

# Optimal Simultaneous Wireless Information and Power Transfer with Low-Complexity Receivers

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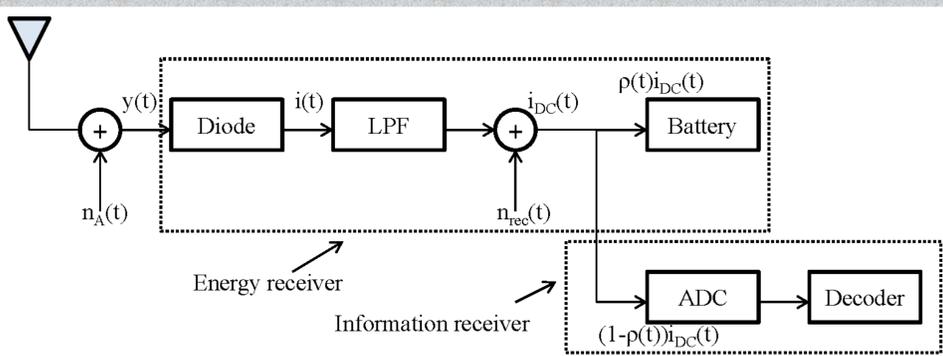
## Motivation

- ✓ In today's widely used devices and internet-of-things (IoT) applications, such as wearables, and sensor networks, energy harvesting (EH) can be seen as the final challenge to true mobility.
- ✓ Harvesting energy from sources using radio frequency signals in communication applications, termed as wireless power transfer (WPT), has received much attention during the last years.
- ✓ Simultaneous wireless information and power transfer (SWIPT) system with an integrated energy and information receiver, with the advantage of low complexity and energy cost.

## Contribution

- A tractable expression of the achievable rate of the integrated receiver.
- Definition of the joint harvested energy-rate outage probability, which is calculated for a point-to-point and multicasting system.
- Minimization of the joint harvested energy-rate outage probability, by optimizing the power-splitting (PS) ratio.

## System Model



The equivalent discrete-time memoryless channel is modeled as

$$Y = l|h|^2PX + Z,$$

or (channel output) = (path loss) × (channel gain) × (average transmit power) × (channel input) + (equivalent processing noise)

➤ channel input:

$$X \geq 0 \in \mathbb{R} \text{ and } \mathbb{E}[X] \leq 1$$

➤ equivalent processing noise caused by the rectifier and the analog-to-digital converter (ADC):

$$Z \sim \mathcal{N}\left(0, \sigma_{\text{rec}}^2 + \frac{\sigma_{\text{ADC}}^2}{(1-\rho)^2}\right) \quad \text{PS factor}$$

**Two systems:**

point-to-point communication

downlink multicasting, the base station transmits the same information to N users, simultaneously.

## Harvested Energy-Rate Trade-off

❖ Harvested energy:  $Q = \rho \zeta l P$  conversion efficiency

❖ Achievable rate:

$$R = \frac{1}{2} \log_2 \left( 1 + \frac{e(l|h|^2P)^2}{2\pi\sigma^2} \right)$$

$$\sigma = \sigma_{\text{rec}}^2 + \frac{\sigma_{\text{ADC}}^2}{(1-\rho)^2}$$

There is no exact expression for the capacity, the proposed one is a lower bound.

## Harvested Energy-Rate Region

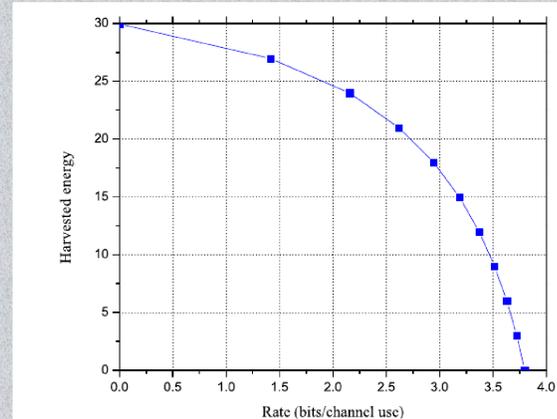


Fig. 1. Harvested energy-rate region with  $P = 100$ ,  $h \sim \mathcal{CN}(0, 1)$ ,  $\zeta = 0.6$ ,  $l = \frac{1}{2}$ ,  $\sigma_{\text{ADC}}^2 = 1$ .

## Joint Harvested Energy-Rate Outage Probability

**Definition:**  $P_o = \Pr(Q \leq q_{\text{th}} \cup R \leq r_{\text{th}})$ ,

energy threshold

rate threshold.

It is proved that the joint harvested energy-rate outage probability for the point-to-point system is given by

$$P_o = 1 - e^{-\max\left\{\frac{q_{\text{th}}}{\rho \zeta l P}, \frac{1}{lP} \sqrt{\frac{2\pi\sigma^2}{e}} (2^{2r_{\text{th}}-1})\right\}}$$

The optimal value of  $\rho \in [0, 1]$  is given by the solution of

$$\rho^4 - 2\rho^3 + \left(1 + \frac{\sigma_{\text{ADC}}^2}{\sigma_{\text{rec}}^2} - \frac{A^2}{2\pi e \sigma_{\text{rec}}^2 B^2}\right) \rho^2 + \frac{2A^2}{\sigma_{\text{rec}}^2 B^2} \rho - \frac{A^2}{\sigma_{\text{rec}}^2 B^2} = 0,$$

where  $A = \frac{q_{\text{th}}}{\zeta l P}$  and  $B = \frac{1}{lP} \sqrt{\frac{2\pi}{e}} \sqrt{2^{2r_{\text{th}}-1}}$ .

## Results

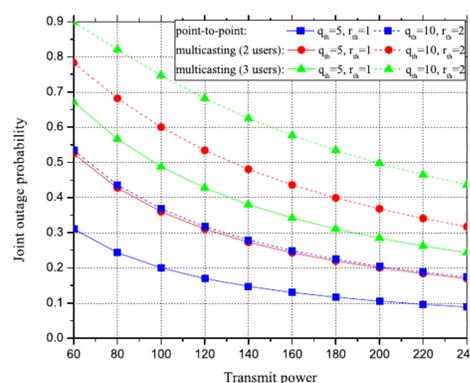


Fig. 2. Outage probability versus transmit power.

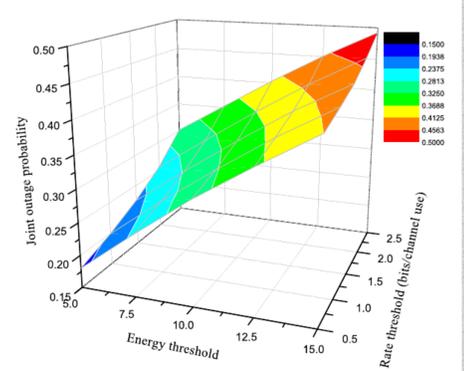


Fig. 3. Outage probability versus energy and rate thresholds in a point system.

## Conclusions

- A tractable expression for the achievable rate is provided.
- The joint harvested energy-rate outage probability is defined, calculated in closed-form expressions for a point-to-point and a multicasting system and minimized by optimizing the PS factor.
- The proposed theoretical framework facilitates the investigation of performance of the integrated receiver and opens the road for future research on this topic.