

# Can LLM Find the Green Circle? Investigation and Human-guided Tool Manipulation for Compositional Generalization

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## Introduction

### Background

- Natural languages are composed by individual components.
- Optimal models should generalize its understanding of components when presented with new combinations.
- LLMs show great generalization ability via in-context learning.

### Research Questions

- Q1: Can prevailing ICL methods perform well on this task?
- Q2: How to improve LLM's ability of compositional generalization?
- Q3: Where does the ability come from?

## Motivation

### Chain-of-Thought (CoT):

step 1: find the yellow circle, ...  
Step 2: find the red square, get obj3 ...  
Step 3: filter the position get obj3, obj5 ...

matching errors

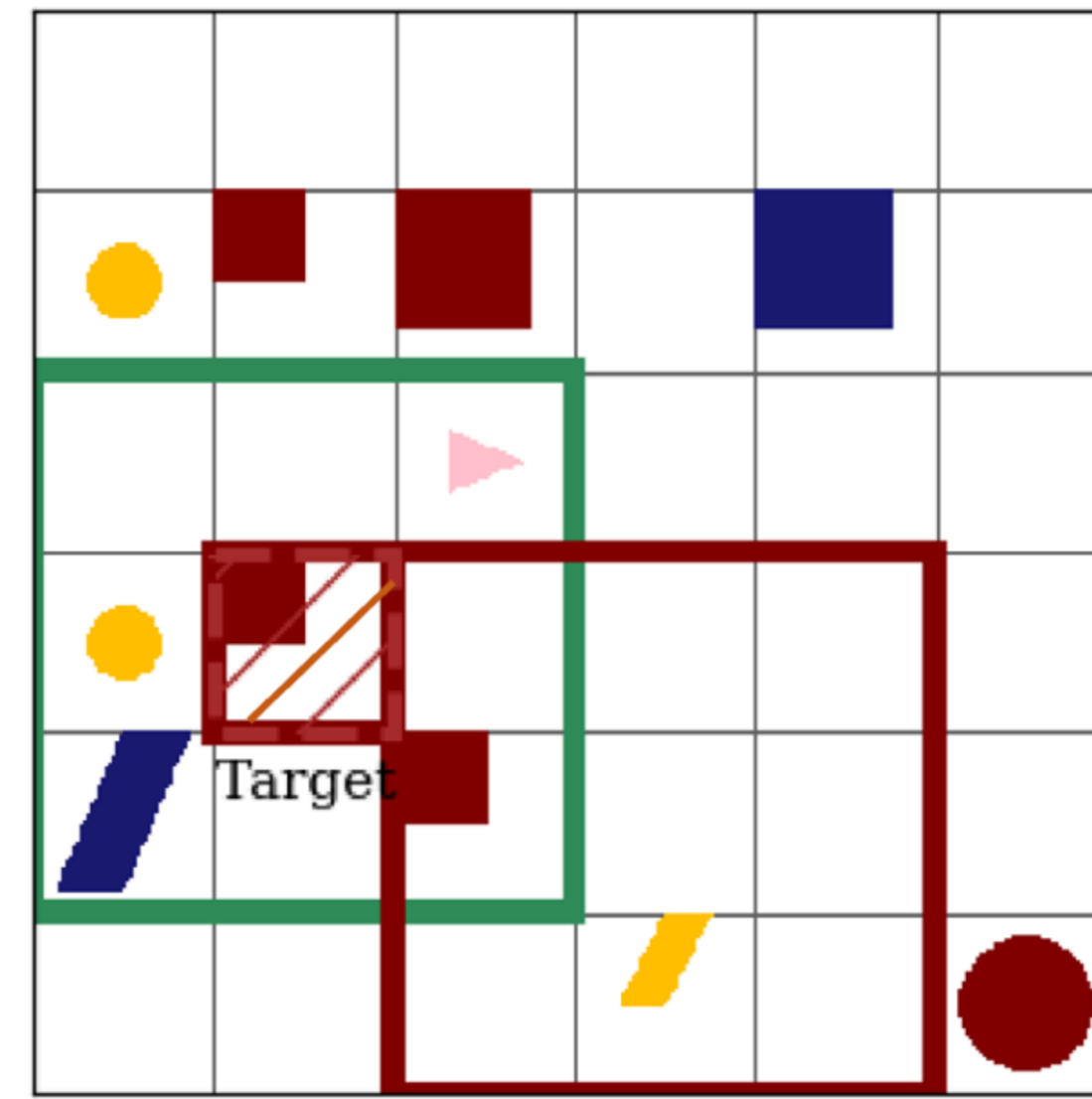
### Program-of-Thought (PoT):

```
step1_size = 'small'
for obj in all_objs:
    if obj['size'] < 2:
        candidates.append(obj)
...
```

code logic errors

cumulative errors

## Task



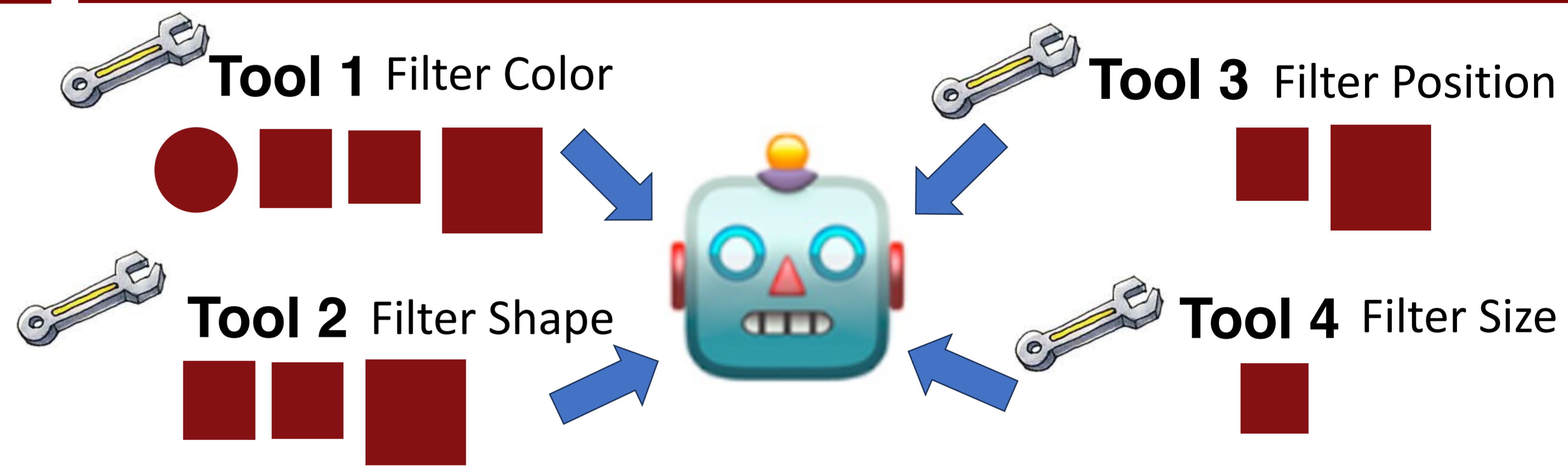
### Compositional

Find the **small red square** that is **inside of** a big box **and in the same row as** a yellow circle.

### Generalization

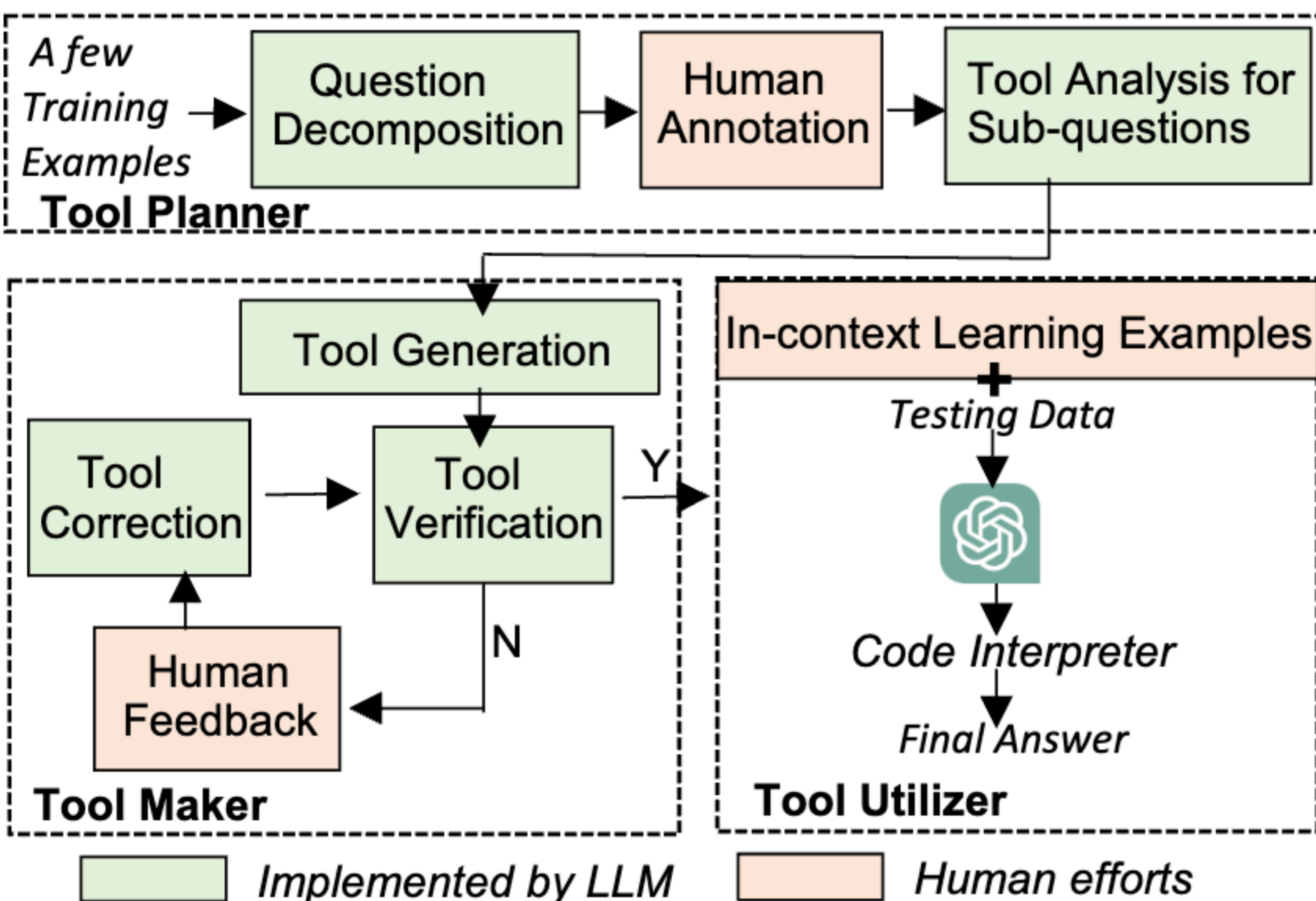
red circle *new phrase* → red square  
green square *training data* → testing data

## Our method



Tool Generation and Usage

## Implementation



- Decompose questions into sub-questions
- Make tools for sub-questions
- Combine tools to solve the whole question
- (Minimal) Human efforts on a few examples to correct LLMs

Input: obj\_0: (column=0, row=2, shape=box, color=green, size=3)  
obj\_1: (column=1, row=3, shape=square, color=red, size=2) ...  
Output: Answer: obj\_1

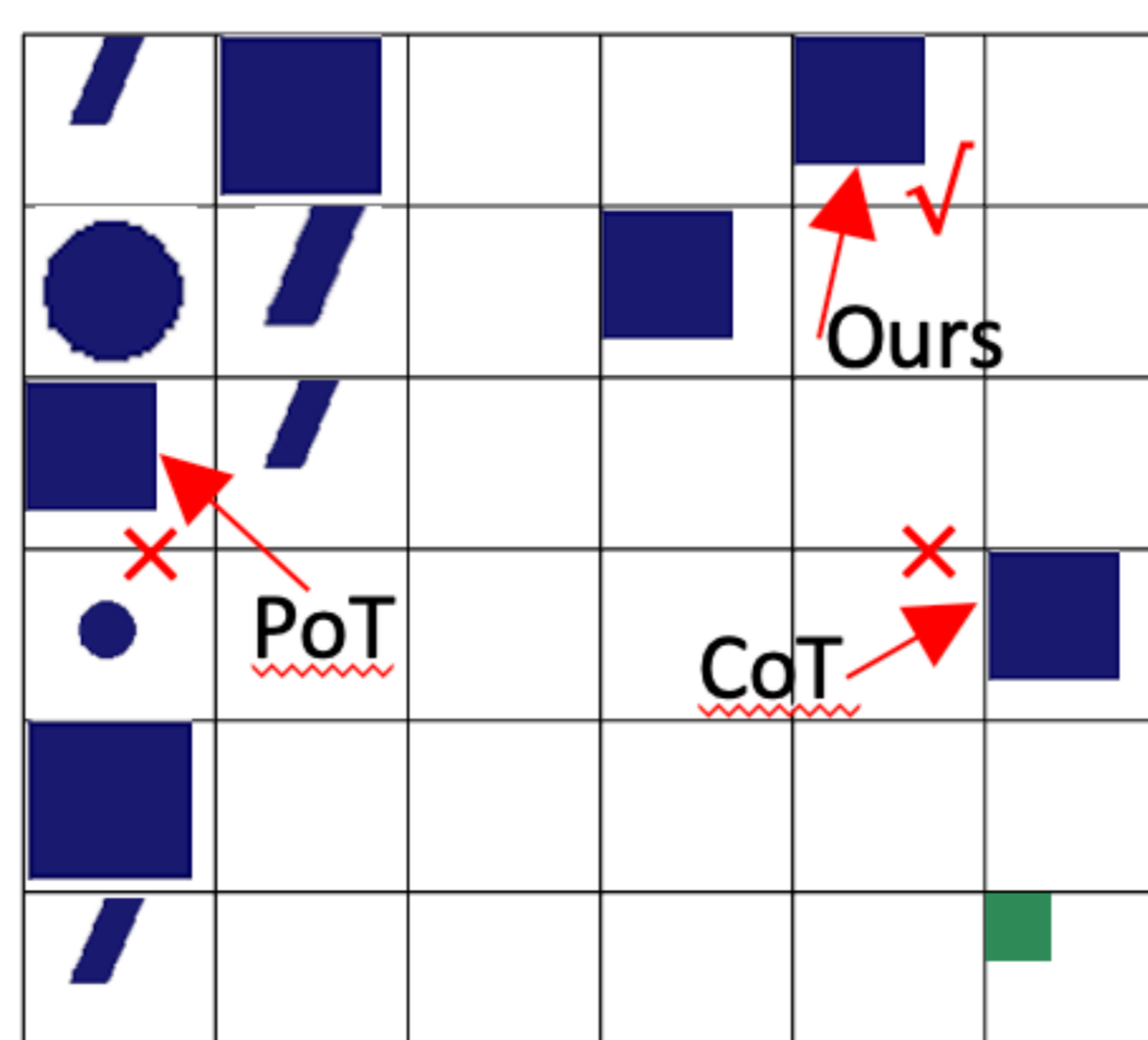
```
step1_color = 'yellow'
cand1 = filter_color(step1_color)
position = 'same row'
cand2 = filter_position(position)
condition_pairs = [(step1_obj, step1_relation)]
answer = combine_relation(condition_pairs)
```

Call Tools  
Parameter Adaptation

## Result

### Case Study

Find the small blue square that is in the same row as a blue cylinder that is in the same column as a blue circle



Replace language with random four letters.

Semantic Representation  
↓  
Symbolic Representation

	semantic			symbolic		
	P1	P2	P3	P1	P2	P3
Zero-Shot	78.6	28.2	20.0	67.6	17.2	14.0
Stand.	78	33.6	22.0	68.8	28.6	20.4
CoT	95.8	43.8	19.0	97.6	37.4	21.0
PoT	100	98.4	97.8	94.4	88.4	81.2
HTM (Ours)	100	99.6	98.6	100	99.8	98.2

The more challenging the test splits, the greater the improvement!  
e.g. Accuracy 27.3% → 95.8% on C2.

The ability arises from pattern combinations rather than relying solely on semantics learned from pretraining.

Dataset	Test Split	Training or Finetuning				In-context Learning				
		MM-LSTM [14]	GCN-LSTM [20]	MM-TRF [15]	Gro-CoT [16]	Zero-Shot [10]	Stand. [11]	CoT [12]	PoT [13]	HTM-(Ours)
ReaSCAN	A1	50.4	92.3	96.7	99.6	31	34.8	40	96.2	98.6
	A2	14.7	42.1	58.9	93.1	24.2	25.2	30.2	93.8	97.6
	A3	50.9	87.5	93.3	98.9	28	28.6	40.2	96.2	98.6
	B1	52.2	69.7	79.8	93.9	20.2	24.6	25.4	77.8	99.4
	B2	39.4	52.8	59.3	86	19.8	33.8	31.8	65.4	100
	C1	49.7	57	75.9	76.3	13.6	19.6	16	79.6	95.4
	C2	25.7	22.1	25.5	27.3	20.2	20.6	15.6	4.8	95.8
AVG	40.4	60.5	69.9	82.2	22.4	26.7	28.4	73.4	97.9	
GSR	S1	86.5	-	94.7	99.9	26.8	39	37.2	91	98.8
	S2	40.1	-	64.4	98.6	26.8	42	31.6	93.6	99.6
	S3	86.1	-	94.9	99.9	29	33.8	38	91.2	99
	S4	5.5	-	49.6	99.7	29	39.4	35.8	89.2	98.8
	S5	81.4	-	59.3	99.5	24	34.4	42.8	61.8	99
	S6	81.8	-	49.5	96.5	26.6	31.2	28.8	84.7	99.2
	AVG	58.9	-	63.5	98.8	27	36.6	35.7	85.3	99.1