

# A watermarking technique to secure printed QR-Codes

## Statistical hypothesis testing

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The QR (Quick Response) code is a two-dimensional barcode, which was designed for storage information and high speed reading applications. Being cheap to produce and fast to read, it becomes actually a popular solution for product labeling.



Ones try to make QR code a solution against counterfeiting. We present a novel technique that permits to create a secure printed QR code which is robust against Scan & Reprint attack. The code, named as W-QR code, is constructed by replacing the background of the standard one by a specific textured pattern

which does not affect the normal reading of the encoded message. Scan & Reprint attacks lead to the degradation of the texture and change its statistical characteristics which can be detected thanks to a statistical test.

### Concept of W-QR Code

#### Construction

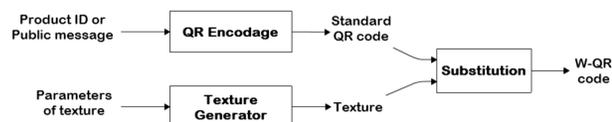


Figure 1: Proposed flowchart for the construction of W-QR

#### Reading and Authentication

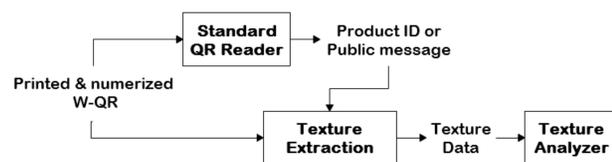


Figure 2: Proposed flowchart for the reading and validation of W-QR

### Clipping Gaussian Noise Texture

The Clipping Gaussian Noise (CGN) texture is characterized by a couple of two parameters  $(\mu, \sigma)$ . A CGN texture is created from a matrix of  $\mu$ -mean and  $\sigma$ -standard deviation Gaussian noise by replacing all the values which are greater than 255 by 255, and all the values which

are smaller than 0 by 0. The replacement creates an artificial clipping effect, which produces a texture saturated in the bright-rank or the dark-rank or both depending on the value of  $(\mu, \sigma)$ .

Denote  $CGN_{\mu, \sigma}$  the texture characterized by the couple  $(\mu, \sigma)$ . The figure below shows an example of the  $CGN_{200, 70}$  texture and its histogram.

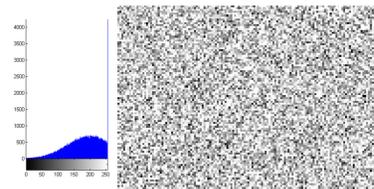


Figure 3: CGN (right to left): the texture and its histogram

### Proposed Statistical Detector

#### Noise Local Variance Model

NLV is the local variance of noise which is calculated within each  $8 \times 8$  block of image [1]. Distribution of NLV values of a given image could be approximated by a Gamma distribution.

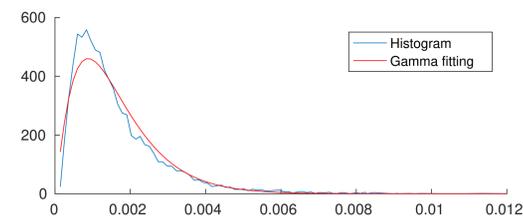


Figure 4: Histogram of block variance compared with its Gamma fitting curve

The distribution of NLV observed from images of falsified textures behaves much differently from the ones of falsified textures.

#### Statistical Test

Denote  $X = \{X_i\}_{i=1, \dots, n}$  the set of all NLV values of an image, where  $i$  is the block index and  $n$  the total number of blocks in the image. We can formulate a hypothesis test as follows:

$$\begin{cases} \mathcal{H}_0 : \{X \sim \mathcal{G}(a, b)\}, & (a, b) \text{ are known} \\ \mathcal{H}_1 : \{X \approx \mathcal{G}(a, b)\} \end{cases} \quad (1)$$

where  $\mathcal{G}(a, b)$  denotes a Gamma distribution with  $a$  and  $b$  respectively the form and scale parameters of the distribution.

From a recent work of José *et al.*, in [2], it follows that we can obtain an estimator of the scale parameter by calculating the covariance between  $X$  and  $Z = \log(X)$ , that is defined as follows:

$$\hat{\beta}_n = \frac{1}{n} \sum_i^n (X_i - \bar{X})(Z_i - \bar{Z}) \quad (2)$$

It is proved that under  $\mathcal{H}_0$ , we have that:

$$S = \frac{\sqrt{n}(\hat{\beta}_n - b)}{\eta} \xrightarrow{d} \mathcal{N}(0, 1) \quad (3)$$

where  $\eta^2 = b^2(1 + a\psi_1(a))$ , and  $\psi_1(\cdot)$  denotes the trigamma function. For a given prescribed false-alarm probability  $\alpha_0$ , we propose a test based on the statistics  $S$  which rejects  $\mathcal{H}_0$  if either  $S < \Phi^{-1}(\alpha_0/2)$  or  $S > \Phi^{-1}(1 - \alpha_0/2)$ , where  $\Phi^{-1}(\cdot)$  denotes the inverse of the cdf of the standard Gaussian random variable.

### Experiments & Results

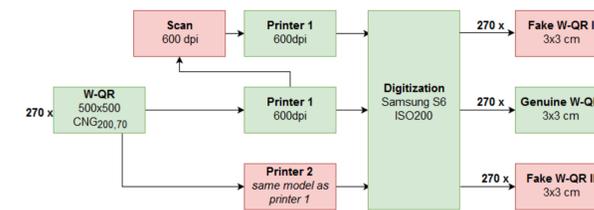


Figure 5: Description of testing database

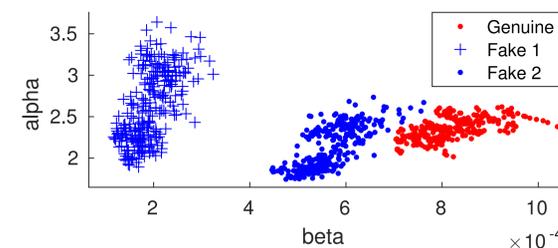


Figure 6: Distribution of couples  $(\beta, \alpha)$  of genuine textures and falsified textures created by Scan&Reprint (labeled as Fake 1) and by printing from numeric code but by another printer (labeled as Fake 2); Each dot or cross represents the couple  $(\beta, \alpha)$  estimated from one image.

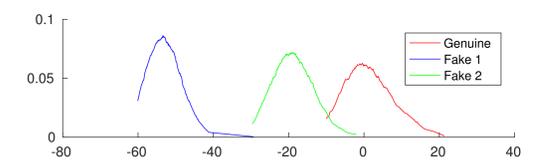


Figure 7: Empirical distribution of the proposed test statistics under different sets of data

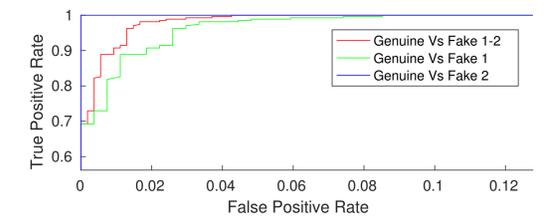


Figure 8: Performance ROC curves

### Conclusion

- A novel watermarking technique is proposed to secure printed QR codes, which may be used as a very cheap solution to fight against counterfeiting. A specific random texture, sensitive to Print&Scan processes, is substituted with the background of standard QR code to create a secure one, the W-QR code.
- A performing statistical detector basing on the NLV model is presented.

### Forthcoming Research

In a recent work, we propose a novel embedding technique, which makes the texture more sensible to Scan&Reprint attacks. The NLV model was also upgraded and new more powerful statistical detector could be constructed.

### References

- [1] H. P. Nguyen, F. Retraint, F. Morain-Nicolier, and A. Delahaies. Face spoofing attack detection based on the behavior of noises. In *2016 IEEE Global Conference on Signal and Information Processing (GlobalSIP)*, pages 119–123, Dec 2016.
- [2] José A. Villaseñor and Elizabeth González-Estrada. A variance ratio test of fit for gamma distributions. *Statistics & Probability Letters*, 96:281–286, January 2015.