



# PARTIAL LEAST SQUARES BASED RANKER FOR FAST AND ACCURATE AGE ESTIMATION

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## 1 INTRODUCTION

- Facial age estimation
- Useful for friendly and secure human robot / computer interactions, age-based access control, family photo management, etc.
- Challenging due to complex dynamics in aging process.

## MOTIVATION

- PLS has many excellent characteristics.
- Rankers show favorable performance by exploiting the ordinal nature of ages.
- Transform the advanced multivariate data analysis (MVA) tool PLS, into a ranker to boost the performance in terms of accuracy, speed and robustness, on the age estimation problem.

## Advantages of PLS based ranker (PLS-Ranker)

- All binary classifiers are jointly learned.
- The proposed adaptive threshold learning strategy makes each basic binary classifier of PLS-Ranker robust to the imbalance problem of its positive and negative training data. Thus boosts ranking accuracy of PLS-Ranker.
- PLS-Ranker simultaneously reduces feature dimension and ranks in high speed even for high-dimensional features.

## PARTIAL LEAST SQUARES BASED RANKER

- Feature matrix  $X$  ( $n \times N$ ): feature vectors of  $n$  training samples.
- Column vector  $y$  ( $n \times 1$ ): scalar age values of  $n$  training samples.
- Suppose the age range is  $1 \sim M_a$ .

### 1. Encoding age for jointly learning all associated binary classifiers

- Encode each scalar age  $y_i$  ( $i = 1, 2, \dots, n$ ) into a  $1 \times (M_a - 1)$  binary row vector  $A(i, :)$ .
- Form an  $n \times (M_a - 1)$  indicator matrix  $A$ .
- $A_{i,j}$  indicates whether the face  $i$  is older than  $j$  years.

$$A_{i,j} = \begin{cases} 1, & \text{if } j < y_i \\ 0, & \text{if } j \geq y_i \end{cases}$$

### 2. Train a linear PLS model

- Use the feature matrix  $X$  and indicator matrix  $A$  to train a linear PLS model.
- Get the regression coefficient matrix  $B_{pls}$ .

### 3. Adaptive threshold learning

#### Imbalance problem

- Reduce ranking to associated binary classifications: Is the face older than  $j$  years?  $j = 1, 2, \dots, M_a - 1$
- Under the reduction framework, the key to improve ordinal ranking is to improve binary classifications.
- However, the positive and negative training samples for each of the binary classifiers can be highly unbalanced.
- The unbalanced positive and negative training samples may shift the optimal thresholds away from 0.5.

#### Learn thresholds from the unbalanced training data

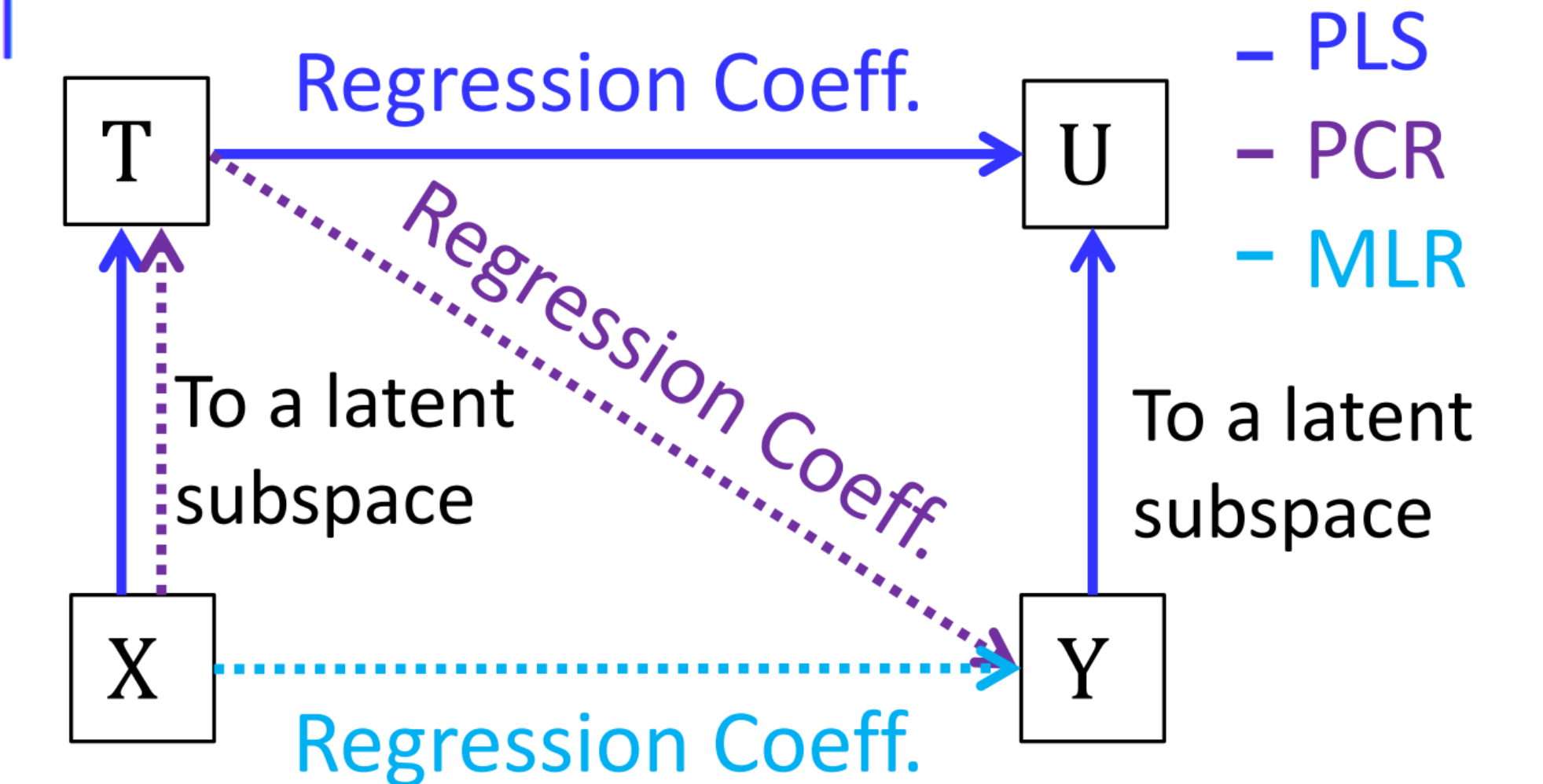
- Apply the trained linear PLS model back to the feature matrix of training set  $X$
- Get a prediction of indicator matrix  $\hat{A}$ :

$$\hat{A} = XB_{pls}$$

- $\hat{A}$  is a real-valued matrix.
- Thresholds are searched in a small range  $S$  around 0.5.
- Determined by the criterion of minimizing the error rate on the training set.



(a) Flow chart of age estimation using PLS-Ranker



(b) MLR, PCR and PLS coefficients calculation

For the  $j$ -th ( $j = 1, 2, \dots, M_a - 1$ ) binary classifier:

$$thr_j = \arg \max_{b \in S} \sum_{i=1}^n f_m(A_{i,j}) \times f_m([\hat{A}_{i,j} \geq b])$$

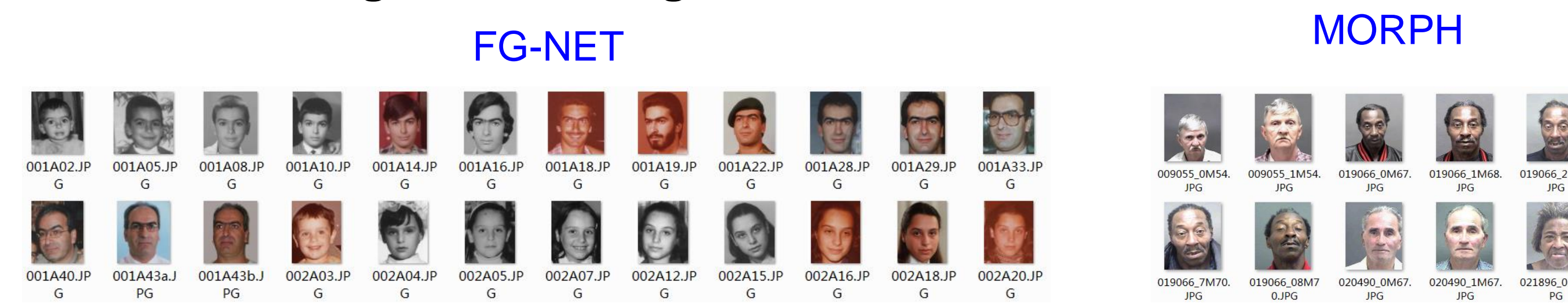
#### Test process

- $x_t$  ( $1 \times N$ ) is mapped to an indicator vector  $\hat{a}_t$  using the trained linear PLS model:  $\hat{a}_t = x_t B_{pls}$
- Threshold each element of  $\hat{a}_t$  into a binary indicator:  $\hat{a}_t(1, j) := [\hat{a}_t(1, j) \geq thr_j] \quad j = 1, 2, \dots, M_a - 1$
- The rank (age) is obtained by summarizing elements in  $\hat{a}_t$ :  $\hat{r}_t = \sum_{j=1}^{M_a-1} \hat{a}_t(1, j) + 1$

## EXPERIMENTS AND DISCUSSIONS

### Datasets

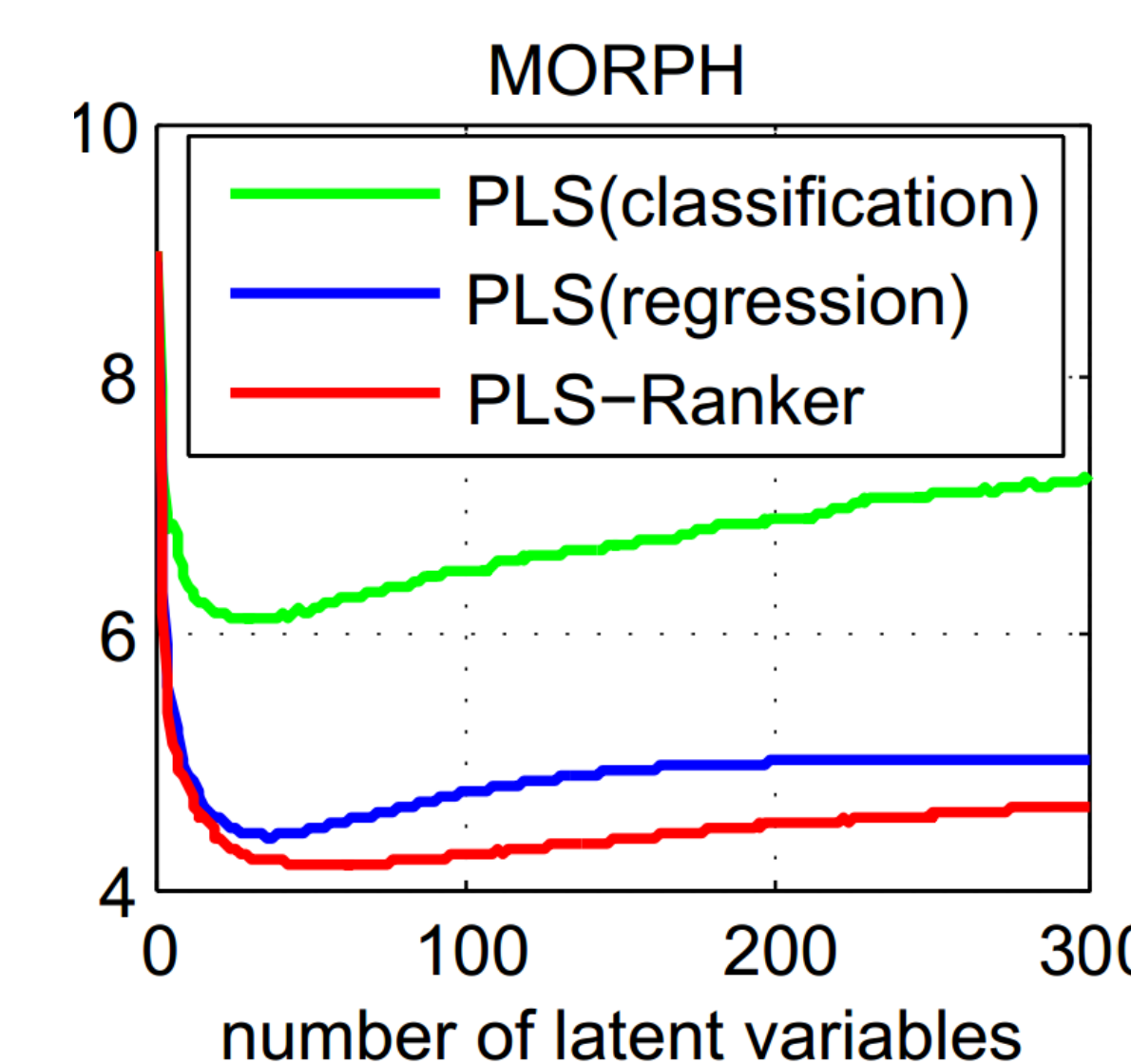
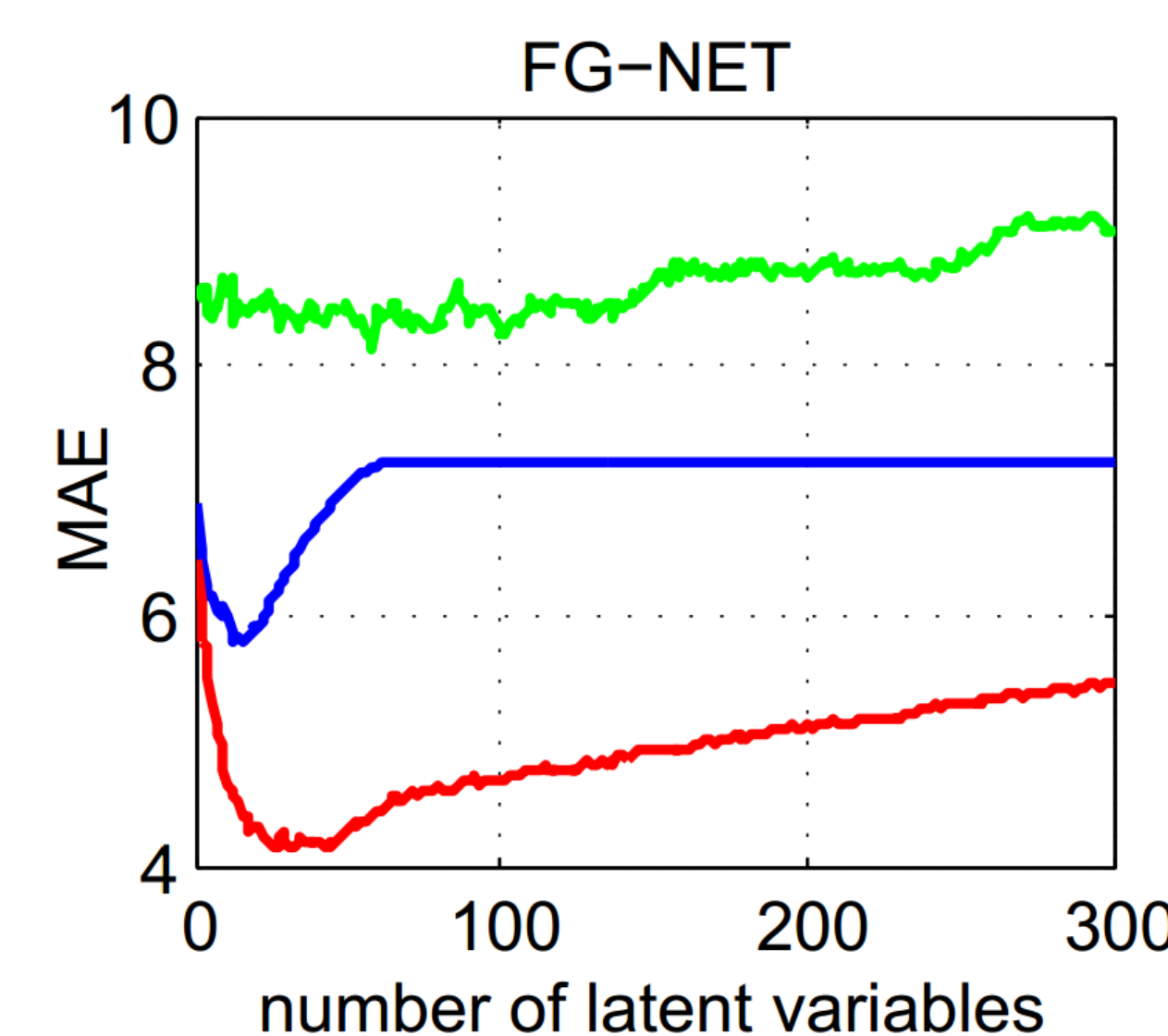
- FG-NET. Leave one person out.
- MORPH. Setting 1 and Setting 2.



### PLS-Ranker vs. PLS

- PLS can be used for classification and metric regression.
- Compare PLS-Ranker with the two usages of PLS on FG-NET and MORPH (Setting 1).

Method	MAE/year (num. of latent var.)	
	FGNET	MORPH
PLS (classification)	8.14 (58)	6.10 (33)
PLS (regression)	5.78 (17)	4.40 (37)
<b>PLS-Ranker</b>	<b>4.14 (45)</b>	<b>4.17 (49)</b>



## Comparison with the state-of-the-art methods on FG-NET and MORPH (Setting 2)

### 1. MAE

Method	MAE/year	
	FGNET	MORPH
MTWGP [2]	4.83	6.28
PLO [14]	4.82	-
AAM+CA-SVR [15]	4.67	5.88
Feat. combine + select [22]	4.49	-
AAM+CS-OHRank [4]	4.48	6.07
Regularized CA-SVR [17]	4.37	-
Deep Feature+SVR [3]	4.26	4.77
<b>AAM+PLS-Ranker</b>	<b>4.14</b>	<b>5.38</b>
<b>BIF+PLS-Ranker</b>	-	<b>3.77</b>

### 2. Training time

Tested on an Intel(R) Core i5-3470 (3.2GHz), 8G RAM PC.

Method	Training time/min	
	FGNET	MORPH
OHRank [4]	$1.30 \times 10^4$	$3.02 \times 10^4$
SVR [23]	$2.69 \times 10^0$	$2.08 \times 10^1$
CA-SVR [15]	$8.91 \times 10^{-1}$	$6.10 \times 10^0$
<b>AAM+PLS-Ranker</b>	<b><math>7.20 \times 10^{-3}</math>(0.43s)</b>	<b><math>2.25 \times 10^{-2}</math>(1.35s)</b>
<b>BIF+PLS-Ranker</b>	-	<b><math>1.25 \times 10^{-1}</math>(7.51s)</b>

- Linear PLS is adopted.
- Simultaneous dimensionality reduction and ranking.
- Usually  $p \ll N$  holds, and more latent variables (big  $p$ ) are not necessarily in practice.

### Robustness to race and gender variations

Results on the multi-source cross-race-and-gender age estimation problem

Train	Test	MAE/year (num. of latent var.)	
		CpDA [20]	PLS-Ranker
BF+WF	BM	6.47	<b>4.55</b> (27)
BF+WF	WM	5.70	<b>3.87</b> (49)
WM+BM	WF	6.58	<b>5.10</b> (80)
WM+BM	BF	6.40	<b>5.49</b> (67)
BF+BM	WF	6.59	<b>5.24</b> (88)
BF+BM	WM	5.23	<b>3.85</b> (63)
WF+WM	BF	6.32	<b>5.65</b> (39)
WF+WM	BM	5.96	<b>4.49</b> (31)
Average		5.99	<b>4.48 (25.31%)</b>

Please see our paper for references and other details.