

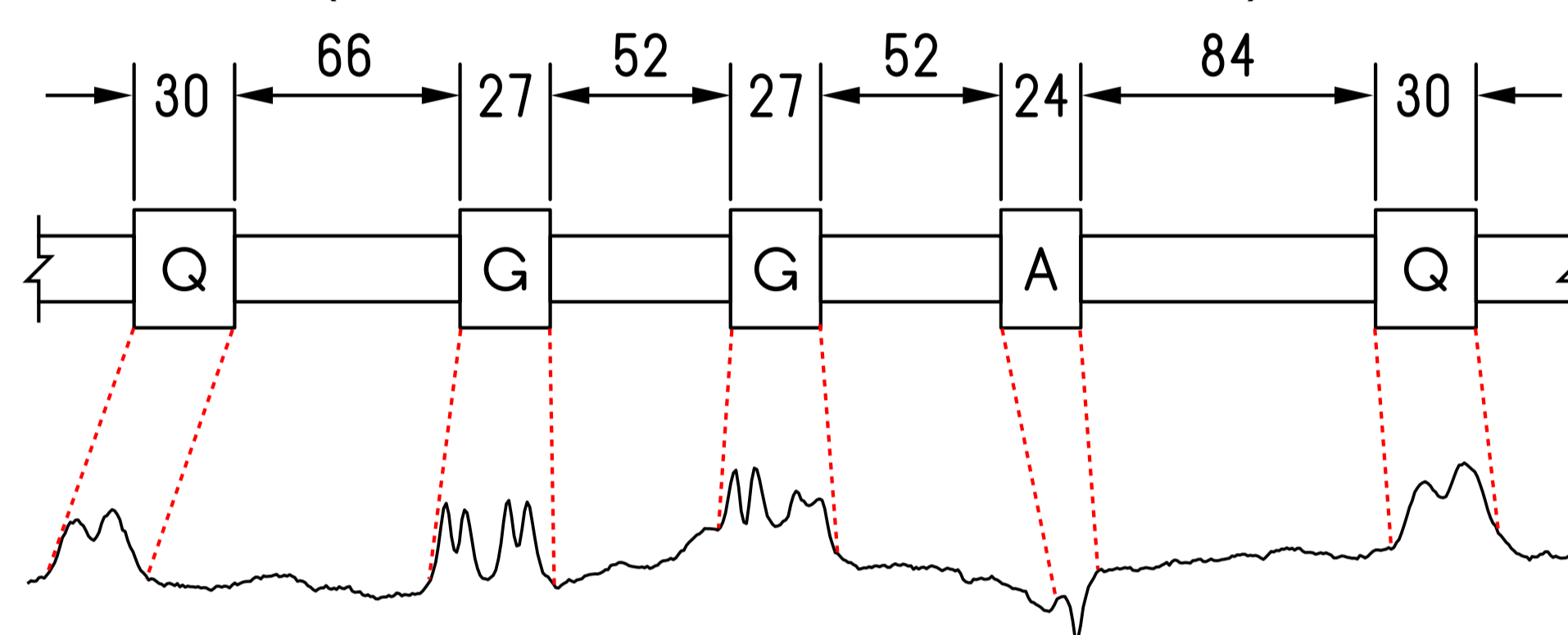
Pattern Localization in Time Series through Signal-To-Model Alignment in Latent Space

Problem

We are given a time series that contains a sequence of patterns, and a theoretical model (the “blueprint”) that lists the expected locations of these patterns (start/end in mm, seconds, ...).

The localization problem consists in estimating the precise (start and end) locations of each of the patterns in the time series.

- ▶ Example 1: Audio-to-score alignment [1].
- ▶ Example 2: Aligning a sensor measurement of a 1D structure to its known blueprint (e.g. in industrial environments). Illustration:



- ▶ In the literature, this localization problem is solved through alignment, typically by using Dynamic Time Warping (see bottom box).
- ▶ But alignment techniques require 2 time series → the second time series is obtained by *synthesis* based on the model.
- ▶ An accurate synthesis technique is key! → requires *domain knowledge*.
- ▶ True patterns may include *variations* that worsen alignment (e.g. “G”).

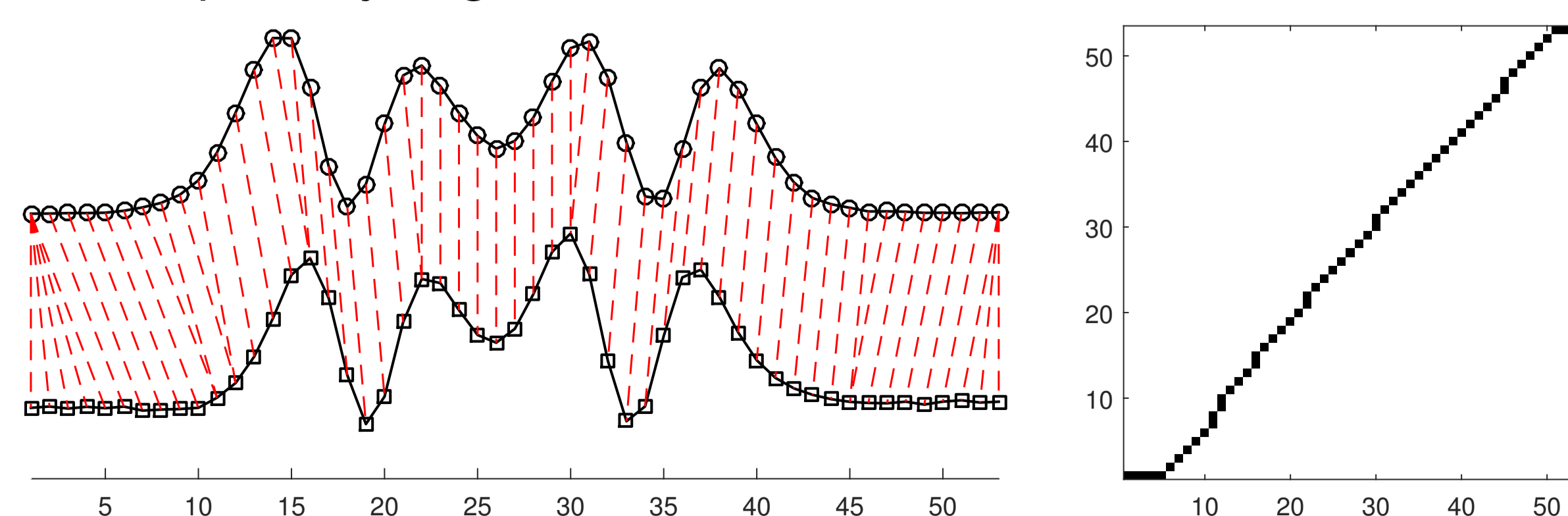
Main idea

Use supervised machine learning to improve the alignment by learning transformations for the true and the synthesized time series into a space in which they are more similar.

- ▶ The optimal transformation is learned by Canonical Correlation Analysis (CCA) (see box to the right).
- ▶ CCA can compensate for the shortcomings of a generic synthesis.

Dynamic Time Warping

Dynamic Time Warping (DTW) is the de-facto standard technique for aligning time series [2]. Given two time series, DTW seeks the warping path that optimally aligns them.



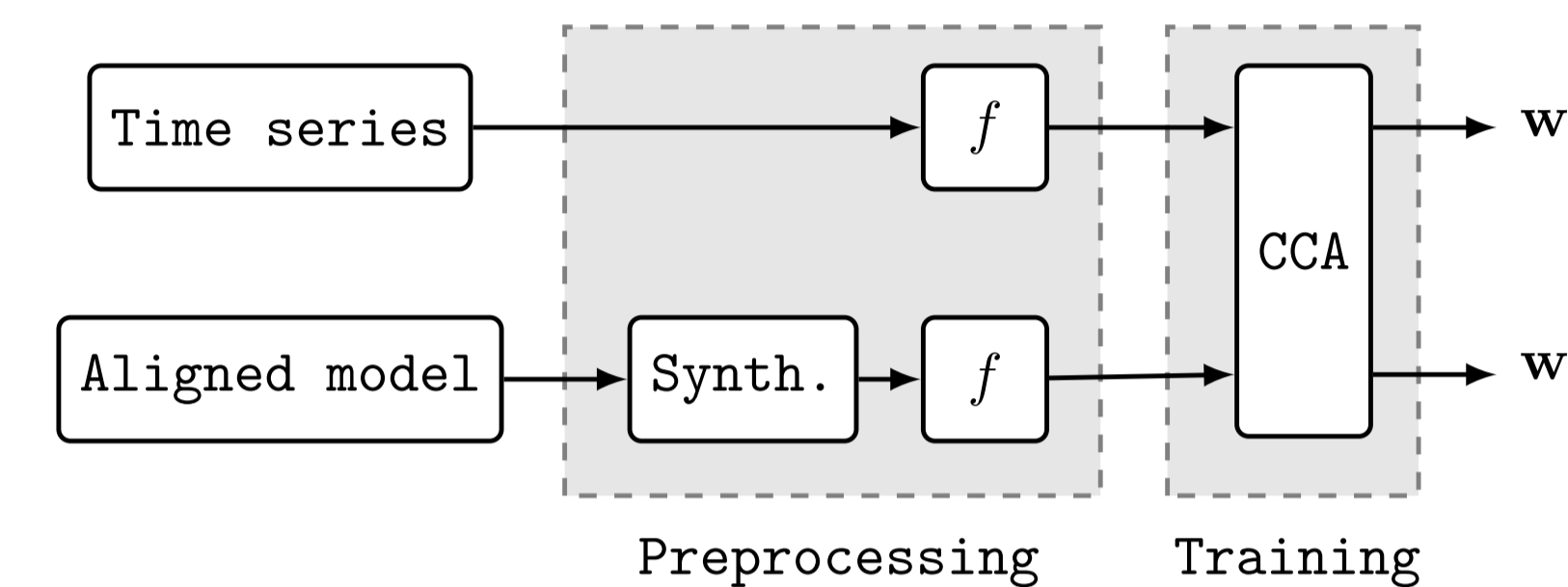
Proposed Machine Learning Framework

Training stage:

Input: A time series and the corresponding *aligned* model (labeled by a domain expert).

1. The model is synthesized into a time series;
2. Both time series may optionally undergo a fixed transformation;
3. CCA is performed.

Output: The coefficients of the 2 CCA transformations.

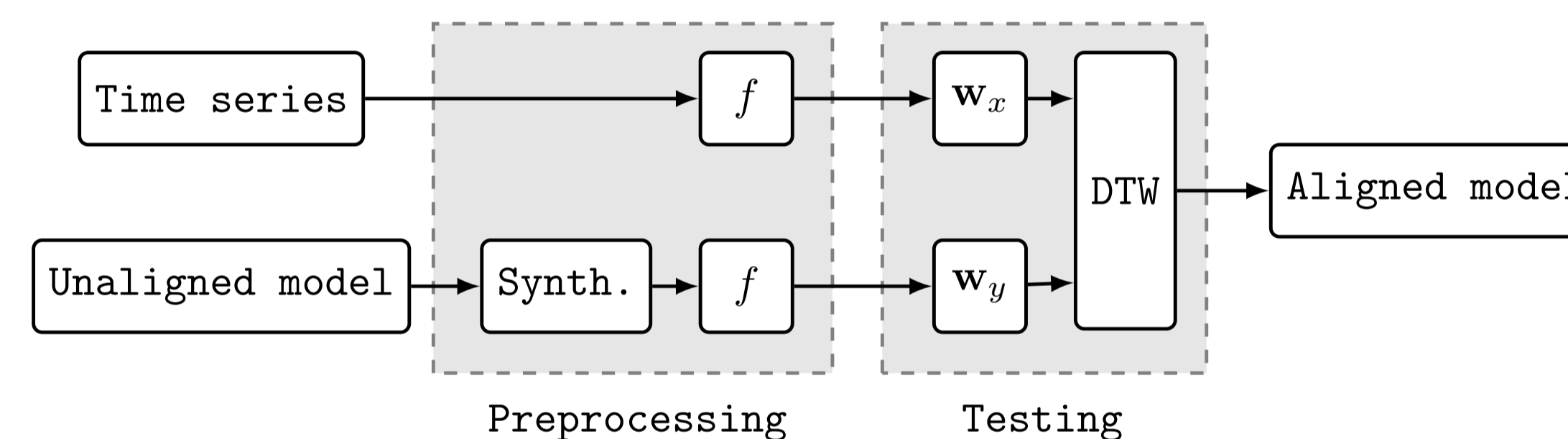


Testing stage:

Input: A time series and the corresponding *unaligned* model.

1. Same preprocessing as in the training stage;
2. Both time series are mapped into the latent space.
3. DTW is applied.

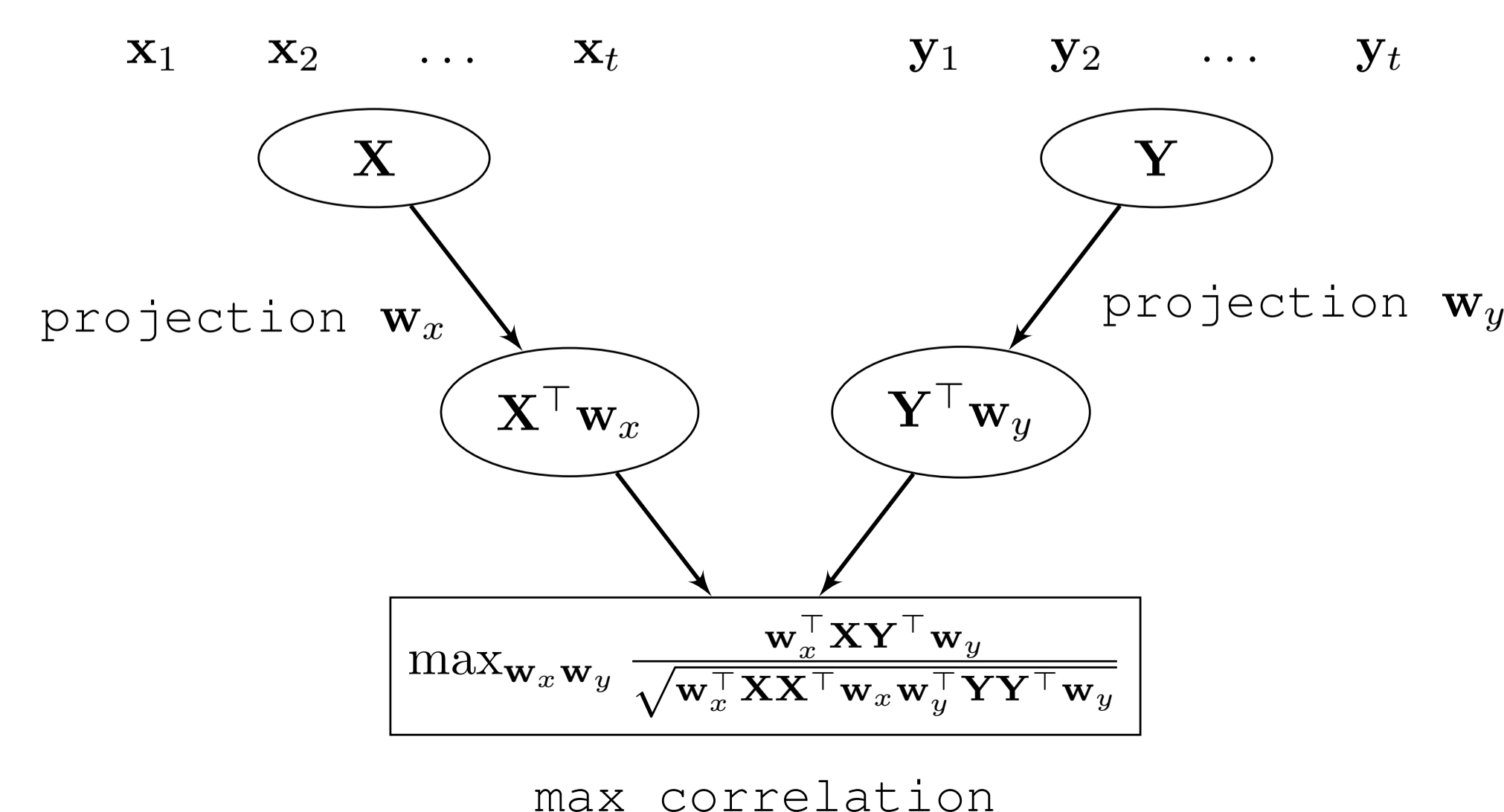
Output: Alignment solution for the time series and the model.



Canonical Correlation Analysis

Given two multidimensional random variables x and y , canonical correlation analysis (CCA) seeks a pair of optimal linear transformations such that the transformed variables are maximally correlated [3].

$$\begin{matrix} x_1[1] & x_1[2] & \dots & x_1[t] & y_1[1] & y_1[2] & \dots & y_1[t] \\ x_2[1] & x_2[2] & \dots & x_2[t] & y_2[1] & y_2[2] & \dots & y_2[t] \\ \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \ddots & \vdots \\ x_m[1] & x_m[2] & \dots & x_m[t] & y_n[1] & y_n[2] & \dots & y_n[t] \end{matrix}$$



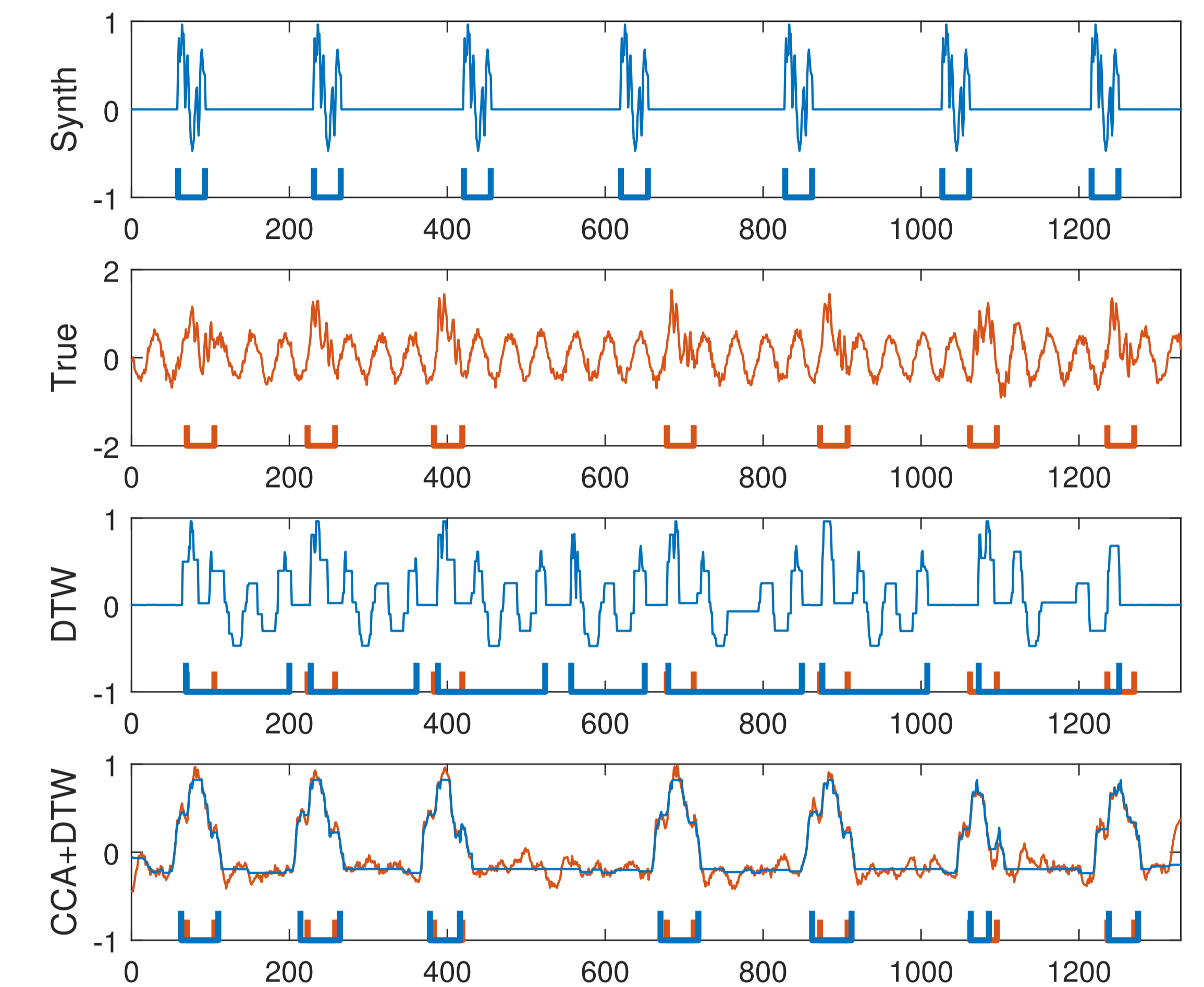
Experiments

Pattern localization for non-destructive testing of heat generator tubes in nuclear power plants (cf. initial illustration). Blueprint (model) is available.

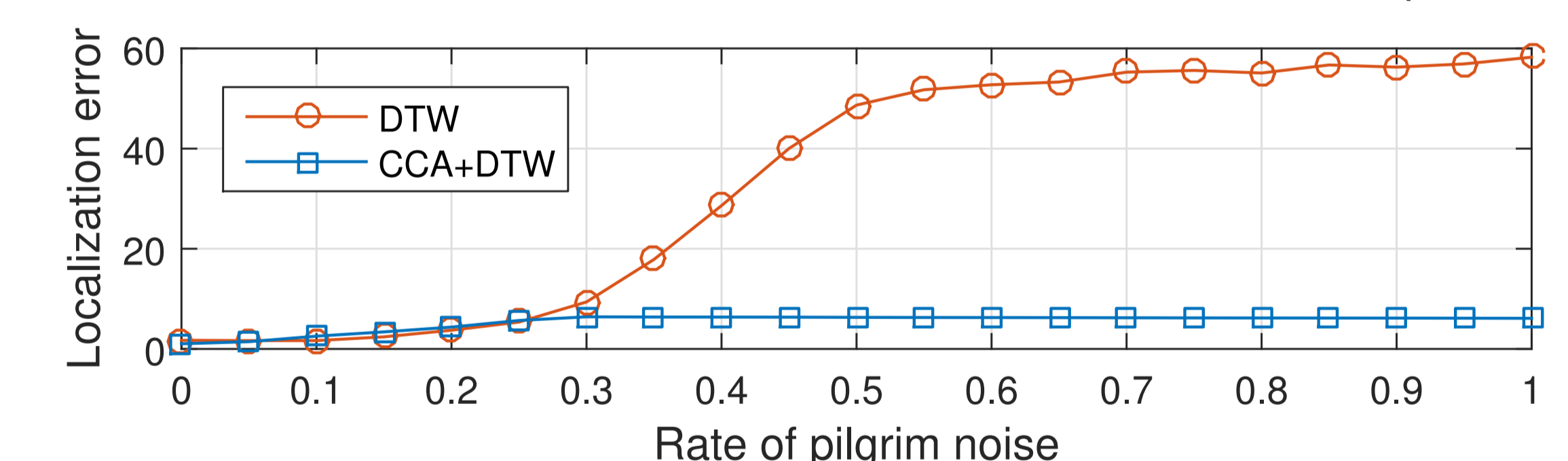
Experiment 1: Training with a single time series (7 patterns).

Synthesis through replication.

Function f : time-embedding of 20 past and 20 future samples.



Experiment 2: Influence of different rates of pilgrim noise (simulated).



Conclusions

- ▶ Pattern localization in a time series for which a model is available.
- ▶ True and synthesized time series are mapped into an optimal latent space (learned by CCA), then aligned by DTW.
- ▶ Results are better and more robust compared to DTW only.
- ▶ Uses little domain-specific knowledge – applicable in many contexts.

References

- [1] John Thickstun, Zaid Harchaoui, and Sham Kakade. Learning features of music from scratch. In *ICLR*, 2017.
- [2] Taras K. Vintsyuk. Speech discrimination by dynamic programming. *Cybernetics*, 4(1):52–57, 1968.
- [3] Harold Hotelling. Relations between two sets of variates. *Biometrika*, 28(3/4):321–377, 1936.