

Zigzag Ordered Walsh Matrix for Compressed Sensing Image Sensor

Hosei University, Japan

Jinyao Zhou

jinyao.zhou.9r@stu.hosei.ac.jp



Guideline

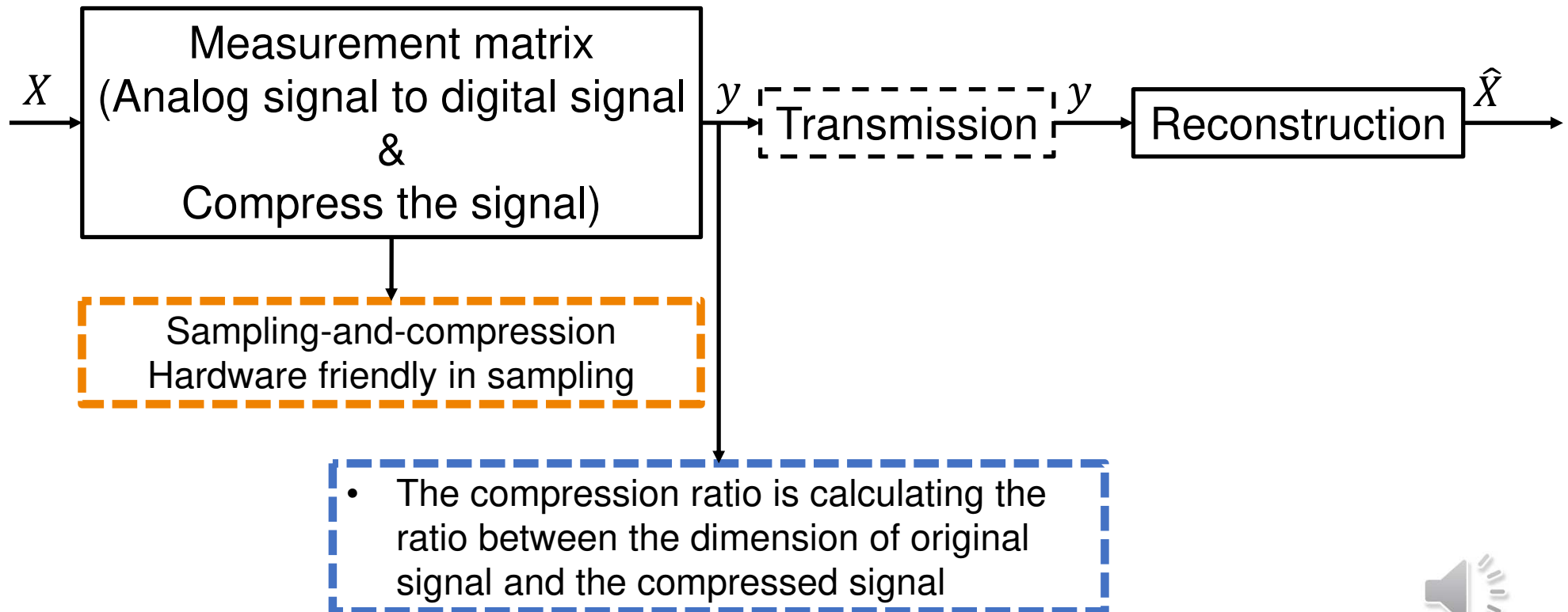
- Introduction
- Proposals
- Experimental results



Introduction



The codec based on Compressed Sensing:



Classic measurement matrix : Hadamard and Walsh

they provide good sensing performance, fast reconstruction, and are hardware friendly

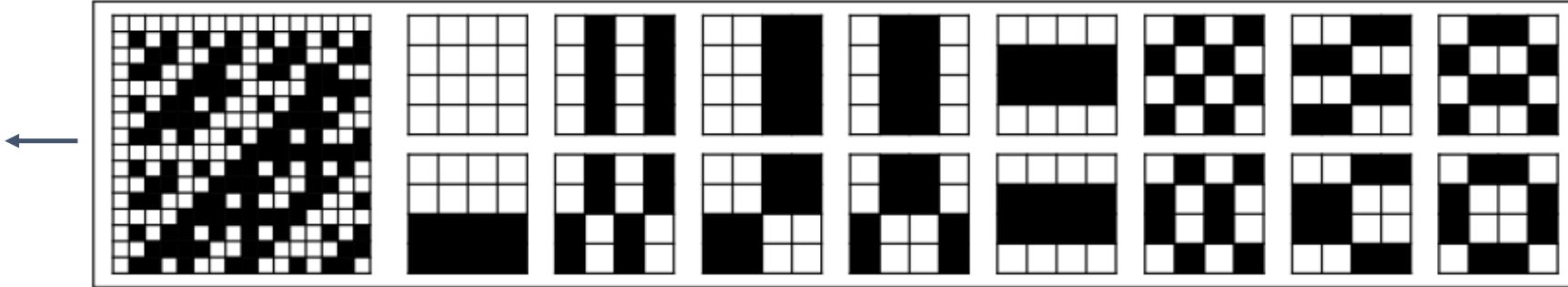
Problems of Hadamard and Walsh :

pretty poor image quality when further reduced sampling rates lower than 60%

To solve problems :

related work: Russian-doll, Cake-cutting, GCS+S method 

example of Hadamard matrix patterns



Related work: Russian-doll, Cake-cutting, GCS+S method :

investigate the effect of Hadamard and Walsh projection order selection on image reconstruction quality by simply reordering orthogonal matrices

Existing Problems :

do not achieve better reconstructed image performance, especially at low SR



Proposals



To solve problems :

we design a measurement matrix that is hardware friendly and provides high-quality results under low sampling rates.

Hardware friendly  chose Walsh matrix

Provides high-quality results under low SR:

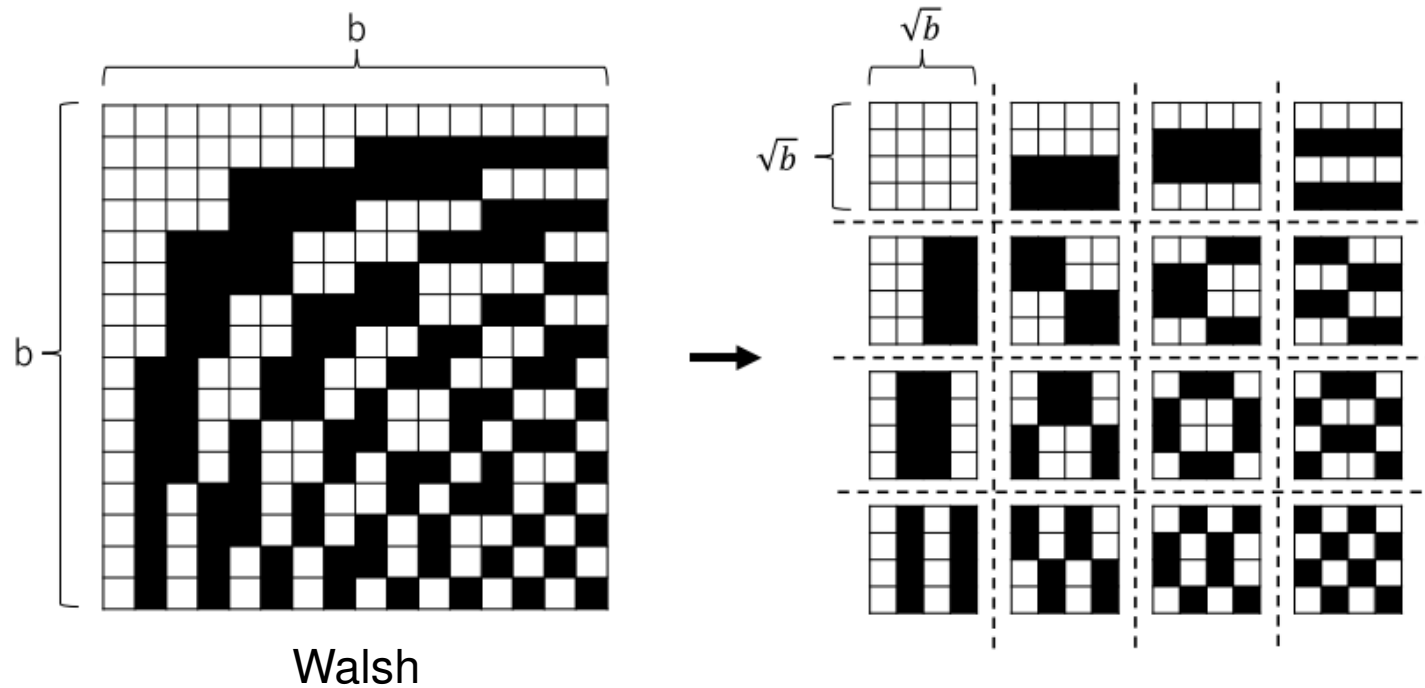
under various SR, **remains the lowest frequency patterns** which are the most critical patterns for determining the image quality



Using zigzag to reorder the patterns of Walsh

The proposed matrix named **Zigzag ordered Walsh (ZoW)**

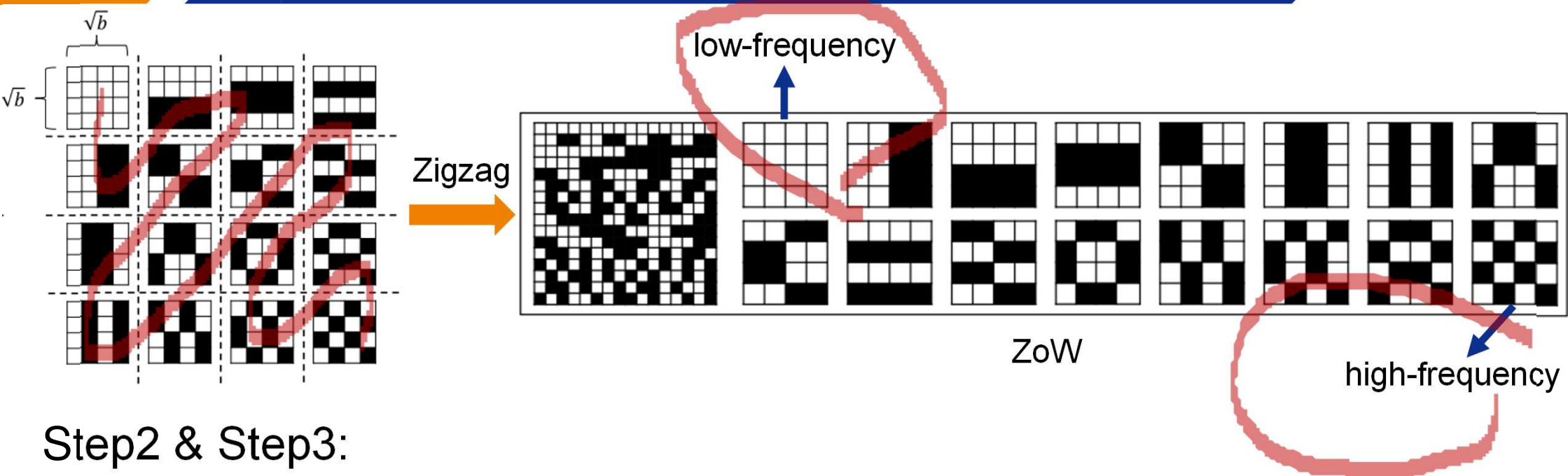




Step1:

we partition the Walsh matrix into several measurement patterns, where the size of each piece is equal to $\sqrt{b} \times \sqrt{b}$





Step2 & Step3:

apply zigzag scramble to the multiple pieces of Walsh matrix and vectorize each piece and stack it back into ZoW matrix



so that ZoW can extract features from low frequency components to high frequency components



Experimental Results



Table 1: Recovery error via PSNR and SSIM comparisons of Toeplitz, Hadamard, Walsh, PoW and ZoW (this work), where $b = 16$ and $SR = 5\%$

Images SR=5%	Toeplitz		Hadamard		Walsh		PoW		this work	
	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
Monarch	15.54	0.11	16.98	0.27	17.31	0.30	17.33	0.30	20.51	0.46
Parrots	19.19	0.12	20.94	0.28	20.68	0.25	20.68	0.24	23.62	0.39
barbara	19.04	0.11	21.16	0.33	20.07	0.21	20.08	0.22	22.74	0.39
boats	18.22	0.07	19.83	0.26	20.87	0.24	20.90	0.25	23.57	0.37
cameraman	17.66	0.08	19.65	0.19	18.87	0.29	18.86	0.28	21.44	0.29
foreman	21.80	0.11	22.80	0.23	24.63	0.32	24.67	0.33	28.01	0.41
house	20.42	0.08	21.80	0.19	22.93	0.25	22.93	0.24	25.64	0.28
lena	19.09	0.12	21.78	0.36	19.74	0.17	19.74	0.17	23.66	0.42
Average	18.87	0.10	20.62	0.26	20.64	0.25	20.65	0.25	23.65	0.38



Table 2: Recovery error via PSNR and SSIM comparisons of Toeplitz, Hadamard, Walsh, PoW and ZoW (this work), where $b = 16$ and $SR = 10\%$

Images SR=10%	Toeplitz		Hadamard		Walsh		PoW		this work	
	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
Monarch	16.01	0.17	17.06	0.29	17.49	0.33	19.83	0.47	22.36	0.58
Parrots	19.72	0.18	21.02	0.31	20.85	0.28	22.88	0.39	25.15	0.49
barbara	19.58	0.19	21.29	0.36	20.14	0.24	22.05	0.36	23.48	0.50
boats	18.95	0.16	20.02	0.31	21.01	0.27	23.13	0.38	25.59	0.50
cameraman	18.23	0.14	19.86	0.25	19.00	0.35	20.64	0.40	23.01	0.42
foreman	22.06	0.16	22.84	0.25	24.84	0.37	27.79	0.47	29.59	0.52
house	20.93	0.15	22.02	0.25	23.22	0.35	25.62	0.38	27.80	0.41
lena	20.04	0.21	21.96	0.41	19.81	0.19	21.88	0.32	25.17	0.53
Average	19.44	0.17	20.76	0.30	20.80	0.30	22.98	0.40	25.27	0.49



Table 3: Recovery error via PSNR and SSIM comparisons of Toeplitz, Hadamard, Walsh, PoW and ZoW (this work), where $b = 16$ and $SR = 15\%$

Images SR=15%	Toeplitz		Hadamard		Walsh		PoW		this work	
	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
Monarch	16.22	0.21	17.13	0.30	21.67	0.57	20.70	0.55	23.98	0.68
Parrots	20.08	0.22	21.10	0.32	24.33	0.46	23.90	0.48	26.47	0.60
barbara	19.93	0.24	21.36	0.37	22.78	0.43	22.69	0.44	24.46	0.62
boats	19.47	0.20	20.09	0.32	24.31	0.46	24.00	0.45	27.28	0.61
cameraman	18.57	0.19	19.96	0.28	21.94	0.47	21.44	0.47	24.29	0.51
foreman	22.12	0.18	22.94	0.26	29.23	0.54	29.05	0.55	31.29	0.62
house	21.60	0.20	22.09	0.27	27.11	0.49	26.61	0.48	29.42	0.51
lena	20.50	0.26	22.03	0.42	23.51	0.43	22.78	0.42	26.82	0.66
Average	19.81	0.21	20.84	0.32	24.36	0.48	23.90	0.48	26.75	0.60



	SR=5%	SR= 10%	SR= 15%	SR=5%	SR= 10%	SR= 15%
Toeplitz	 PSNR: 20.42 SSIM: 0.08	 PSNR: 20.93 SSIM: 0.15	 PSNR: 21.60 SSIM: 0.20	 PSNR: 21.80 SSIM: 0.11	 PSNR: 22.06 SSIM: 0.16	 PSNR: 22.12 SSIM: 0.18
Hadamard	 PSNR: 21.80 SSIM: 0.19	 PSNR: 22.02 SSIM: 0.25	 PSNR: 22.09 SSIM: 0.27	 PSNR: 22.80 SSIM: 0.23	 PSNR: 22.84 SSIM: 0.25	 PSNR: 22.94 SSIM: 0.26
Walsh	 PSNR: 22.93 SSIM: 0.25	 PSNR: 23.22 SSIM: 0.35	 PSNR: 27.11 SSIM: 0.49	 PSNR: 24.63 SSIM: 0.32	 PSNR: 24.84 SSIM: 0.37	 PSNR: 29.23 SSIM: 0.54
PoW	 PSNR: 22.93 SSIM: 0.24	 PSNR: 25.62 SSIM: 0.38	 PSNR: 26.61 SSIM: 0.48	 PSNR: 24.67 SSIM: 0.33	 PSNR: 27.79 SSIM: 0.47	 PSNR: 29.05 SSIM: 0.55
this work	 PSNR: 25.64 SSIM: 0.28	 PSNR: 27.80 SSIM: 0.41	 PSNR: 29.42 SSIM: 0.51	 PSNR: 28.01 SSIM: 0.41	 PSNR: 29.59 SSIM: 0.52	 PSNR: 31.29 SSIM: 0.62



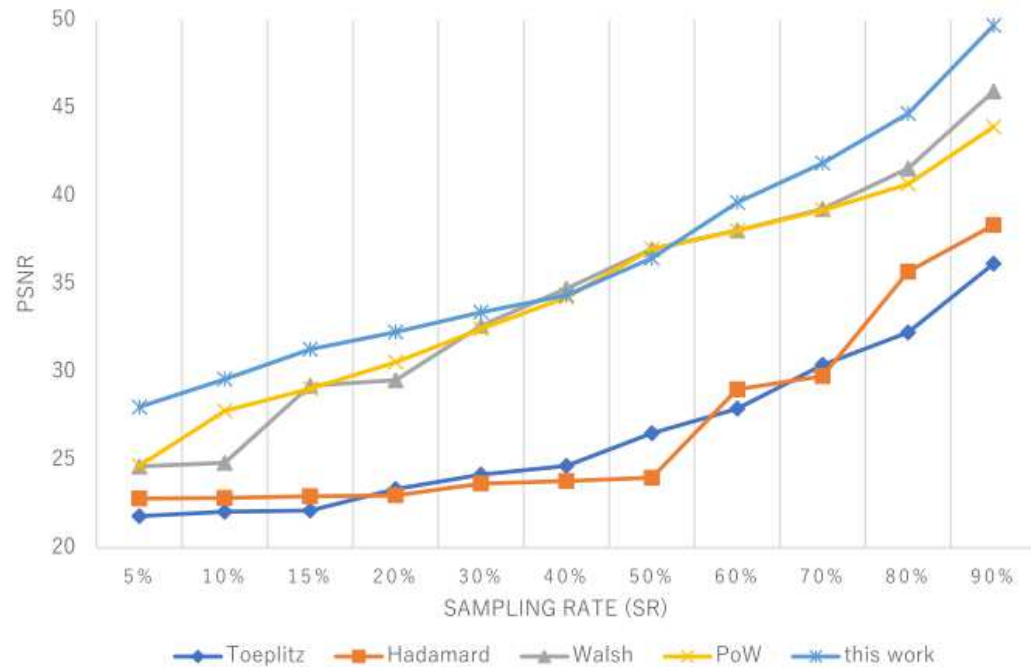


Figure 5: Comparison of recovery error via PSNR of Toeplitz, Hadamard, Walsh, PoW and ZoW (this work), where $b = 16$, $n = b \times b = 256$, and $SR \in \{5\%, 10\%, 15\%, \dots, 90\%\}$.

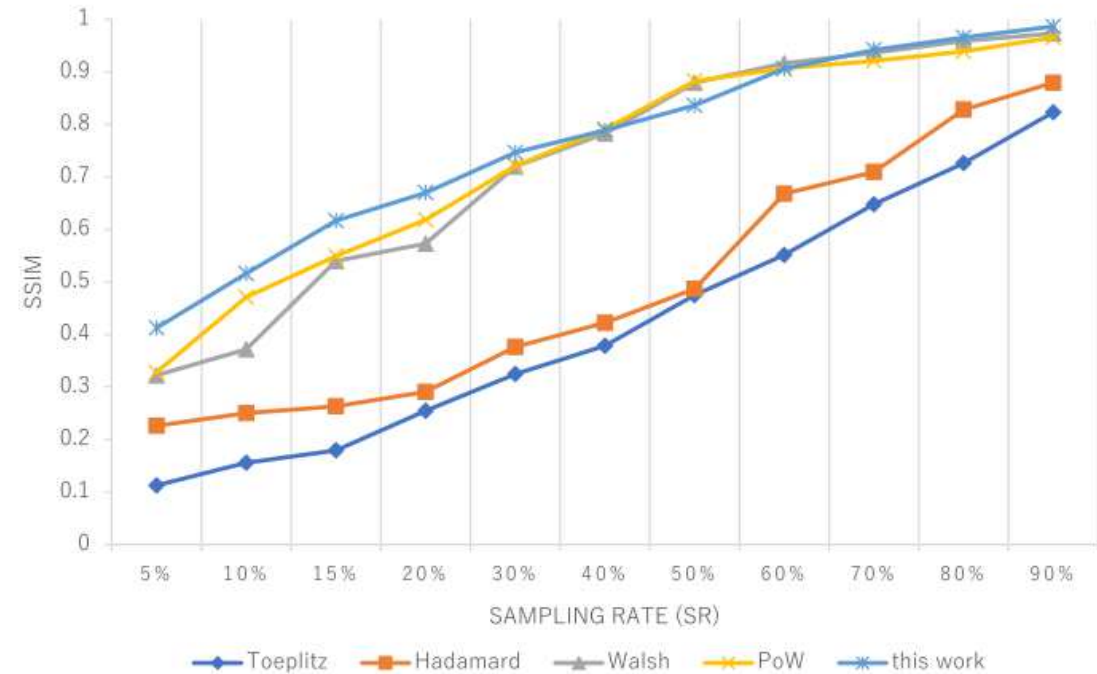


Figure 6: Comparison of recovery error via SSIM of Toeplitz, Hadamard, Walsh, PoW and ZoW (this work), where $b = 16$, $n = b \times b = 256$, and $SR \in \{5\%, 10\%, 15\%, \dots, 90\%\}$.



Conclusion

- The Walsh matrix provides good sensing performance and high reconstruction efficiency with hardware friendly
- we proposed a new structured measurement matrix called the Zigzag ordered Walsh matrix (ZoW) by using zigzag to reorder the patterns of Walsh
- the low-frequency patterns are in the upper-left corner, and the frequency increases according to the zigzag scan order so that under various sampling rates ZoW can extract features from low frequency components to high frequency components.

Thank you

For your listening

