

Sparse Modeling of The Early Part of Noisy Room Impulse Responses with Sparse Bayesian Learning

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 May 2022



1. Background

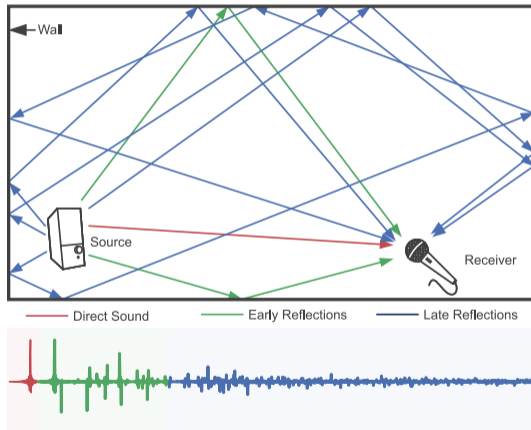
2. Proposed Method

3. Results

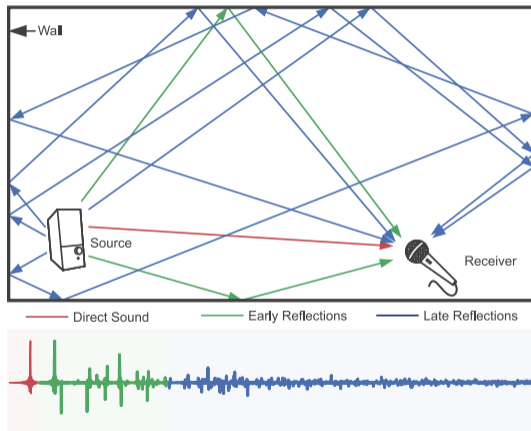
4. Conclusions

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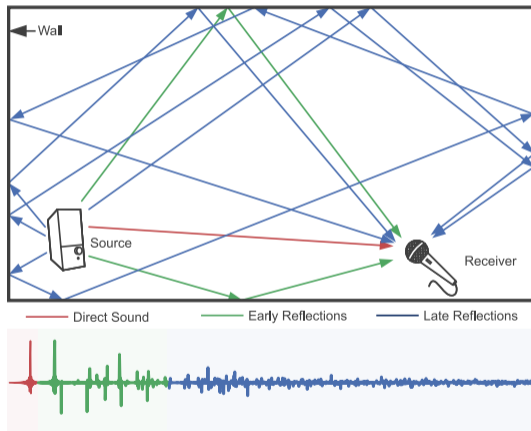
- A RIR in reverberation environment consists of
 - **Direct Sound**
 - **Early Reflections**
 - **Late Reflections**
- The early part (Direct Sound + Early Reflections) of a RIR is relatively sparse.
- Modeling of the early part of RIRs have many applications, such as
 - Room Geometry Reconstruction
 - Augmented and Virtual Reality
 - Dereverberation



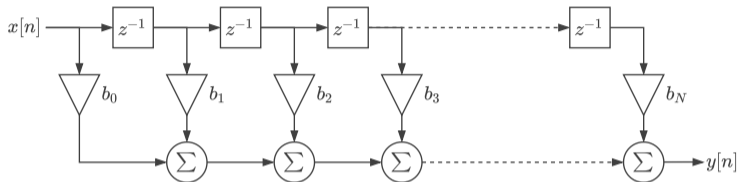
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- RIRs typically are modeled as **long** FIR filters which may have thousands of coefficients.



- ℓ_1 -regularization technology (LASSO) can be used to reduce the coefficient number of the early part of RIRs.

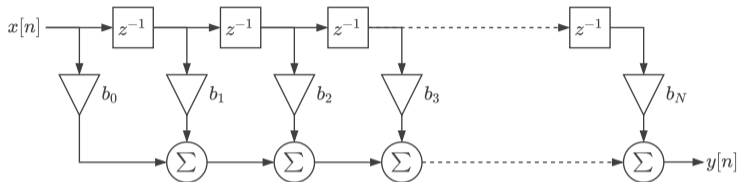
LASSO

- Being **sensitive** to regularization parameters and requiring finding optimal regularization parameters.
 - Grid-search is **computational heavy**.
 - Cross-validation requires **training data**.

Sparse Bayesian Learning (SBL)

- Being **insensitive** to user parameters.
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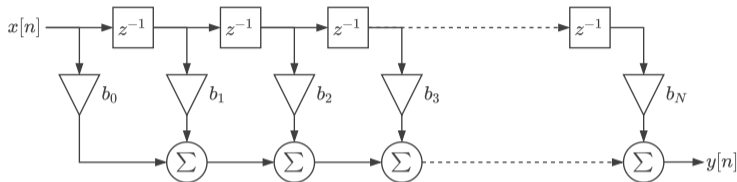
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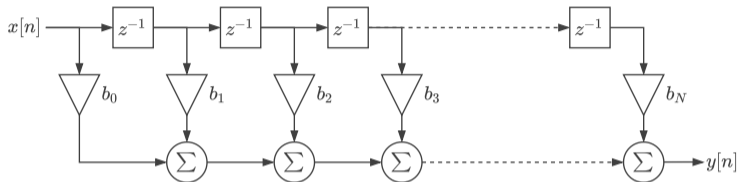
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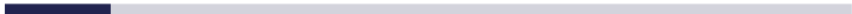
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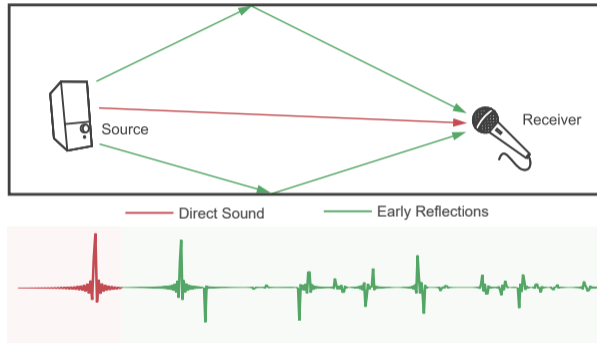
- Discretizing the RIR measurements in the time-delay domain:

$$r((n-1)T_s) = \sum_{m=1}^M \beta_m s((n-1)T_s - (m-1)T_\Delta) + w((n-1)T_s)$$

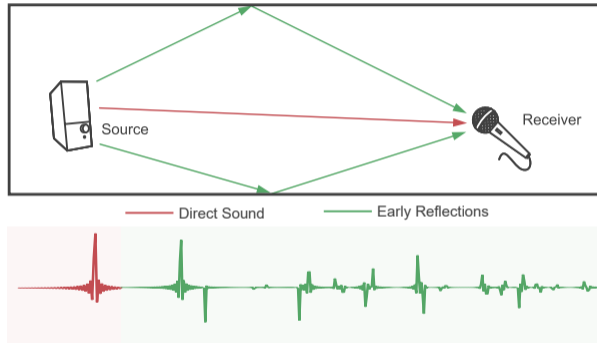
Measurements (blue arrow pointing to $r((n-1)T_s)$)
 Source Signal (green arrow pointing to $s((n-1)T_s - (m-1)T_\Delta)$)
 Model Coefficients (red arrow pointing to β_m)
 Noise (orange arrow pointing to $w((n-1)T_s)$)

- Converting to matrix form:

$$\begin{array}{c} \text{Measurement} \\ \mathbf{y} \\ \left[\begin{array}{c} \square \\ \square \\ \square \\ \square \\ \square \end{array} \right] \end{array} = \begin{array}{c} \text{Redundant Dictionary} \\ \Phi \\ \left[\begin{array}{cccccc} \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \end{array} \right] \end{array} \times \begin{array}{c} \text{Model Coefficients} \\ \mathbf{x} \\ \left[\begin{array}{c} \square \\ \square \\ \square \\ \square \\ \square \end{array} \right] \end{array} + \begin{array}{c} \text{Noise} \\ \mathbf{w} \\ \left[\begin{array}{c} \square \\ \square \\ \square \\ \square \\ \square \end{array} \right] \end{array}$$



- Typical Scene: the early part of a RIR contains **very few** impulse responses.
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Measurement y (Known) = Redundant Dictionary Φ (Determined by the Source Signal) \times Model Coefficients x (Unknown) + Noise w (Unknown)

The diagram shows the equation $y = \Phi x + w$ with visual representations of each term:

- Measurement y (Known):** A vertical column of 6 blue squares.
- Redundant Dictionary Φ (Determined by the Source Signal):** A 6x8 grid of green squares.
- Model Coefficients x (Unknown):** A vertical column of 8 red squares.
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- **Problem 1:** Given y , how to recover x with the a priori that x is sparse?
- **Problem 2:** If the source signal is unknown, how to determine Φ ?

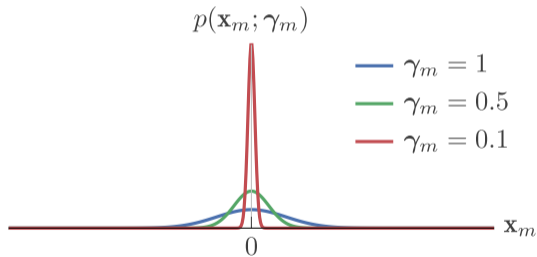
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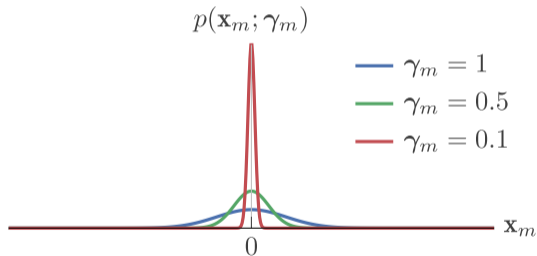
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- **Prior:** SBL assumes the m -th component of \mathbf{x} follows a zero-mean Gaussian distribution with variance γ_m .

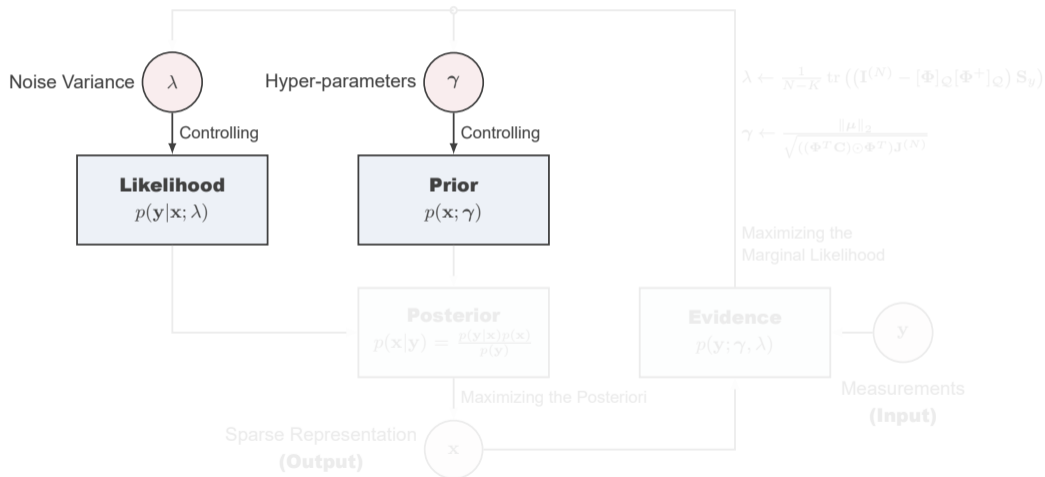


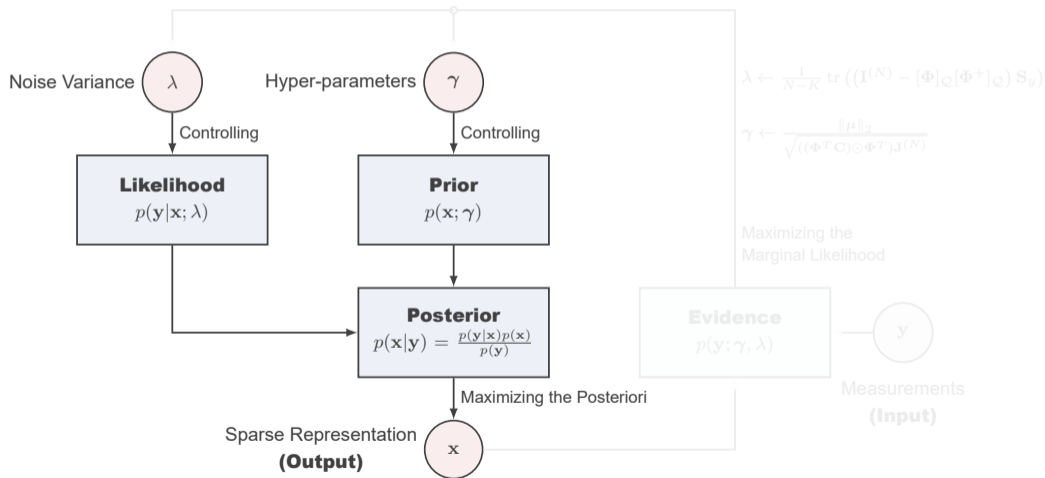
- **Likelihood:** SBL assumes the noise follows a zero-mean Gaussian distribution with variance λ .

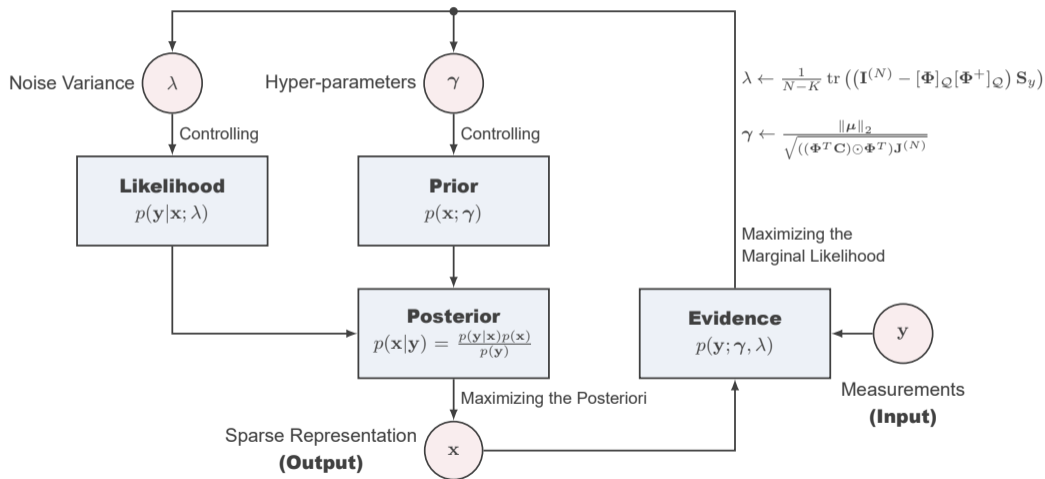
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- **Source Signal:** Assume the source signal is a Gaussian-modulated pulse.

$$\text{Gaussian-modulated pulse} = \exp(-\theta^2 t^2) \times \cos(2\pi \xi t)$$

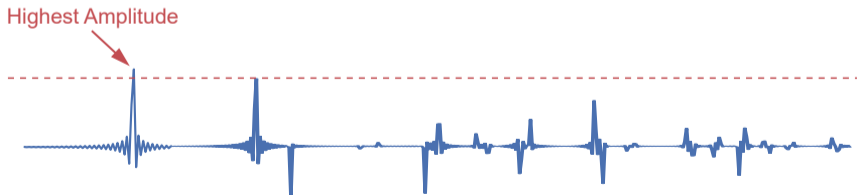
- **Direct Sound:** Assume the direct sound has the highest amplitude and is the time-delayed and scaled version of the source signal.



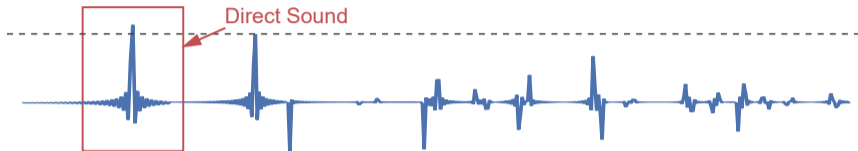
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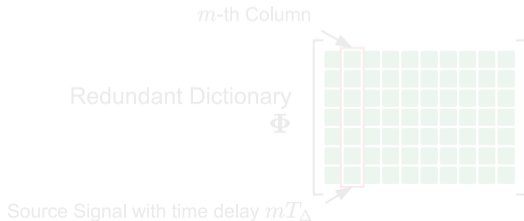
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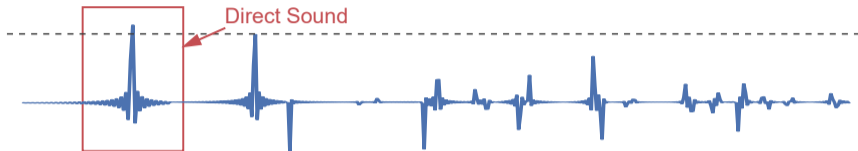
- The direct sound can be extracted by using a **rectangle window** around the peak.



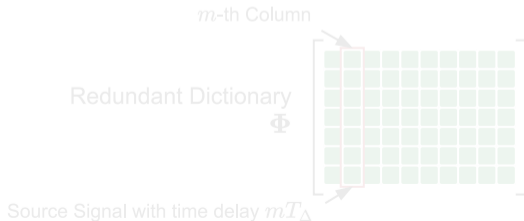
- The parameters of the Gaussian-modulated pulse can be estimated by minimizing the **mean square error** between the measured and reconstructed direct sound.
- The dictionary can be built with the various **time-delayed** source signal.



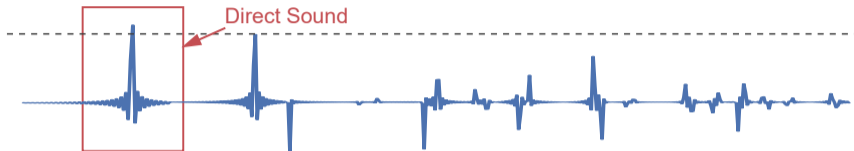
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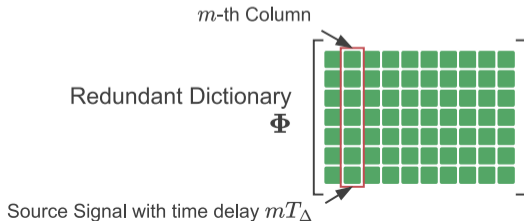
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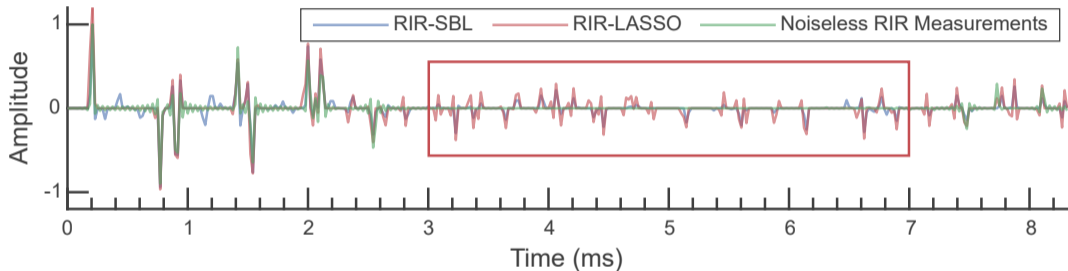


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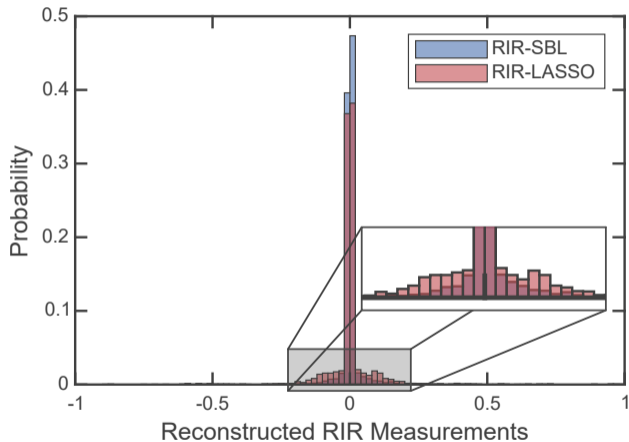
3. Results



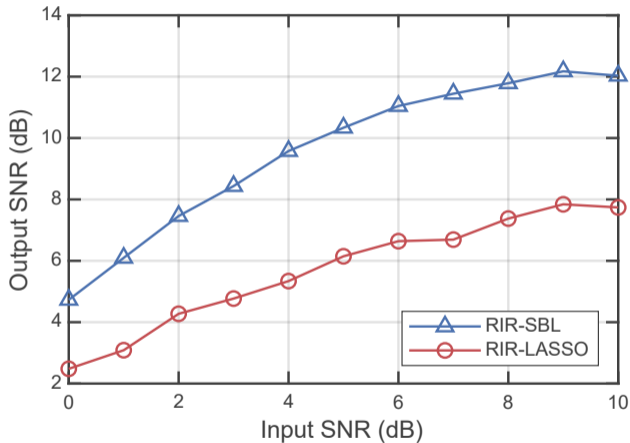


- For the simulated RIR measurements¹, RIR-SBL shows less noise sensitiveness to the noise than RIR-LASSO in the time interval [3,7] ms.

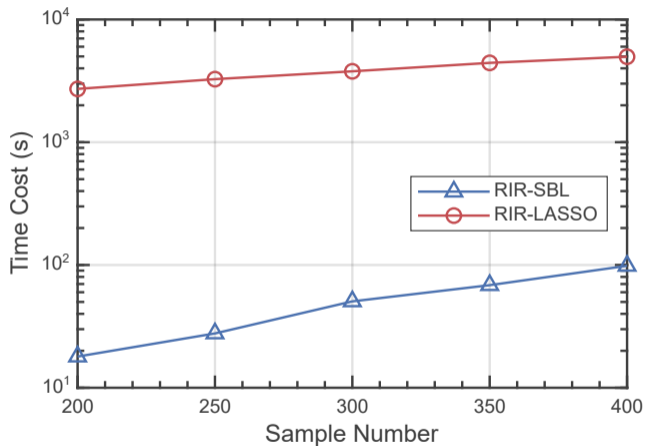
¹The simulated noiseless RIR measurements are generated by the image method using the gpuRIR library.



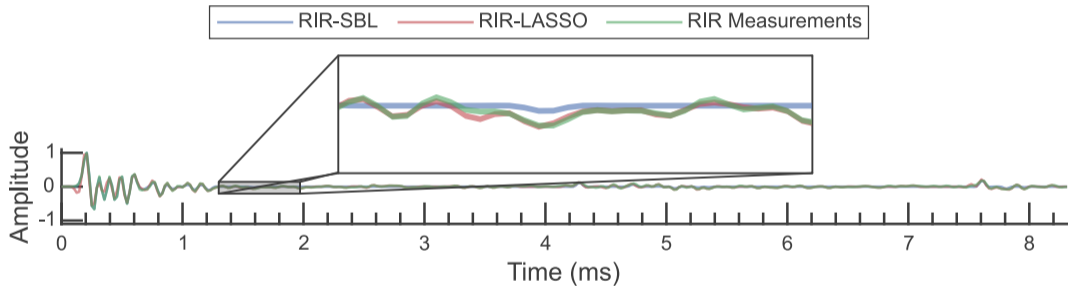
- The reconstruct RIR measurements of RIR-SBL is sparser than that of RIR-LASSO.



- RIR-SBL provides an improvement in the output SNR compared to RIR-LASSO.

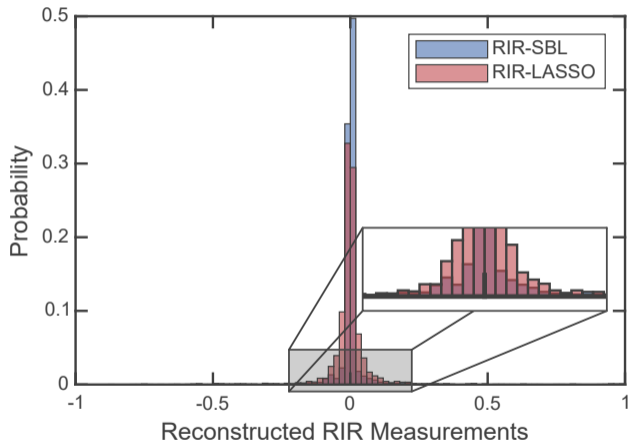


- RIR-SBL requires much less computation than RIR-LASSO.



- For the real-world RIR measurements², RIR-SBL performs better in noise reduction.

²The real-world RIR measurements are taken from the acoustic characterization of environments (ACE) database.



- RIR-SBL is more sparse-promoting than RIR-LASSO in real-world RIR processing.

4. Conclusions

- The proposed RIR-SBL works well in **noisy conditions** and can improve the output SNR.
- RIR-SBL is **computationally efficient**.
- RIR-SBL can effectively exploit the sparse structure of the early part of RIRs to promote the **sparsity** of the model.

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Thank You!