

# A Novel Approach to Joint User Selection and Precoding for Multiuser MISO Downlink Channels

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## Objective

Joint design of user selection (US) and precoding for the design criteria of weighted sum rate (WSR) maximization s.t total power constraint

## System Model

- Single cell MISO system; Down link scenario
- full frequency and time resources reuse
- $M$  Tx ants;  $N (\geq M)$  single antenna users (UEs)
- Independent data to selected UEs; Utmost  $M$  selected UEs
- Rx signal of all UEs,  $\mathbf{y}$ , is
 
$$\begin{bmatrix} y_1 \\ \vdots \\ y_N \end{bmatrix} = \begin{bmatrix} \dots \mathbf{h}_1^H \dots \\ \vdots \\ \dots \mathbf{h}_N^H \dots \end{bmatrix} \begin{bmatrix} \vdots \\ \mathbf{w}_1 \dots \mathbf{w}_N \\ \vdots \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_N \end{bmatrix} + \begin{bmatrix} \vdots \\ \mathbf{n} \\ \vdots \end{bmatrix}$$
- $y_i, \mathbf{h}_i, \mathbf{w}_i, x_i, n_i$  are the received signal, downlink channel and precoding vector, data and noise of user  $i$ .

## Prior work and contribution

### Prior work:

- US and precoding as two decoupled problems
- Joint problem formulation with disjoint update of US and precoding variables

**Scope of improvement:** US and precoding are coupled  $\rightarrow$  the joint solution outperforms aforementioned techniques

**Contribution:** Joint solution to joint problem

## Weighted sum rate maximization

$$\max_{\mathbf{W}, \mathcal{S}} \sum_{i \in \mathcal{S}} \beta_i \log(1 + \gamma_i)$$

$$\text{s.t. } C_1: \sum_{i=1}^N \|\mathbf{w}_i\|_2^2 \leq P_T; C_2: |\mathcal{S}| \leq M$$

where  $\beta_i$  and  $\gamma_i = \frac{|\mathbf{h}_i^H \mathbf{w}_i|^2}{\sigma^2 + \sum_{j \neq i} |\mathbf{h}_i^H \mathbf{w}_j|^2}$  are the weight and SINR of user  $i$ , and  $\mathcal{S}$  is the set of selected users, and  $P_T$  is the total power.

## Joint formulations with binary variables in literature

$$\max_{\mathbf{W}, \boldsymbol{\eta}} \sum_{i=1}^N \eta_i \beta_i \log(1 + \gamma_i) \text{ or } \sum_{i=1}^N \beta_i \log(1 + \eta_i \gamma_i)$$

$$\text{s.t. } C_1: \eta_i \in \{0, 1\}, \forall i$$

$$C_2: \sum_{i=1}^N \eta_i \leq M; C_3: \sum_{i=1}^N \|\mathbf{w}_i\|_2^2 \leq P_T$$

### Drawbacks

- Multiplication  $\implies$  Coupled formulation
- Alternative update of  $\mathbf{W}$  and  $\boldsymbol{\eta}$

## Proposed formulation

$$\text{Key: } \|\mathbf{w}_i\|_2^2 = \begin{cases} 0; \text{Not selected} \\ \neq 0; \text{selected} \end{cases}$$

### Reformulation with binary slack variable

$$\mathcal{P}_1: \max_{\mathbf{W}, \mathbf{P}, \boldsymbol{\eta}} \sum_{i=1}^N \beta_i \log(1 + \gamma_i)$$

$$\text{s.t. } C_1: \eta_i \in \{0, 1\}, \forall i,$$

$$C_2: \|\mathbf{w}_i\|_2^2 \leq \eta_i P_i, \forall i$$

$$C_3: \sum_{i=1}^N \eta_i \leq M; C_4: \sum_{i=1}^N P_i \leq P_T$$

**Novelty:** Decoupling of  $\mathbf{W}$  and  $\boldsymbol{\eta}$

**Usefulness:** Amenable to joint optimization

**Remark:** Nonconvex obj and  $\boldsymbol{\eta} \implies$  MINLP

## WSR as DC problem

**Addressing non-convexity:** Epigraph form

$$\mathcal{P}_2: \max_{\mathbf{W}, \mathbf{P}, \boldsymbol{\eta}, \boldsymbol{\zeta}} \sum_{i=1}^N \beta_i \log(\zeta_i)$$

$$\text{s.t. } C_1, C_2, C_3, C_4$$

$$C_5: 1 + \gamma_i \geq \zeta_i, \forall i$$

$$C_6: \gamma_i \geq 1, \forall i$$

$C_5$  as a DC constraint:

$$1 + \gamma_i \geq \zeta_i \implies \frac{\sigma^2 + \sum_{j=1}^N |\mathbf{h}_i^H \mathbf{w}_j|^2}{\sigma^2 + \sum_{j \neq i} |\mathbf{h}_i^H \mathbf{w}_j|^2} \geq \zeta_i$$

$$\implies \underbrace{\frac{\sigma^2 + \sum_{j=1}^N |\mathbf{h}_i^H \mathbf{w}_j|^2}{\zeta_i}}_{\text{jointly convex in } \mathbf{W}, \zeta_i \text{ for } \zeta_i > 0} \geq \underbrace{\sigma^2 + \sum_{j \neq i} |\mathbf{h}_i^H \mathbf{w}_j|^2}_{\text{convex}}$$

**Binary to continuous:** Penalization method

$$\mathcal{P}_4: \max_{\mathbf{W}, \mathbf{P}, \boldsymbol{\eta}, \boldsymbol{\zeta}} \sum_{i=1}^N (\beta_i \log(\zeta_i) + \lambda P(\eta_i))$$

difference of concave

$$\text{s.t. } C_1: 0 \leq \eta_i \leq 1, \forall i$$

$$C_5: \underbrace{\sigma^2 + \sum_{j \neq i} |\mathbf{h}_i^H \mathbf{w}_j|^2}_{\text{difference of convex functions}} - \frac{\sigma^2 + \sum_{j=1}^N |\mathbf{h}_i^H \mathbf{w}_j|^2}{\zeta_i} \leq 0, \forall i,$$

$$C_2, C_3, C_4, C_6$$

### Remarks:

- $P(\eta_i) \triangleq \eta_i \log \eta_i + (1 - \eta_i) \log(1 - \eta_i)$  is convex
- Maximization of  $P(\eta_i)$  yields  $\eta_i \in \{0, 1\}$  for appropriate  $\lambda$
- $\mathcal{P}_4$  is a DC problem: DC objective s.t DC and convex constraints
- Efficient than SDP based DC formulation: No rank ambiguity and less complex
- $\mathcal{P}_4$  is solved using Convex-concave procedure (CCP)
- Feasible initial point  $\implies$  convergence to a stationary point for CCP based solution

## SAJSP a CCP based Solution

Execute the following two steps until convergence:

- Convexify  $\mathcal{P}_4$  around previous point using affine approximations of nonconvex parts
- Solve the convexified problem globally

## Simulation Results

- $\{\beta_i\}_{i=1}^N = 1, \lambda = 1, P_T = 10$  dB
- Results are averaged over 500 iterations
- SUS-ZF/MMSE: Channel orthogonality based user selection followed by ZF/MMSE precoding
- SUS-ZF is used as a initial feasible point

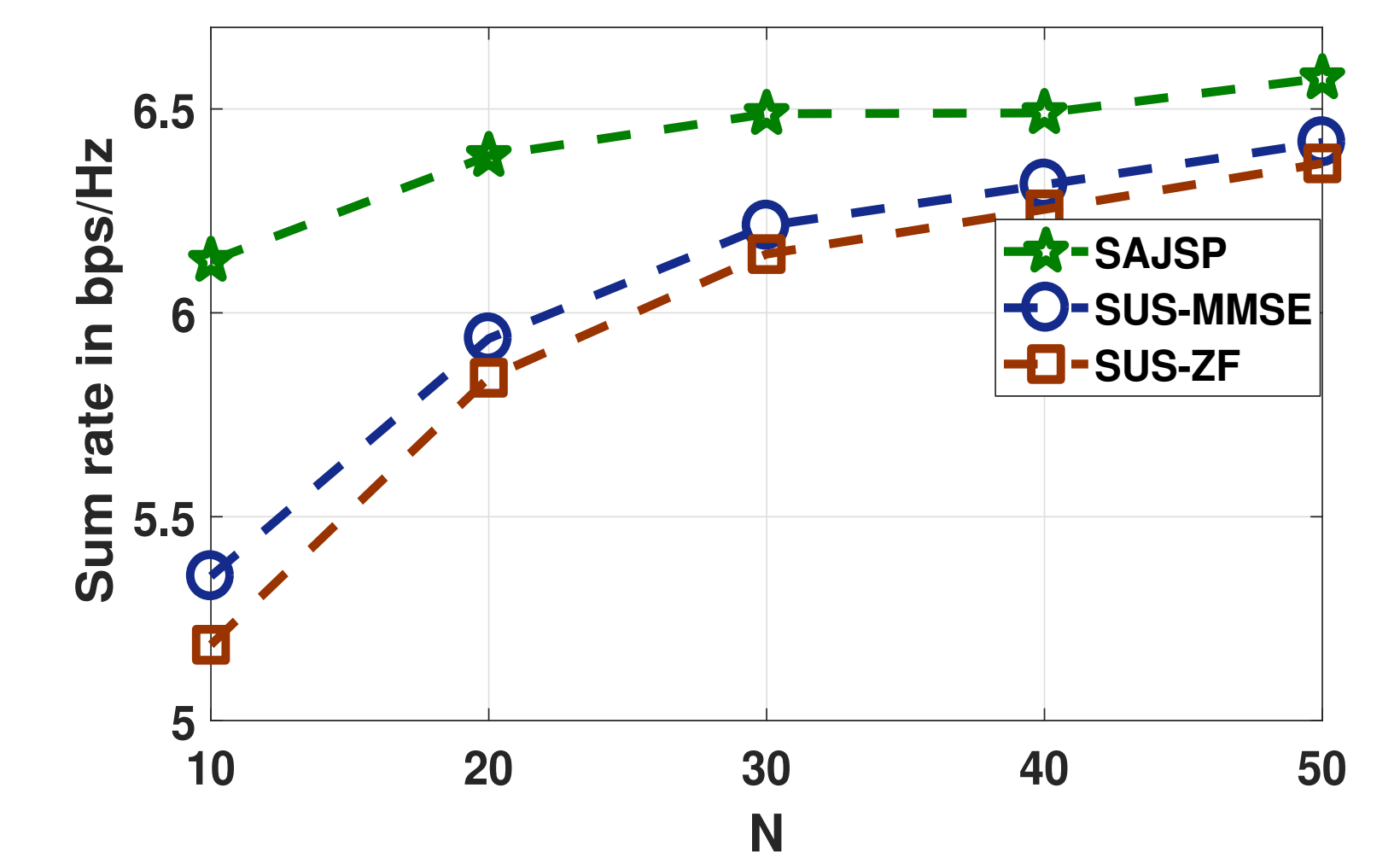


Figure 1: WSR versus  $N$  for  $M=4$  and  $N=[10:10:50]$

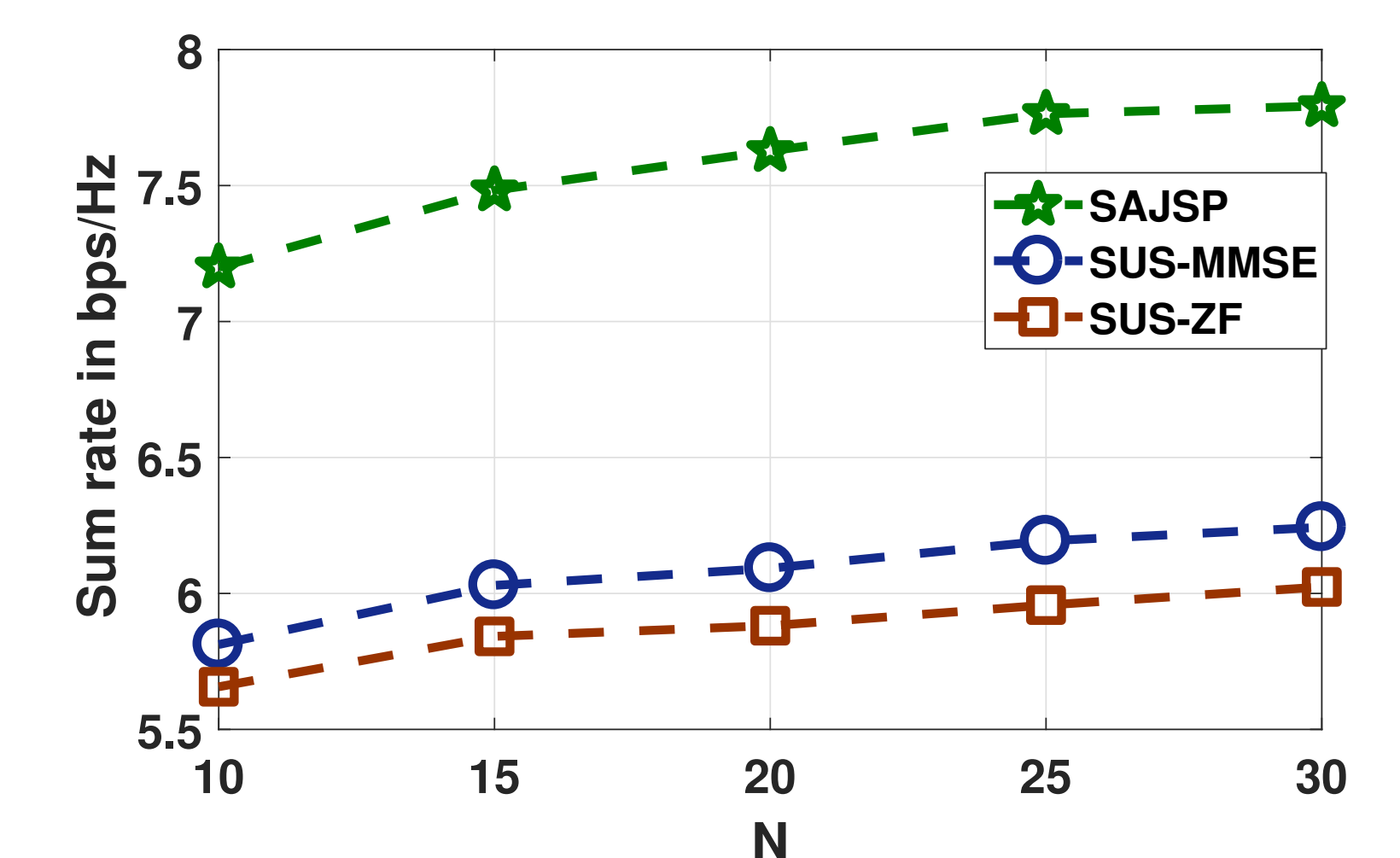


Figure 2: WSR versus  $N$  for  $M=8$  and  $N=[10:5:30]$ .

## Conclusions

Novel formulation  $\rightarrow$  DC reformulation  $\rightarrow$  CCP based solution  $\rightarrow$  efficacy through simulations