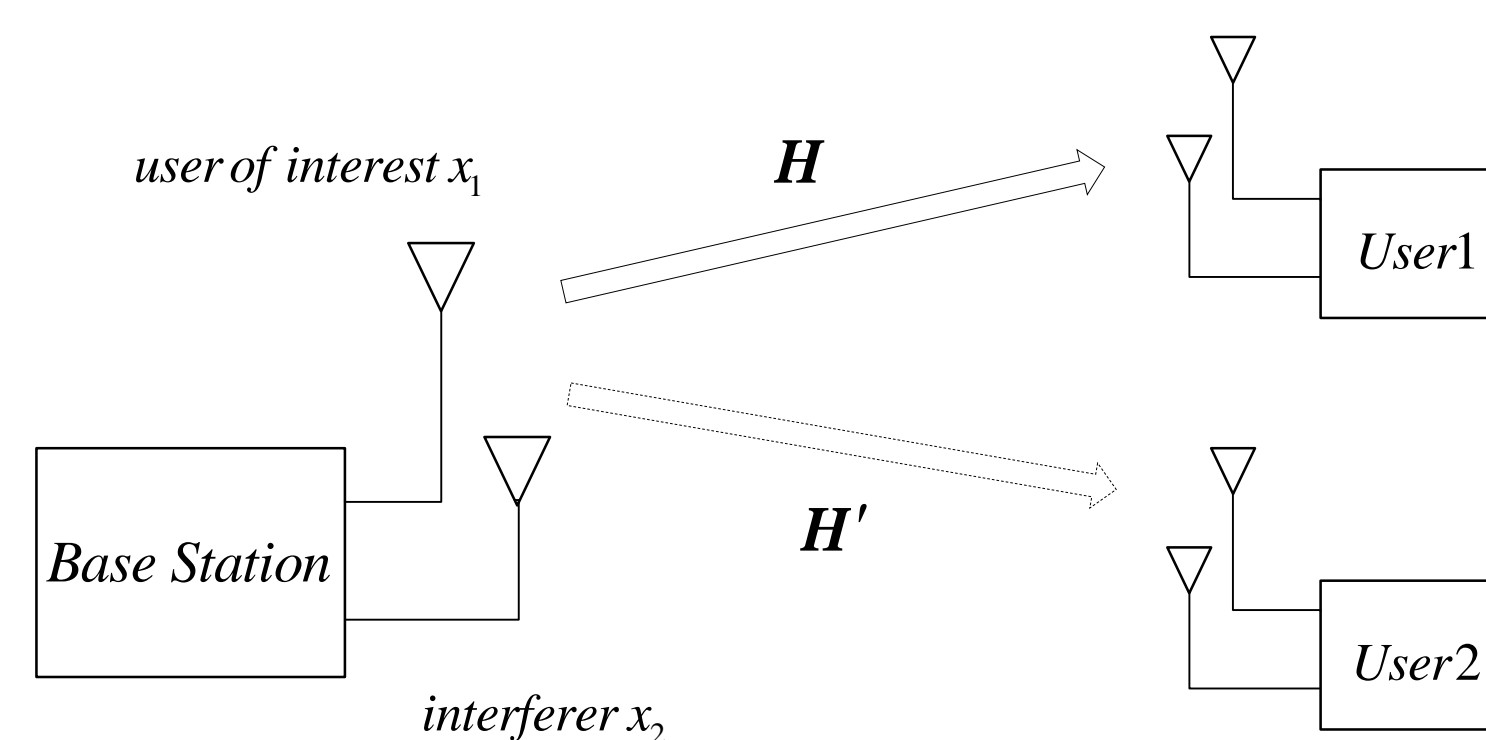
$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n}$$

- $\mathbf{H} = N_r \times N_t$  channel matrix
- $\mathbf{x}$  transmitted QAM symbols
- $\mathbf{n}$  complex additive white Gaussian noise with zero mean and variance  $\sigma^2 = \frac{N_t}{\text{SNR}}$

We consider the case  $N_r = N_t = 2$   $\mathbf{y} = \mathbf{h}_1 x_1 + \mathbf{h}_2 x_2 + \mathbf{n}$

$\bar{\Lambda}$  is the constellation of user of interest

$\Lambda_0$  is  $\emptyset$  (no interference) -  $\Lambda_1$  is QPSK -  $\Lambda_2$  is 16-QAM -  $\Lambda_3$  is 64-QAM



## Proposed Joint MC and Detection

Bayesian formulation: 4-ary hypothesis testing

$$\begin{cases} \theta_0: \mathbf{y} \sim P(\mathbf{y}; x_1 \in \bar{\Lambda}, x_2 \in \Lambda_0) \\ \theta_1: \mathbf{y} \sim P(\mathbf{y}; x_1 \in \bar{\Lambda}, x_2 \in \Lambda_1) \\ \theta_2: \mathbf{y} \sim P(\mathbf{y}; x_1 \in \bar{\Lambda}, x_2 \in \Lambda_2) \\ \theta_3: \mathbf{y} \sim P(\mathbf{y}; x_1 \in \bar{\Lambda}, x_2 \in \Lambda_3) \end{cases}$$

$$P(\mathbf{y}; \Lambda_n) = \sum_{x_1 \in \bar{\Lambda}, x_2 \in \Lambda_n} P(\mathbf{y}|x_1, x_2)P(x_1, x_2)$$

$$\hat{n}_{\text{Log-MAP}} = \underset{n=0,1,2,3}{\operatorname{argmax}} \left( \log \frac{1}{|\Lambda_n|} + \sum_{x_1 \in \bar{\Lambda}, x_2 \in \Lambda_n} \exp \left( -\frac{1}{\sigma^2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 \right) \right)$$

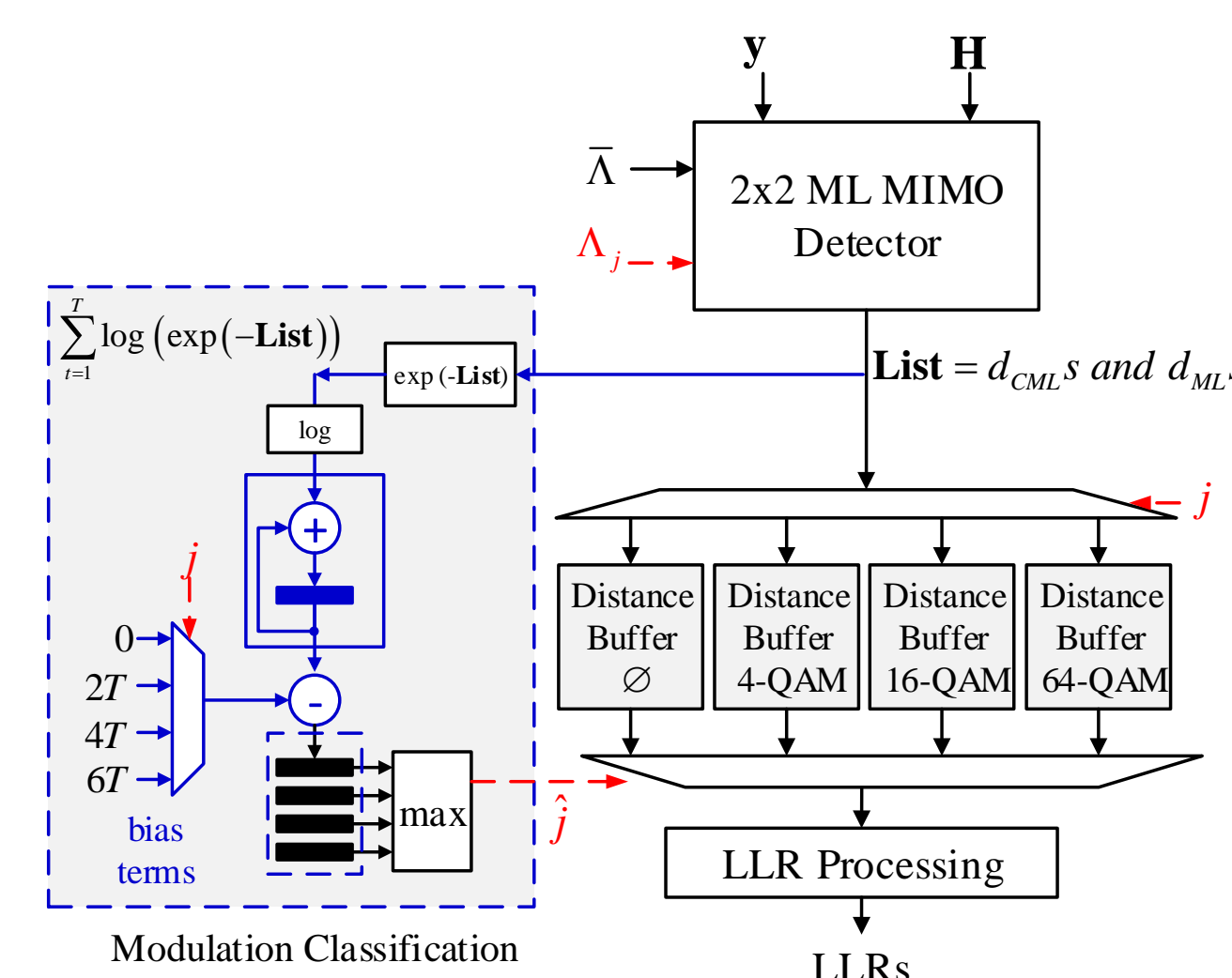
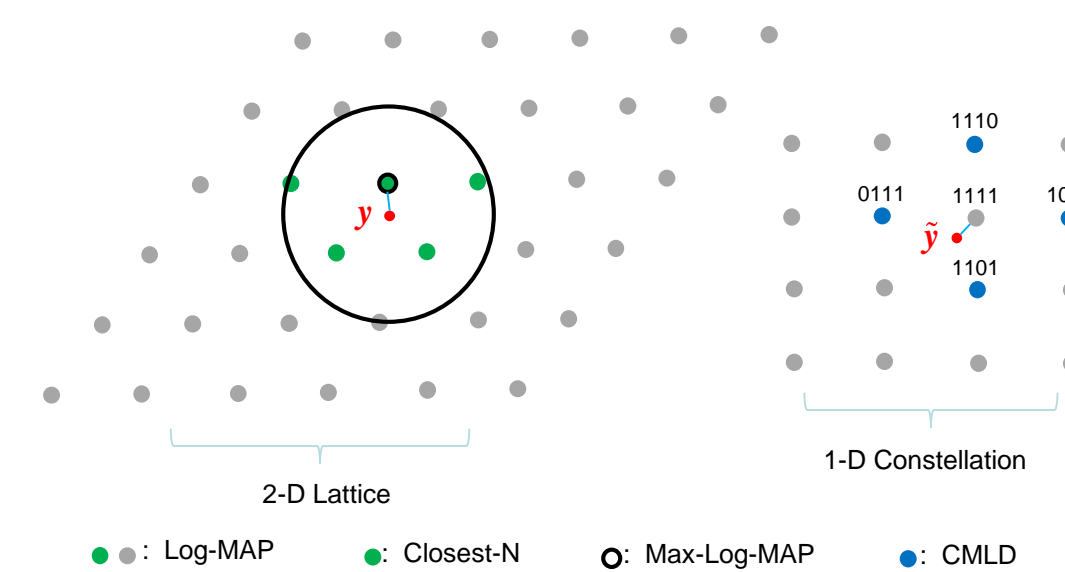
$$d_{\text{ML},n} = \min_{x_1 \in \bar{\Lambda}, x_2 \in \Lambda_n} \varphi(\mathbf{x}) \quad \varphi(\mathbf{x}) = \frac{1}{\sigma^2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2$$

$$\hat{n}_{\text{Max-Log-MAP}} = \underset{n=0,1,2,3}{\operatorname{argmax}} \left( \log \frac{1}{|\Lambda_n|} - d_{\text{ML},n} \right)$$

In general, for a group of distance metrics  $S$ , and after  $T$  observations:

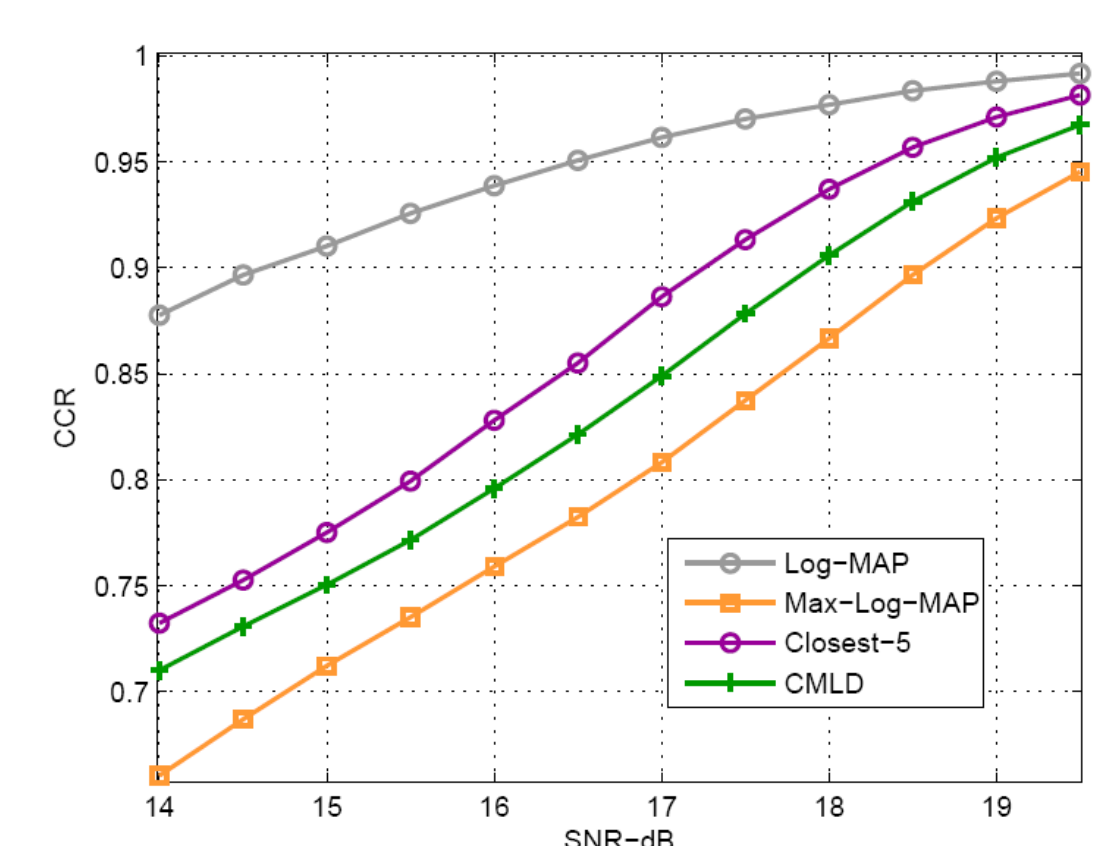
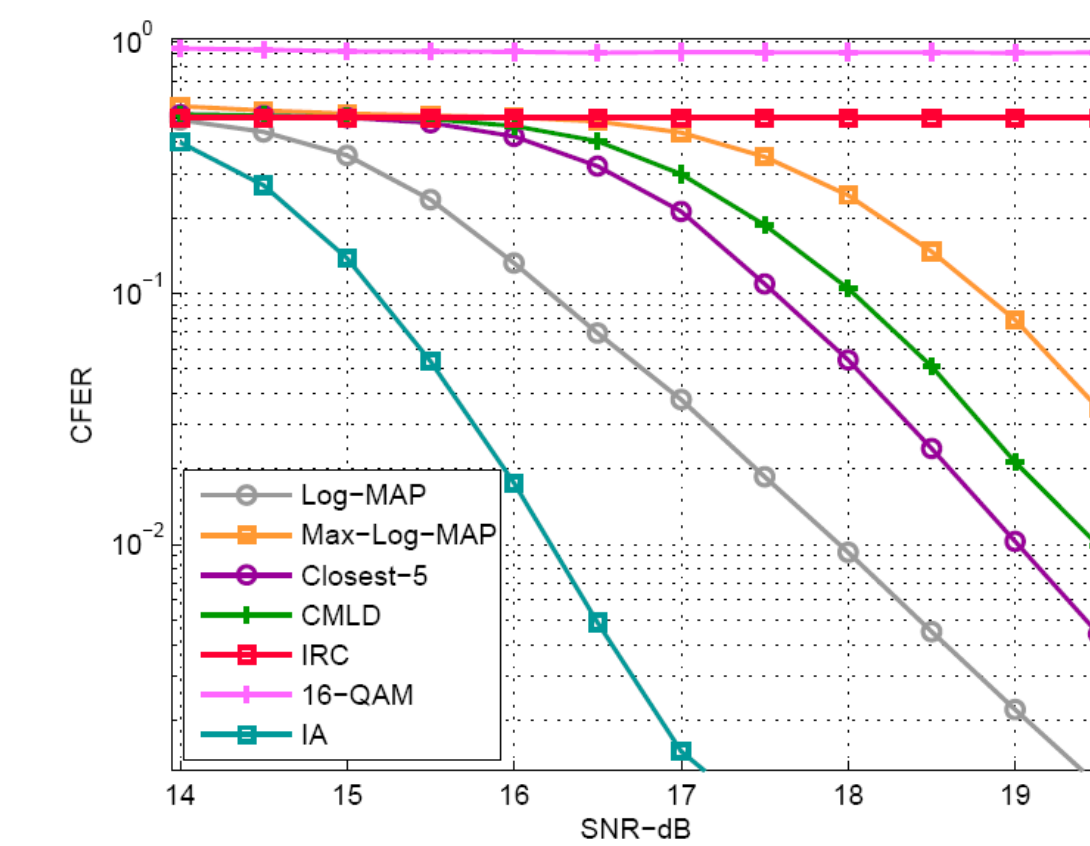
$$\hat{n} = \underset{n=0,1,2,3}{\operatorname{argmax}} \sum_{t=1}^T \left( \log \frac{1}{|\Lambda_n|} + \sum_{\mathbf{x} \in S} \exp \left( -\frac{1}{\sigma^2} \|\mathbf{y} - \mathbf{H}\mathbf{x}\|^2 \right) \right)$$

- Closest\_N:  $S$  consists of points corresponding to smallest N distance metrics.
- CMLD:  $S$  consists of points corresponding to ML and counter-ML distances.



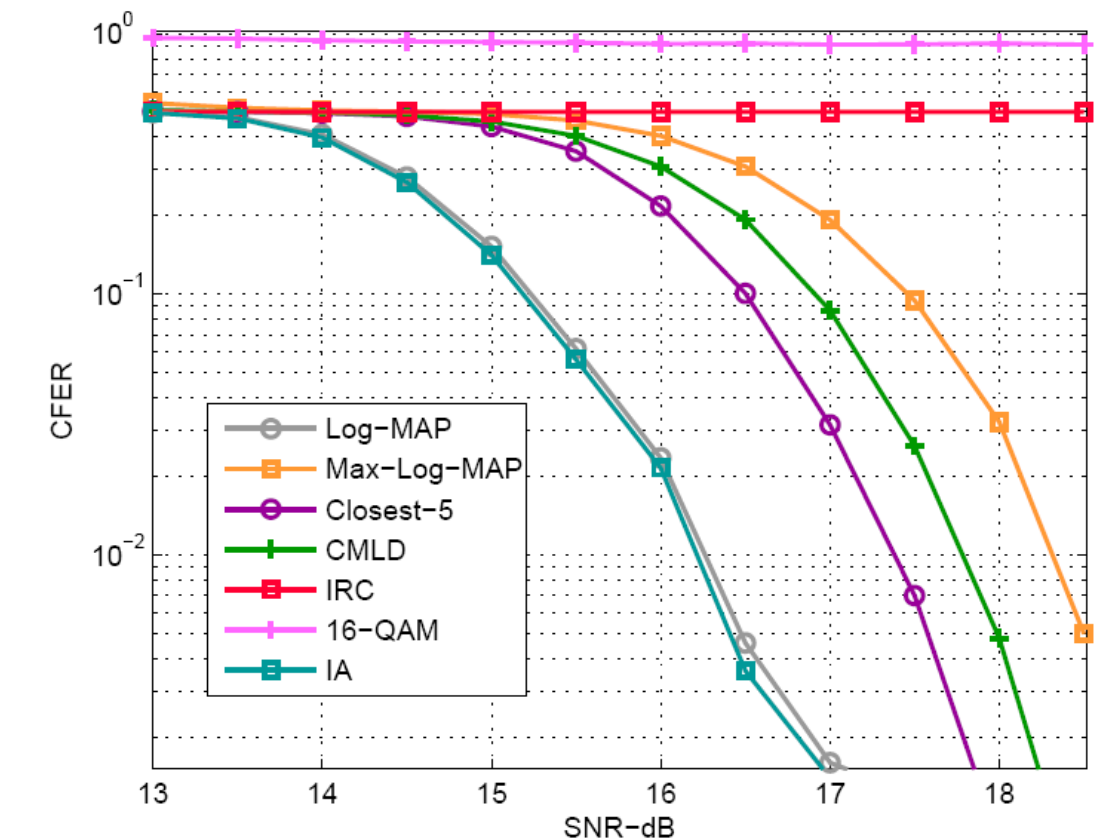
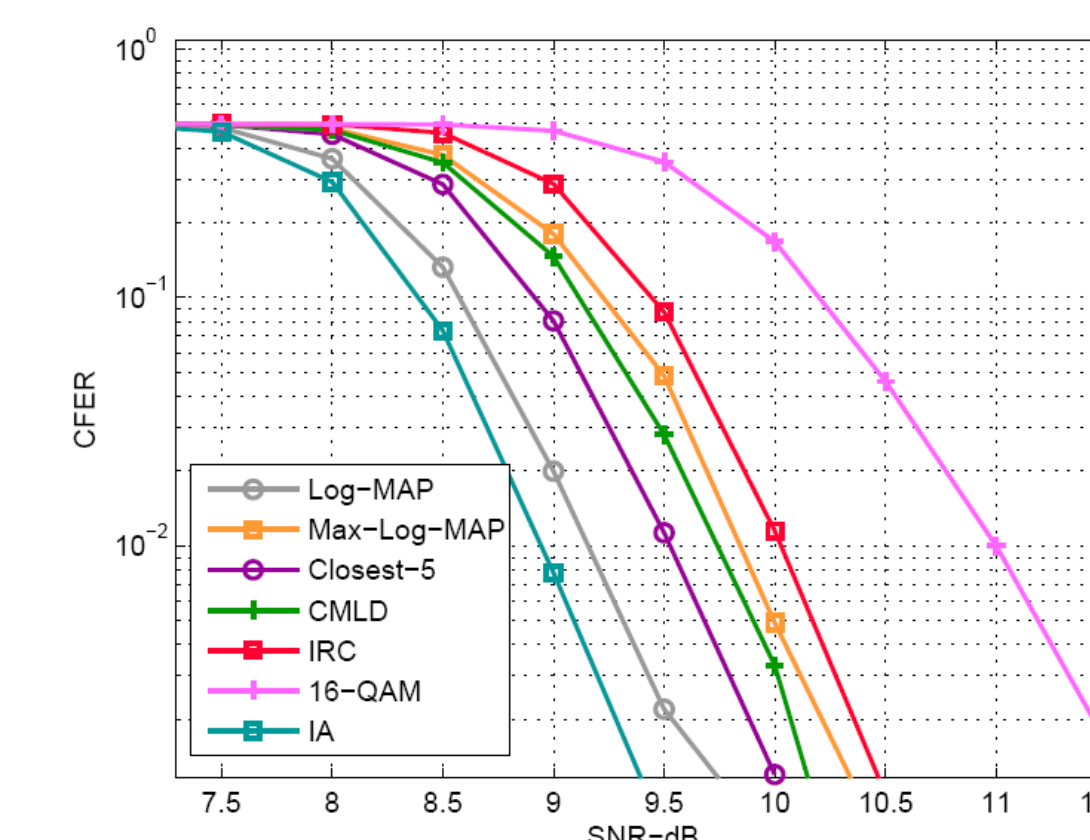
## Results

- Correct Classification Ratio (CCR) of classifiers
- Coded frame error rate (CFER) of detectors



CFER Performance - T = 12 - Correlated Channels

CCR Performance - T = 12 - Correlated Channels



CFER Performance - T = 12 - Uncorrelated Channels

CFER Performance - T = 52 - Correlated Channels

Approach	S	L	E	D
Log-MAP	All	T	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$
Closest_N	Closest N	T	$T \times 4 \times N$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$
CMLD	ML+CMLs of $\mathbf{x}$	T	$T \left[ 4 \times (K_1 + 1) + (K_2^{(0)} + K_2^{(1)} + K_2^{(2)} + K_2^{(3)} + 4) \right]$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$
CMLD1	ML+CMLs of $x_1$	T	$4 \times T \times (K_1 + 1)$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$
CMLD2	ML+CMLs of $x_2$	T	$T (K_2^{(0)} + K_2^{(1)} + K_2^{(2)} + K_2^{(3)} + 4)$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$
Max-Log-MAP	ML	T	$4 \times T$	$T \times  \bar{\Lambda}  \times ( \Lambda_0  +  \Lambda_1  +  \Lambda_2  +  \Lambda_3 )$

## In the Context of WiFi

- From 52 to 234 data tones
- large number of OFDM symbols ( $L$ )
- Constant interferer over T tones and L symbols
- MC executes on one OFDM symbol in the frame
- $\frac{3}{L}$  % increase in distance computations
- $L$  takes values from 8 to more than 1024