

c-trie++: A Dynamic Trie Tailored for Fast Prefix Searches

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Problem Definition (1/4)

【Problem】 Dynamic Prefix Search

Maintain a data structure for a dynamic set $S = \{T_1..T_k\}$ of strings that, given a query pattern P , can compute the pair

- a) $\max \{l : P[1..l] = T_i[1..l] \text{ for some } i \in [1..k]\}$ and
- b) $I_P = \{i : T_i[1..l] = P[1..l]\}$ efficiently.

Example:

$S = \{T_1, T_2, T_3, T_4, T_5\}$

$T_1 = \text{idea}$

$T_2 = \text{inter}\text{face}$

$T_3 = \text{inter}\text{net}$

$T_4 = \text{infinite}$

$T_5 = \text{laboratory}$

$P = \text{inter}$

$\text{output} = (5, \{2, 3\})$

Problem Definition (2/4)

【Problem】 Dynamic Prefix Search

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$T_1 = \text{idea}$

$T_2 = \text{interface}$

$T_3 = \text{internet}$

$T_4 = \text{infinite}$

$T_5 = \text{laboratory}$

$P = \text{inner}$

output = (2, {2, 3, 4})

Problem Definition (3/4)

【Problem】 Dynamic Prefix Search

Maintain a data structure for a dynamic set $S = \{T_1..T_k\}$ of strings that, given a query pattern P , can compute the pair

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b) $I_P = \{i : T_i[1..l] = P[1..l]\}$ efficiently.

Example:

$S = \{T_1, T_2, T_3, T_4, T_5, T_6\}$

$T_1 = \text{idea}$

$T_2 = \text{interface}$

$T_3 = \text{internet}$

$T_4 = \text{infinite}$

$T_5 = \text{laboratory}$

$T_6 = \text{indexing}$

Supports insertion of a string into S .

$\text{insert}(T_6)$

Problem Definition (4/4)

【Problem】 Dynamic Prefix Search

Maintain a data structure for a dynamic set $S = \{T_1..T_k\}$ of strings that, given a query pattern P , can compute the pair

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Example:

$S = \{T_1, T_2, T_3, T_4, \textcolor{red}{T_5}, T_6\}$

$T_1 = \text{idea}$

$T_2 = \text{interface}$

$T_3 = \text{internet}$

$T_4 = \text{infinite}$

~~$T_5 = \text{laboratory}$~~

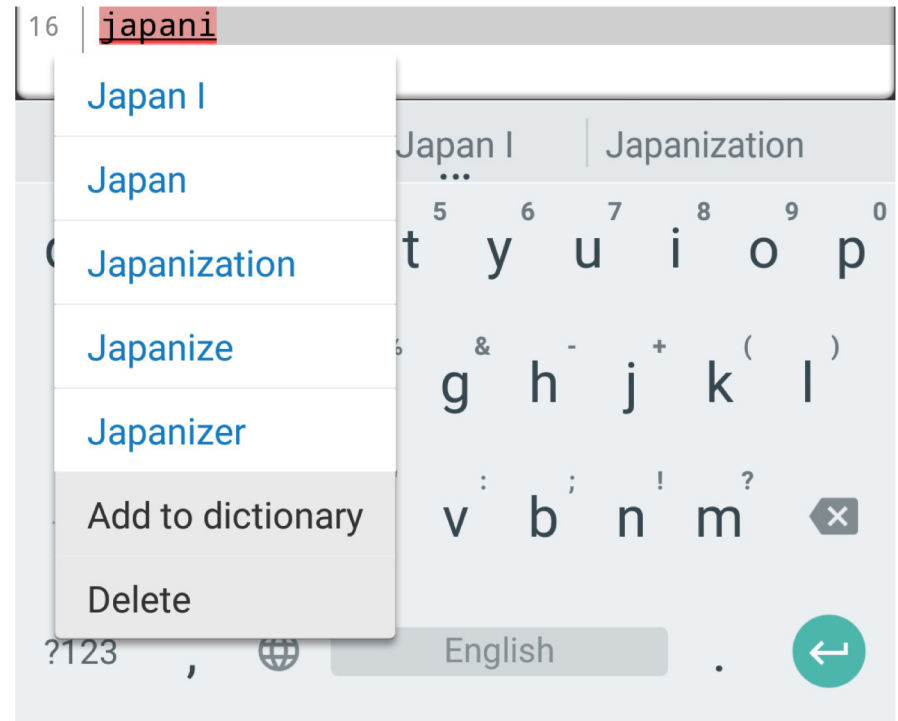
$T_6 = \text{indexing}$

Supports deletion of a string from S .

~~$\text{delete}(T_5)$~~

Introduction (1/3)

- prefix search applications
 - **input method editors**
 - query auto-completion
 - range query filtering

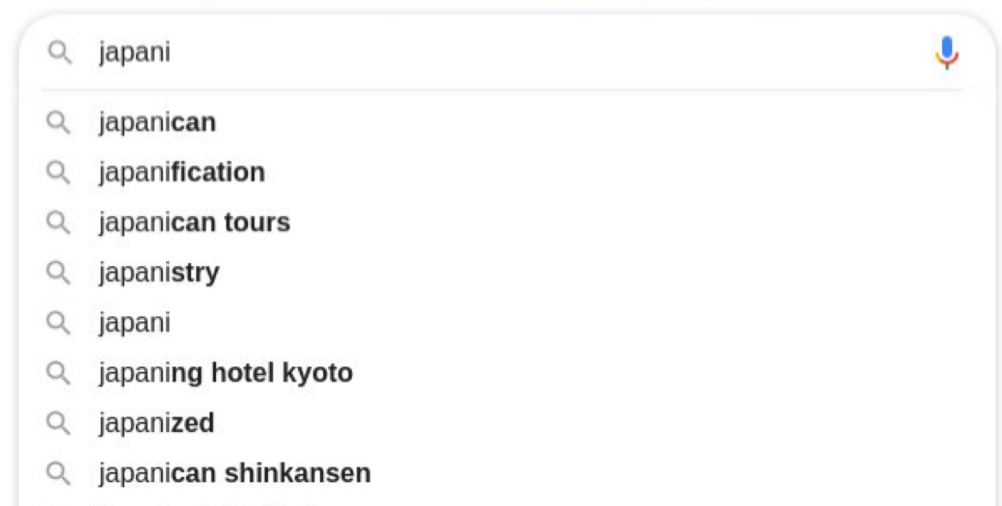


(entering japani on an Android phone)

Introduction (2/3)

- prefix search applications
 - input method editors
 - **query auto-completion**
 - range query filtering

(entering japani on google)



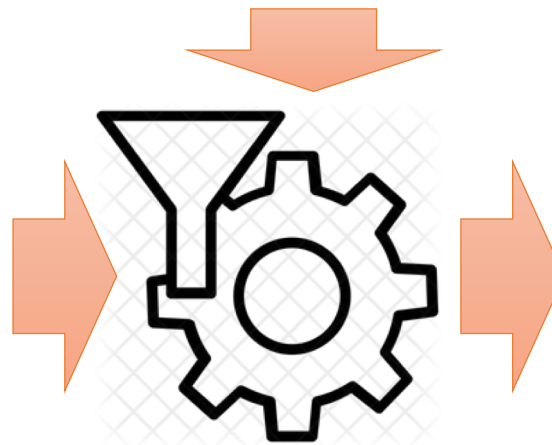
Introduction (3/3)

- prefix search applications
 - input method editors
 - query auto-completion
 - **range query filtering**

UserQueries

User	Date	Word
661	12/03/2020	refund-ticket
457	11/03/2020	trip-cancellation
139	01/03/2020	corona-virus
:	:	:

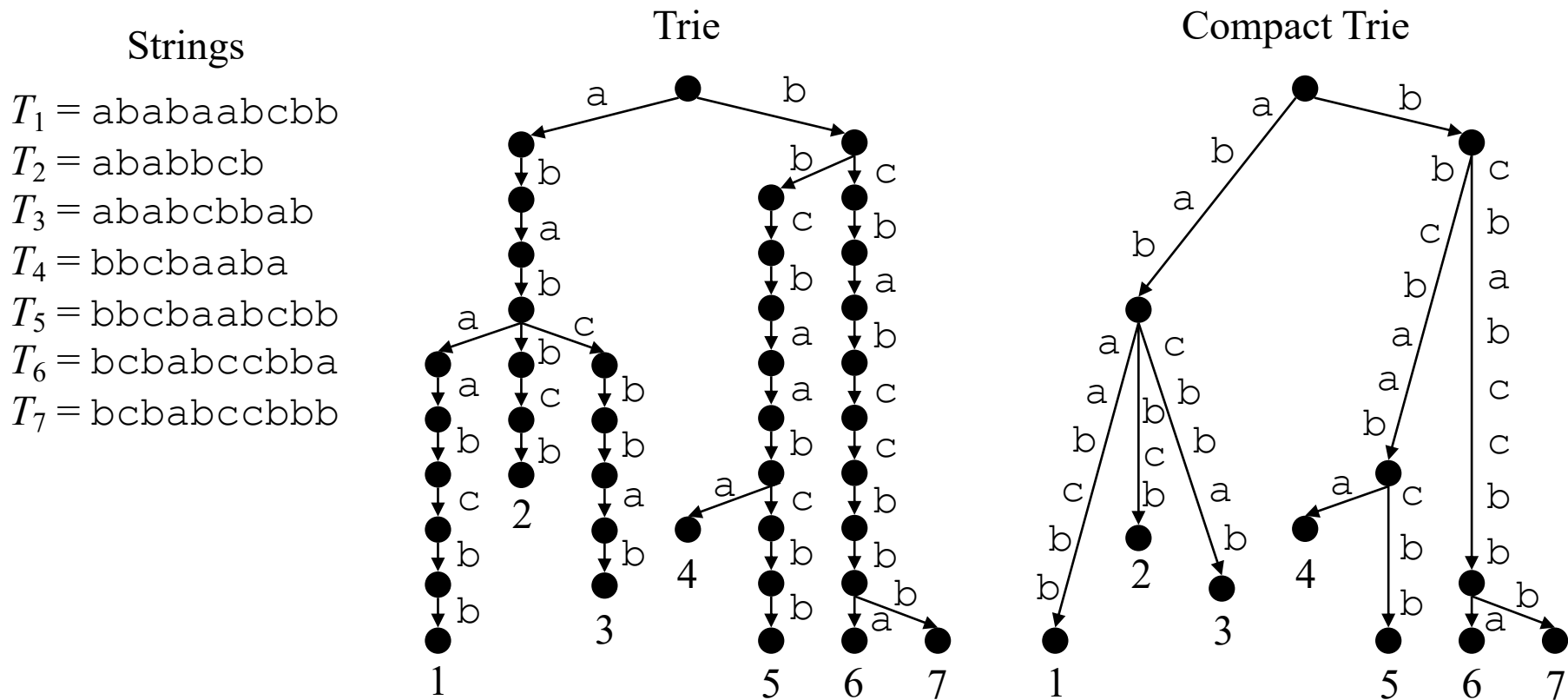
```
SELECT User, Word
FROM UserQueries
WHERE Word LIKE 'japani%'
AND ...
```



User	Word
79	japanican
83	japanification
89	japanistry
97	japani

Compact Trie [Morrison, 1968]

- Trie : represents strings where common prefixes are compressed to a single path (front encoding).
- Compact Trie : reduces the number of nodes by replacing branchless path segments with a single edge.



Previous Works for Dynamic Prefix Search (1/2)

	Space [bits]	Prefix Search Time in Expectation
Trie	$O(T \log T)$	$O(m + occ)$
Compact Trie [Morrison, 1968]	$ T \log \sigma + \Theta(k \log k)$	$O(m + occ)$

$|T|$: trie size (front encoding size)

$k = |S|$, $m = |P|$, $\sigma = |\Sigma|$, Σ : alphabet, occ : number of occurrences

Previous Works for Dynamic Prefix Search (2/2)

	Space [bits]	Prefix Search Expected Time
Trie	$O(T \log T)$	$O(m + occ)$
Compact Trie [Morrison, 1968]	$ T \log \sigma + \Theta(k \log k)$	$O(m + occ)$
Z-Fast Trie [Belazzougui et al., 2010]	$ T \log \sigma + \Theta(kw)$	$O(m / \alpha + occ + \log (m \log \sigma))$
Packed C-Trie [Takagi et al., 2017]	$ T \log \sigma + \Theta(kw)$	$O(m / \alpha + occ + \log w)$

$|T|$: trie size (front encoding size)

$n = \sum_i |T_i|$, $k = |S|$, $m = |P|$, $\sigma = |\Sigma|$, Σ : alphabet, occ : number of occurrences

w : machine word size ($w = \Omega(\log n)$), $\alpha = O(w / \log \sigma)$

Our Contribution for Dynamic Prefix Search

	Space [bits]	Prefix Search Expected Time
Trie	$O(T \log T)$	$O(m + occ)$
Compact Trie [Morrison, 1968]	$ T \log \sigma + \Theta(k \log k)$	$O(m + occ)$
Z-Fast Trie [Belazzougui et al., 2010]	$ T \log \sigma + \Theta(kw)$	$O(m / \alpha + occ + \log (m \log \sigma))$
Packed C-Trie [Takagi et al., 2017]	$ T \log \sigma + \Theta(kw)$	$O(m / \alpha + occ + \log w)$
C-Trie++ [Ours]	$ T \log \sigma + \Theta(kw)$	$O(m / \alpha + occ + \log \min\{\alpha, m\})$

$\alpha < w$ always holds.

$|T|$: trie size (front encoding size)

$n = \sum_i |T_i|$, $k = |S|$, $m = |P|$, $\sigma = |\Sigma|$, Σ : alphabet, occ : number of occurrences

w : machine word size ($w = \Omega(\log n)$), $\alpha = O(w / \log \sigma)$

Word Packing

In the word RAM model with word size w bits, we can compare ($=$, $<$, $>$) two $O(w)$ bits integers in $O(1)$ time.

$\Rightarrow$ Let $\alpha = w / \log \sigma$.

i	d	e	a
01101001	01100100	01100101	01100001

a character uses $\lceil \log \sigma \rceil$ bits
 $\Rightarrow$ strings of length α use $O(w)$ bits

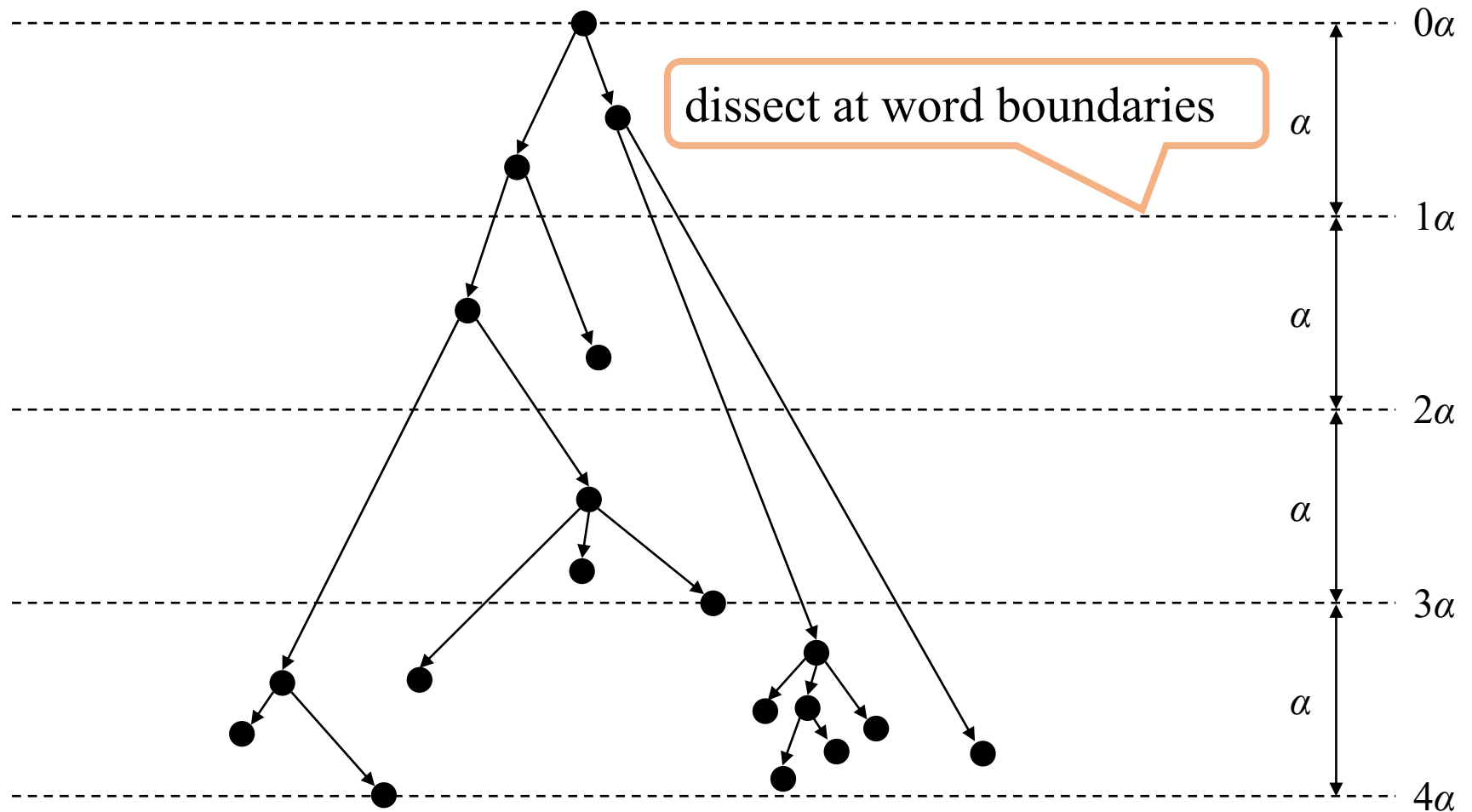
e.g.
64-bits architecture
 $\sigma = 256$
 $w = 32$
 $\alpha = 4$

We can compare two strings of length α in $O(1)$ time.

$\Rightarrow$ We can compare two strings of length m in $O(m / \alpha)$ time.

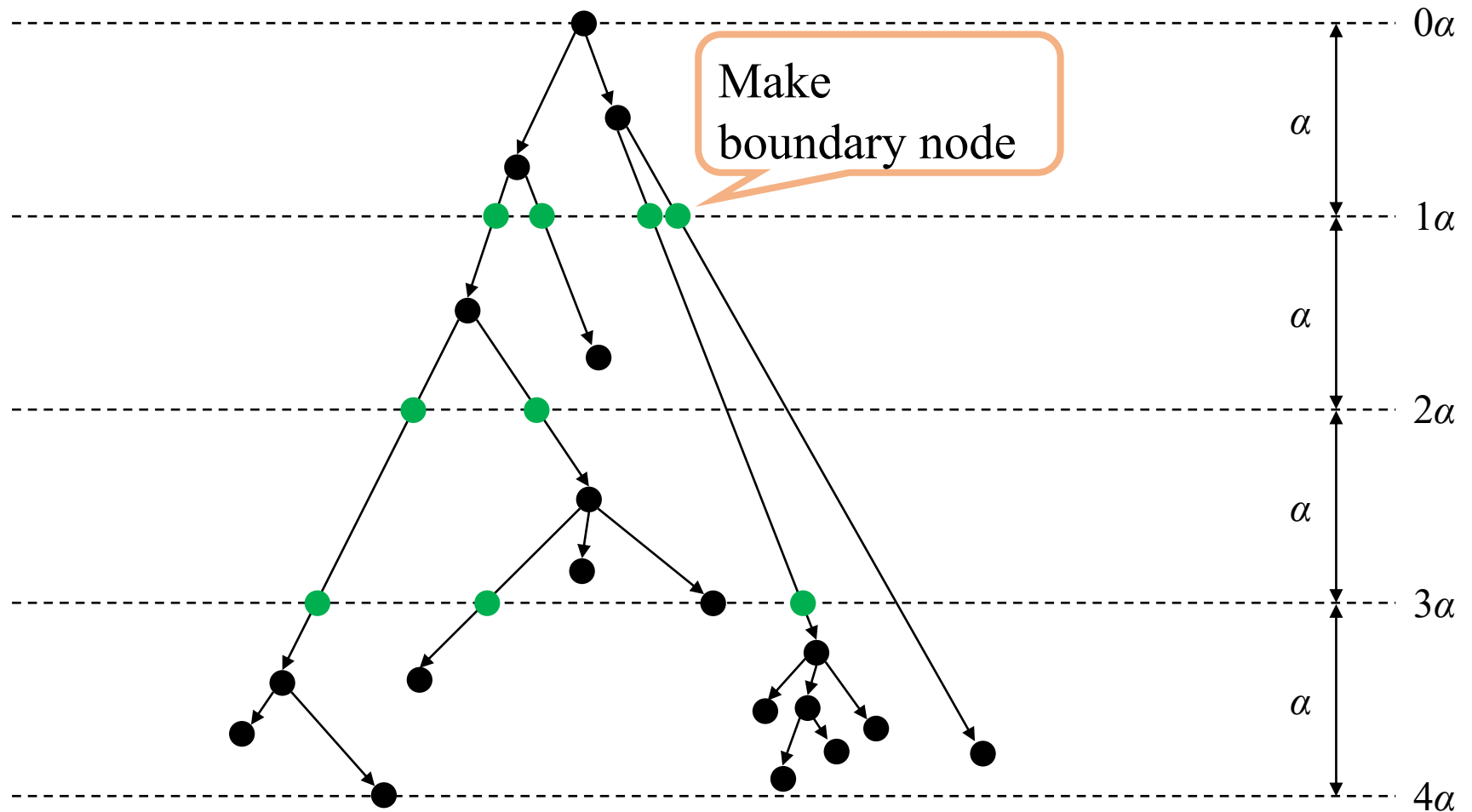
Introduction of Micro Trie (1/4)

Compact Trie



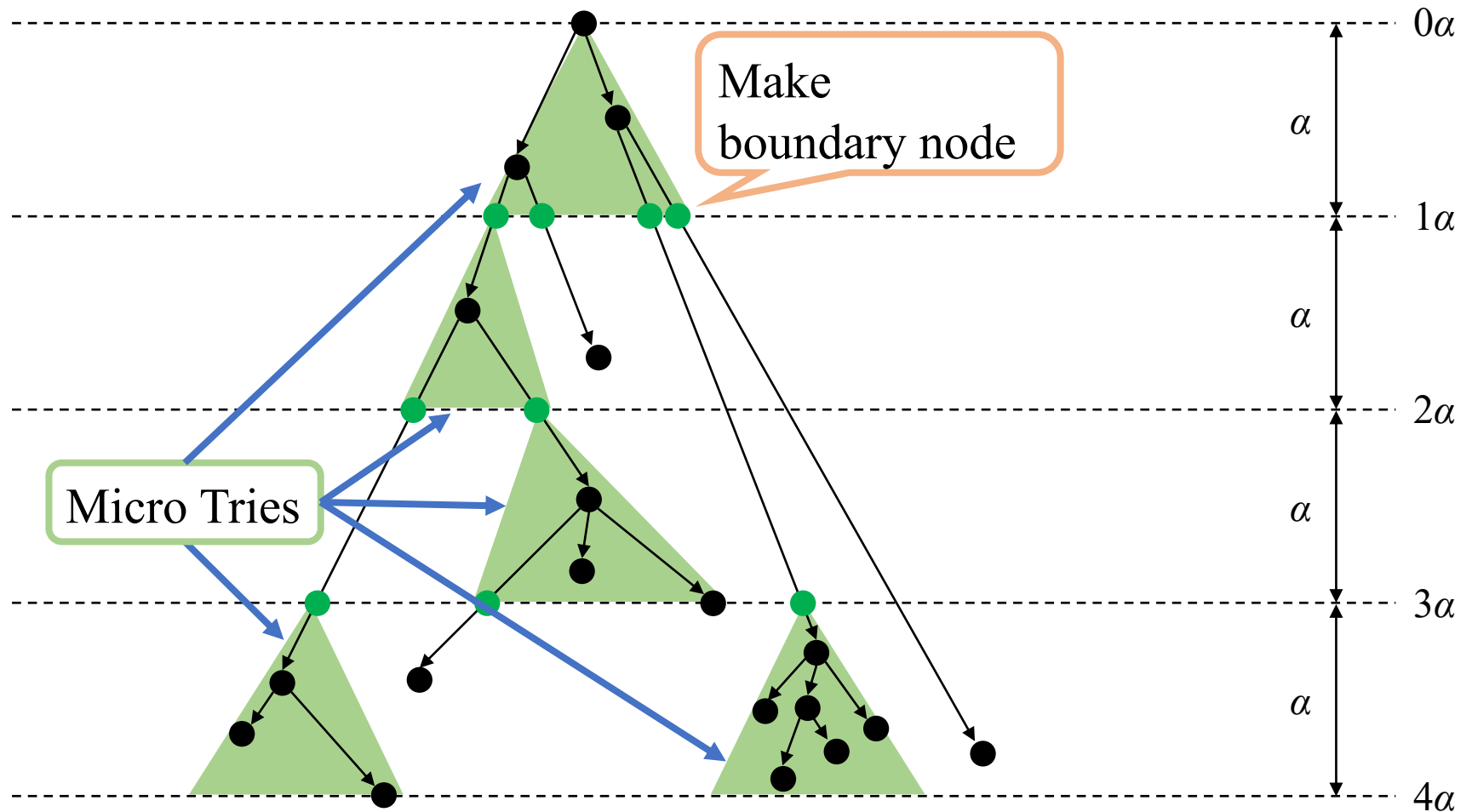
Introduction of Micro Trie (2/4)

Compact Trie



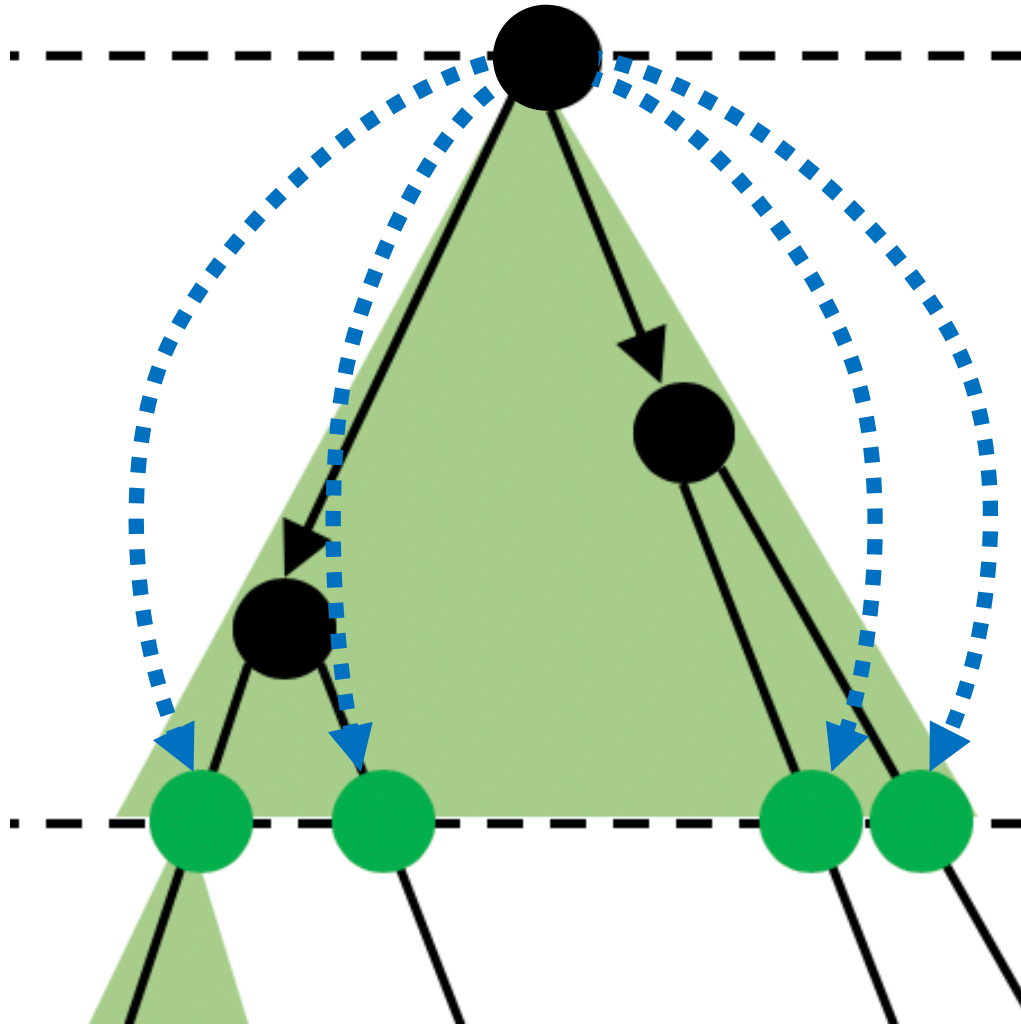
Introduction of Micro Trie (3/4)

C-Trie++



Introduction of Micro Trie (4/4)

Equip each Micro Trie with a Hash Table

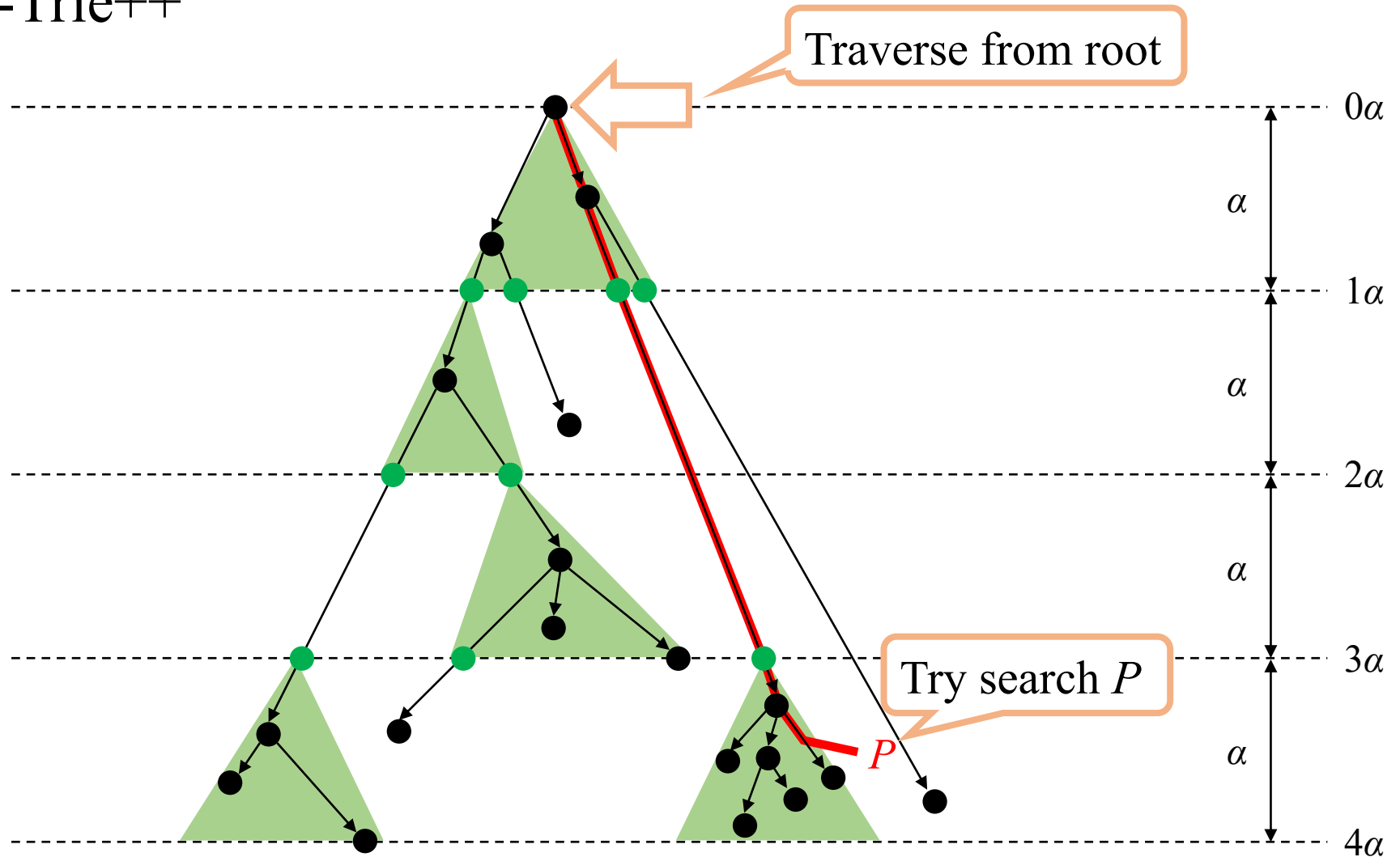


Hash Table:

- jump from root to leaf in $O(1)$ expected time.
- key: string of length α
- value: leaf node

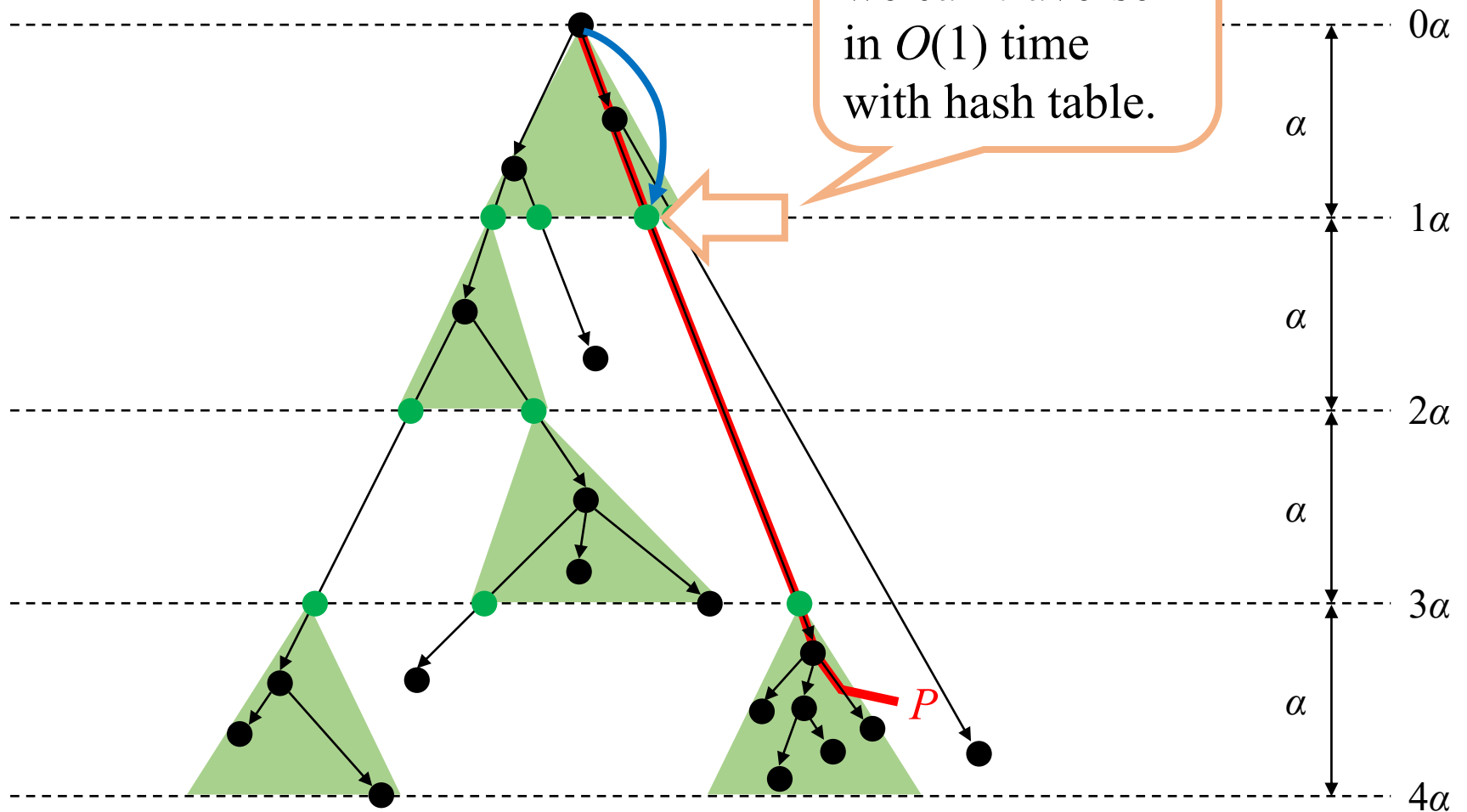
Trie Traversal (1/5)

C-Trie++



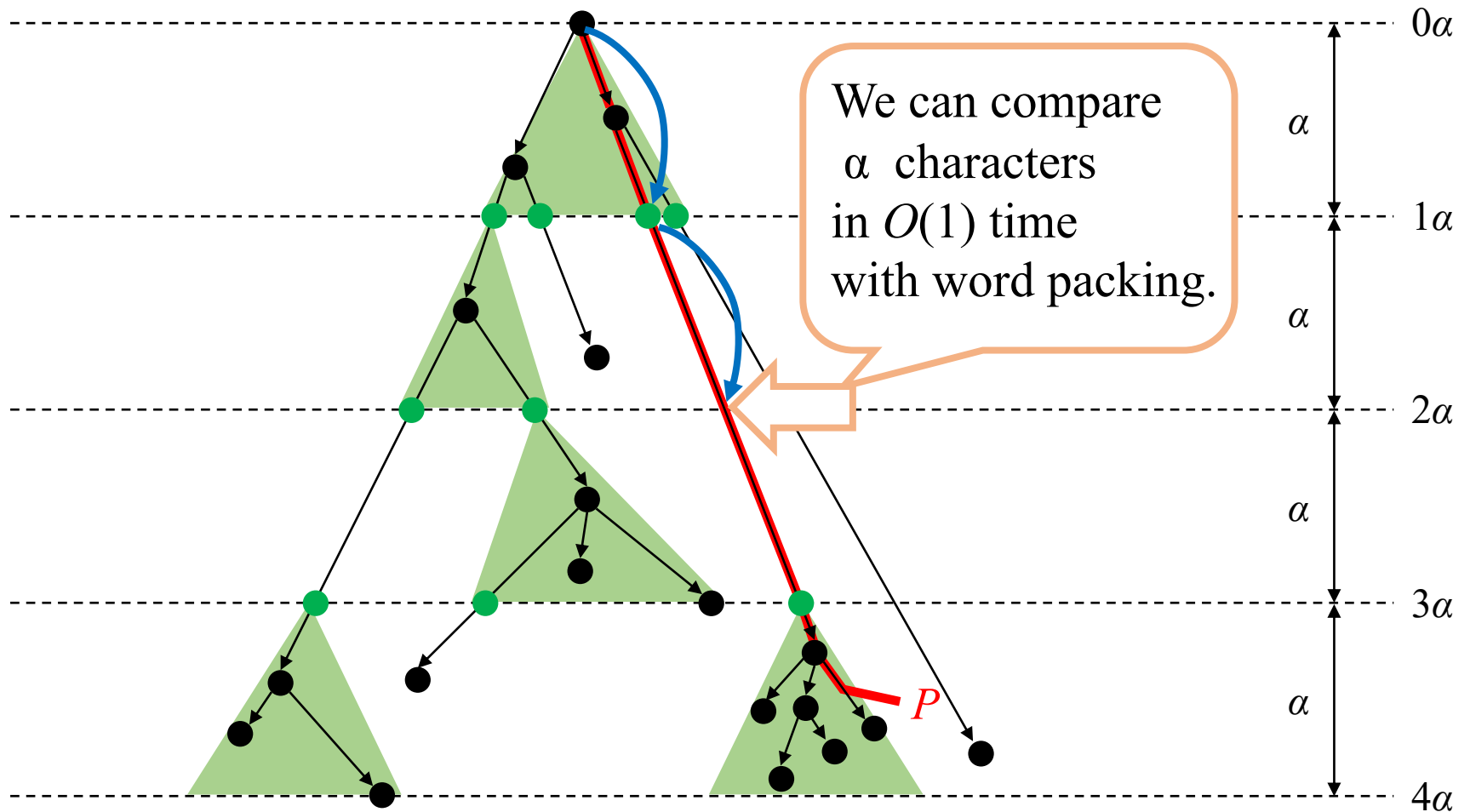
Trie Traversal (2/5)

C-Trie++



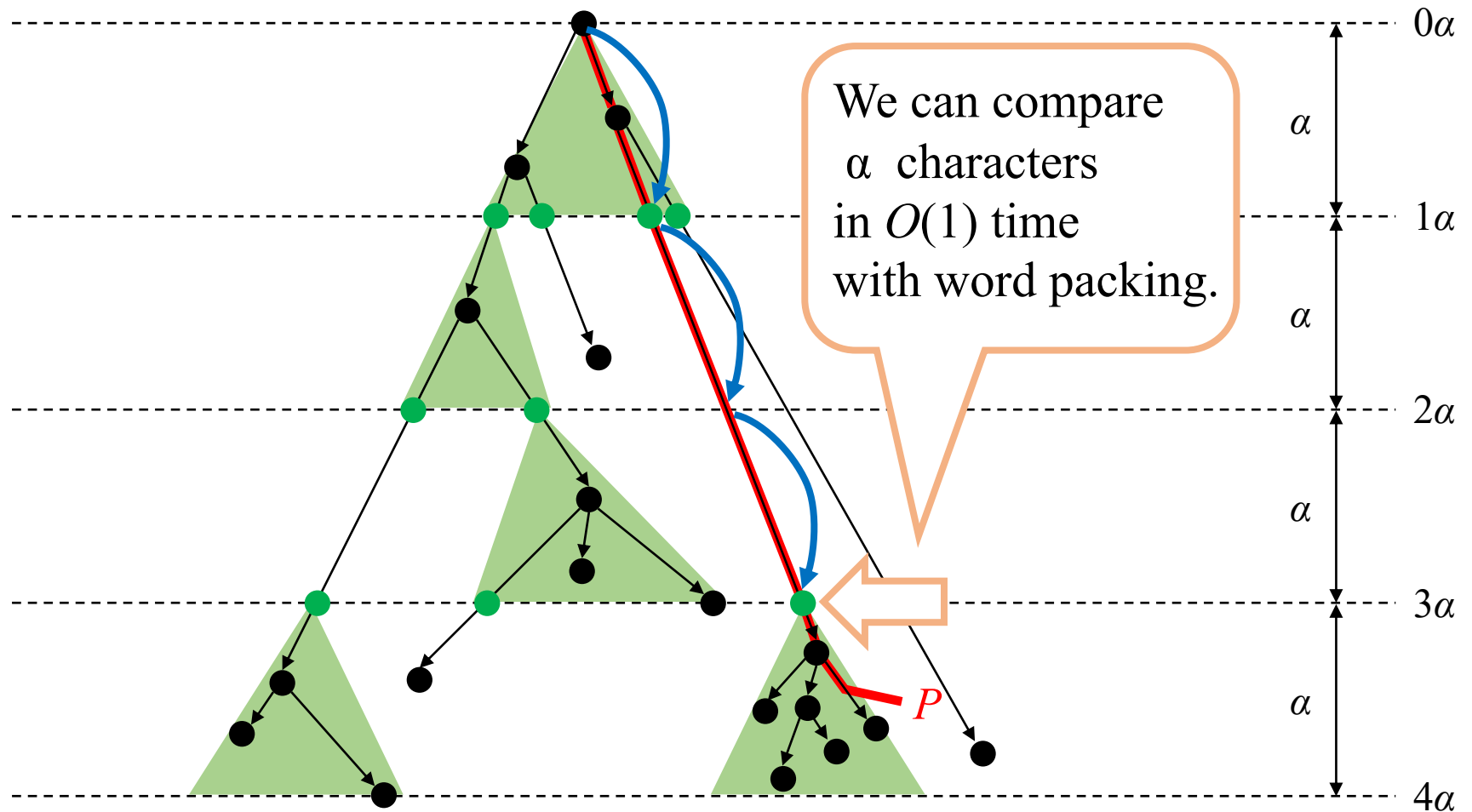
Trie Traversal (3/5)

C-Trie++



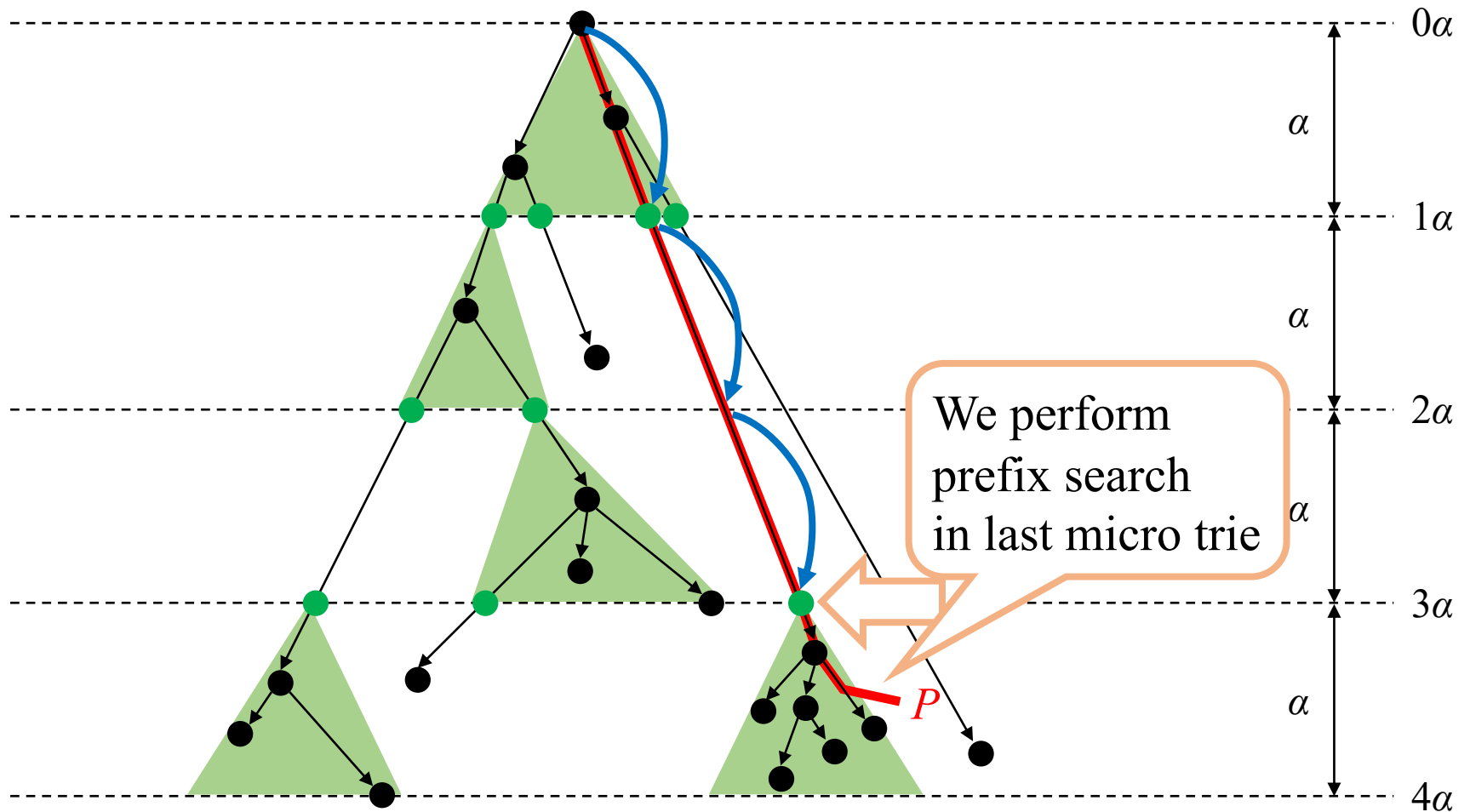
Trie Traversal (4/5)

C-Trie++



Trie Traversal (5/5)

C-Trie++

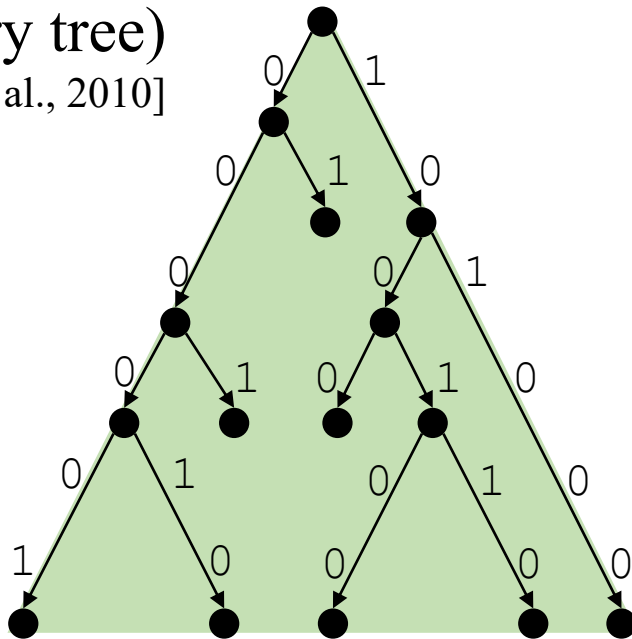


Dynamic Prefix Search in Micro Tries

- We improve prefix search (expected) time in micro trie
 - Belazzougui et al., 2010 : $O(\log(m \log \sigma) + occ)$
 - Takagi et al., 2017 : $O(\log w + occ)$
 - **This work** : $O(\log \min\{\alpha, m\} + occ)$

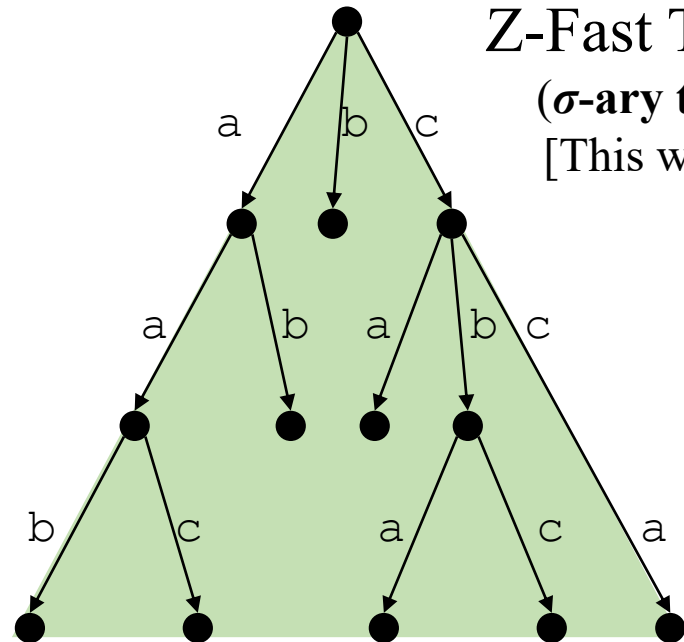
Z-Fast Trie
(binary tree)

[Belazzougui et al., 2010]



Alphabet Aware
Z-Fast Trie

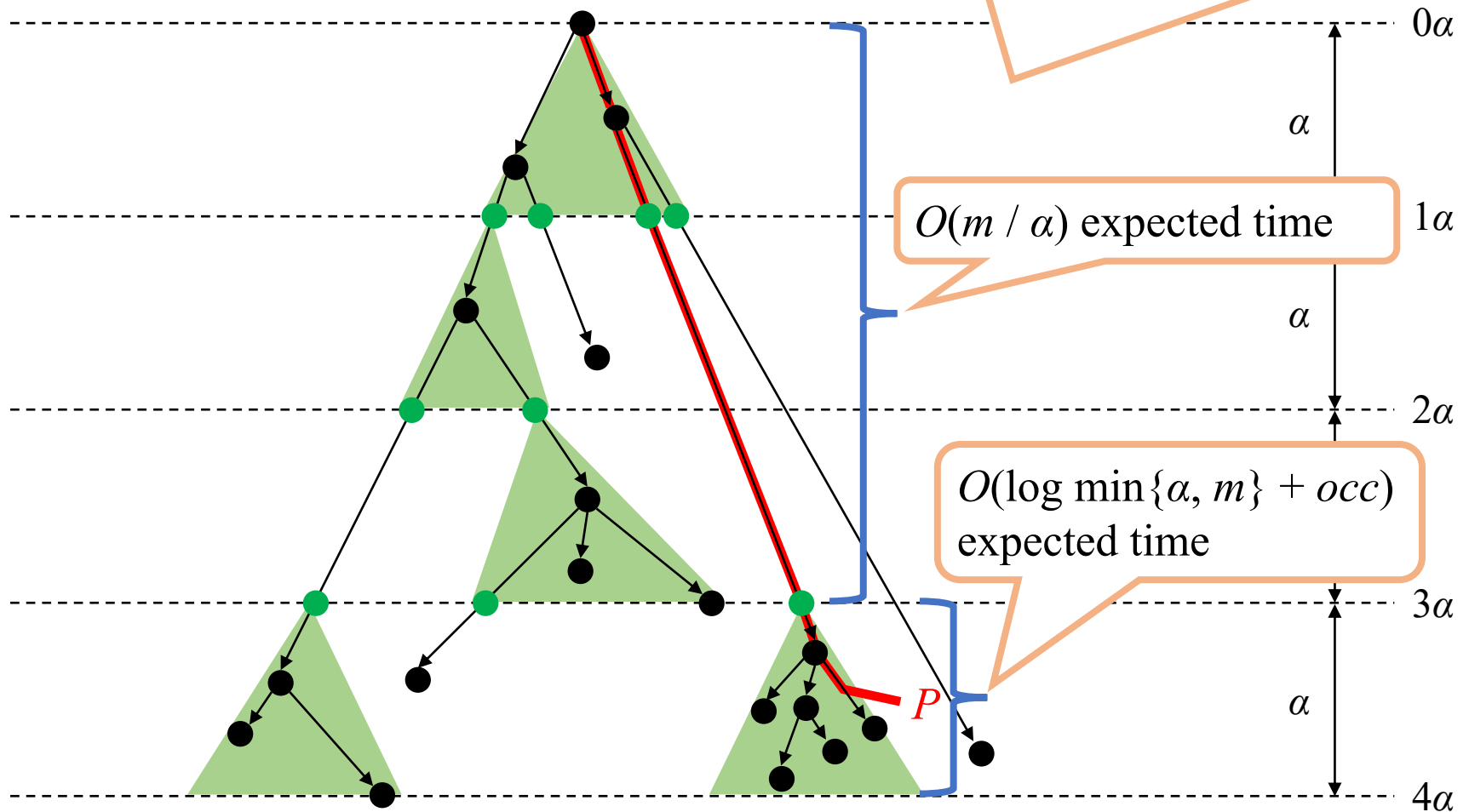
(σ -ary tree)
[This work]



Prefix Search Time

C-Trie++

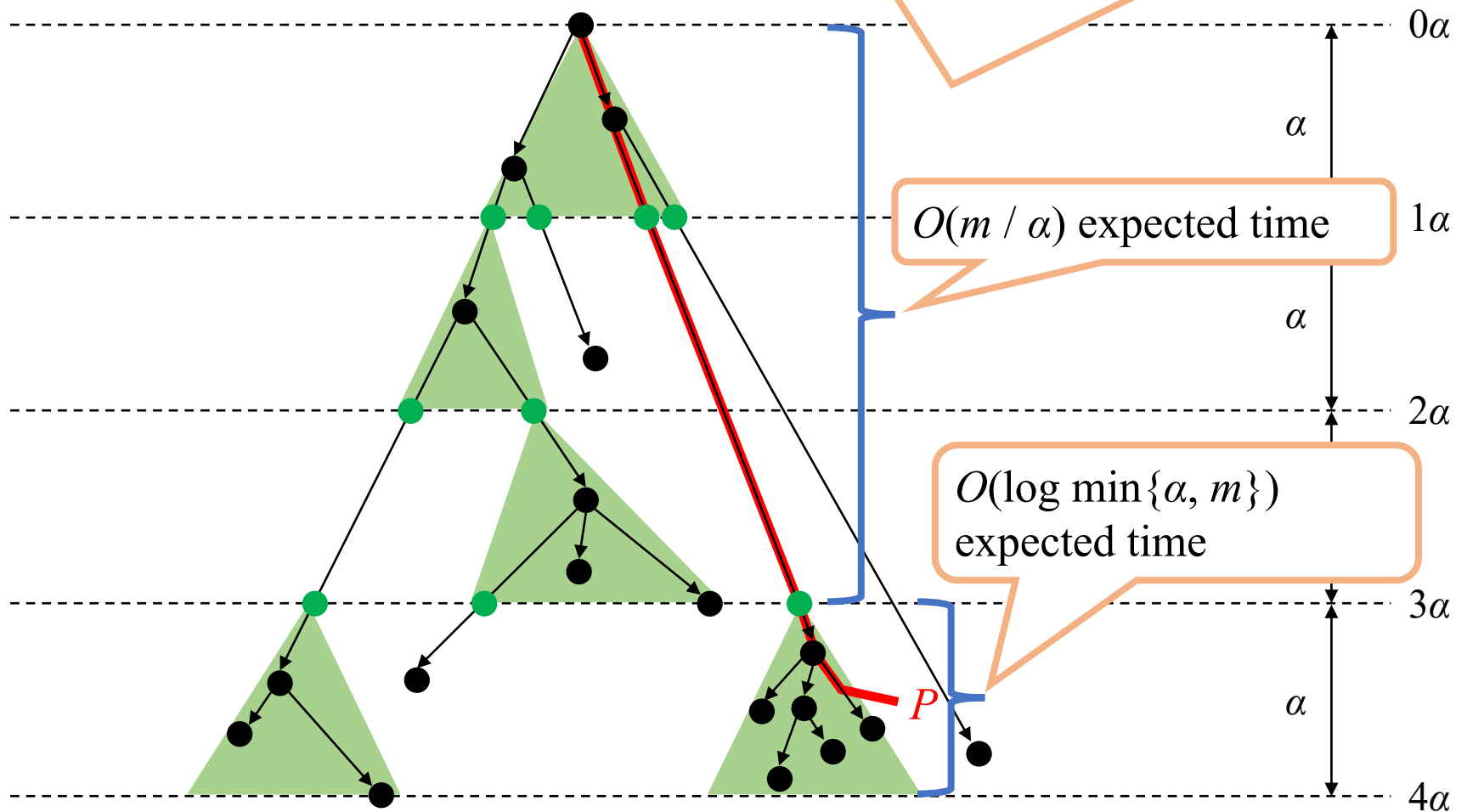
total : $O(m / \alpha + \log \min\{\alpha, m\} + occ)$ expected time



Insertion Time

C-Trie++

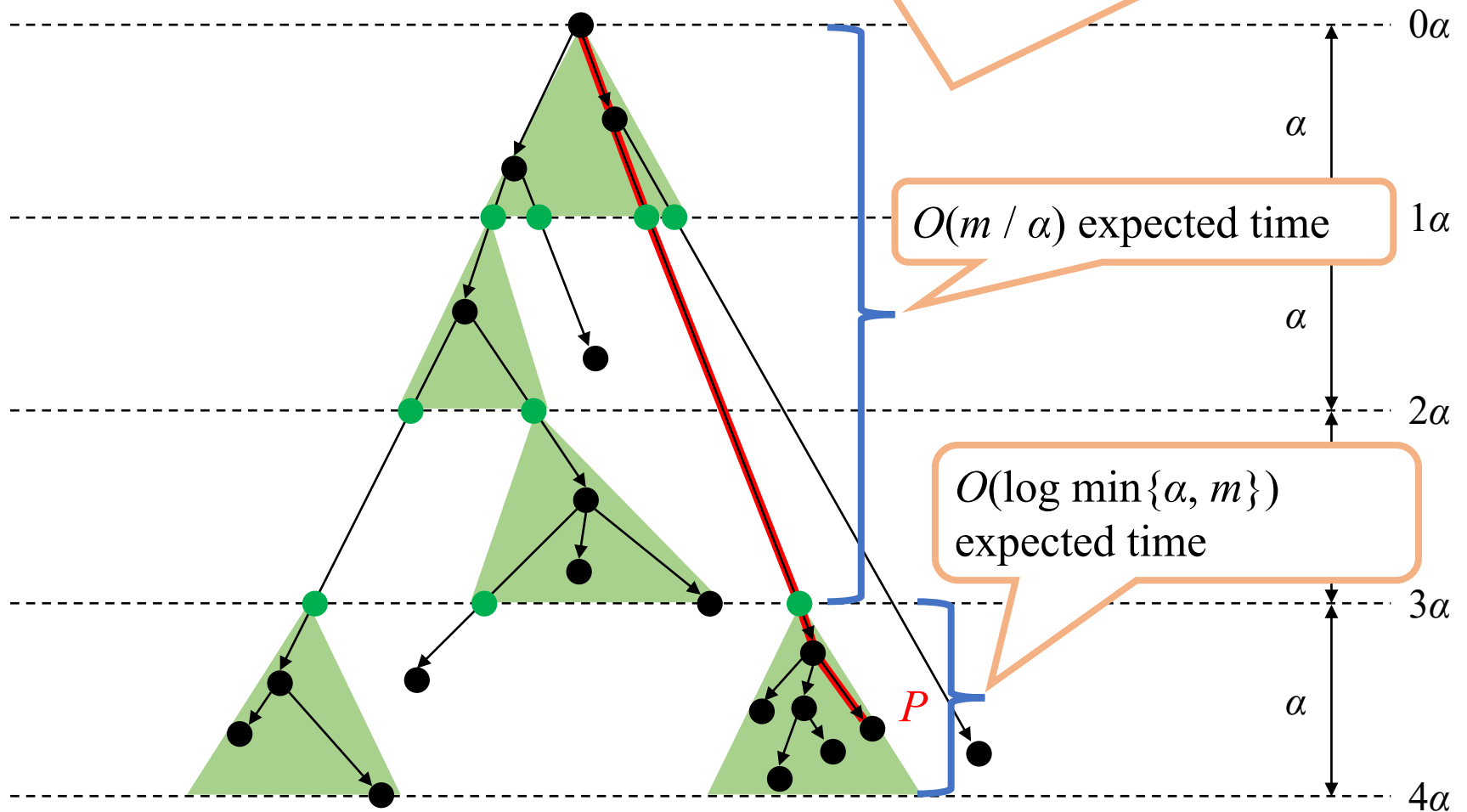
total : $O(m / \alpha + \log \min\{\alpha, m\})$ expected time



Deletion Time

C-Trie++

total : $O(m / \alpha + \log \min \{\alpha, m\})$ expected time



Experimental Setup

- CPU : Intel Xeon X5560 @2.80 GHz
- Memory : 198GB
- OS : CentOS 6.10
- Language : C++
- Implementations
 - Compact Trie [Takagi et al.]
 - Z-Fast Trie [Ours]
 - Packed C-Trie [Takagi et al.]
 - **C-Trie++** [Ours]

Datasets

□ Characteristics

Datasets	size[MB]	σ	$k[10^3]$	average length	avg. LCP	C-Tries nodes[10^3]
proteins	864.14	26	2,982	302.8	38.8	5,778
dblp.xml	164.89	96	2,950	57.6	34.4	5,899

- We split a data set into strings at delimiters such as carriage returns, which form our input set S .
- In our experiment for prefix search, we took the prefixes of length 10%, 20%, ..., 100% of the strings of S as patterns, and measured the average query time.

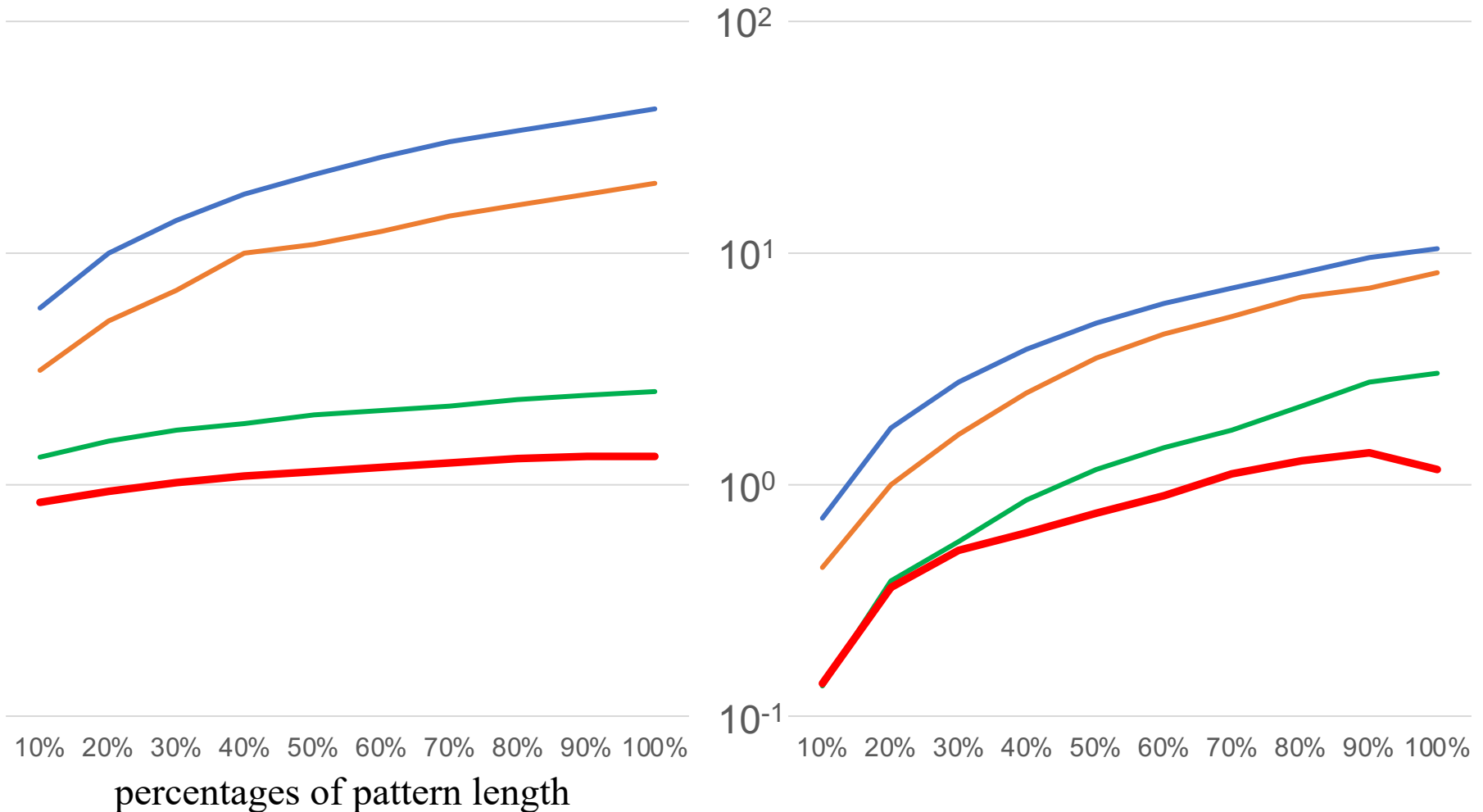
Experimental Results

Prefix Search Time [microsec]

Compact Trie Packed C-Trie
Z-Fast Trie C-Trie++

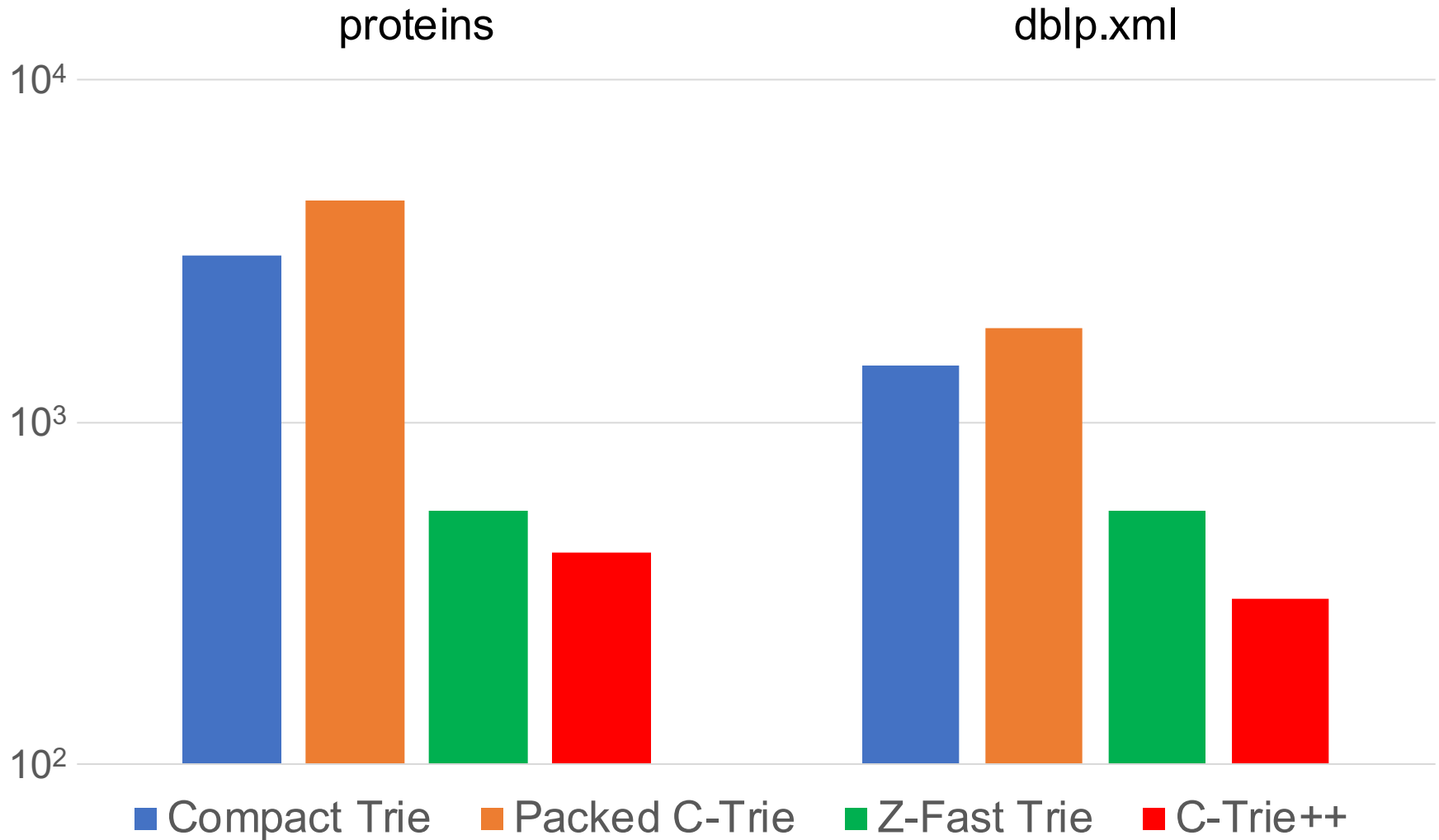
proteins

dblp.xml



Experimental Results

Memory Usage [MB]



Conclusions

□ Summary

- We proposed c-trie++:
 - ◆ Space: $|T| \log \sigma + \Theta(kw)$ bits.
 - ◆ Prefix Search : $O(m / \alpha + \log \min\{\alpha, m\} + occ)$ time.
 - ◆ Insert : $O(m / \alpha + \log \min\{\alpha, m\})$ time.
 - ◆ Delete : $O(m / \alpha + \log \min\{\alpha, m\})$ time.
- Our computational experiments support the claim that c-trie++ is the fastest trie for prefix search.

□ Future Work

- Use SIMD instruction sets that allow larger machine word sizes (here $w = 64$ bits).