



# Multichannel Identification of Room Acoustic Systems with Adaptive Filters based on Orthonormal Basis Functions

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Adaptive Digital Filters for Room Acoustics Modeling

Multichannel Identification Algorithm

Simulation Results

Conclusions



- ▶ Adaptive Digital Filters for Room Acoustics Modeling

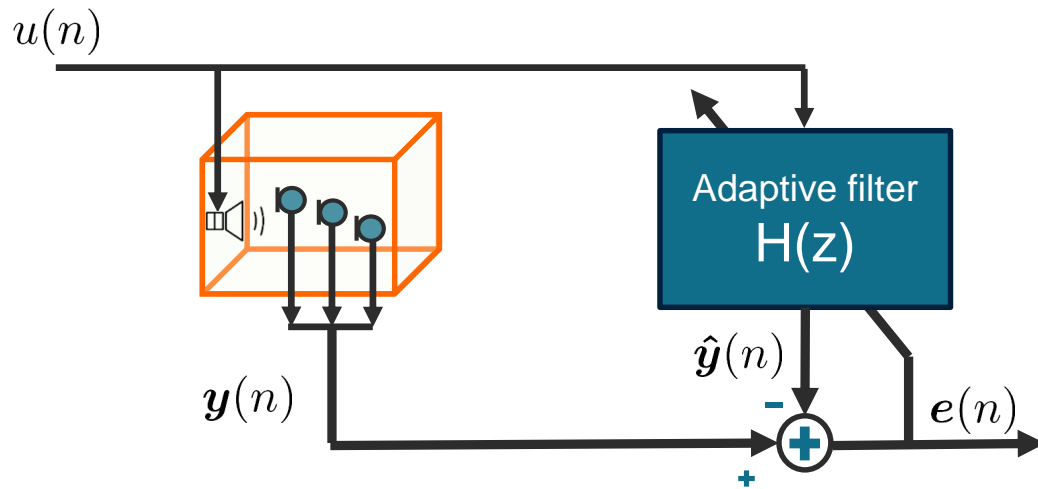
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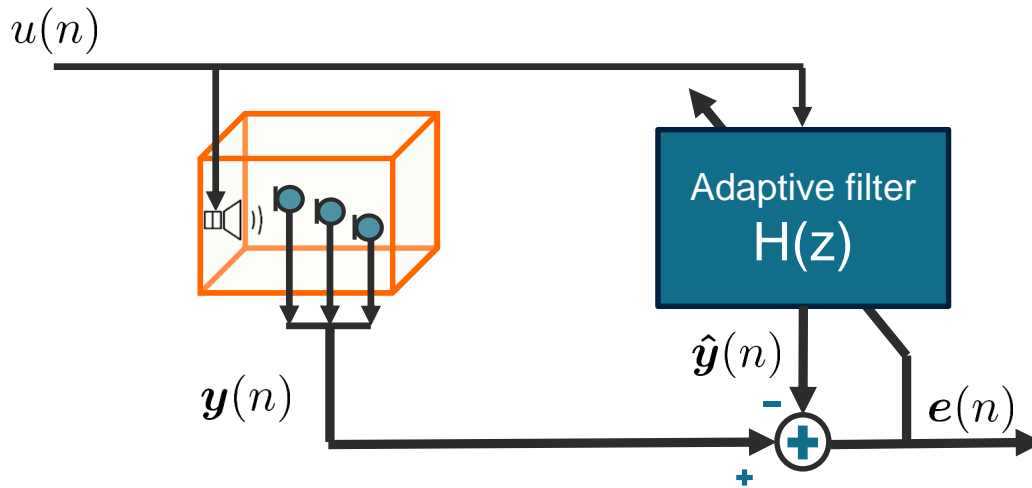
# Adaptive Filters for Room Acoustics



- Modeling of RTFs
- Filter Adaptation
  - Track variations of RTFs
- SIMO system

$$\underset{a,b}{\text{minimize}} e^2(n) = [\mathbf{y}(n) - \hat{\mathbf{y}}(n)]^2$$

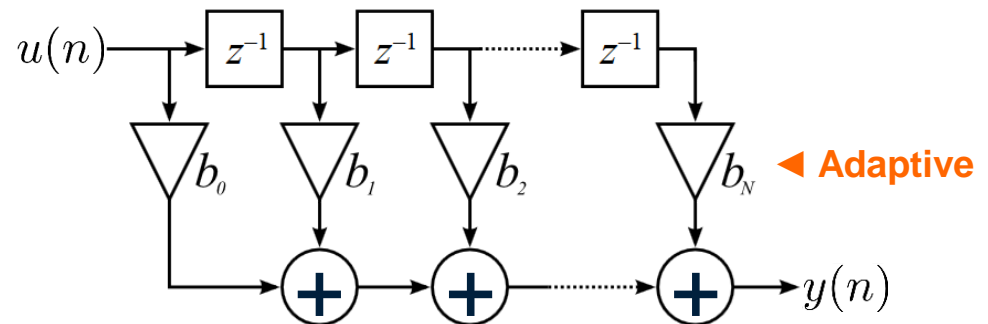
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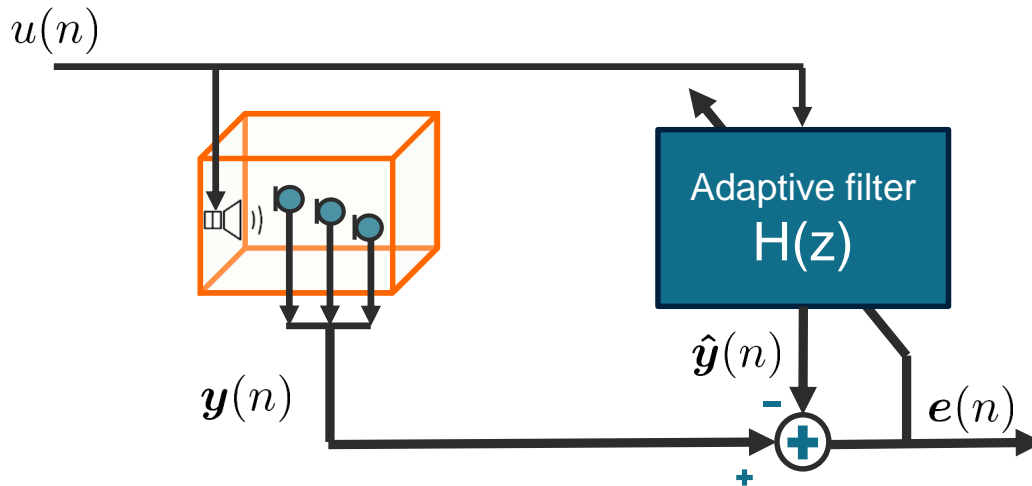
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  - Simple
  - Global convergent adaptation



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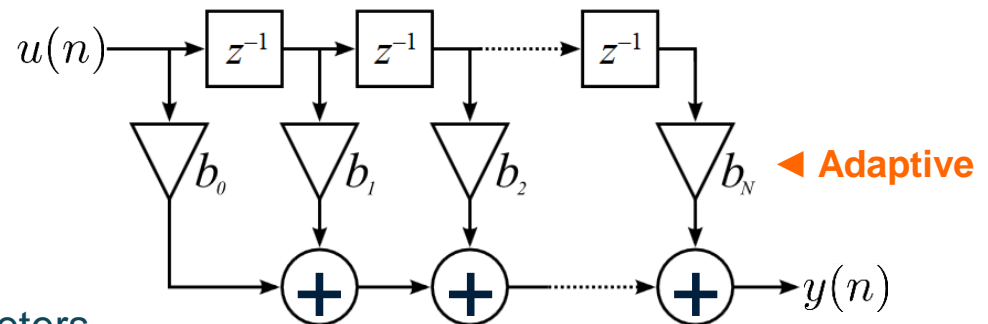
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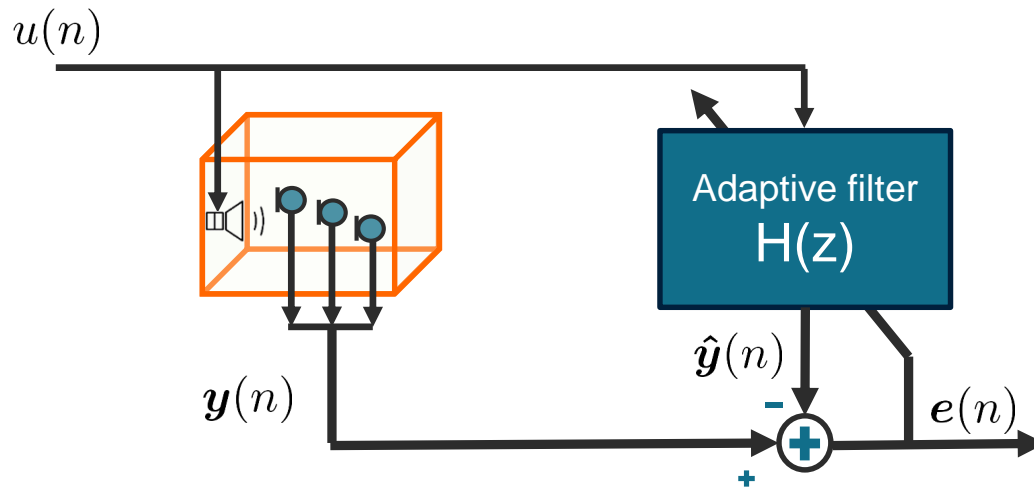
- Simple
- Global convergent adaptation

Problems:

- Large number of adaptive parameters
  - Excessive computational burden
  - Excess MSE (misadjustment)



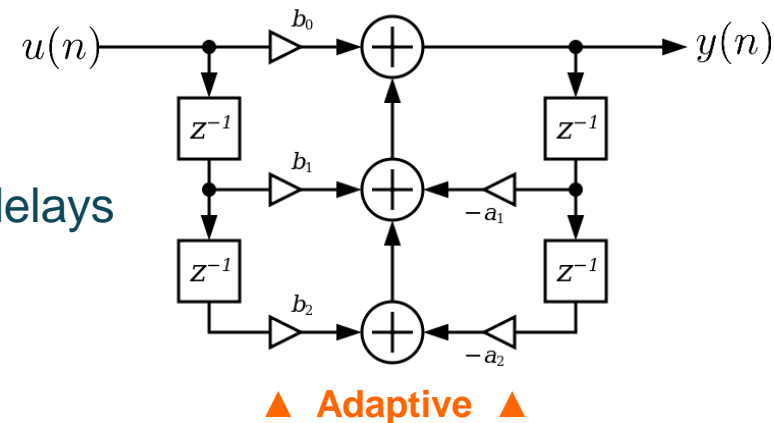
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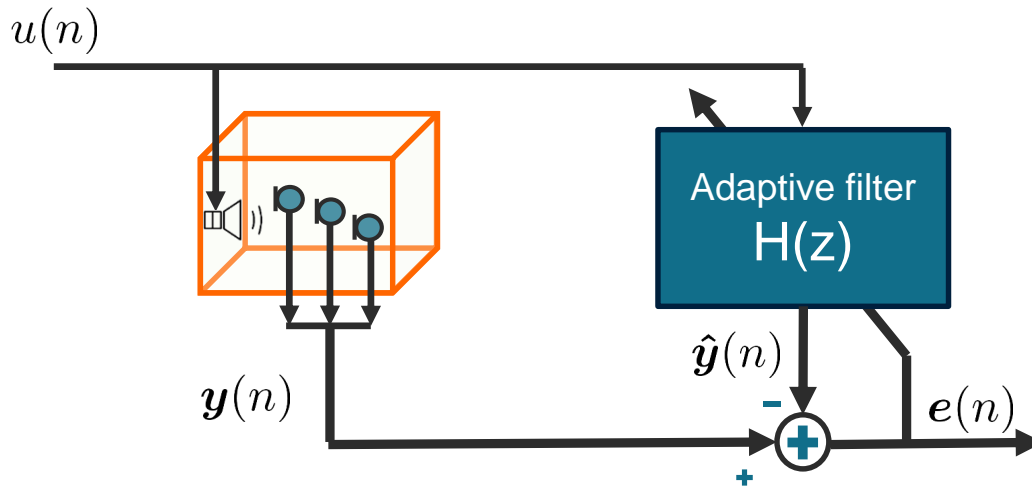
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  - Reduced number of parameters
  - Can describe both resonances and time-delays



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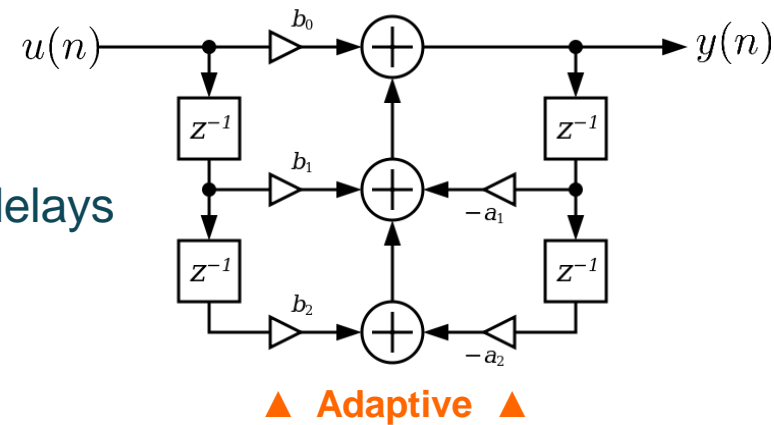
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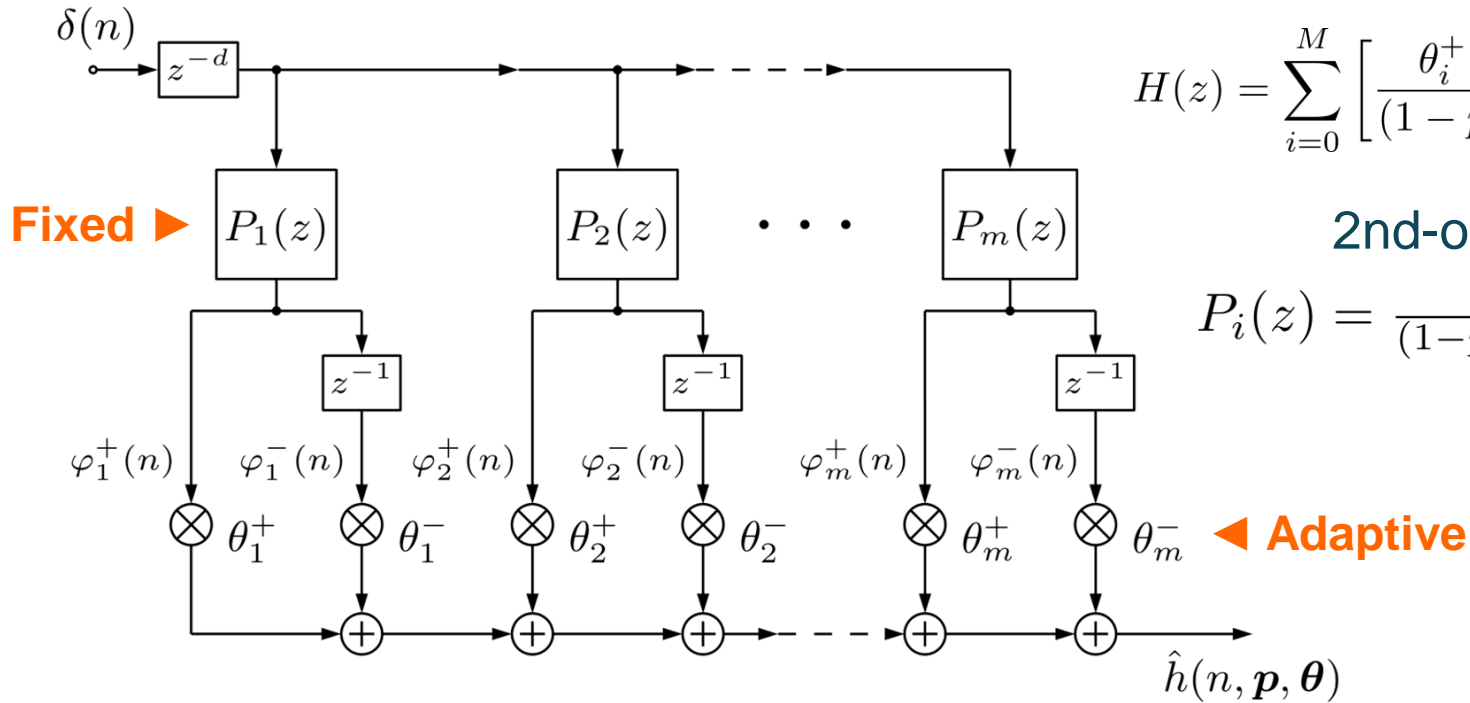
Problems:

- Higher complexity of the adaptive algorithm
- Slower convergence rate of adaptation
- Possible instability or convergence to local minima





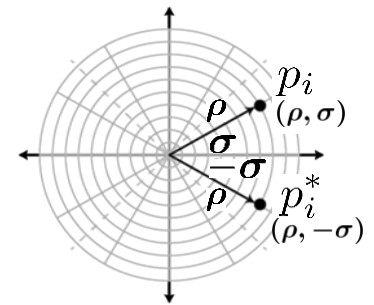
# Fixed-Pole Adaptive IIR Filters (FPAF)



$$H(z) = \sum_{i=0}^M \left[ \frac{\theta_i^+(n) + \theta_i^-(n)z^{-1}}{(1 - p_i z^{-1})(1 - p_i^* z^{-1})} \right]$$

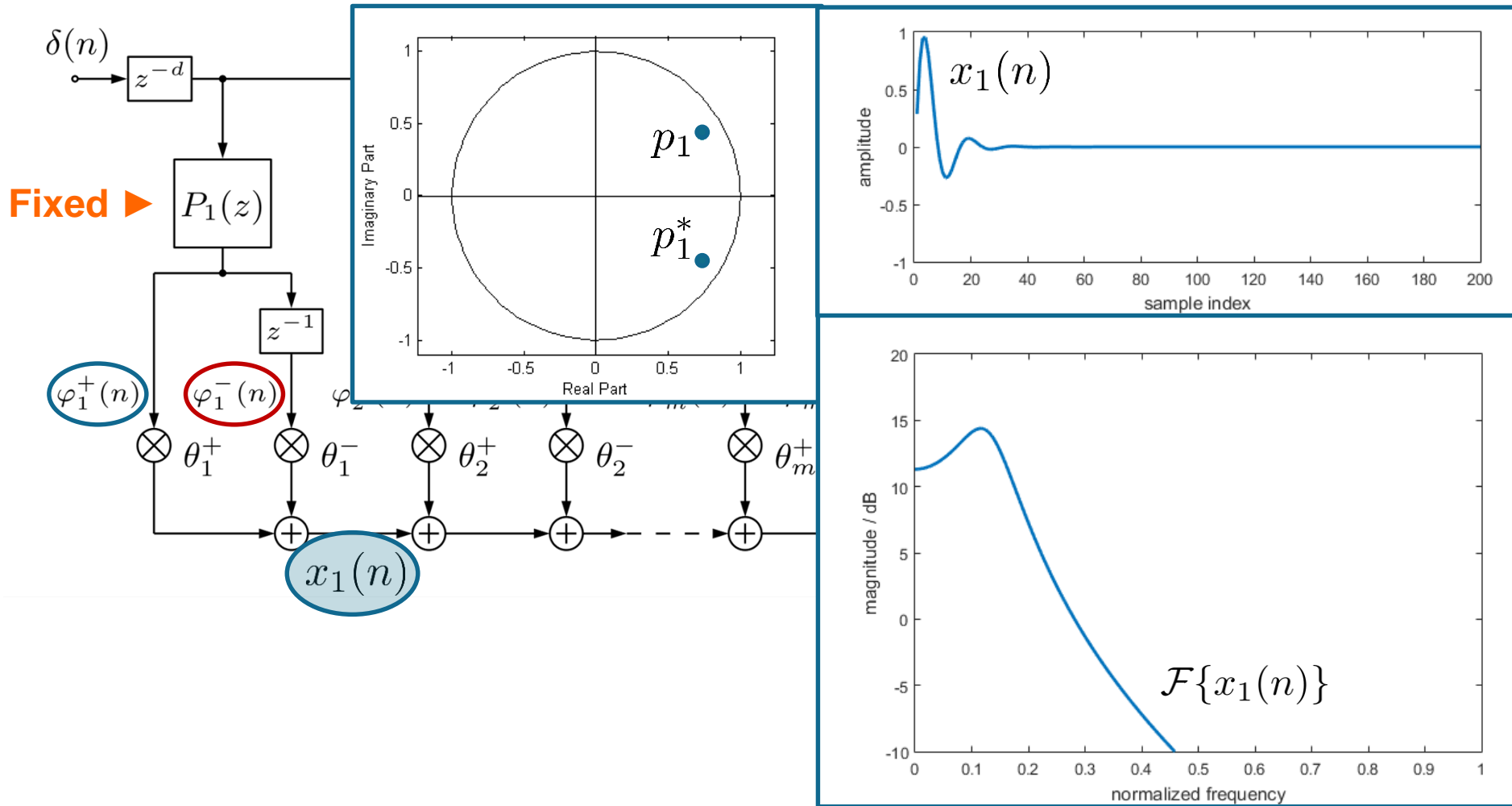
2nd-order resonator

$$P_i(z) = \frac{1}{(1 - p_i z^{-1})(1 - p_i^* z^{-1})}$$



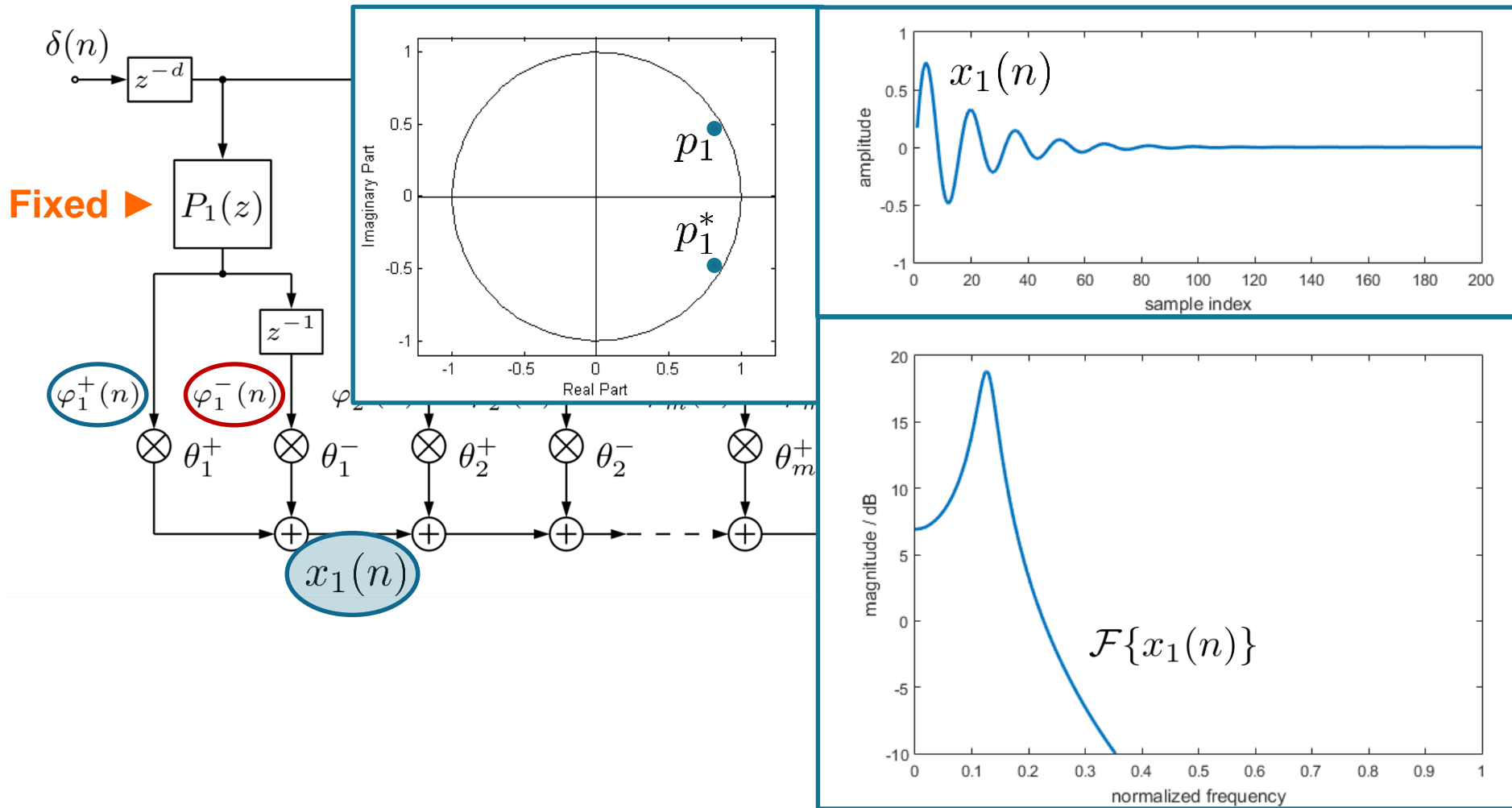
$$p_i = \rho_i e^{j\sigma_i}$$

# Fixed-Pole Adaptive IIR Filters (FPAF)



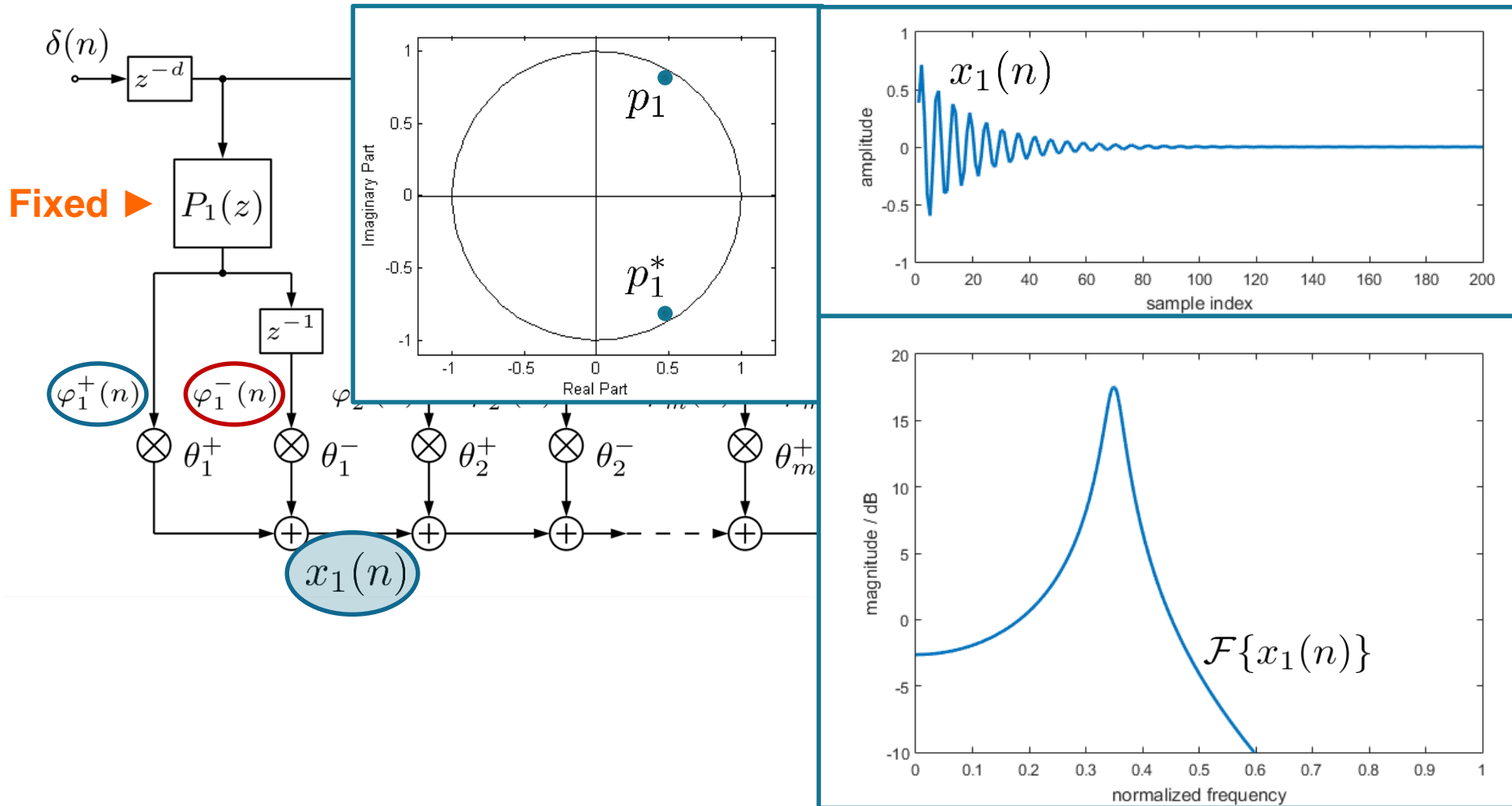
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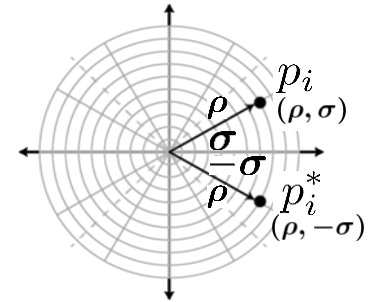
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# FPAFs for Room Acoustics

- FPAF Impulse Response

$$h(\mathbf{r}, n) = \sum_{i=0}^M 2|g_i(n)|\rho_i^n \cos(\sigma_i n + \angle g_i(n))$$

$$n = t/T, \quad n = 0, 1, \dots, \quad T : \text{sampling time}$$



$$p_i = \rho_i e^{-j\sigma_i} : \text{pole}$$

$$g_i(n) = \frac{p_i \theta_i^+(n) + \theta_i^-(n)}{p_i - p_i^*}$$

# FPAFs for Room Acoustics

- FPAF Impulse Response

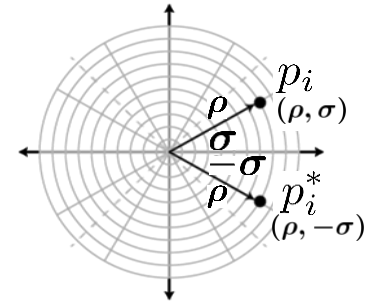
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$n = t/T$ ,  $n = 0, 1, \dots$ ,  $T$  : sampling time

- Room Impulse Response (RIR)

$$h(\mathbf{r}, t) = \sum_{i=0}^{\infty} c_i(\mathbf{r}) e^{-\zeta_i t} \cos(\omega_i t + \phi_i(\mathbf{r}))$$

$\mathbf{r} = (\mathbf{r}_0, \mathbf{r}_s)$  : receiver-source position



$p_i = \rho_i e^{-j\sigma_i}$  : pole

$\rho_i = e^{-\zeta_i T}$  : radius

$\sigma_i = \omega_i T$  : angle

# FPAFs for Room Acoustics

- FPAF Impulse Response

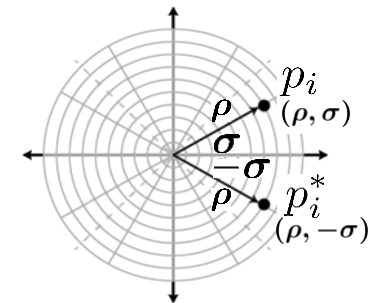
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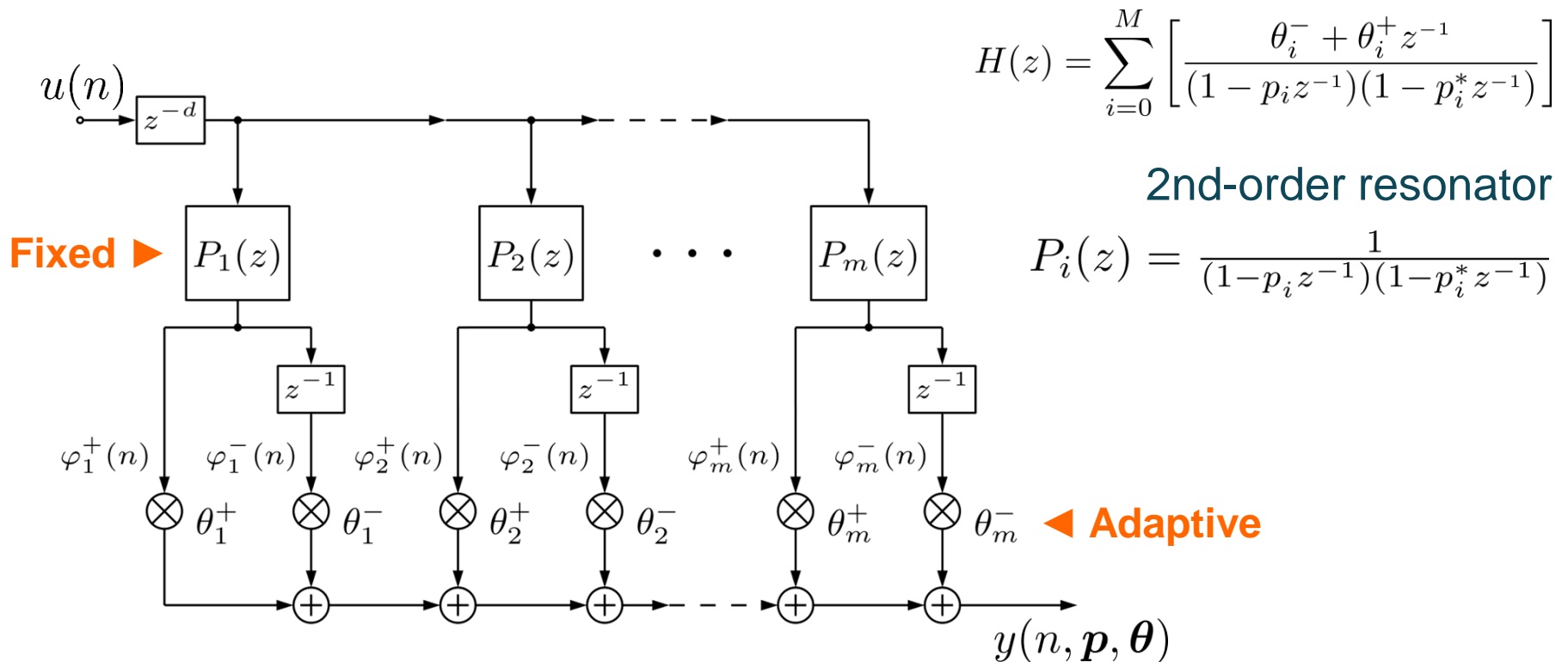
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## IDEA:

Use a digital filter whose impulse response is a linear combination of a finite number of exponentially decaying sinusoids (discrete in time)

- Fixed poles (common resonance frequencies and damping constants)
- Adaptive linear coefficients (variable amplitude and phase)

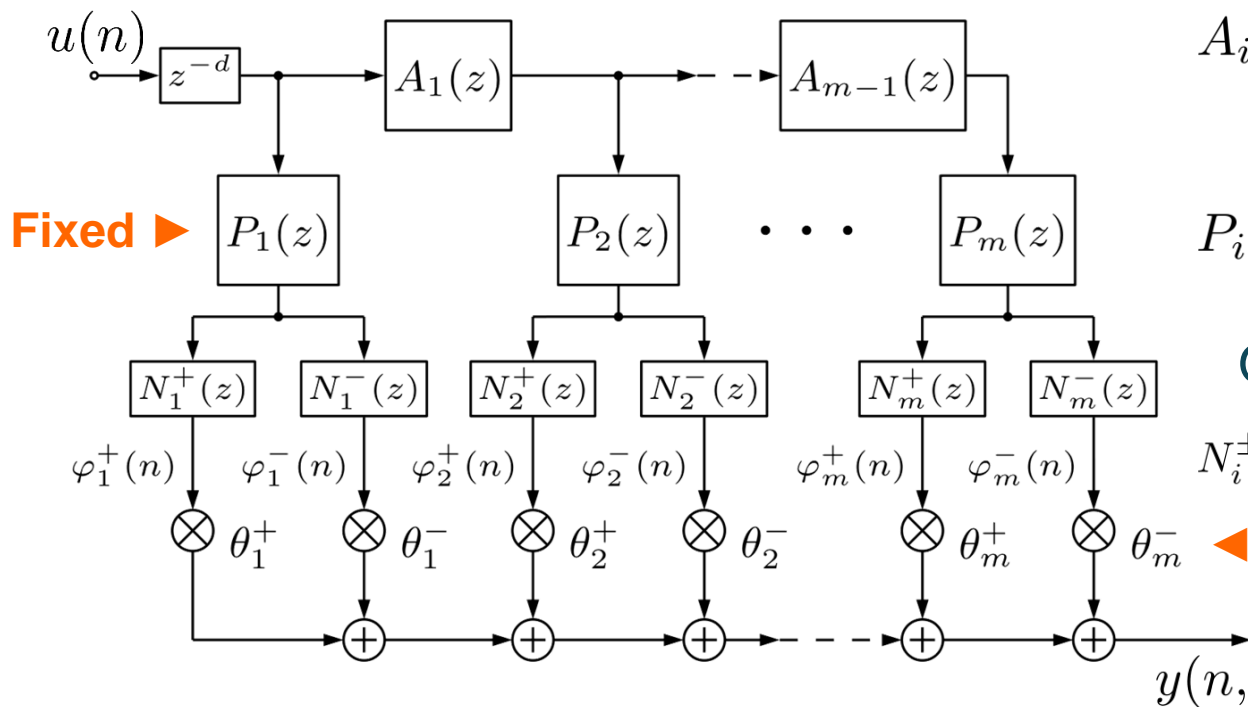
# Fixed-Pole Adaptive IIR Filters (FPAF)



- **Filter output**     $y(n, \mathbf{p}, \boldsymbol{\theta}) = \boldsymbol{\varphi}^T(n, \mathbf{p})\boldsymbol{\theta}(n)$   
 $\boldsymbol{\varphi}(n) = [\varphi_1^\pm(n), \dots, \varphi_m^\pm(n)]^T$  ← Intermediate signals vector  
 $\boldsymbol{\theta}(n) = [\theta_1^\pm(n), \dots, \theta_m^\pm(n)]^T$  ← Adaptive linear coefficients vector



# OBF filters (Kautz filters)



All-pass filter

$$A_i(z) = \frac{(z^{-1} - p_i)(z^{-1} - p_i^*)}{(1 - p_i z^{-1})(1 - p_i^* z^{-1})}$$

2nd-order resonator

$$P_i(z) = \frac{1}{(1 - p_i z^{-1})(1 - p_i^* z^{-1})}$$

Orthonormalization filter

$$N_i^\pm(z) = |1 \pm p_i| \sqrt{\frac{1 - |p_i|^2}{2}} (z^{-1} \mp 1)$$

◀ **Adaptive**

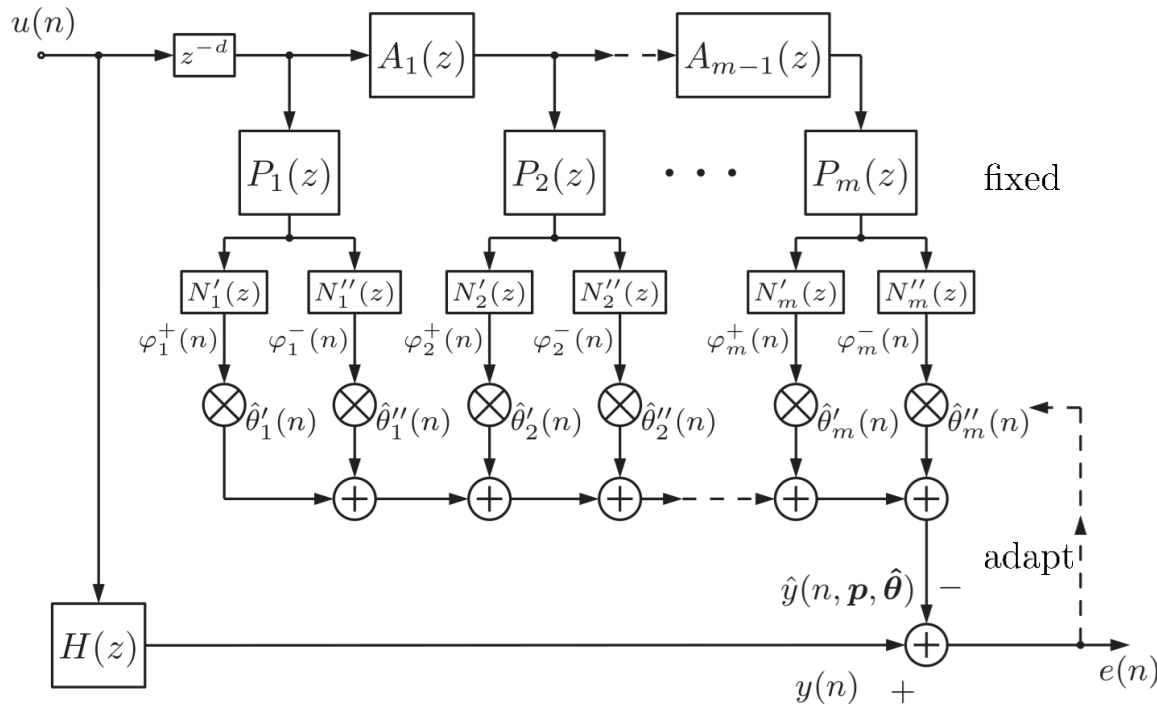
- Filter output  $y(n, \mathbf{p}, \boldsymbol{\theta}) = \boldsymbol{\varphi}^T(n, \mathbf{p}) \boldsymbol{\theta}(n)$
- OBF filters and FPAFs span the same approximation space

# FPAFs and OBF filters

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- Advantages:
  - **Accuracy** : poles are moved closer to the real poles of the system
  - **Flexibility** : poles can be arbitrarily fixed in the filter structure
  - **Stability** : poles can be fixed inside the unit circle
  - **Linearity** : the filter structure is linear in the tap-coefficients  $\theta$ 
    - Transversal filter structure  $\rightarrow$  Global convergence of adaptation
    - Same complexity of adaptation algorithm as FIR filters
  - **Orthogonality** (only OBF filters)
    - Good trade-off between accuracy and number of parameters
    - Repeated poles and pole addition/deletion
    - Numerically well-conditioning (no order restriction)
    - Faster global convergence

# Adaptive OBF Filter



$$K_i^\pm(z, \mathbf{p}_i) = N_i^\pm(z) P_i(z) \prod_{j=1}^{i-1} A_j(z)$$

$$\varphi_i^\pm(n) = K_i^\pm(z, \mathbf{p}_i) u(n)$$

$$e(n) = y(n) - \hat{y}(n)$$

$y(n)$  : output signal

$$\hat{y}(n) = \boldsymbol{\varphi}^T(n) \hat{\boldsymbol{\theta}}(n)$$

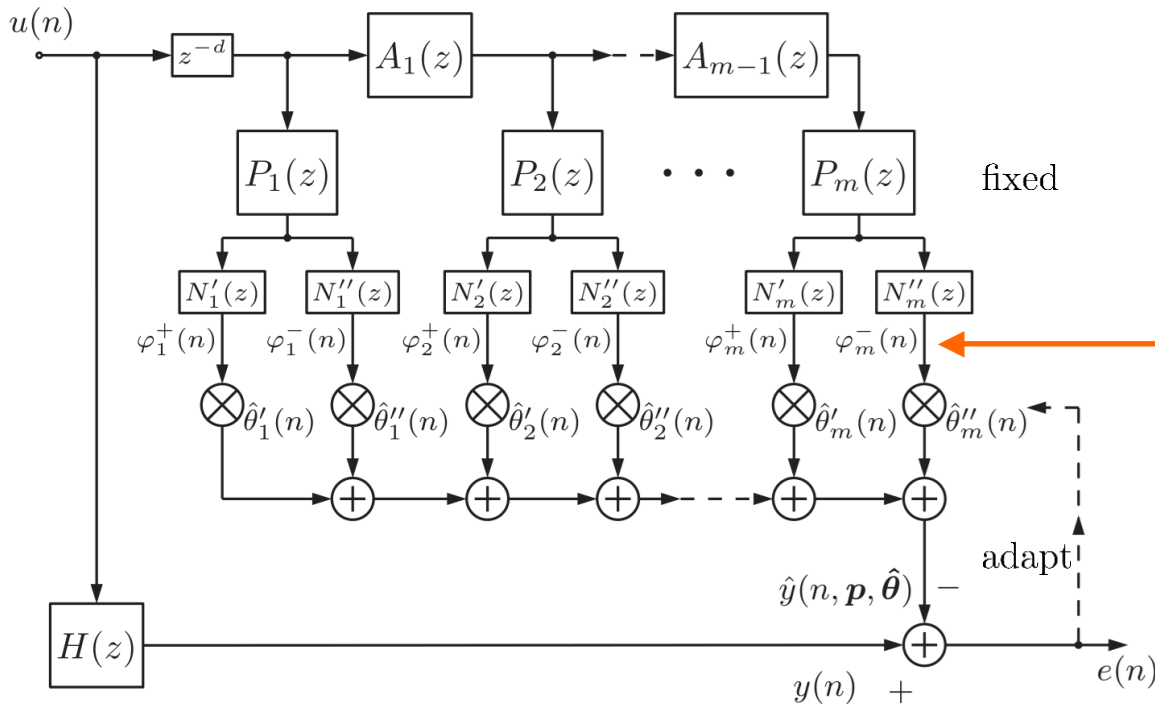
$$\boldsymbol{\varphi}(n) = [\varphi_1^\pm(n), \dots, \varphi_m^\pm(n)]^T$$

$$\hat{\boldsymbol{\theta}}(n) = [\hat{\theta}_1^\pm(n), \dots, \hat{\theta}_m^\pm(n)]^T$$

Adaptation Rule

$$\hat{\boldsymbol{\theta}}(n+1) = \hat{\boldsymbol{\theta}}(n) + \mathbf{L}(n)e(n)$$

# Adaptive OBF Filter - LMS



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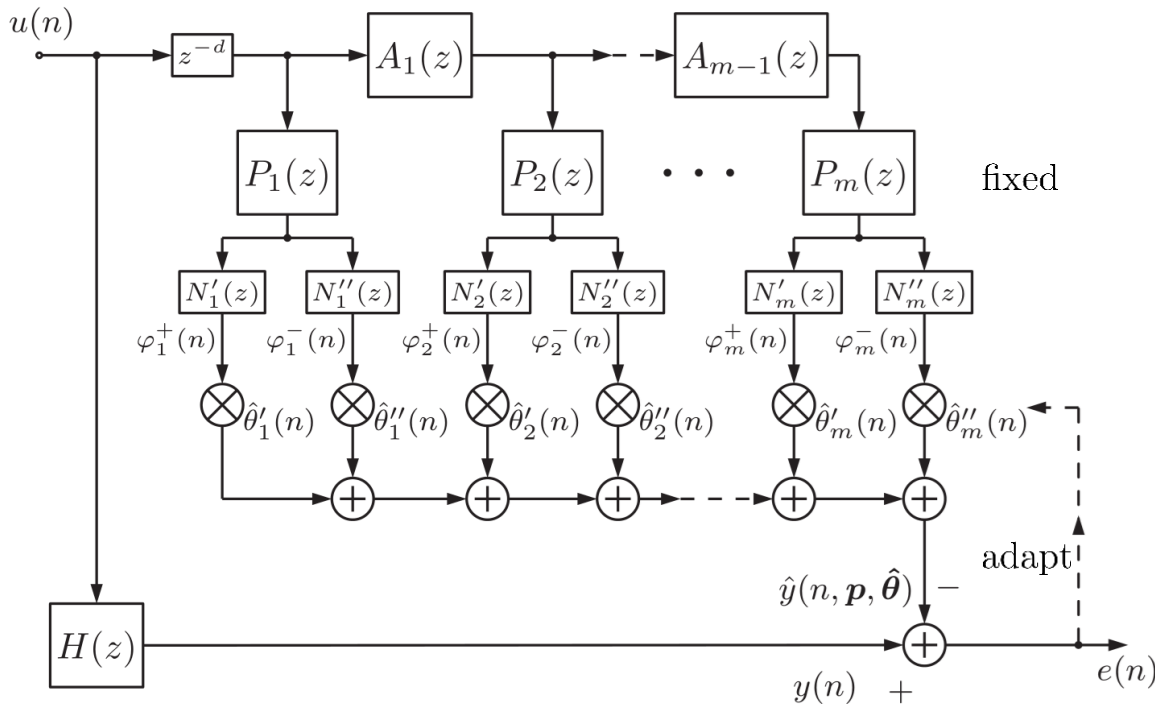
$$\boldsymbol{\varphi}(n) = [\varphi_1^\pm(n), \dots, \varphi_m^\pm(n)]^T$$

Regression vector

Adaptation Rule - LMS

$$\hat{\boldsymbol{\theta}}(n+1) = \hat{\boldsymbol{\theta}}(n) + \mu \boldsymbol{\varphi}(n) e(n)$$

# Adaptive OBF Filter - LMS



$$\varphi(n) = [\varphi_1^\pm(n), \dots, \varphi_m^\pm(n)]^T$$

$$\mathbf{R} = E\{\varphi(n)\varphi^T(n)\}$$

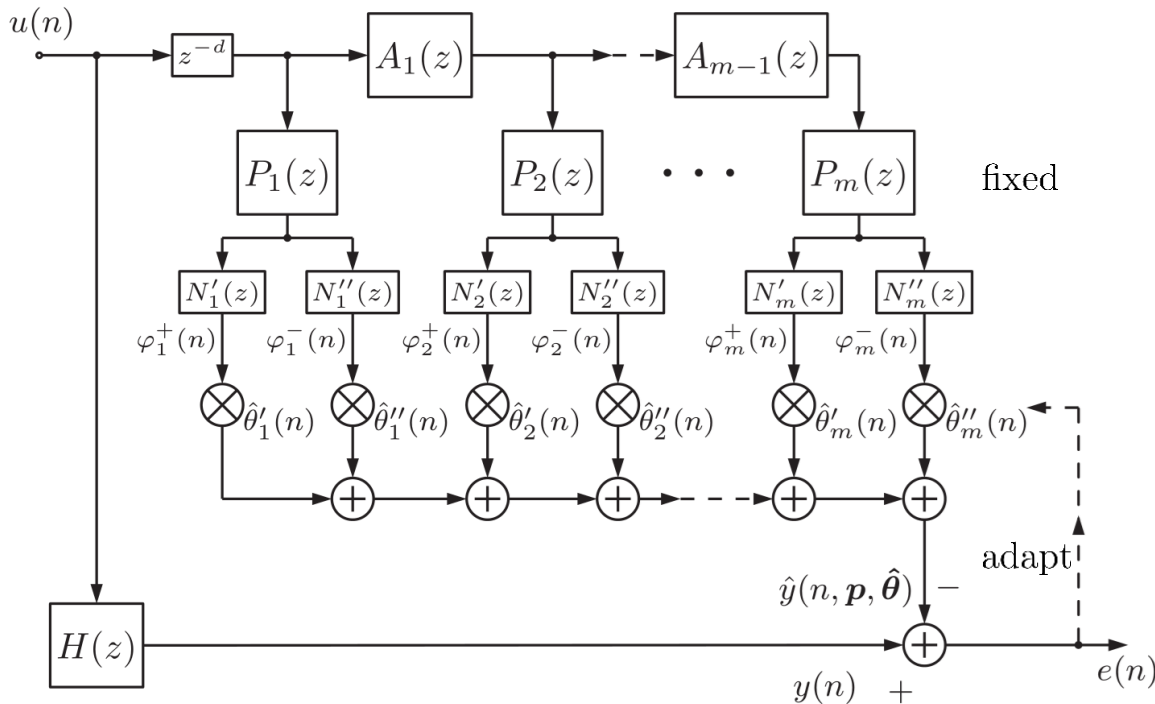
Convergence rate in the mean  
no faster than

$$\left(1 - \frac{\lambda_{\min}}{\lambda_{\max}}\right)^n = \left(1 - \frac{1}{C(\mathbf{R})}\right)^n$$

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For white input signal  $\Phi_u(\omega) = c$

$$\mathbf{R} = c\mathbf{I}, C(\mathbf{R}) = 1$$

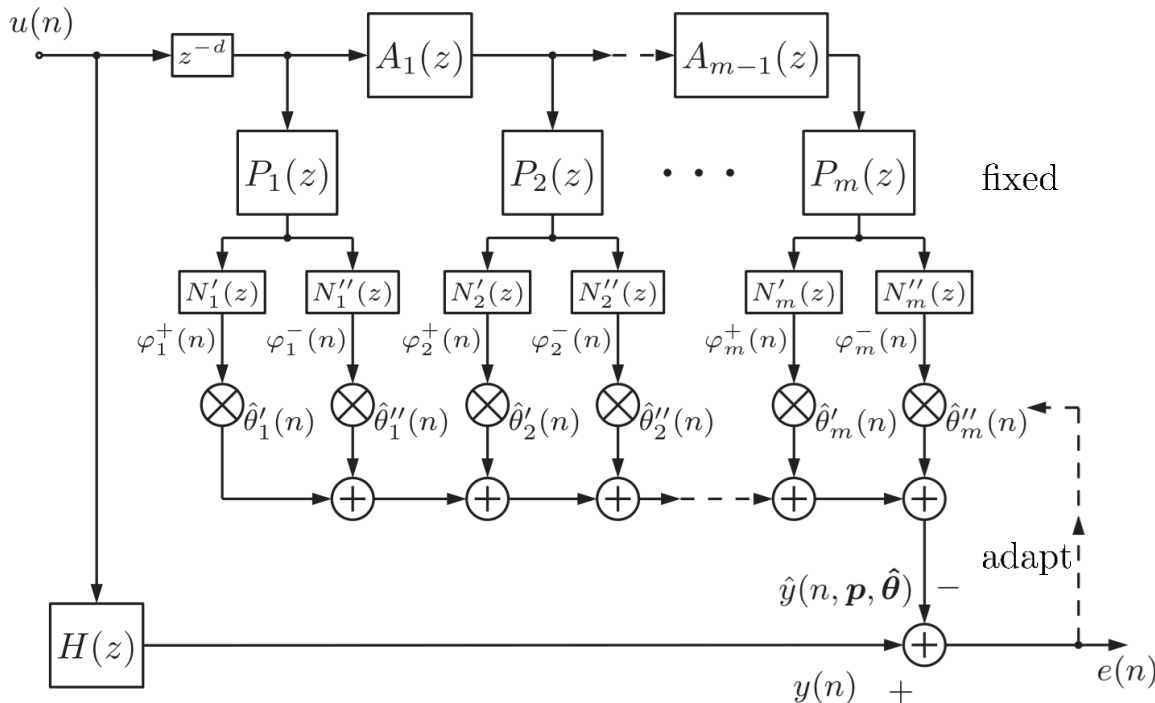
For nonwhite input signal \*

$$C(\mathbf{R}) \approx \frac{\max_{\omega} \Phi_u(\omega)}{\min_{\omega} \Phi_u(\omega)}$$

Adaptation Rule - LMS

$$\hat{\boldsymbol{\theta}}(n+1) = \hat{\boldsymbol{\theta}}(n) + \mu \varphi(n) e(n)$$

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**Performance depends  
on the choice of  
the fixed pole parameters**

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## Adaptive Digital Filters for Room Acoustics Modeling

### ▶ Multichannel Identification Algorithm

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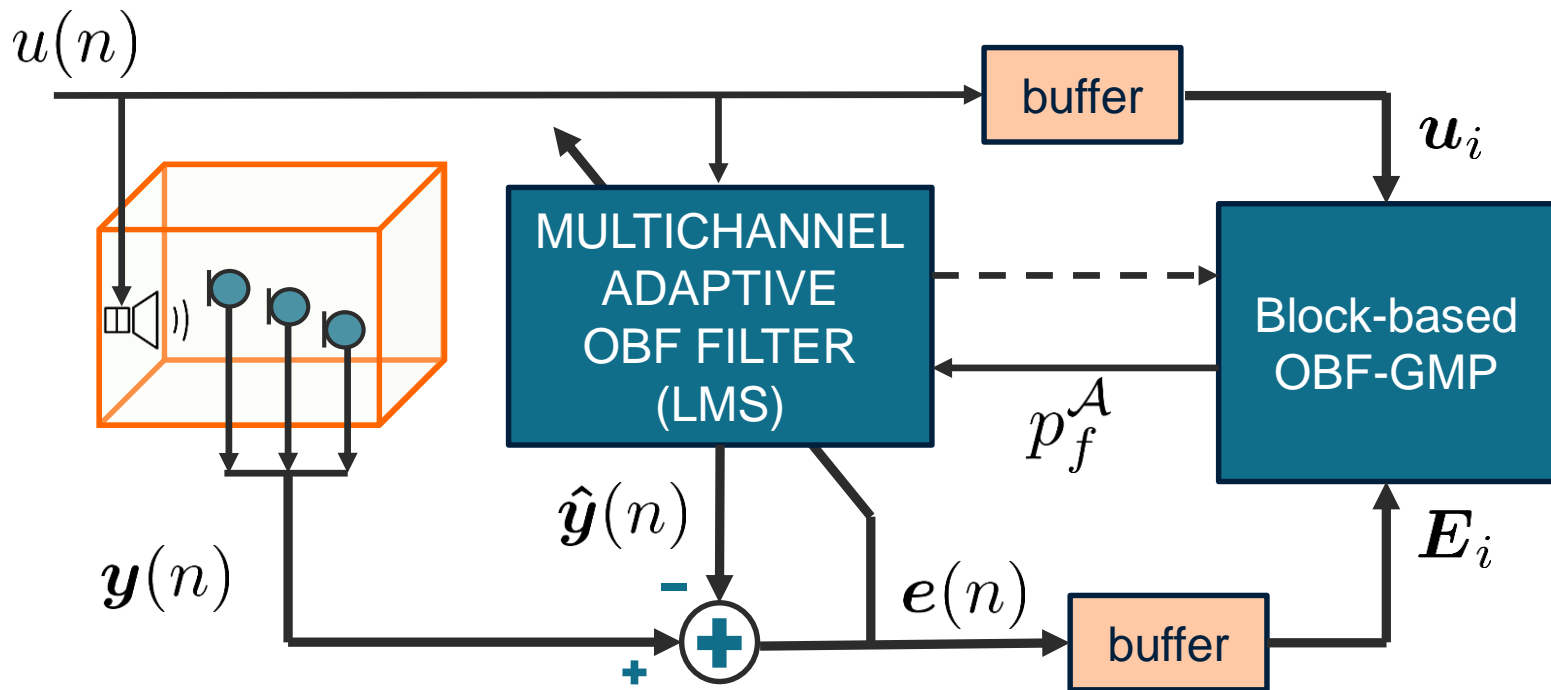
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# Multichannel identification algorithm

## Multi-channel pole estimation (SIMO)

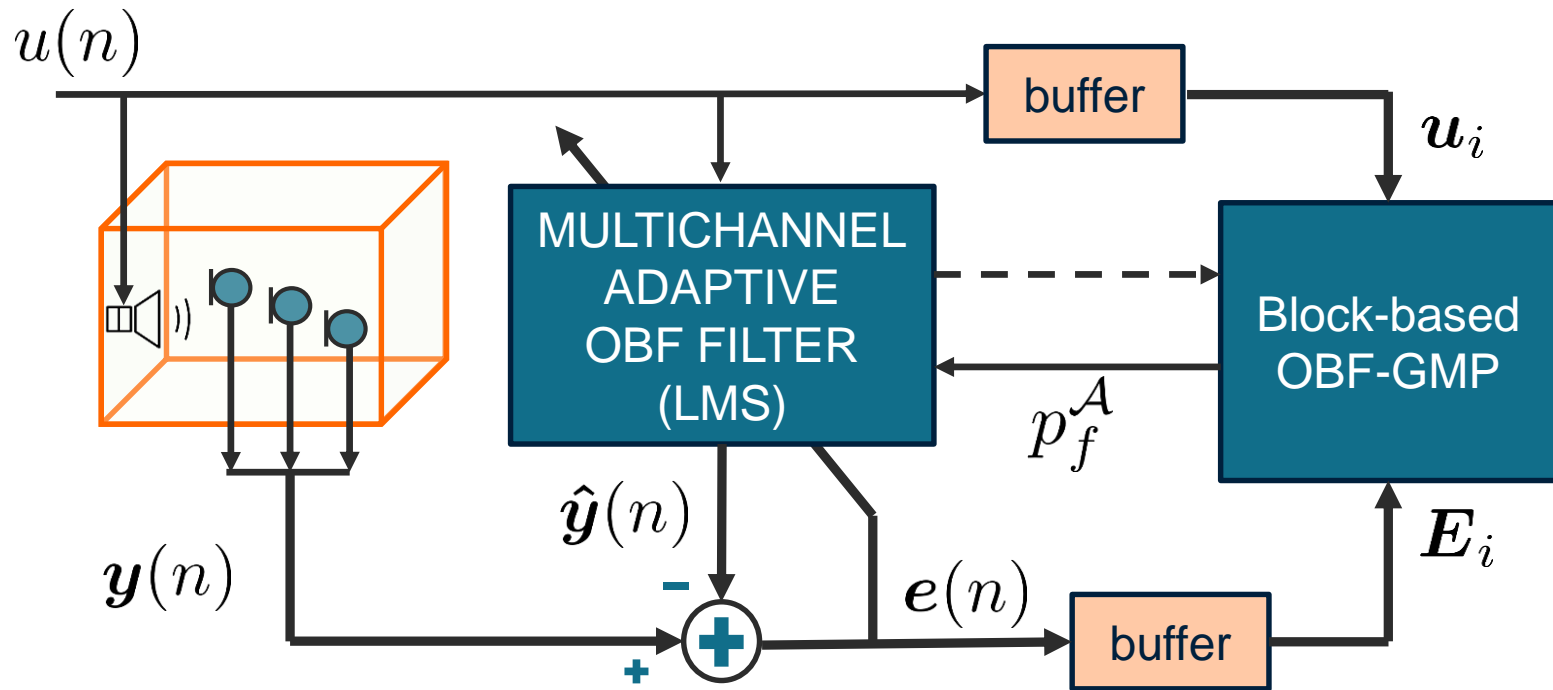
- Estimate the fixed poles of an **adaptive** OBF filter from **multi-channel I/O data**



# Multichannel identification algorithm

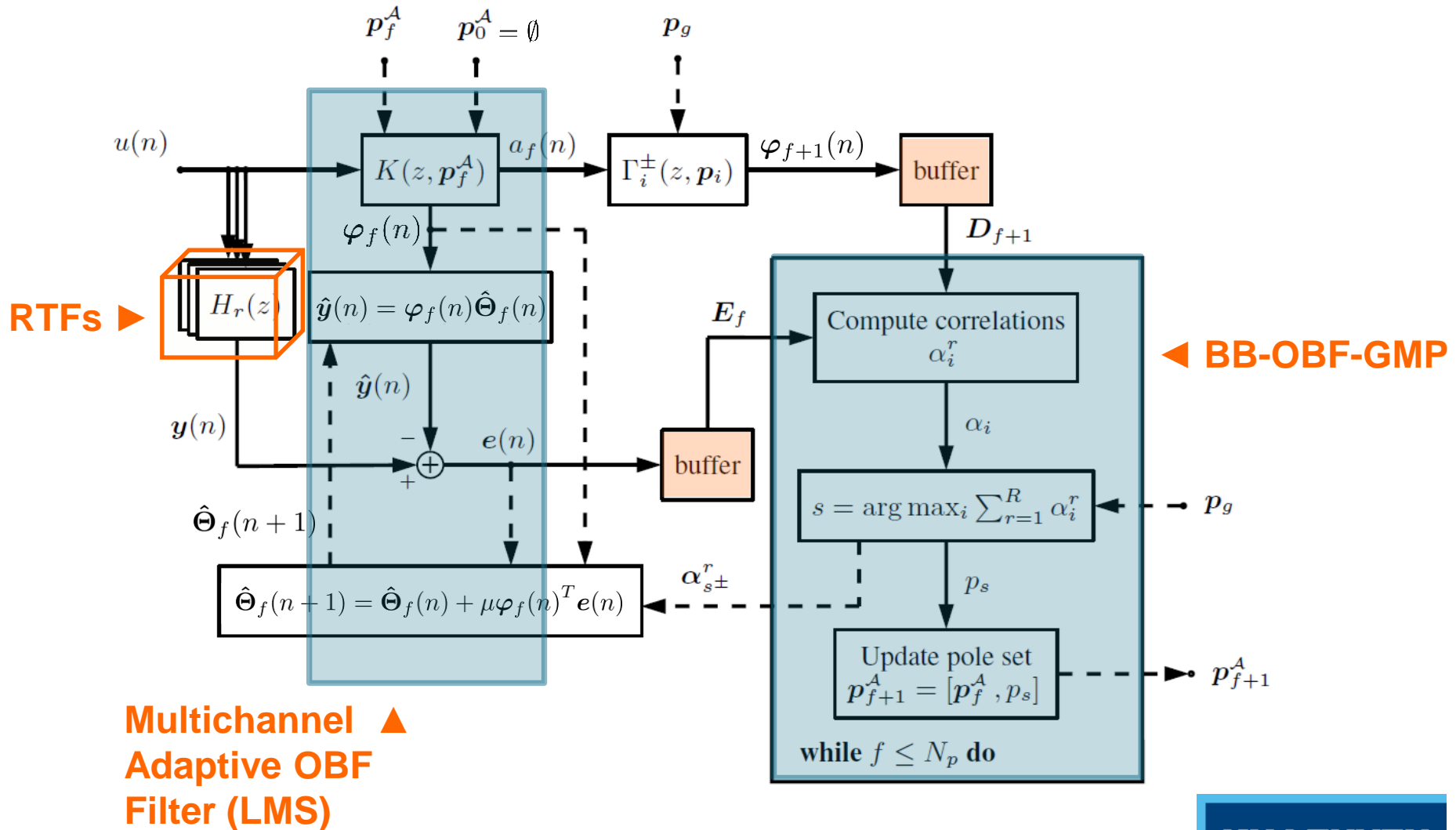
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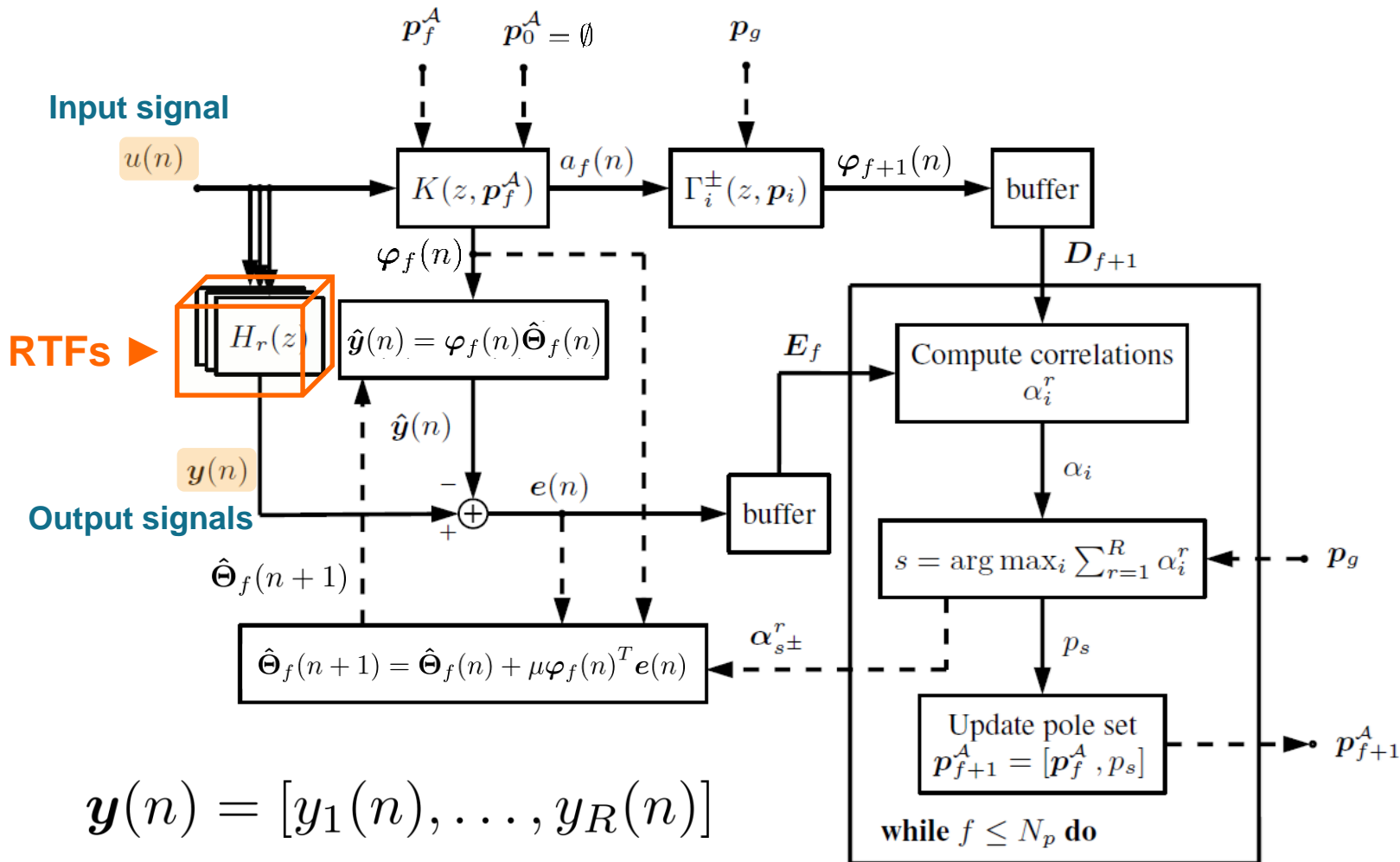


$$\underset{\mathbf{p}_f^A, \hat{\Theta}(n)}{\text{minimize}} \quad e^2(n) = (\mathbf{y}(n) - \hat{\mathbf{y}}(n))^2 = \left( \mathbf{y}(n) - \boldsymbol{\varphi}^T(\mathbf{p}_f^A, n) \hat{\Theta}(n) \right)^2$$

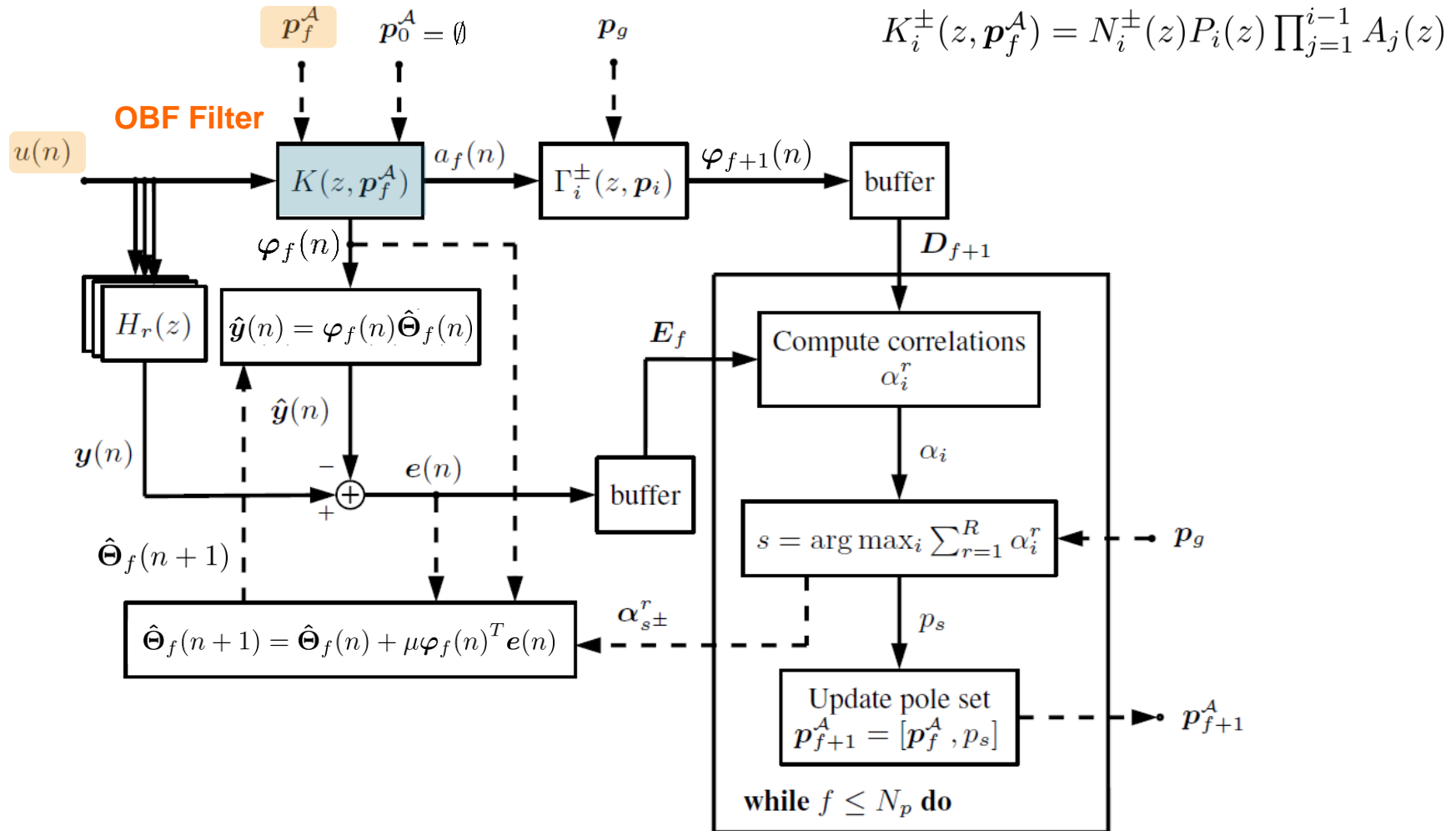
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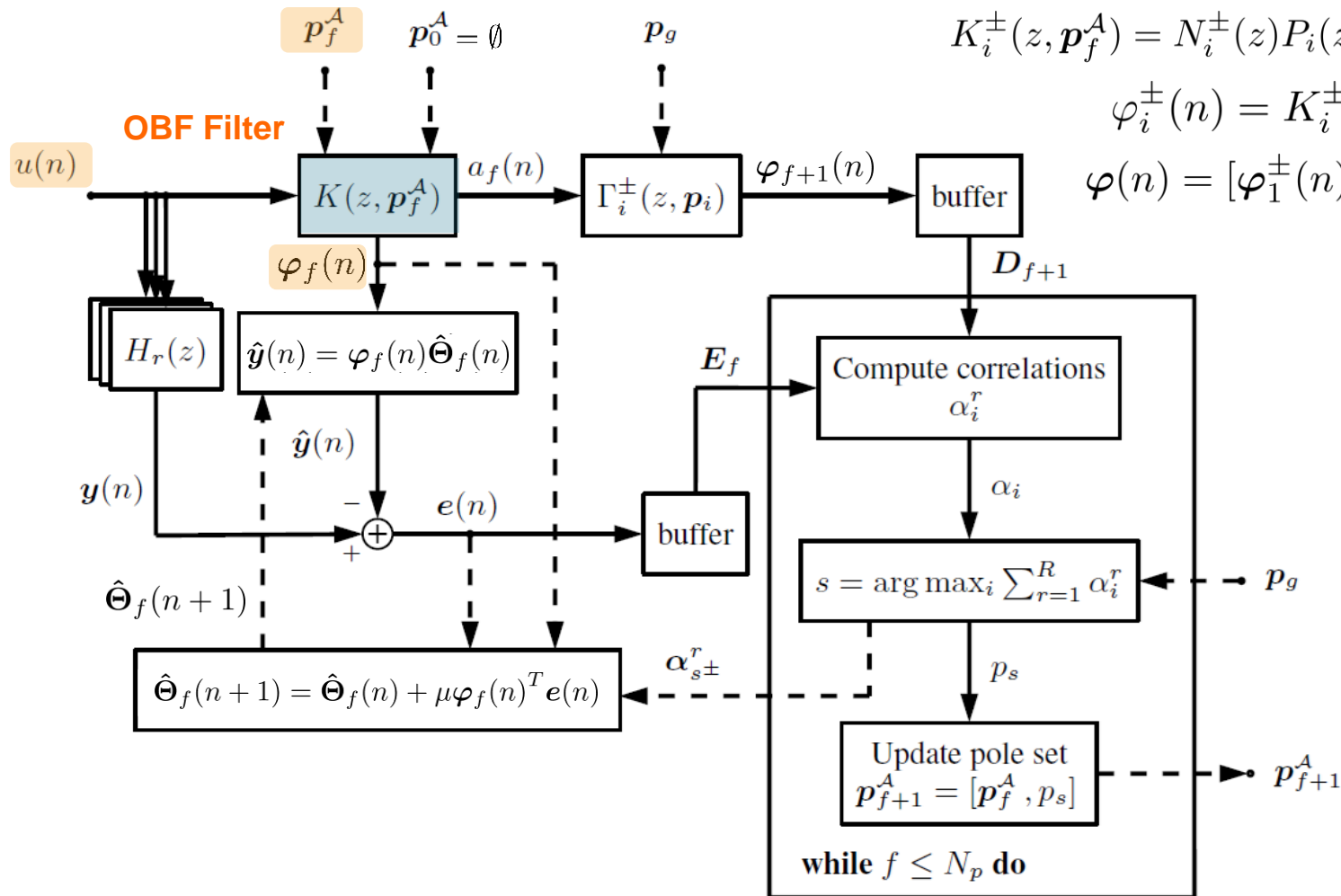
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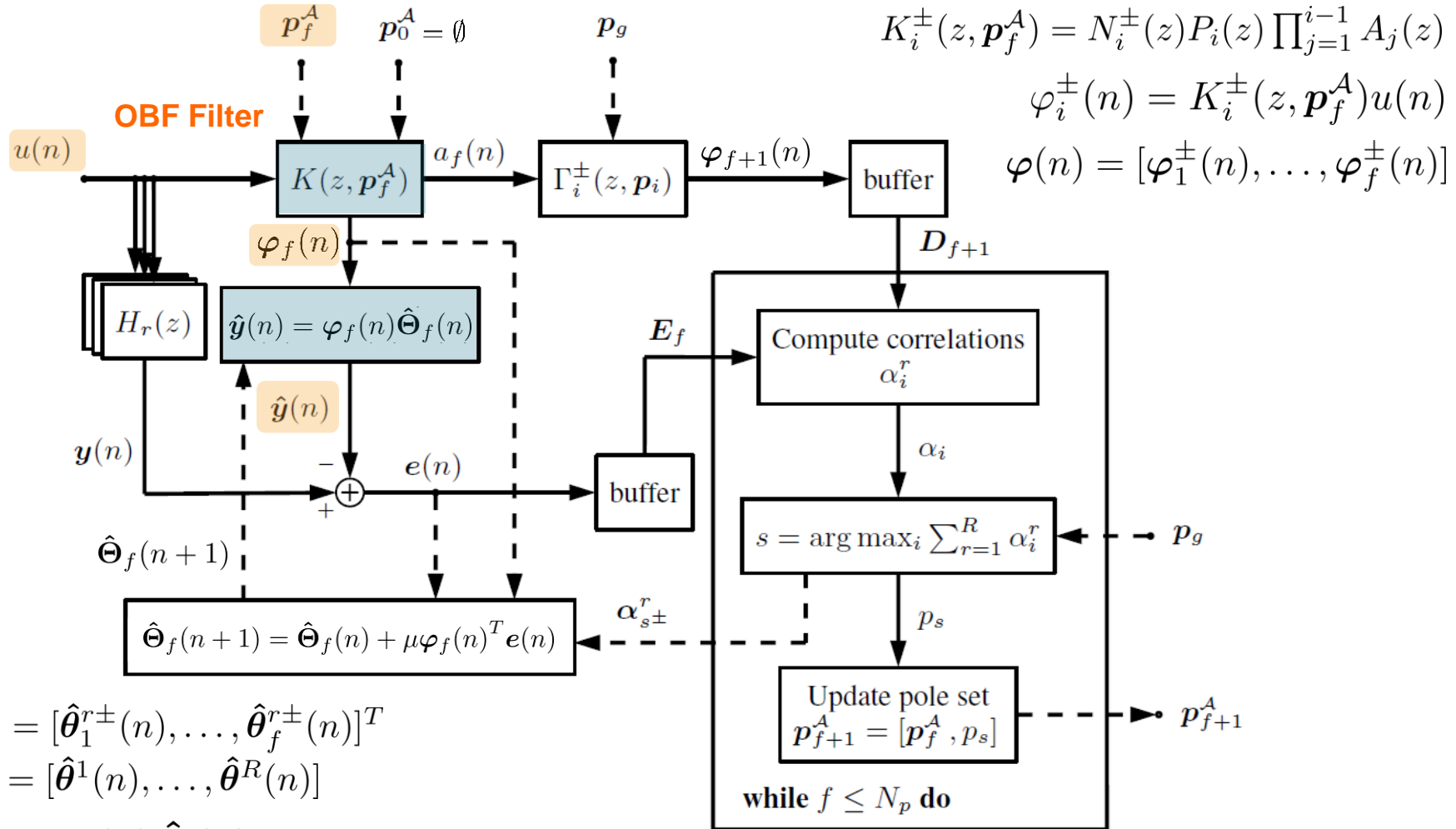
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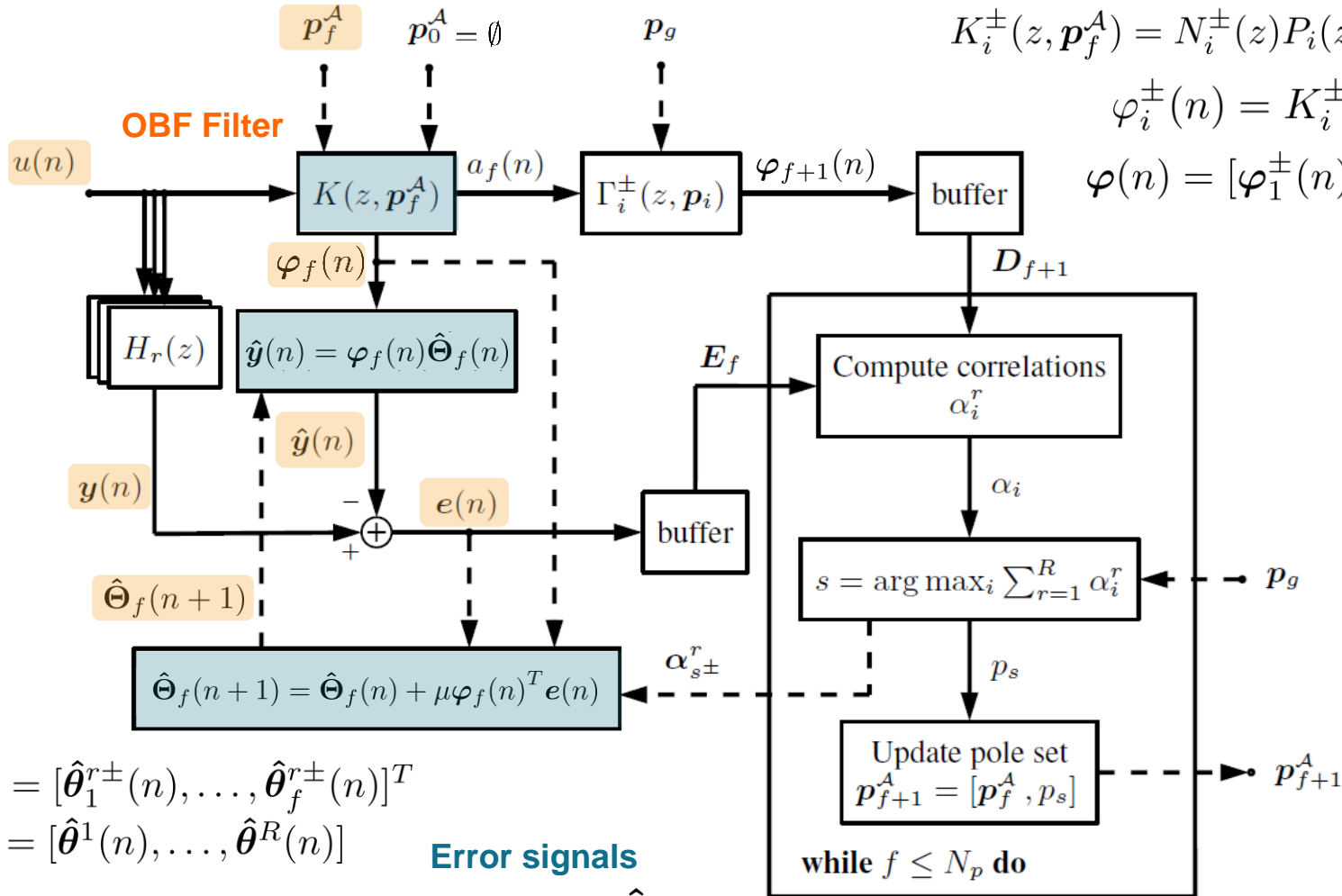


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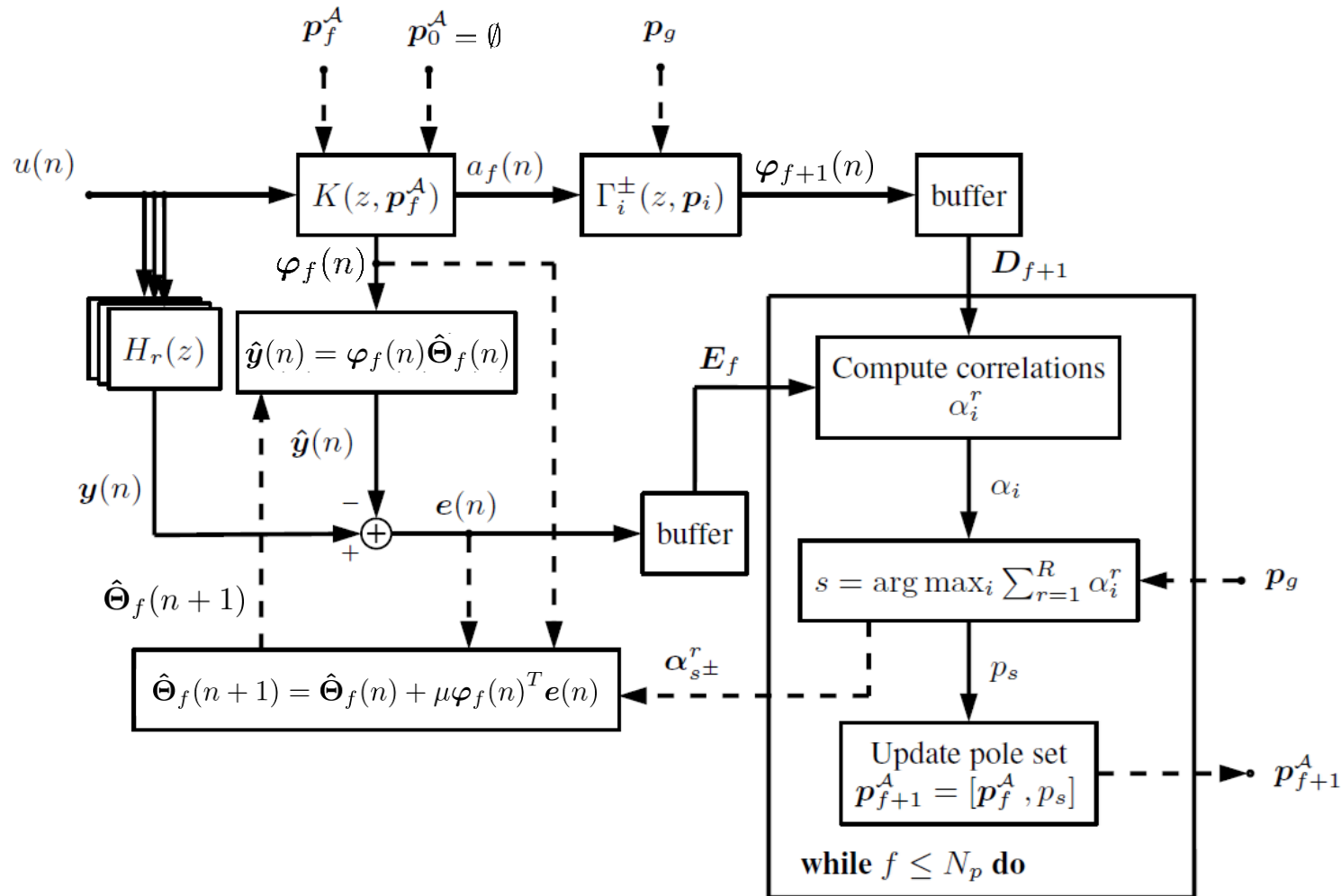




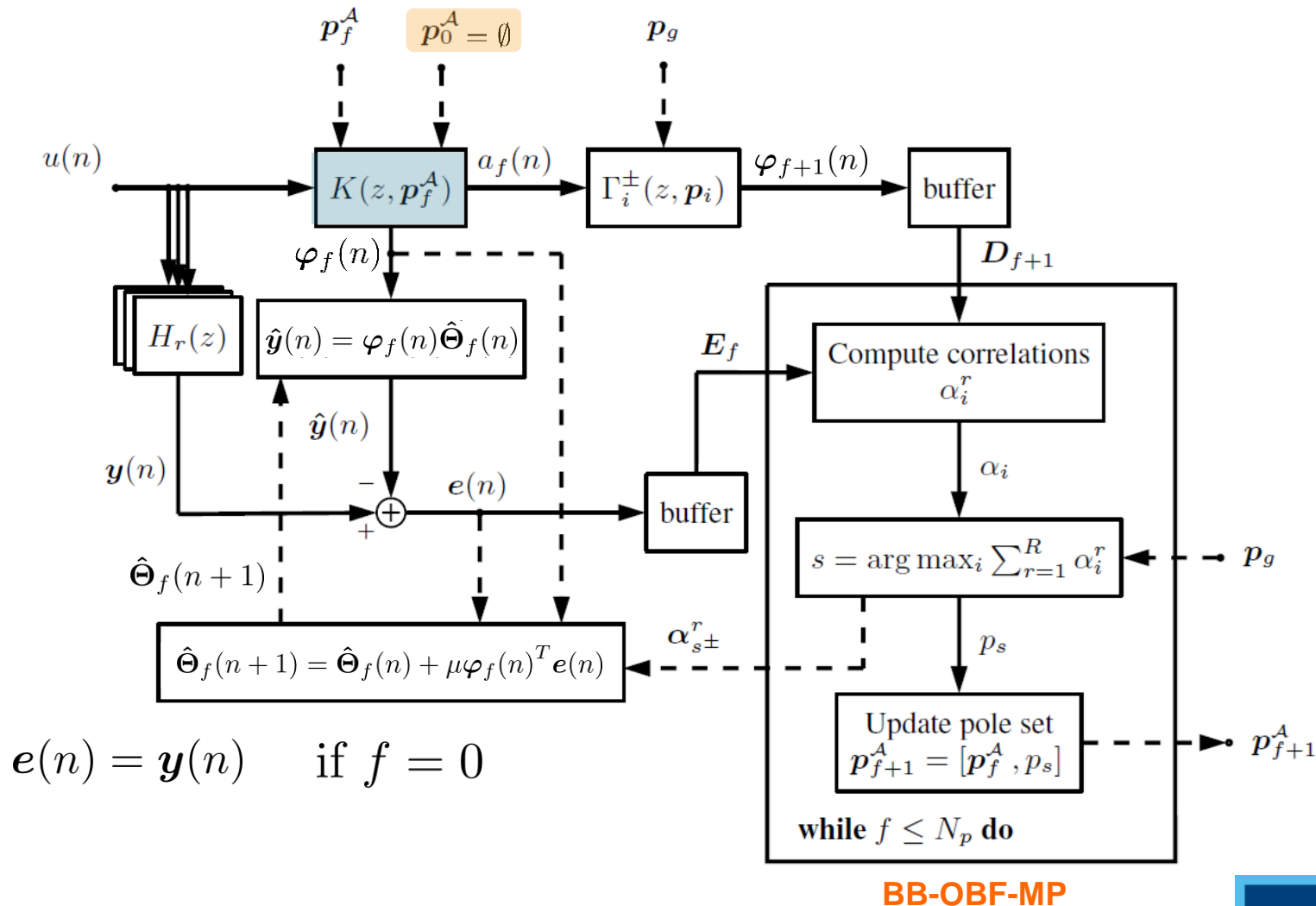
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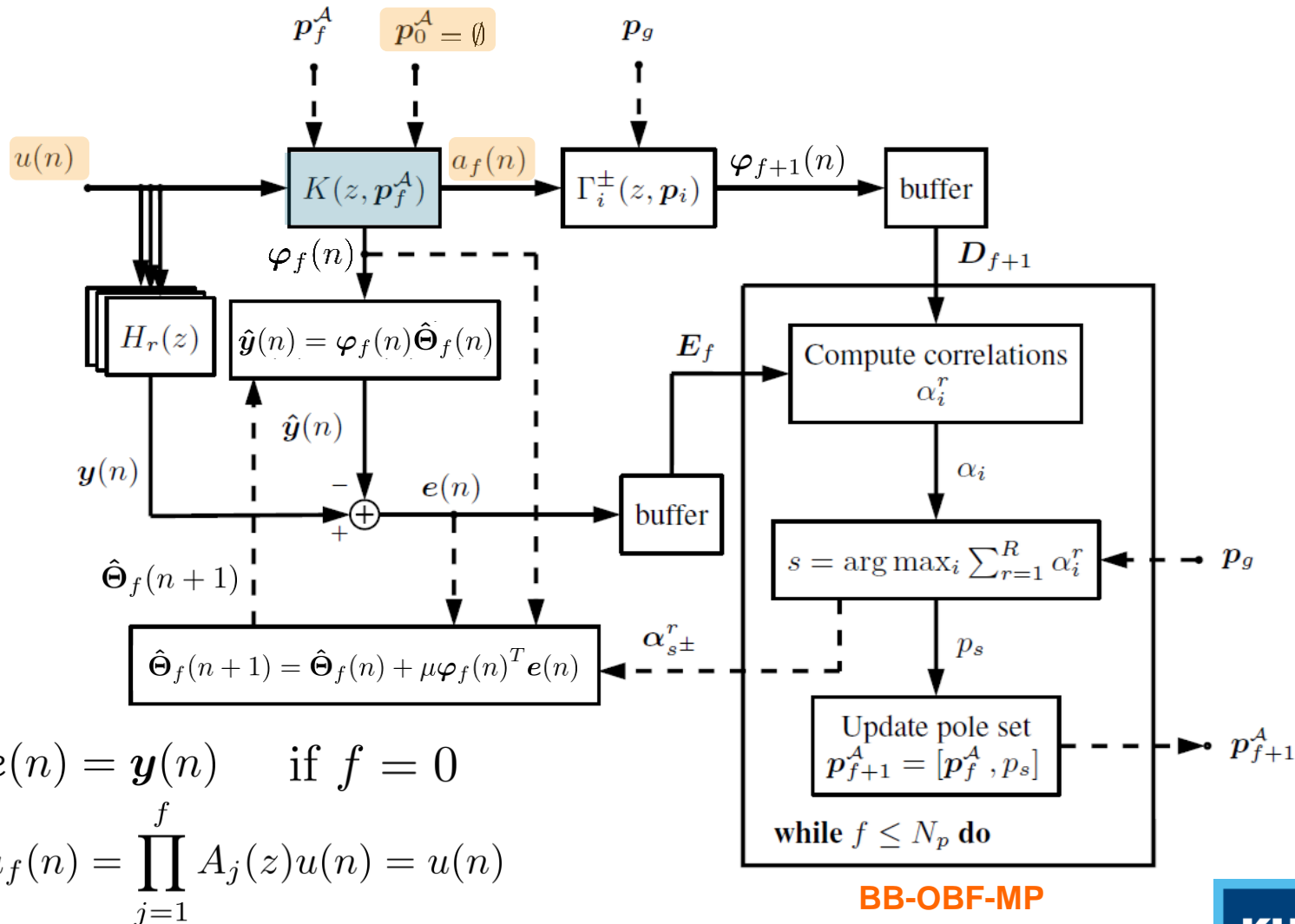


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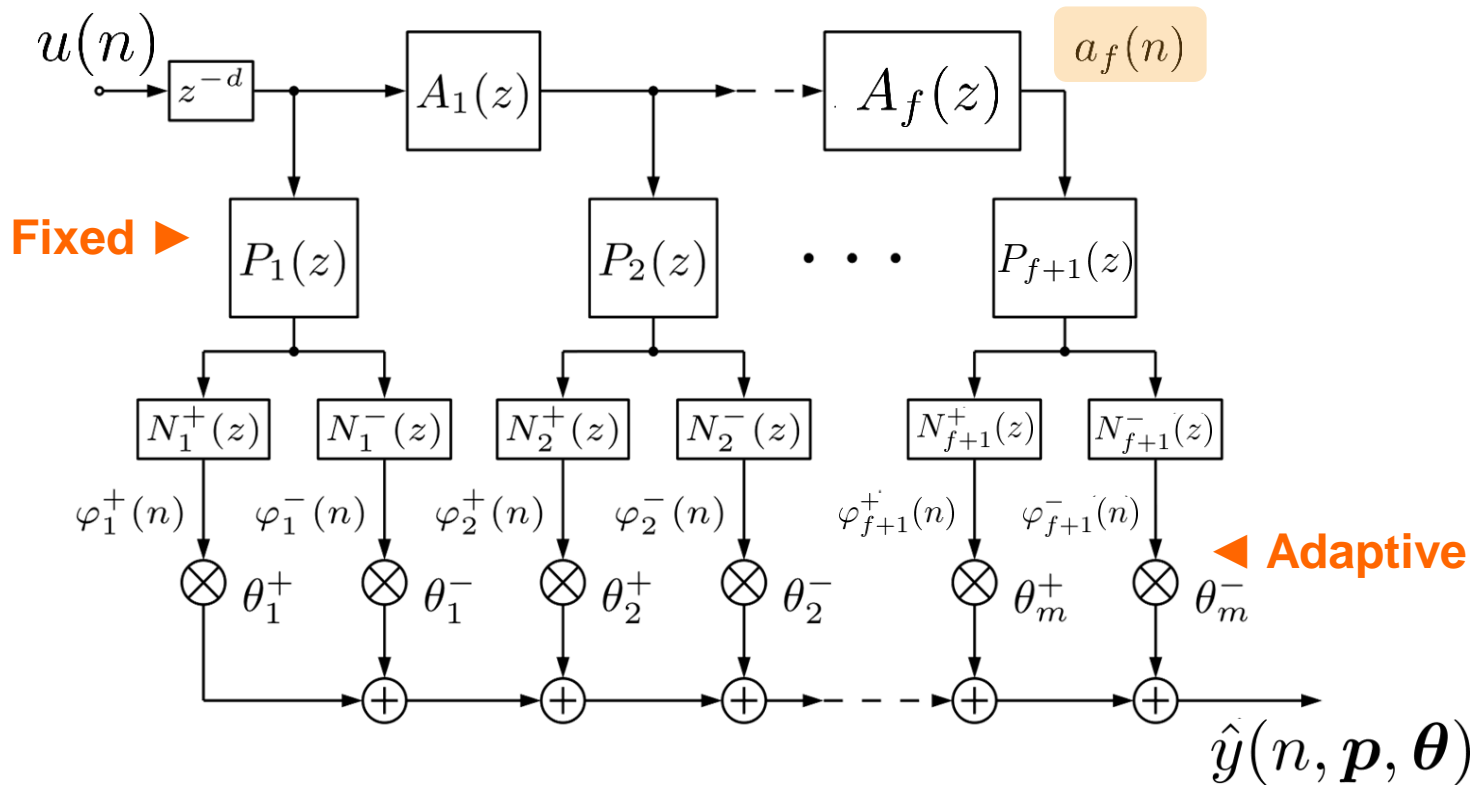


$$e(n) = y(n) \quad \text{if } f = 0$$

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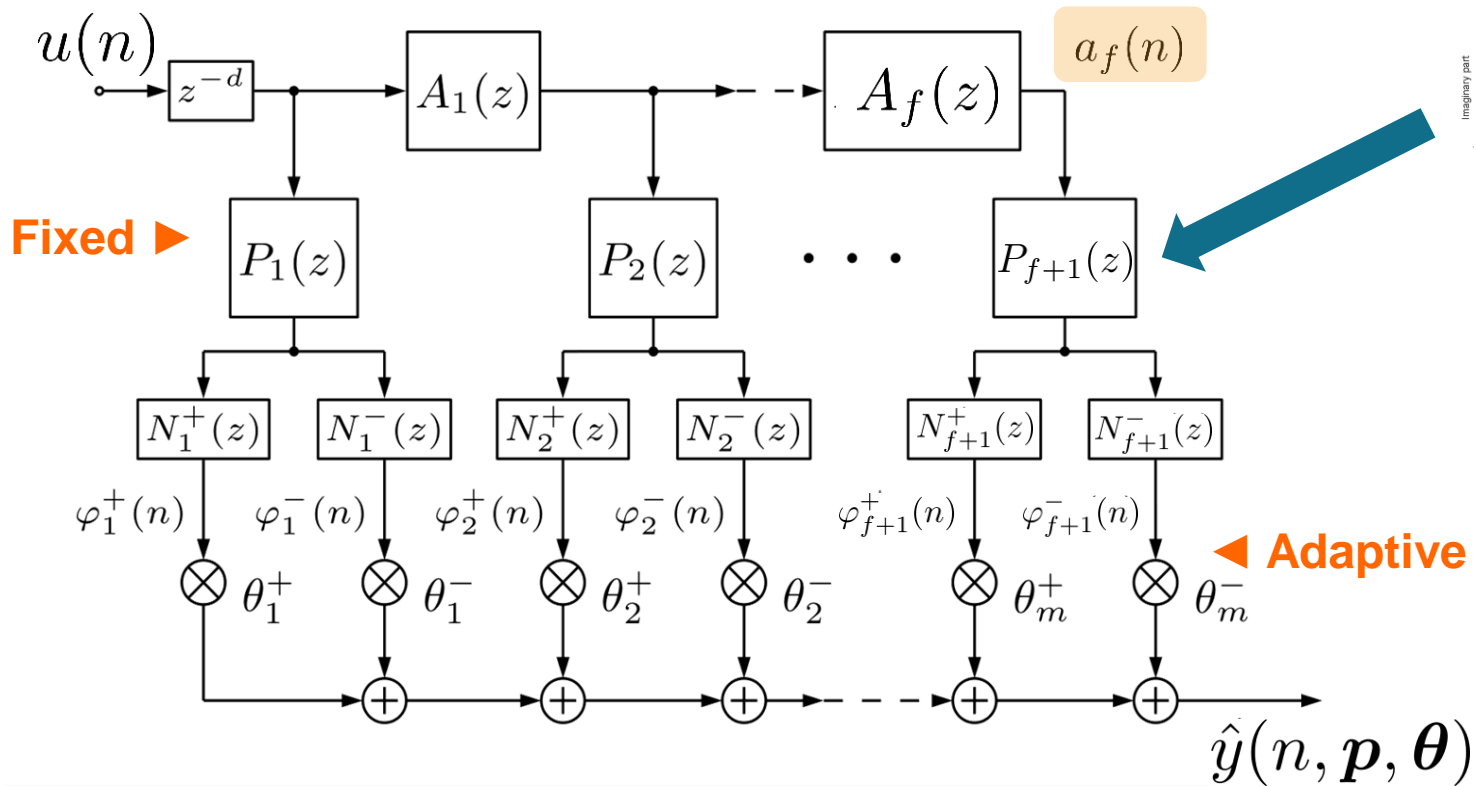


# OBF filters (Kautz filters)

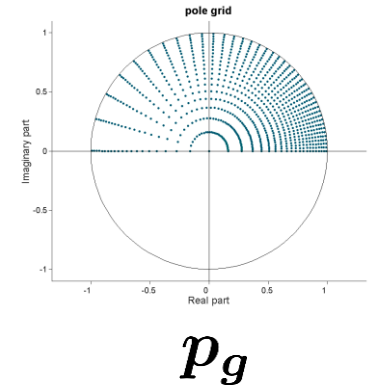


$$a_f(n) = \prod_{j=1}^f A_j(z)u(n)$$

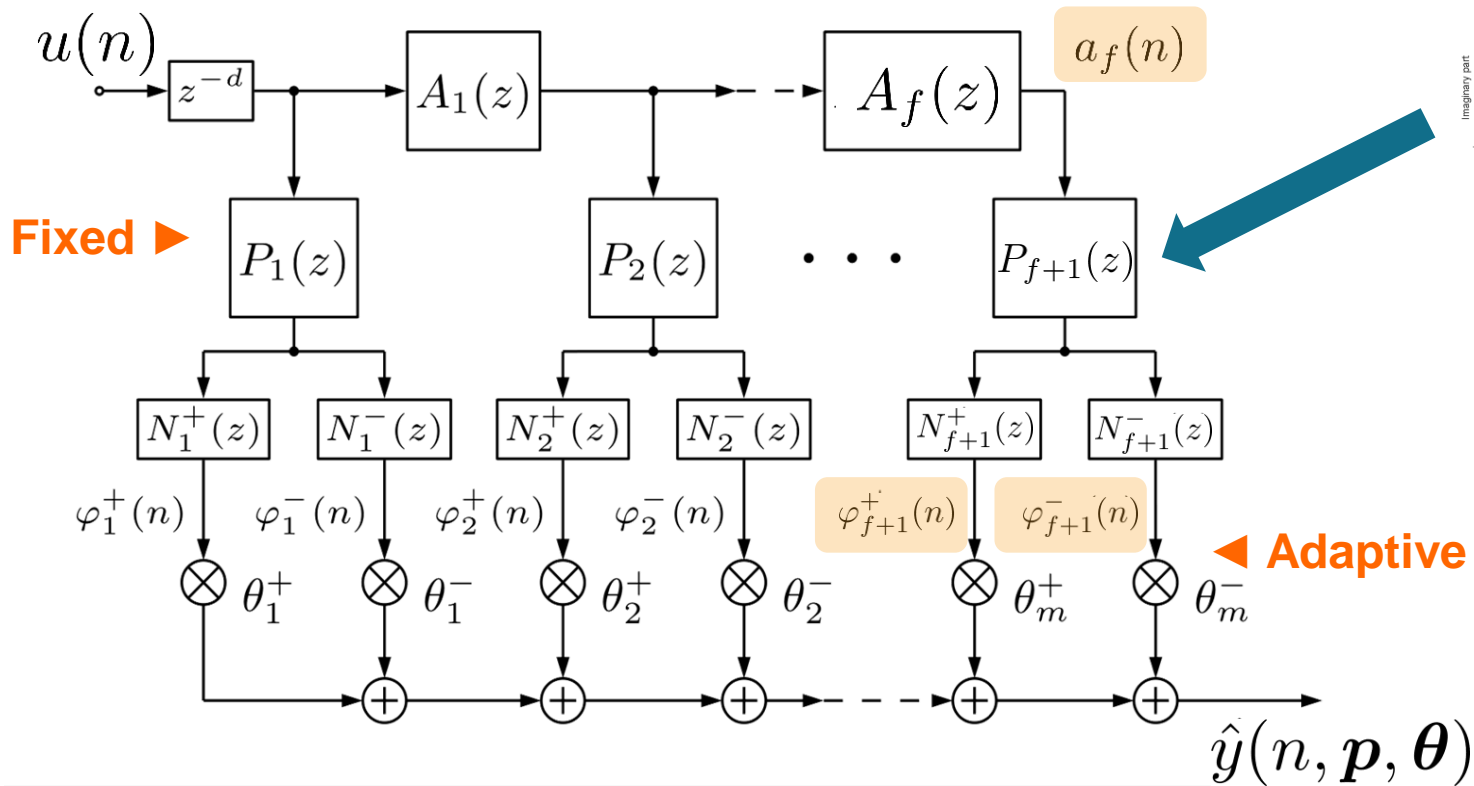
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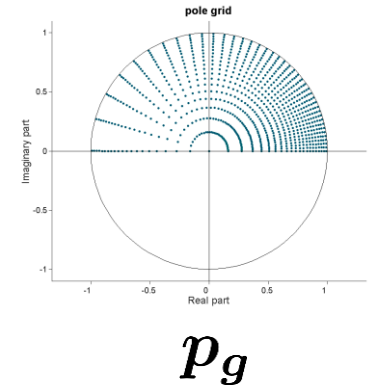
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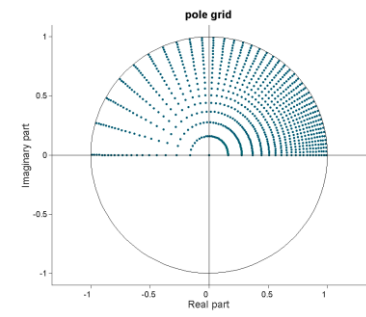
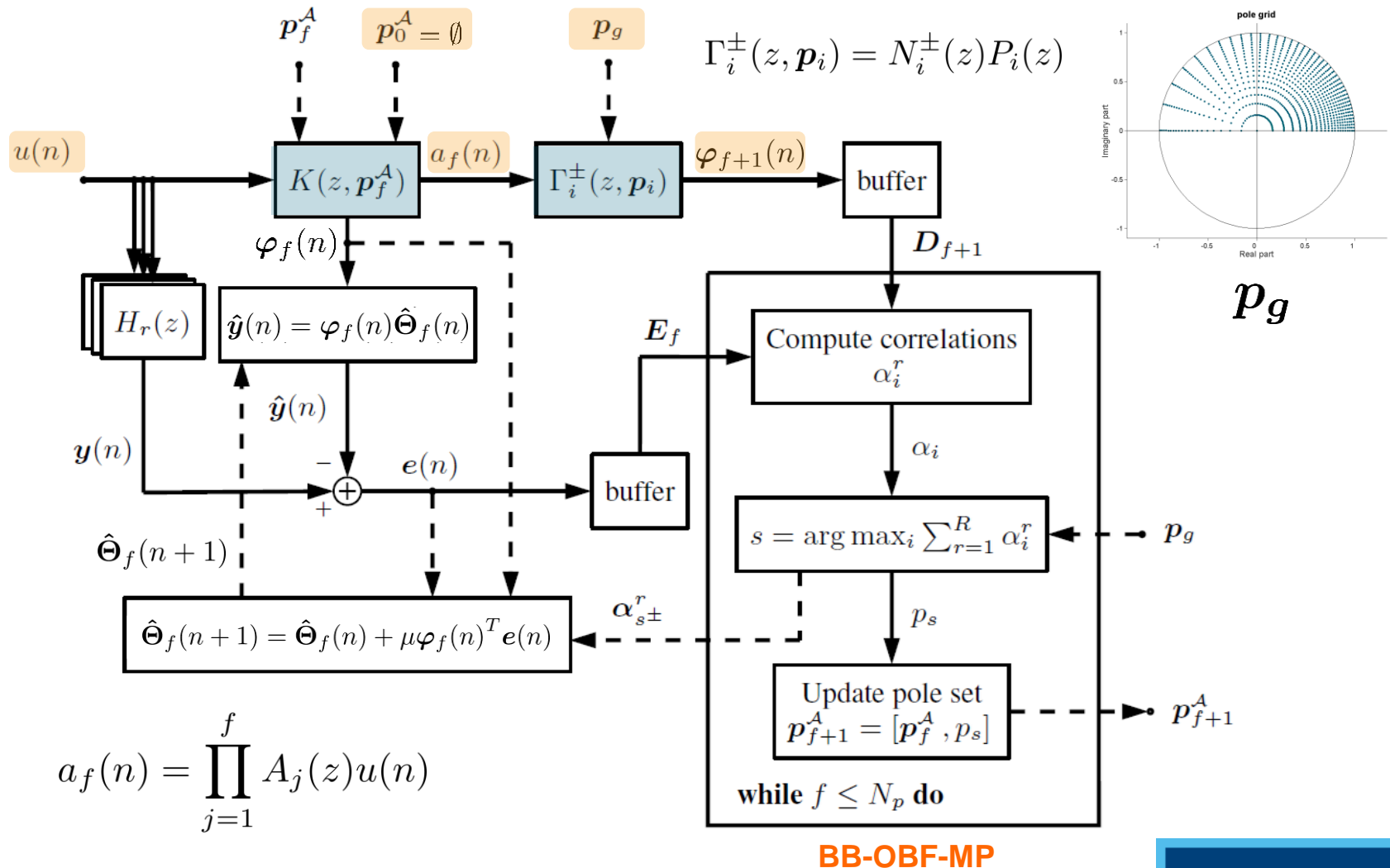
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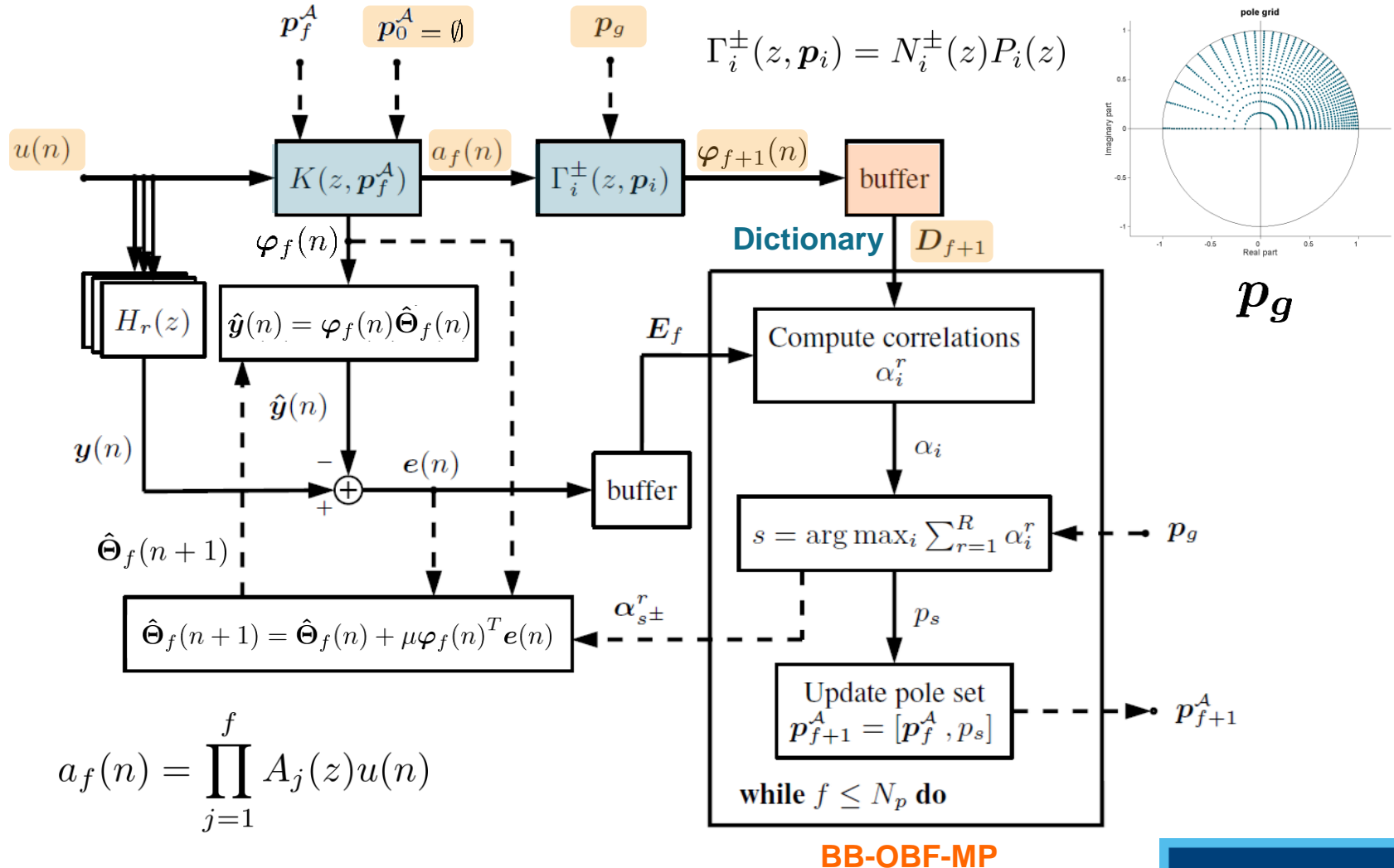
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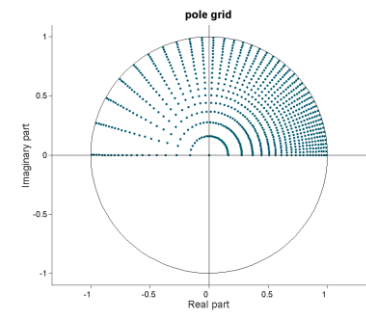
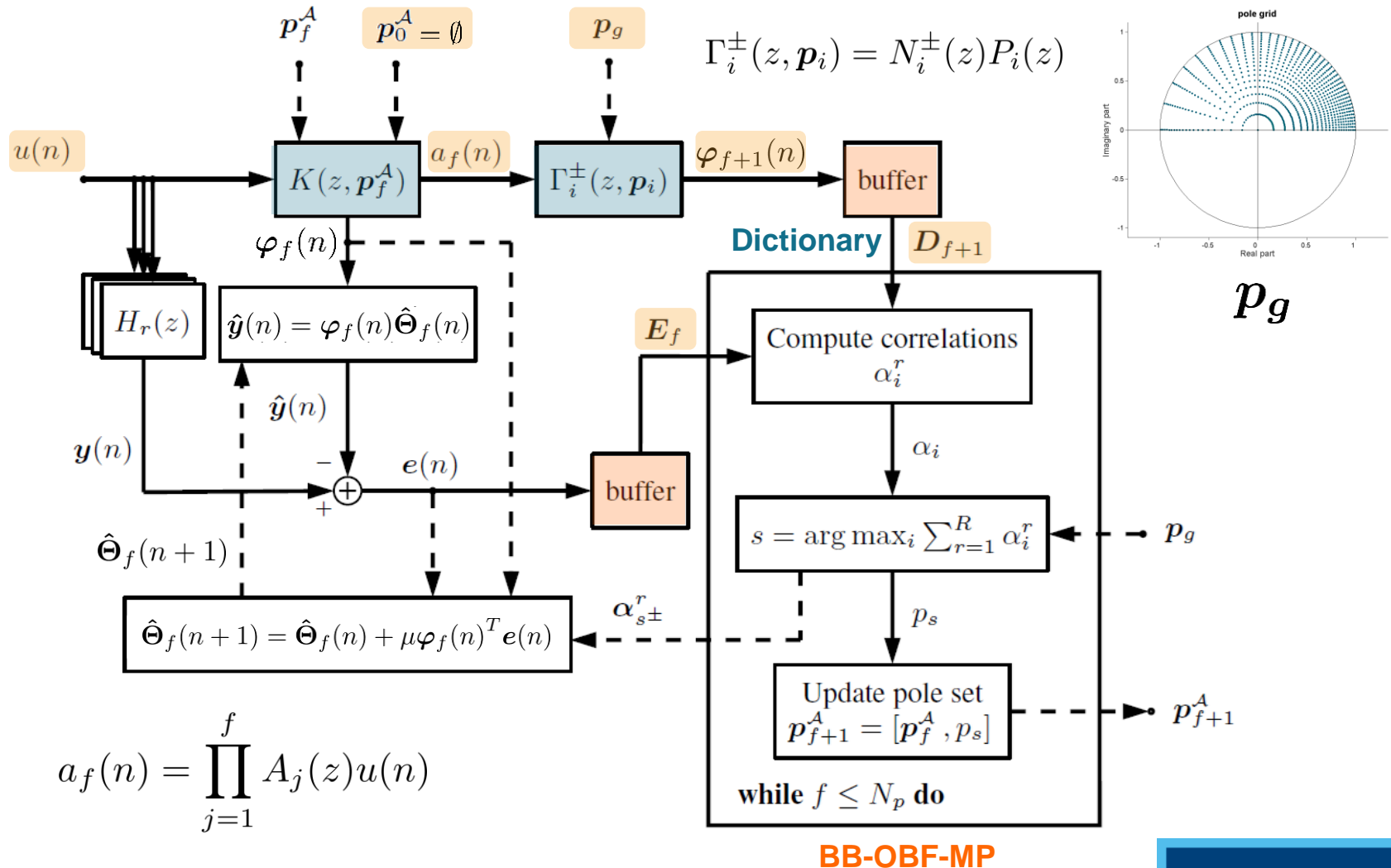


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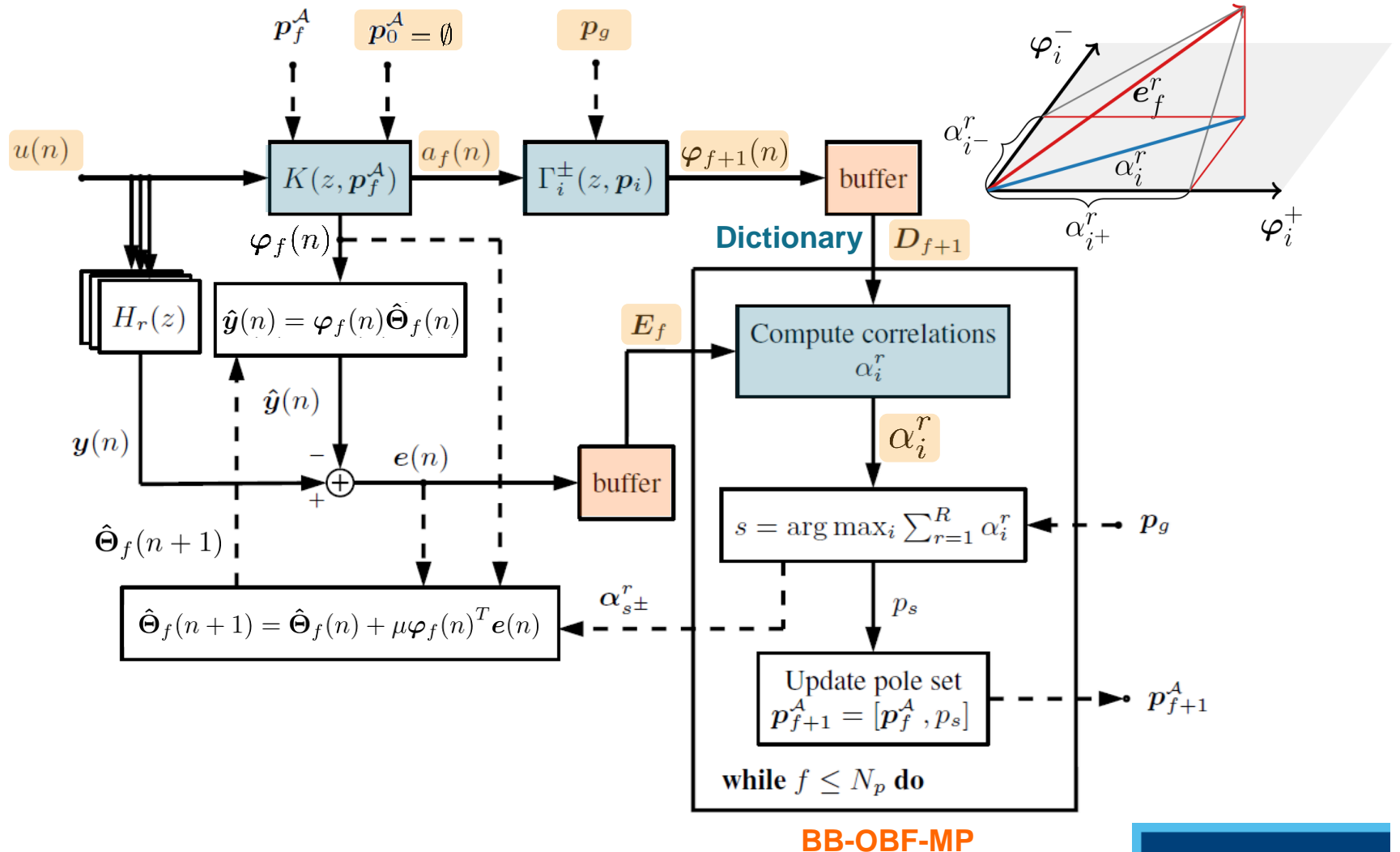
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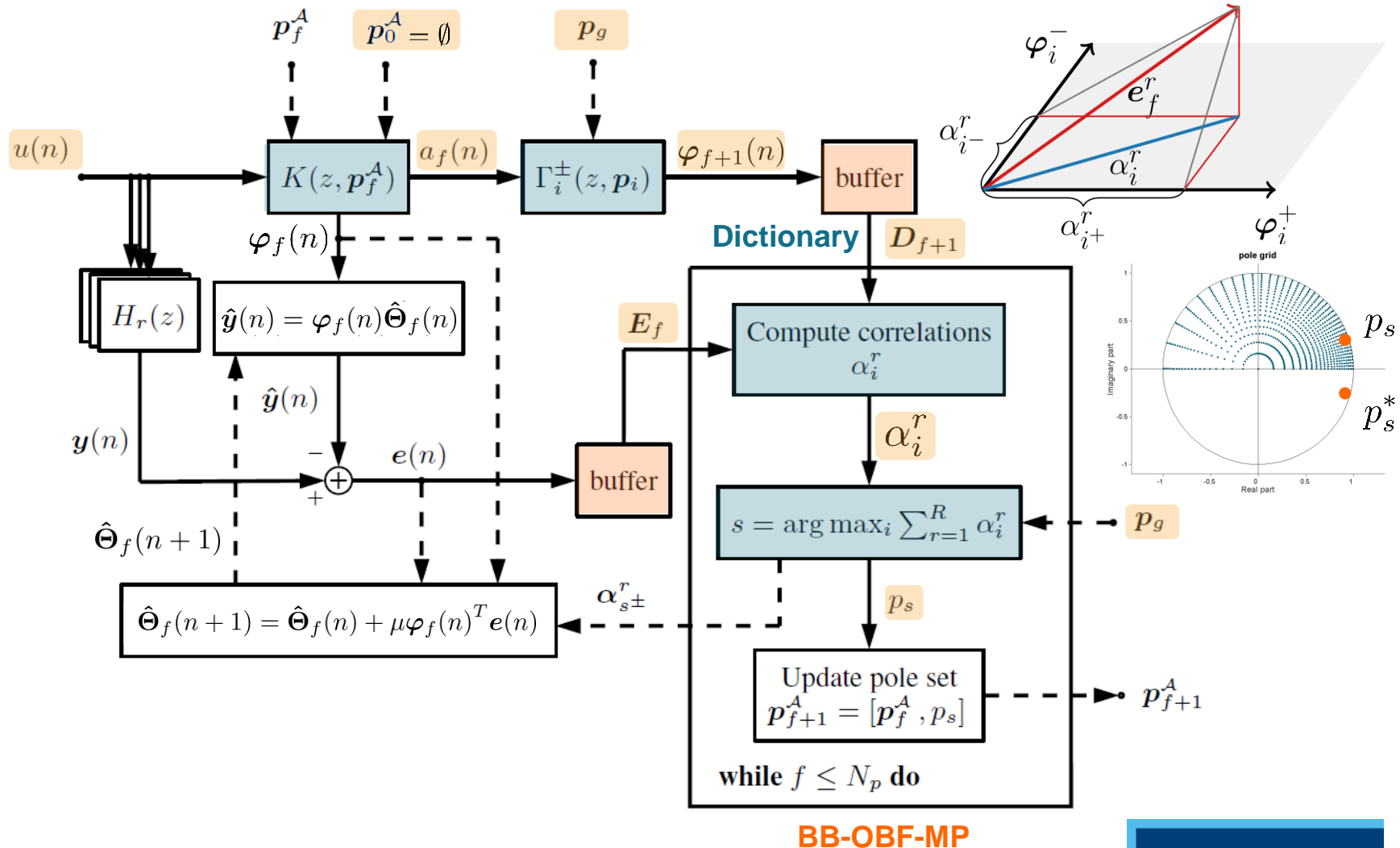
$p_g$

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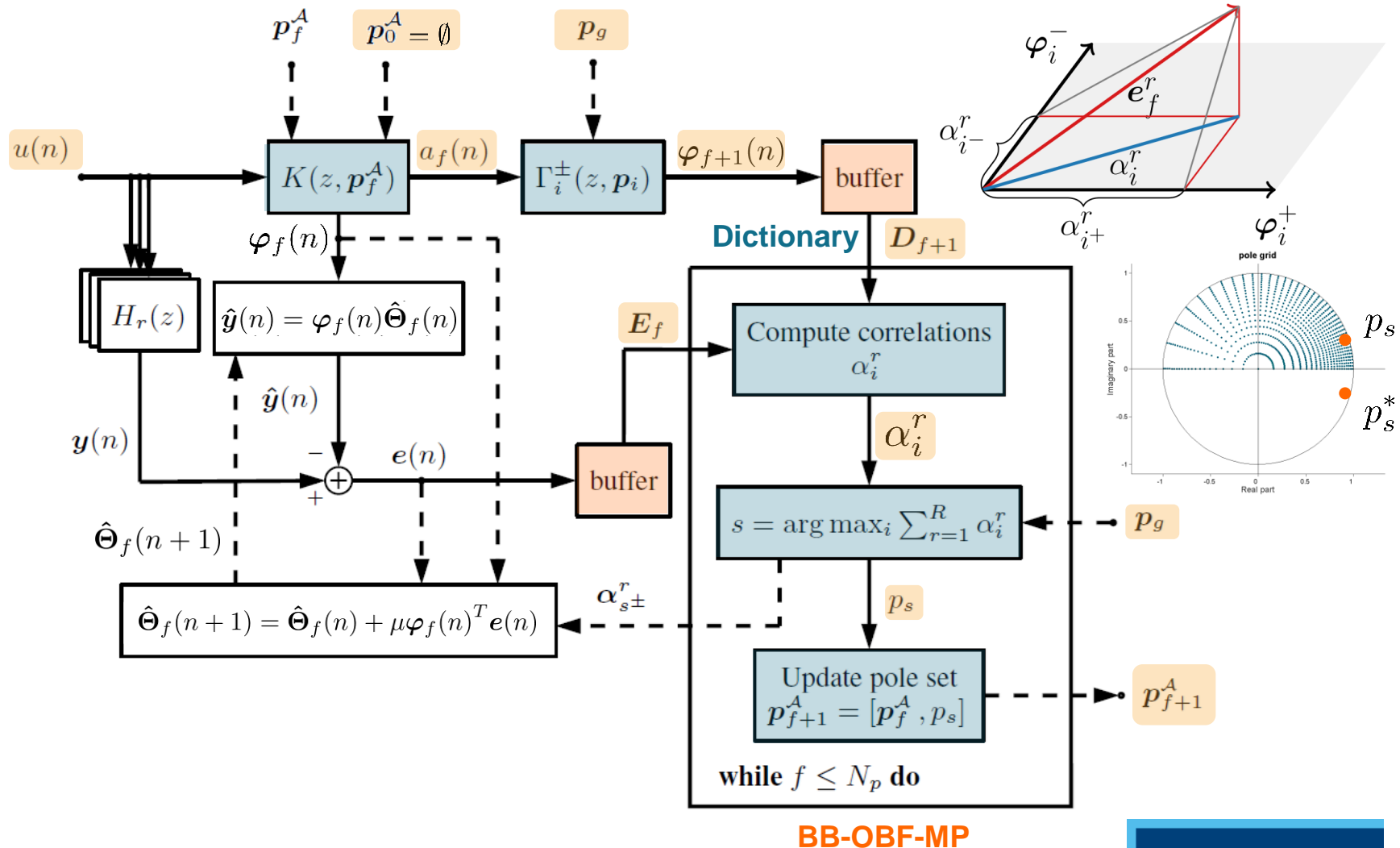
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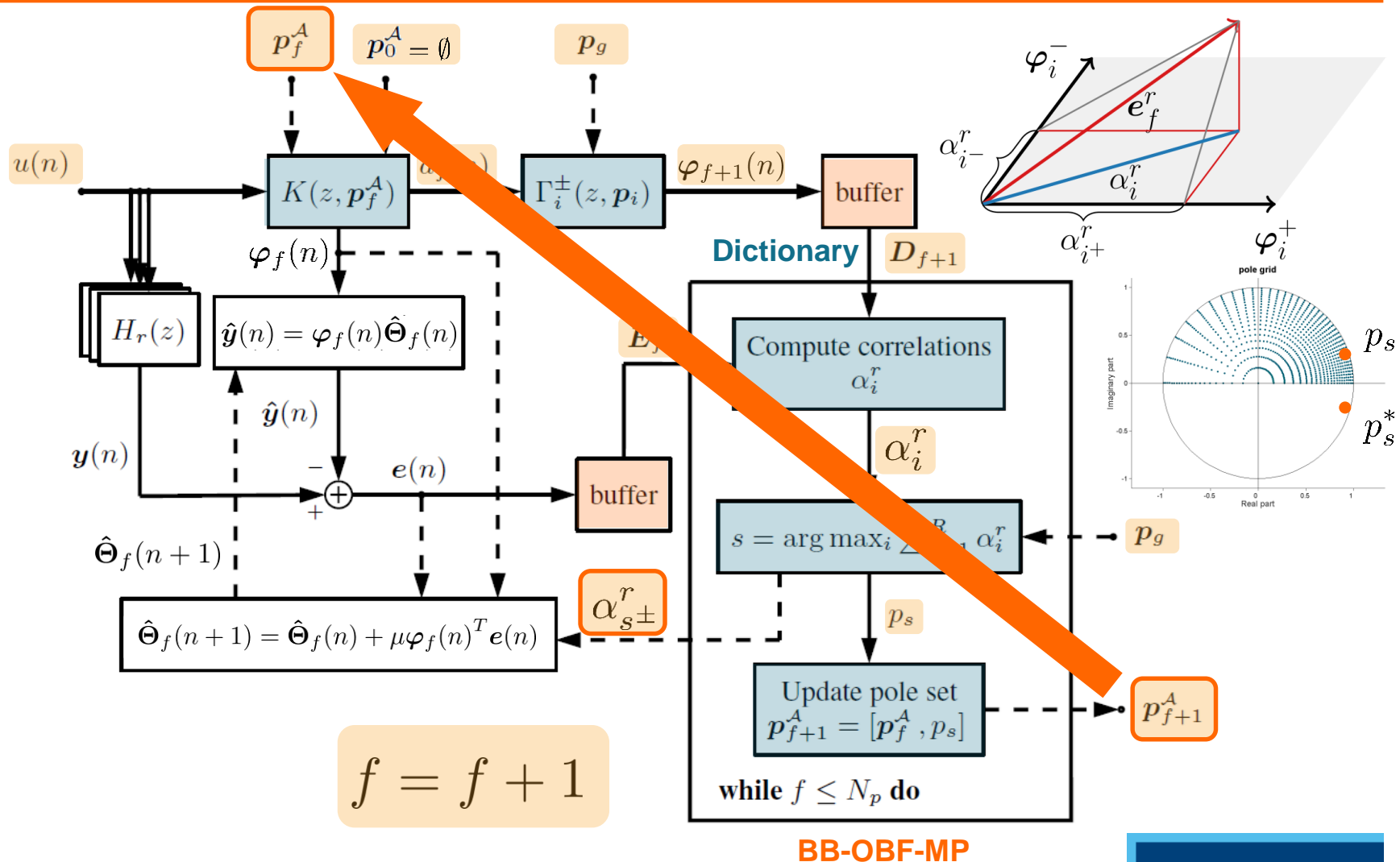
# Multichannel identification algorithm



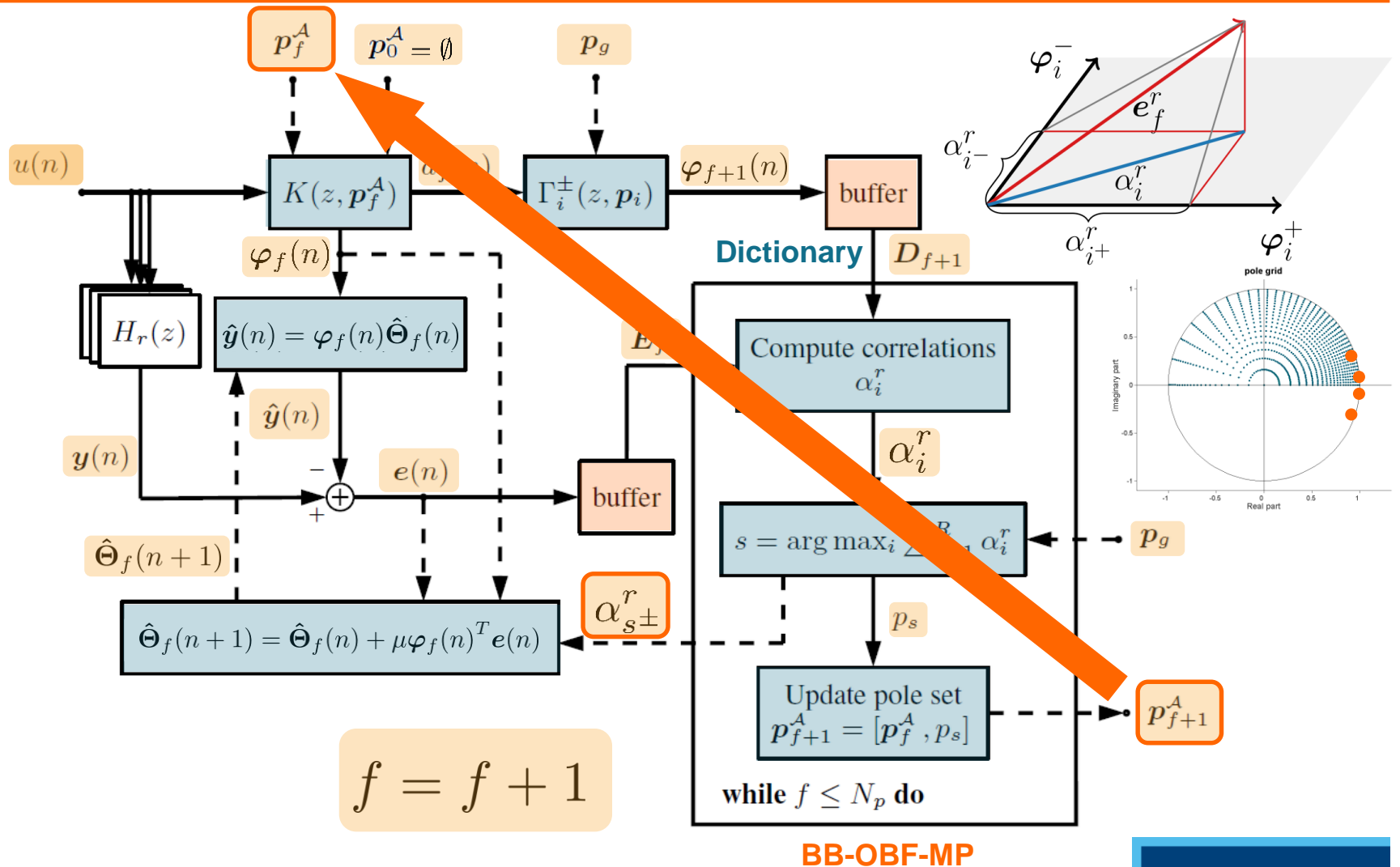
# Multichannel identification algorithm



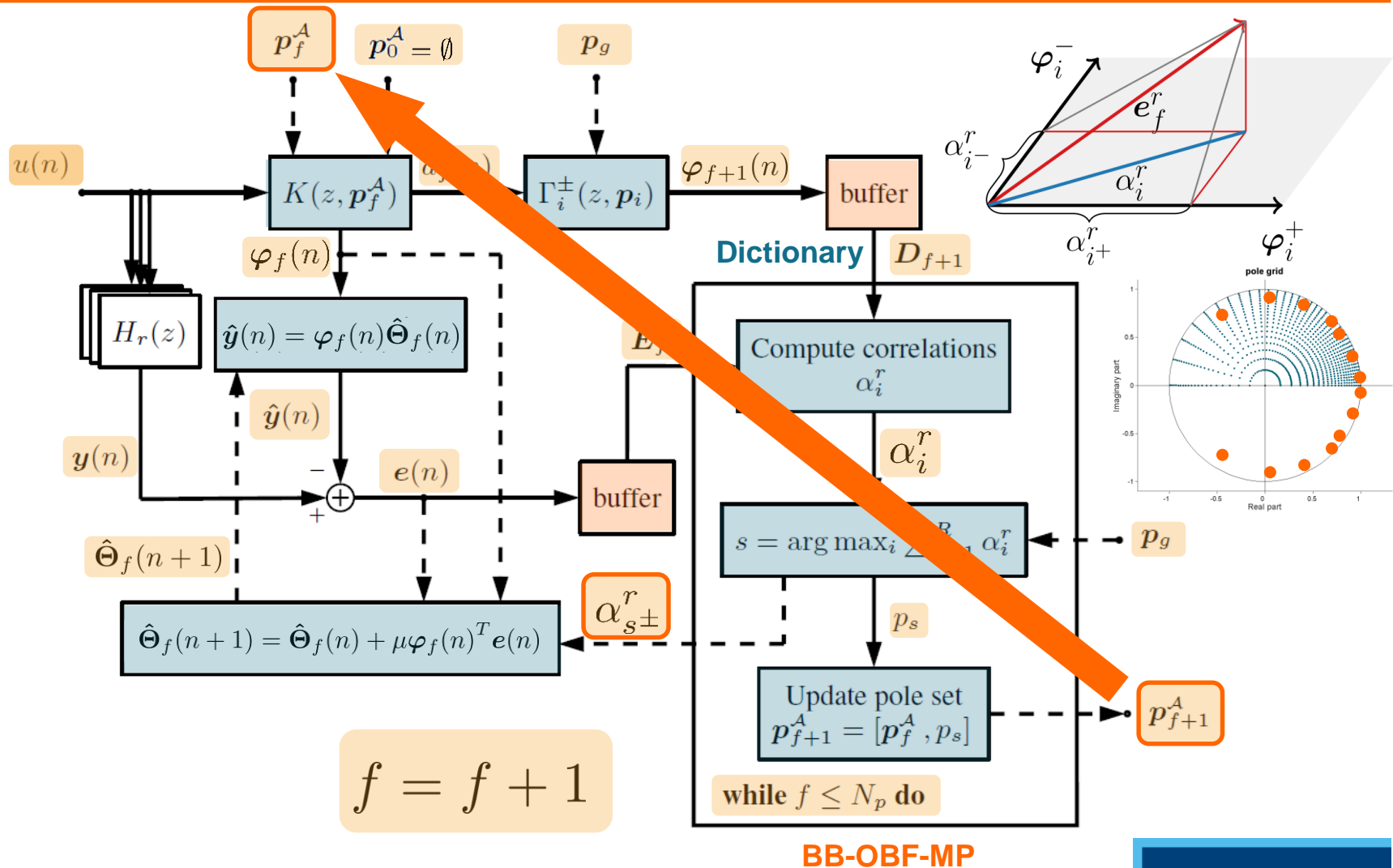
# Multichannel identification algorithm



# Multichannel identification algorithm



# Multichannel identification algorithm





## Adaptive Digital Filters for Room Acoustics Modeling

- ▶ Multichannel Identification Algorithm

### Simulation Results

### Conclusions



Adaptive Digital Filters for Room Acoustics Modeling

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# SUBRIR database – BANG & OLUFSEN



- unoccupied, standard domestic listening room [ISO 628-13]
- source: 2 subwoofers - Genelec 1094A (12-150 Hz) and 7050 (25-120 Hz)
- exponential sine sweep technique (3s sweeps)
- 2 mics, 2 subs, 24 s-m positions: 96 RIRs  
4 source positions, 6 microphone positions



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## Room Description

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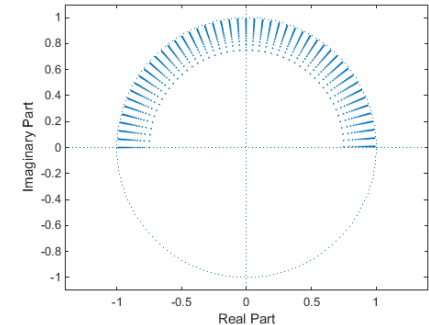
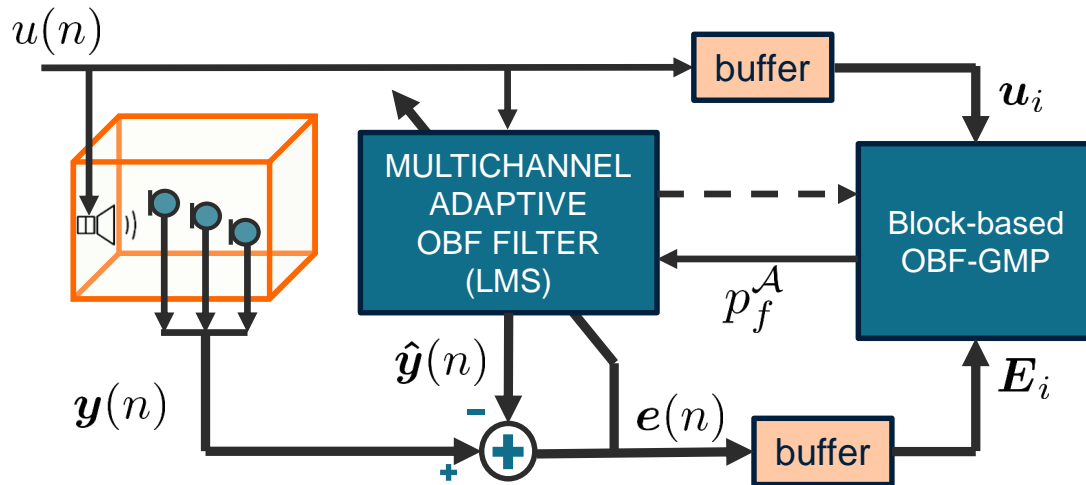
Dimensions	6.35L x 4.09W x 2.40H (m)
Volume	62.3 m <sup>3</sup>
Floor/Ceiling Materials	Wood/Wood (& Rockwool)
Reverb Time	$T_{31.5\text{Hz}} = 1.44s$ $T_{40\text{Hz}} = .69s$ $T_{50\text{Hz}} = 0.74s$ $T_{63\text{Hz}} = 0.53s$ $T_{100\text{Hz}} = 0.47s$ $T_{125\text{Hz}} = 0.62s$

**available for download (coming soon)**

<http://www.dreams-itn.eu/index.php/dissemination/downloads/subrir>

**KU LEUVEN**

# Training – system identification



**Pole grid:**  
3000 poles  
300 angles  
10 radii

Poles estimated from input-output data

Input data = white noise sequence

Output data = input data convolved with  $h(n)$

$N_p = 20$ : number of pole pairs = 40 adaptive coeffs.

$R = 6$ : number of RIRs

$M = 10$ : number of realizations of I/O data

$V = 120$ : combinations of 2 sources - 3 microphones

$VMR = 7200$ : number of estimated pole sets of 20 poles

# Validation setup

Compare the performances in the approximation of RIRs using an FIR filter and an adaptive OBF filter with fixed common poles

Data sets of the same size as the training set, but different combinations:

**Set 1:** same 2 source positions, 3 different microphone positions

**Set 2:** 2 different source positions, 3 different microphone positions

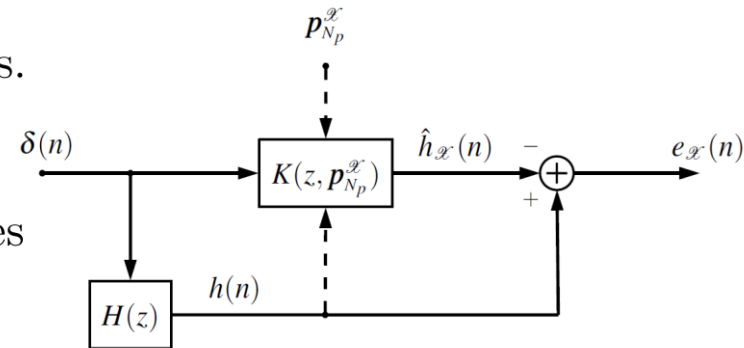
$N_p = 20$ : number of pole pairs = 40 adaptive coeffs.

$R = 6$ : number of RIRs

$M = 10$ : number of realizations of I/O data

$V = 120$ : combinations of 2 sources - 3 microphones

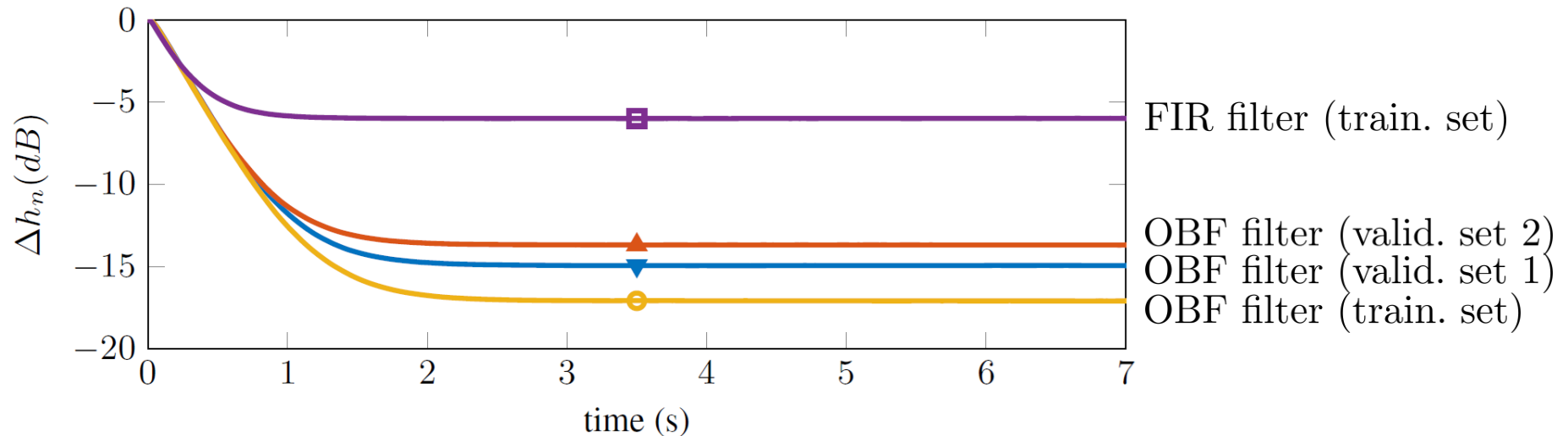
$VMR = 7200$ : number of I/O data sequences



$$\Delta h_n = 10 \log_{10} \left[ \frac{1}{VMR} \sum_{v=1}^V \sum_{m=1}^M \sum_{r=1}^R \frac{\|\mathbf{h}^r - \hat{\mathbf{h}}_{v,m}^{r,n}\|_2^2}{\|\mathbf{h}^r\|_2^2} \right]$$

Average misadjustment

# Validation results



- Orthogonality assures
  - **numerical well-conditioning**
  - **fast convergence** of the filter adaptation (same as FIR filters)
- Reduced estimation error compared to FIR filters
- Robust to variations in the RTF → poles can be fixed after estimation

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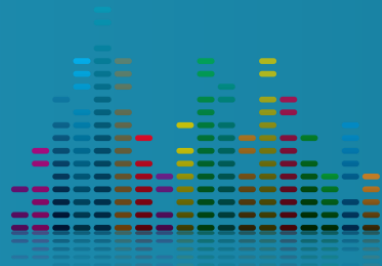


# Conclusions

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## ▶ Summary

- OBF filters for modeling and identifying room acoustic systems motivated by the physical definition of the RIR and by the concept of common acoustical poles (and variable zeros)
- Scalable, stable and well-conditioned Identification algorithm for the estimation of the poles of adaptive OBF filters from multichannel I/O data
- Same convergence rate of adaptation as FIR filters
- Reduced estimation error compared to FIR filters
- Estimated common set of poles robust to variations in the RTF



# DREAMS

<http://www.dreams-itn.eu/>



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