

Edge Preserving Multiscale Image Decomposition with Customized Domain Transform Filters

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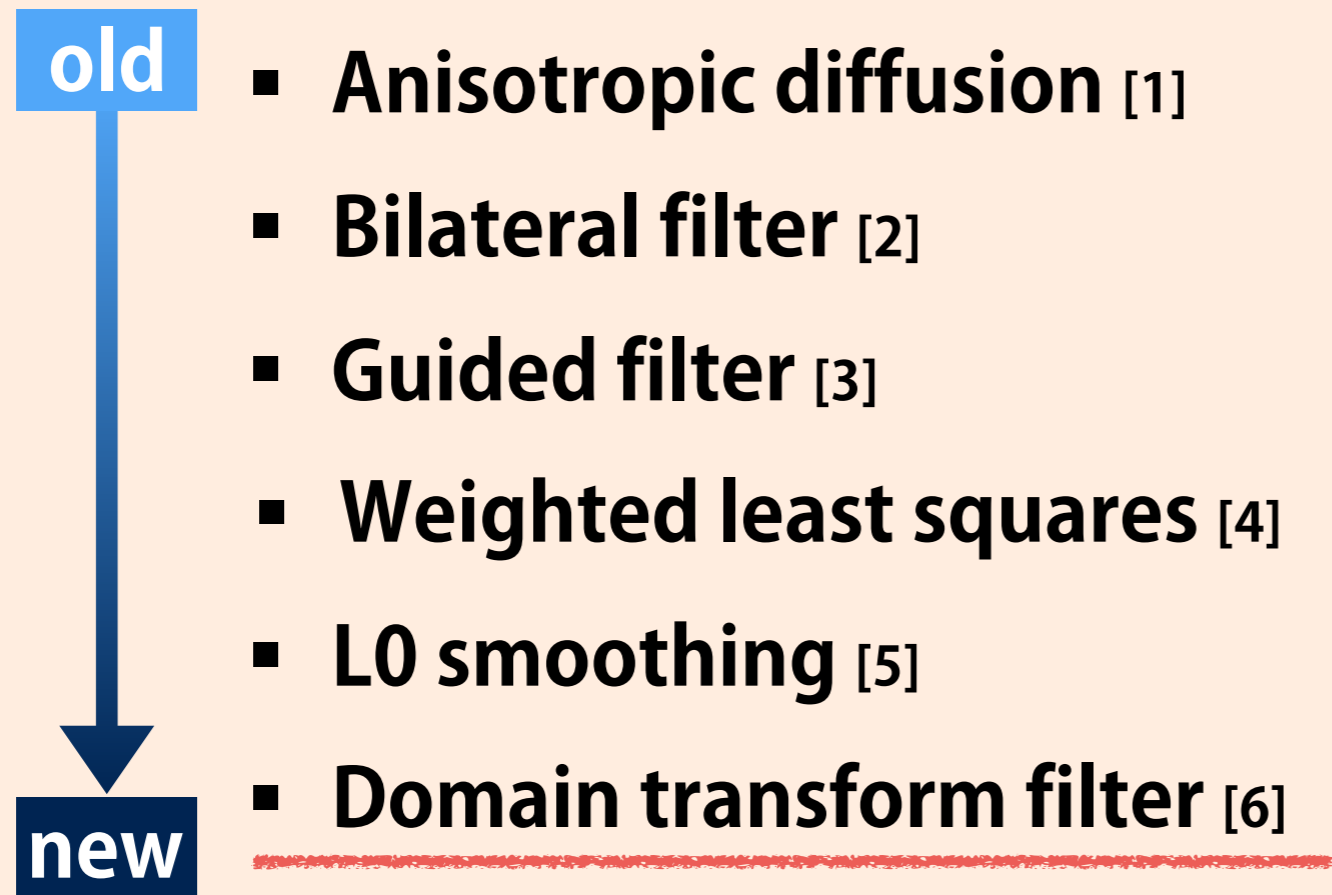
Akie Sakiyama

Yuichi Tanaka

- ① **introduction**
- ② **conventional method**
 - **domain transform filter**
- ③ **objective and proposed method**
- ④ **experiment**
- ⑤ **conclusion**

INTRODUCTION

- edge has important information of signals and images
- many edge preserving smoothing filters have been proposed



[1] P. Perona and J. Malik, "Scale-space and edge detection using anisotropic diffusion," IEEE Trans. Pattern Anal. Mach. Intel., vol. 12, no. 7, pp. 629 - 639, Jul. 1990.

[2] C. Tomasi and R. Manduchi, "Bilateral filtering for gray and color images," in Proc. IEEE Int. Conf. Computer Vision, pp. 839 - 846, Jan. 1998.

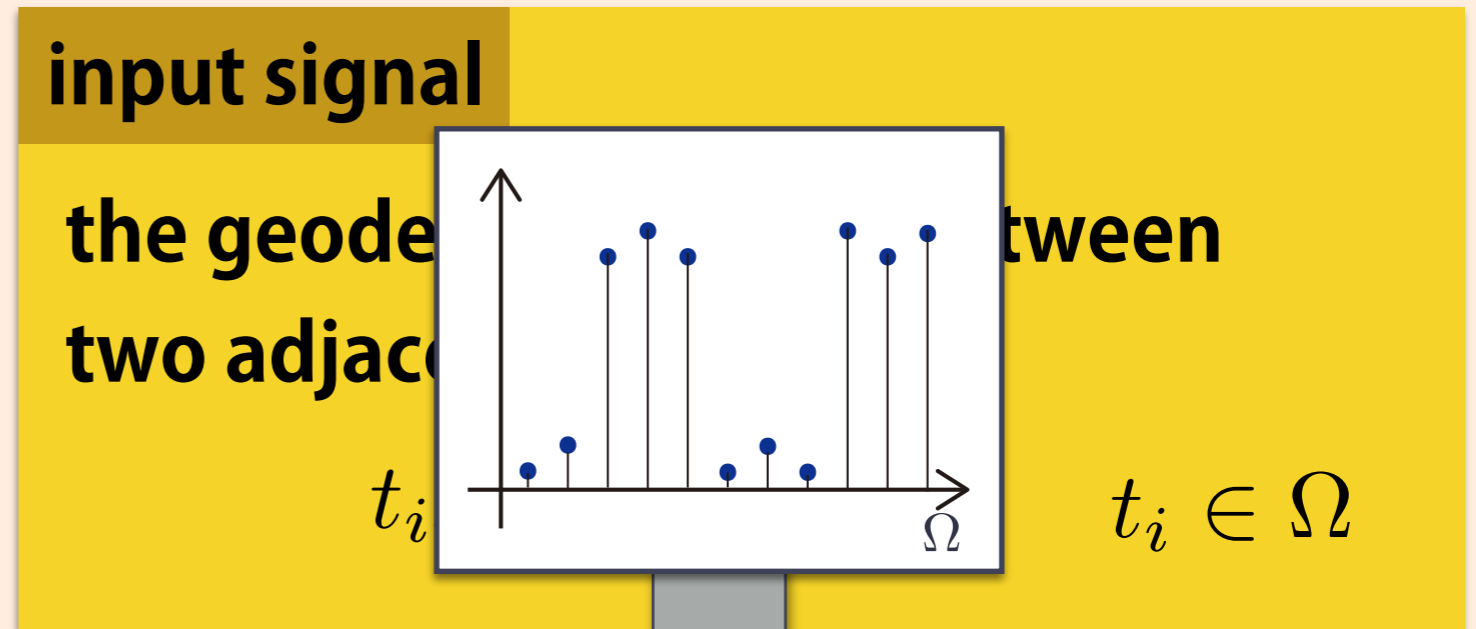
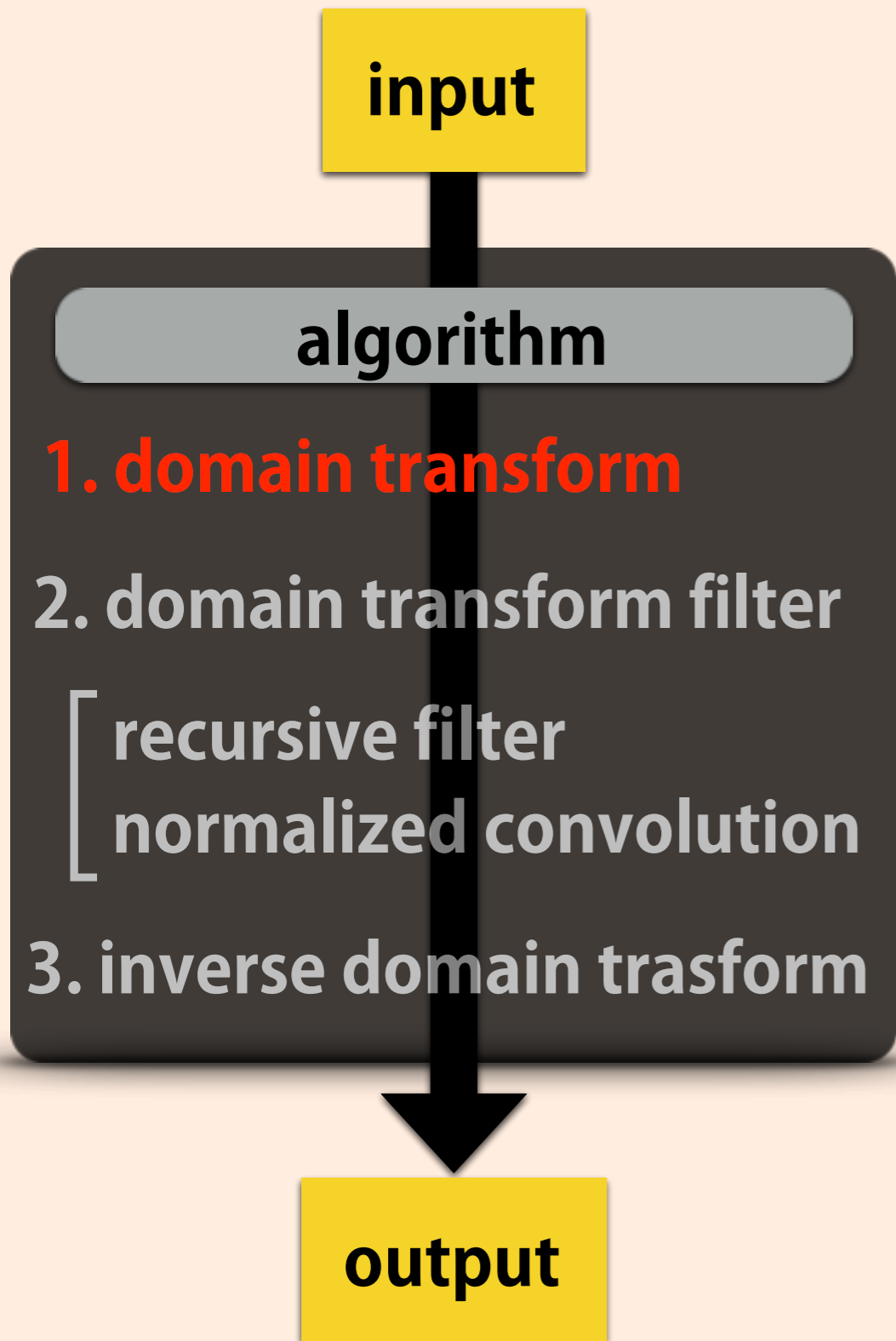
[3] K. He, J. Sun, and X. Tang, "Guided Image Filtering," in Proc. European Conf. Computer Vision, pp. 1-14, 2010.

[4] Z. Farbman, R. Fattal, D. Lischinski and R. Szeliski, "Edge-preserving decompositions for multi-scale tone and detail manipulation," ACM Trans, Graph., vol. 27, no. 3. p67, 2008.

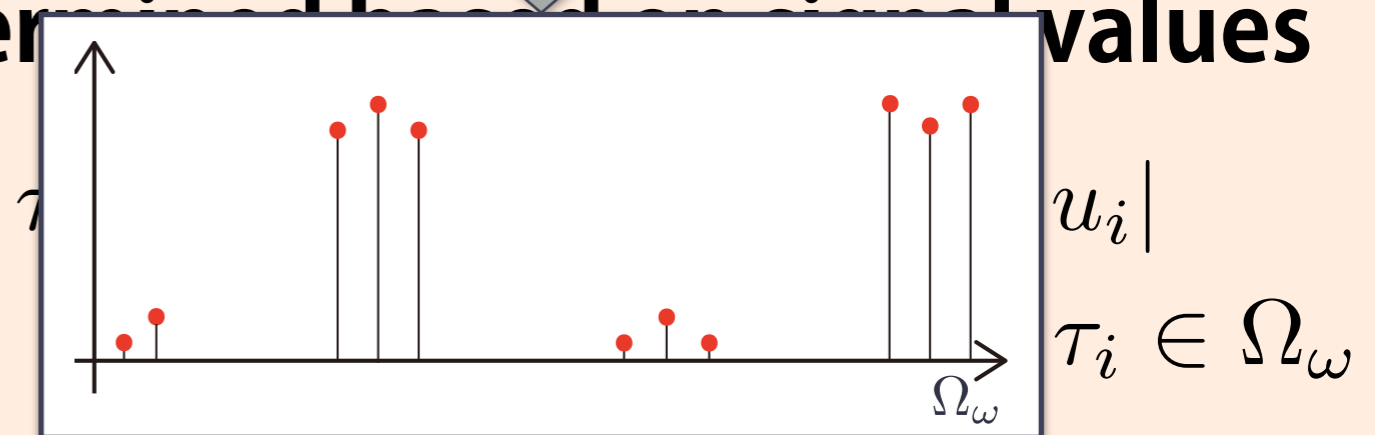
[5] L. Xu, C. Lu, Y. Xu, and J. Jia, "Image smoothing via L0 gradient minimization," ACM Trans. Graph., vol. 30, no. 6, p. 174, Dec. 2011.

[6] E. S. L. Gastal and M. M. Oliveira, "Domain transform for edge-aware image and video processing," in Proc. ACM SIGGRAPH, vol. 30, no. 4, p. 69, 2011.

domain transform filter



1. Domain Transform (DT)
the geodesic distance is determined by their signal values



u : signal value

t : coordinate of before DT

τ : coordinate of after DT

Ω : domain of before DT

Ω_ω : domain of after DT

domain transform filter

input

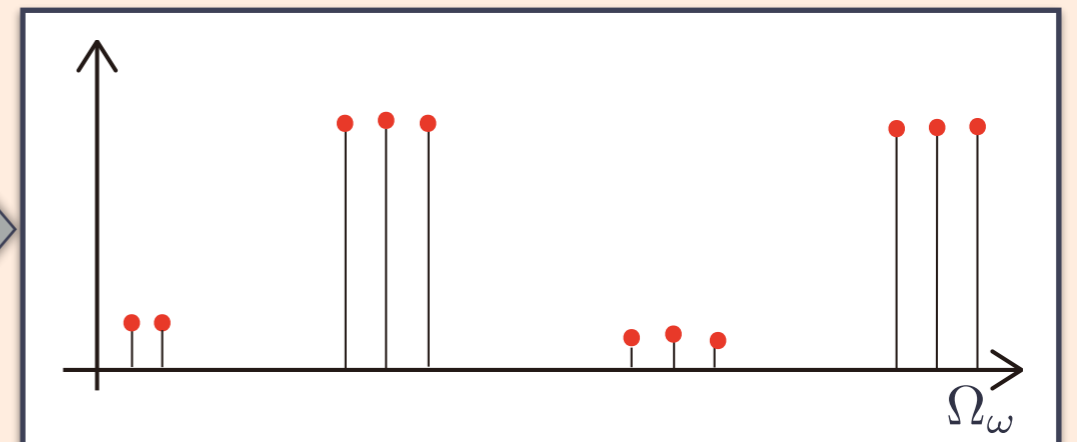
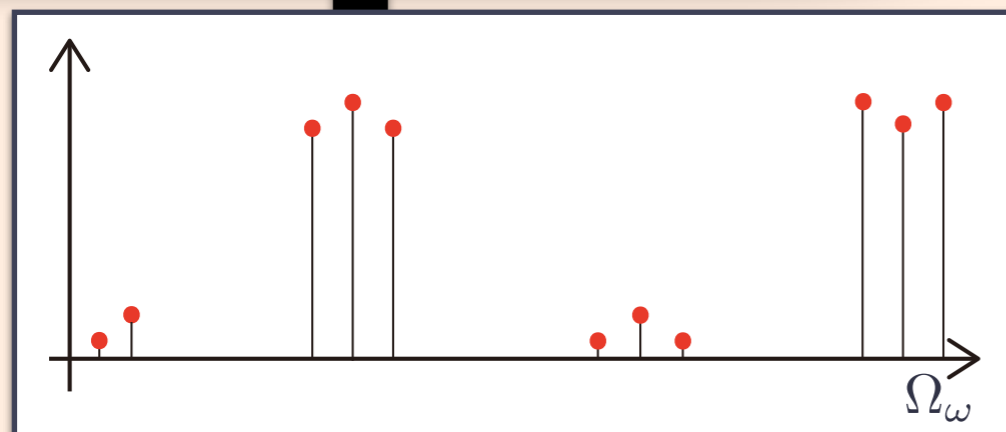
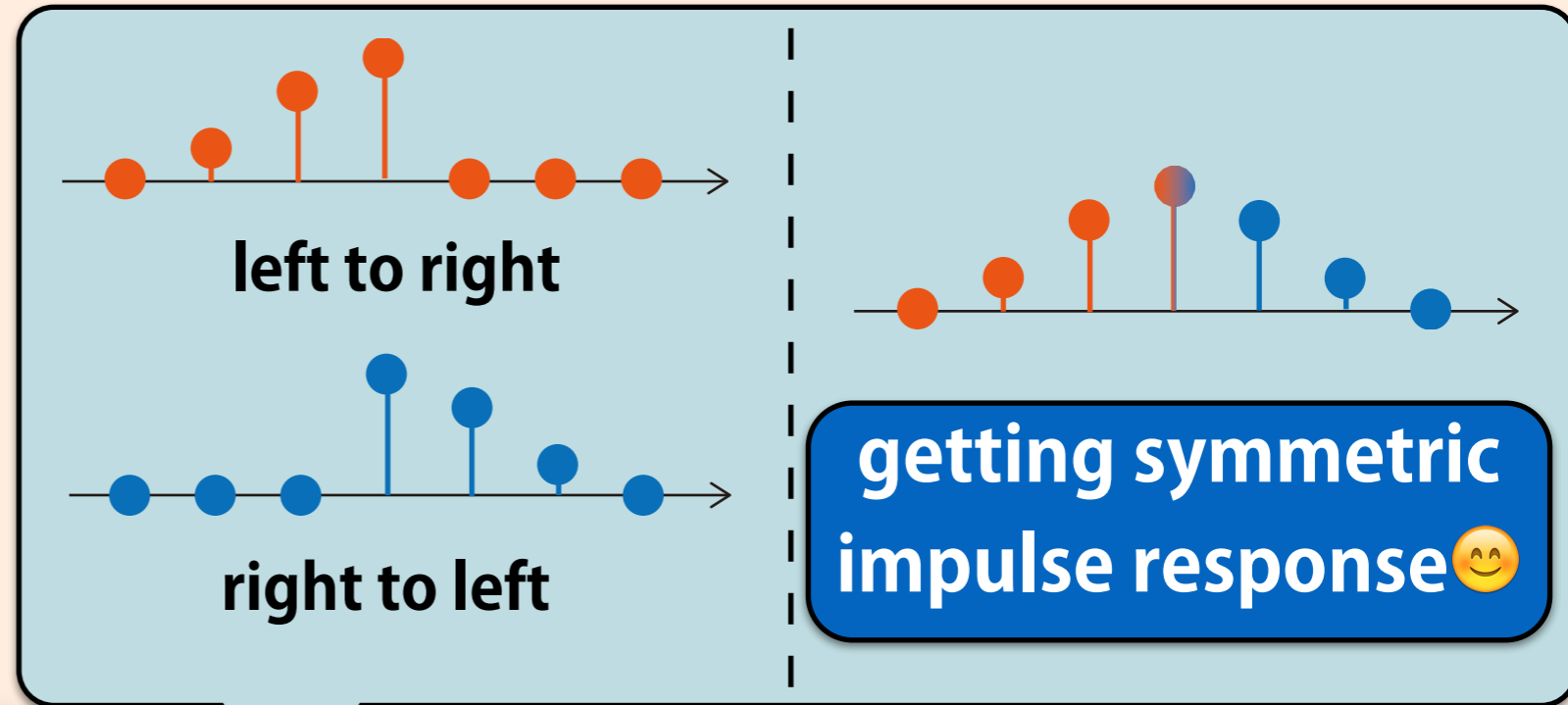
algorithm

1. domain transform
2. domain transform filter
 - recursive filter
 - normalized convolution
3. inverse domain transform

Recursive Filter (RF)

type of filter which reuses output as input in the next step

$$y_i = \left(1 - a^{(\tau_i - \tau_{i-1})}\right) u_i + a^{(\tau_i - \tau_{i-1})} y_{i-1}$$



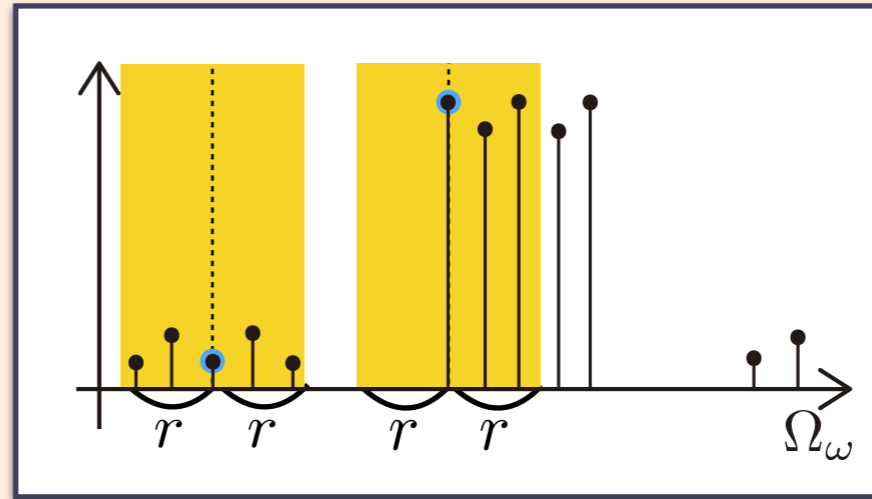
domain transform filter

input

algorithm

1. domain transform
2. domain transform filter
 - recursive filter
 - normalized convolution**
3. inverse domain transform

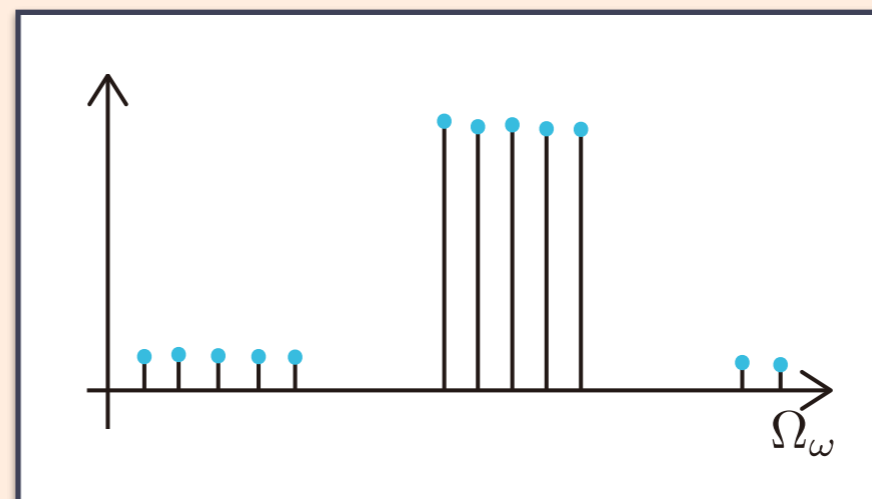
output



Normalized Convolution (NC)

- the average of signal is calculated within r from τ_i in Ω_ω

$$y_i = \frac{\sum_{k \in \Omega_\omega} \delta\{|\tau_i - \tau_k| \leq r\} u_i}{\sum_{k \in \Omega_\omega} \delta\{|\tau_i - \tau_k| \leq r\}}$$



δ : boolean function

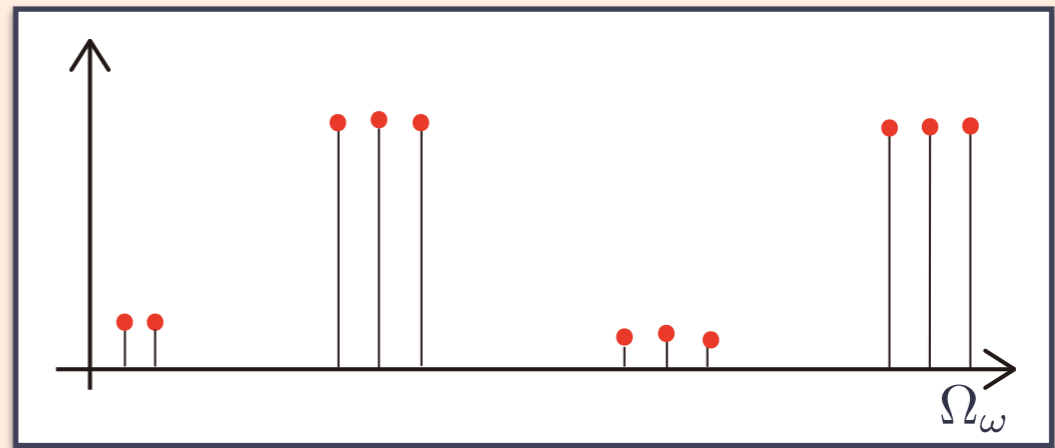
domain transform filter

input

algorithm

1. domain transform
2. domain transform filter
 - recursive filter
 - normalized convolution
3. inverse domain transform

output

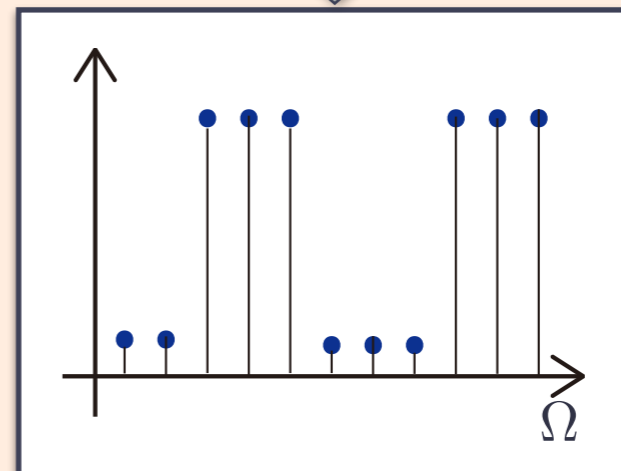


3. inverse domain transform

output signal

equispaced signal is obtained

$$t_{i+1} - t_i := 1 \quad t_i \in \Omega$$



- ① introduction
- ② conventional method
 - domain transform
- ③ **objective and proposed method**
- ④ experiment
- ⑤ conclusion

OBJECTIVE

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original DTF

good points

- fast edge preserving smoothing method
- can be used to many image processing applications

bad points

- in the case of noisy input...
it is difficult to calculate appropriate distance between signals
→ the performance becomes bad
- ⚠ it is highly sensitive to noise ⚠

OBJECTIVE

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multiscale DTF

⚠ it is highly sensitive to noise ⚠

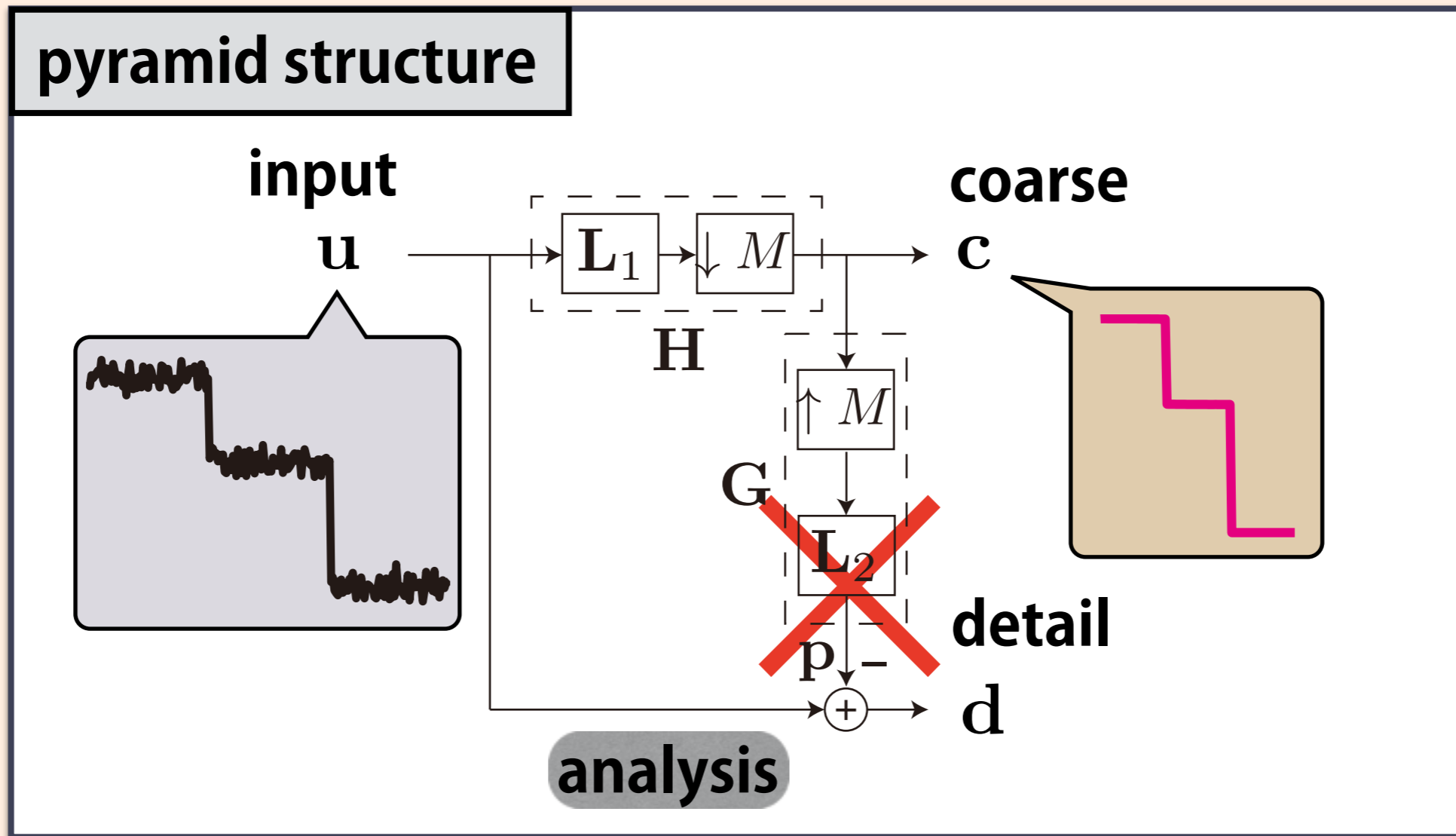


to be robust to noise

multiscale image decomposition method based on the DTF

- uses a similar structure to Laplacian pyramid [6]
- designs optimal filter based on DTF
- realizes several image processing applications

PYRAMID STRUCTURE



- objective function : $\arg \min_c (\|Gc - Fu\|_2^2 + \lambda \|Ac\|_2^2)$

p should be similar to the output of DTF

c : piecewise smoothness

G : lowpass filter

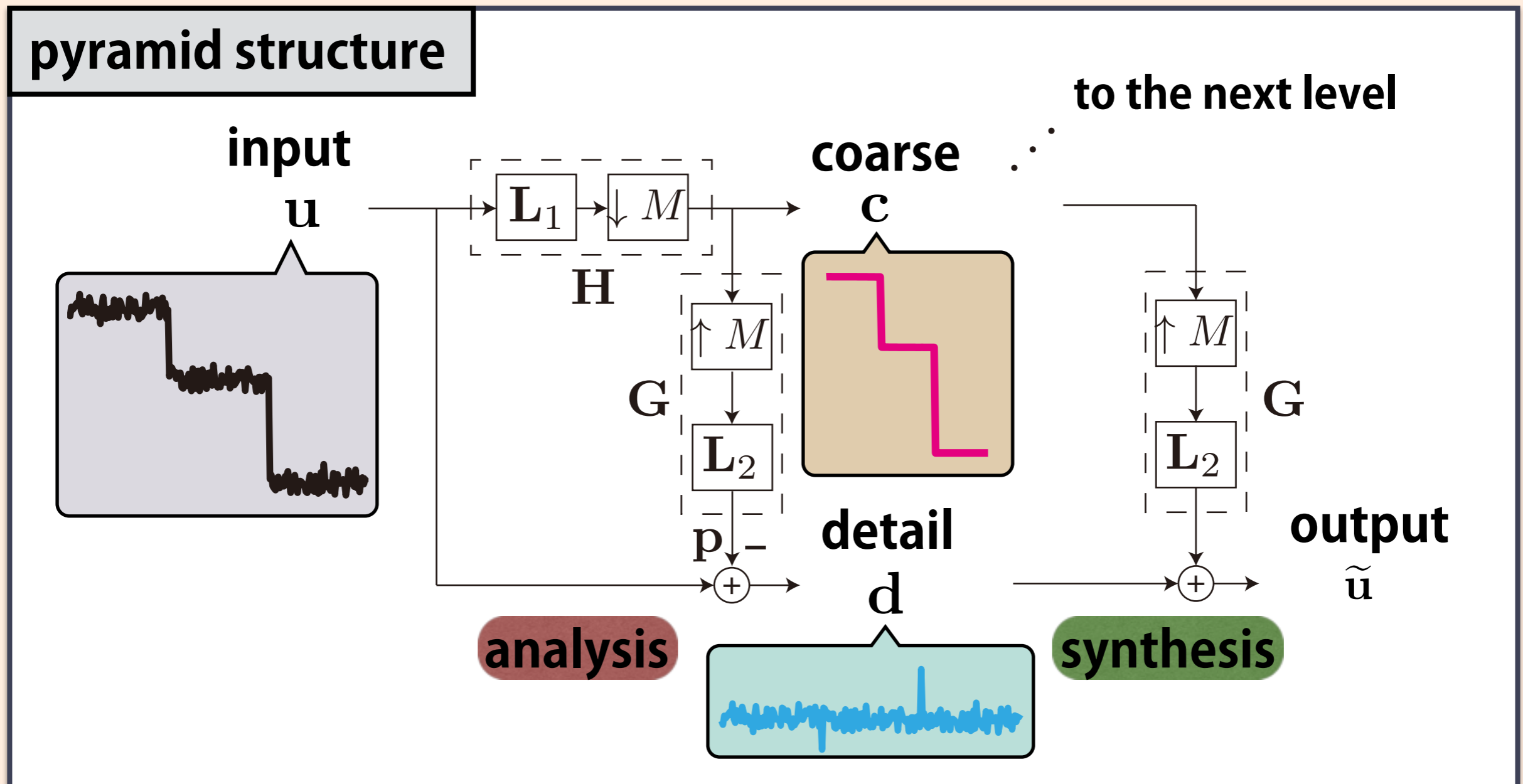
A : highpass filter

F : domain transform filter (DTF)

PYRAMID STRUCTURE

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- **objective function** : $\arg \min_{\mathbf{c}} (\|\mathbf{G}\mathbf{c} - \mathbf{F}\mathbf{u}\|_2^2 + \lambda \|\mathbf{A}\mathbf{c}\|_2^2)$
 $\mathbf{c} = (\mathbf{G}^T \mathbf{G} + \lambda \mathbf{A}^T \mathbf{A})^{-1} \mathbf{G}^T \mathbf{F} \mathbf{u}$
- **optimized filter** : $\mathbf{H} = (\mathbf{G}^T \mathbf{G} + \lambda \mathbf{A}^T \mathbf{A})^{-1} \mathbf{G}^T \mathbf{F}$ $\mathbf{c} = \mathbf{H}\mathbf{u}$

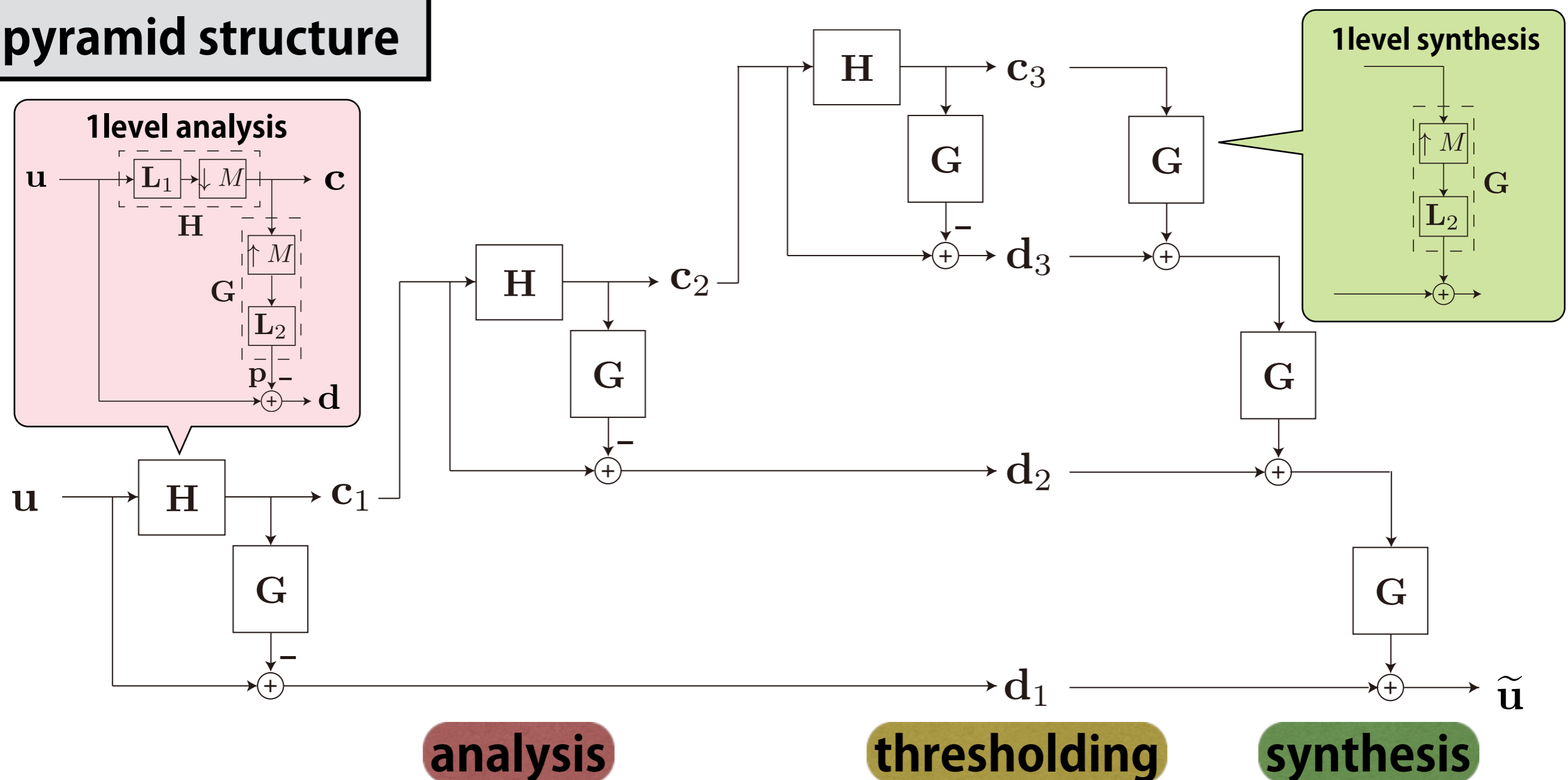


PYRAMID STRUCTURE

- process of the proposed method

input image \rightarrow analysis \rightarrow thresholding \rightarrow synthesis \rightarrow output

pyramid structure



- ① introduction
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- ③ objective and proposed method
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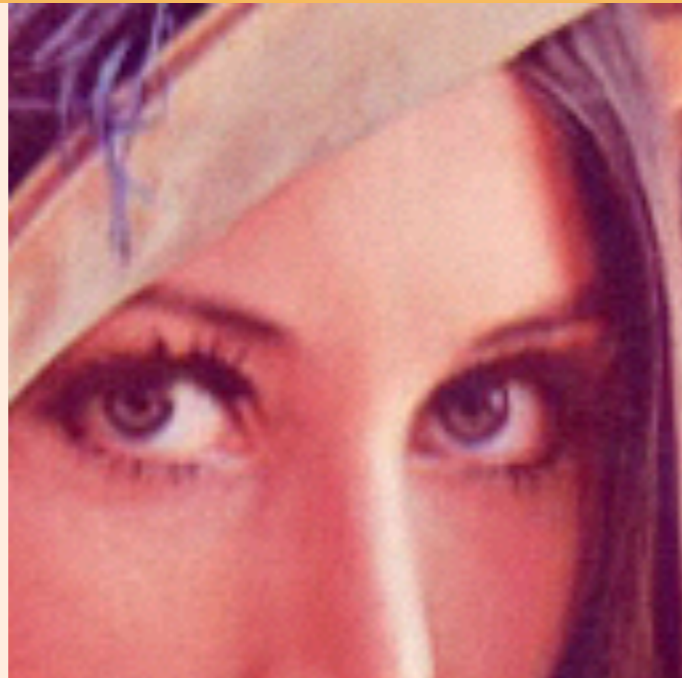
applications

- edge preserving smoothing
 - noise free images
 - noisy images
- detail enhancement

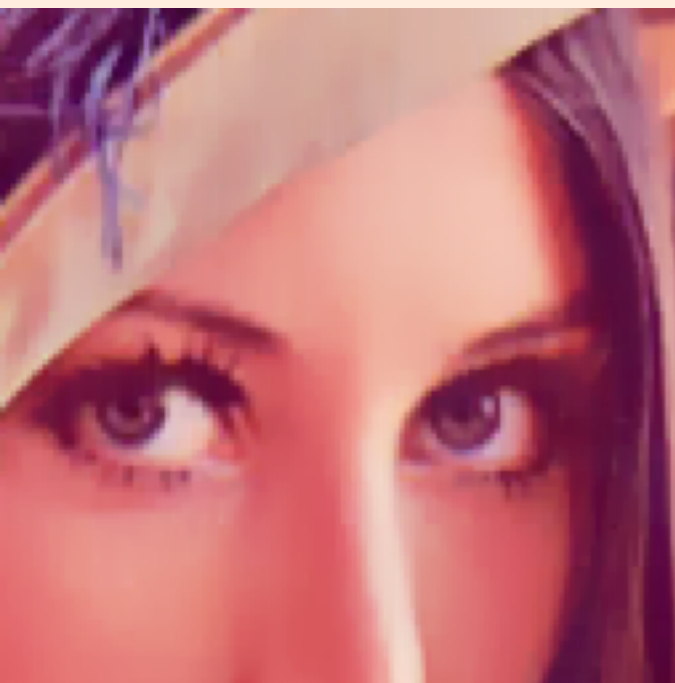
conditions

- **conventional method: original DTF**
 - **DTF: RF / NC**
 - **parameter sigma: controlling smoothing strength**
- **proposed method: multiscale DTF**
 - **DTF: RF / NC**
 - **parameter: controlling thresholding strength**

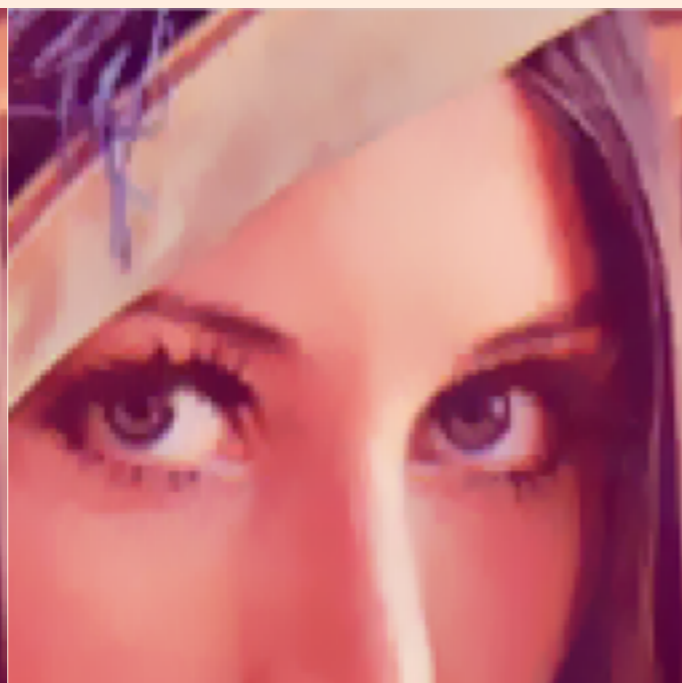
EDGE PRESERVING SMOOTHING



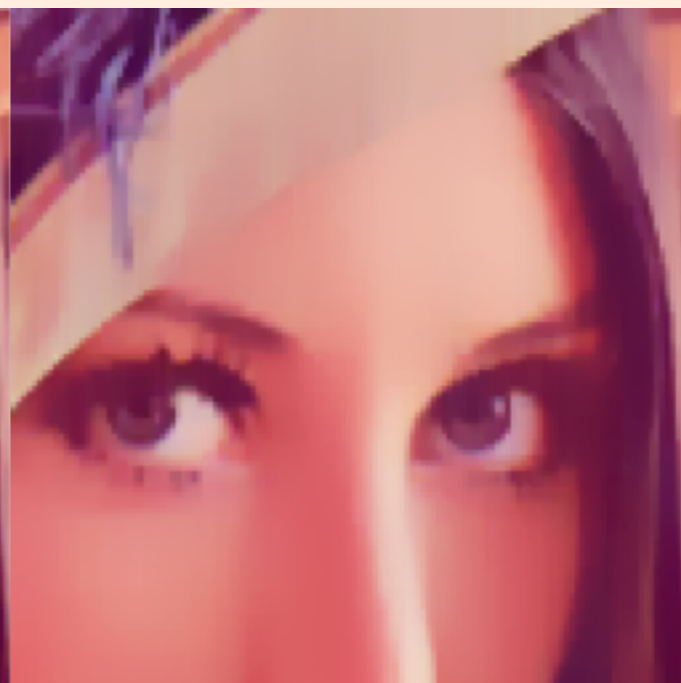
noise-free image



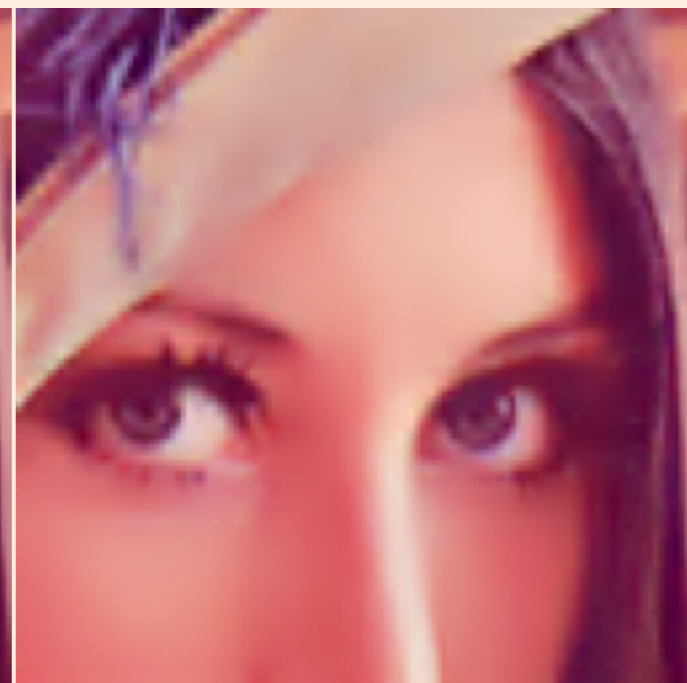
original RF



original NC

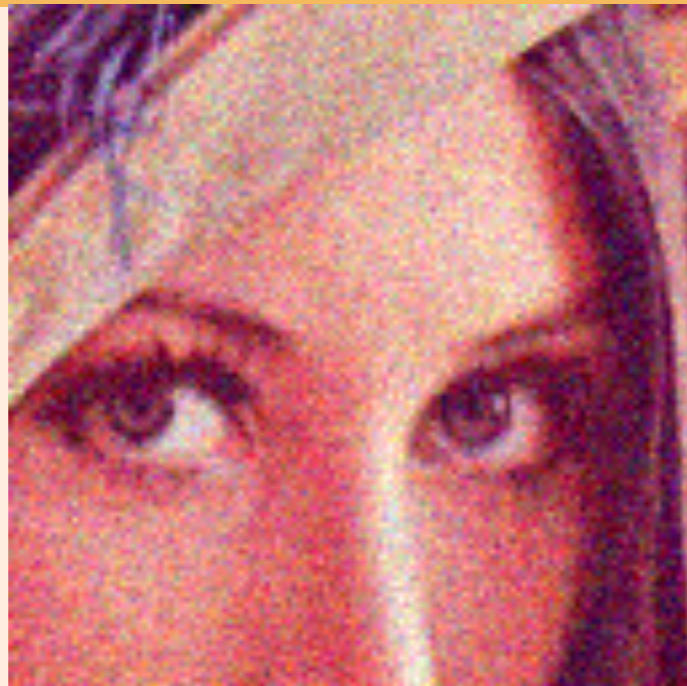


multiscale RF



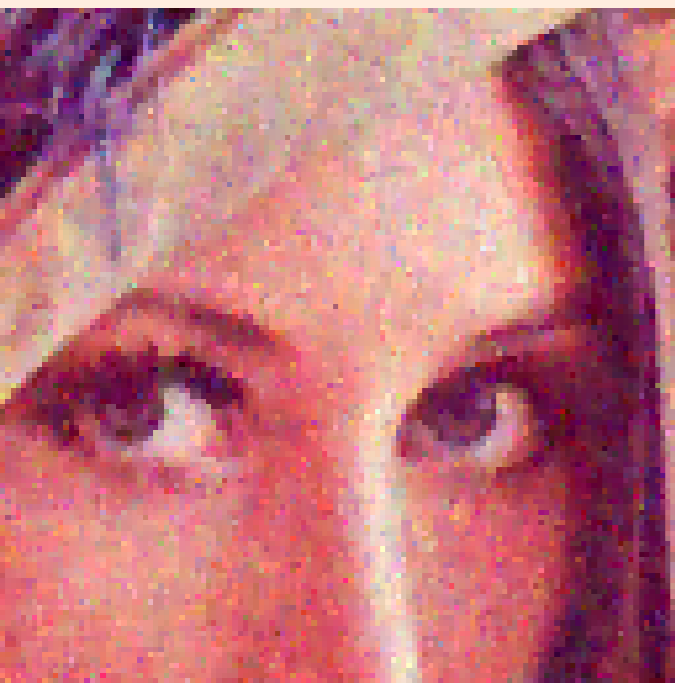
multiscale NC

EDGE PRESERVING SMOOTHING

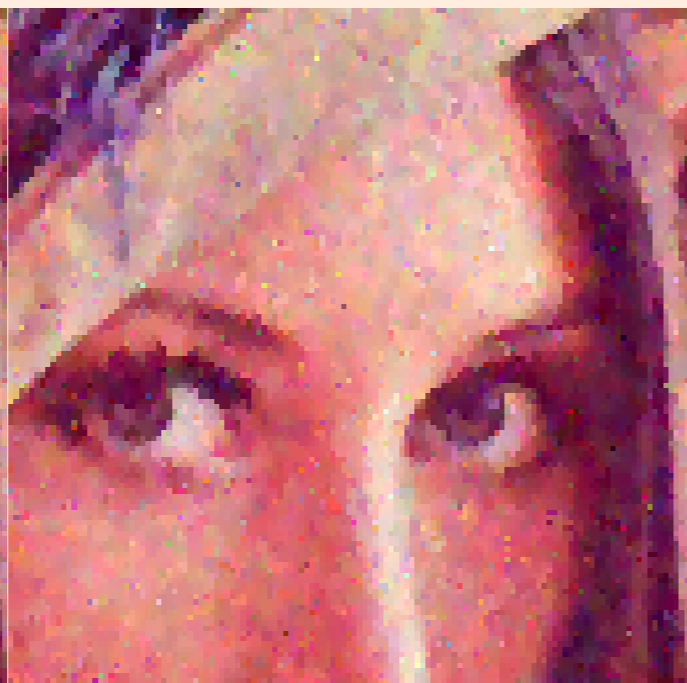


noisy image

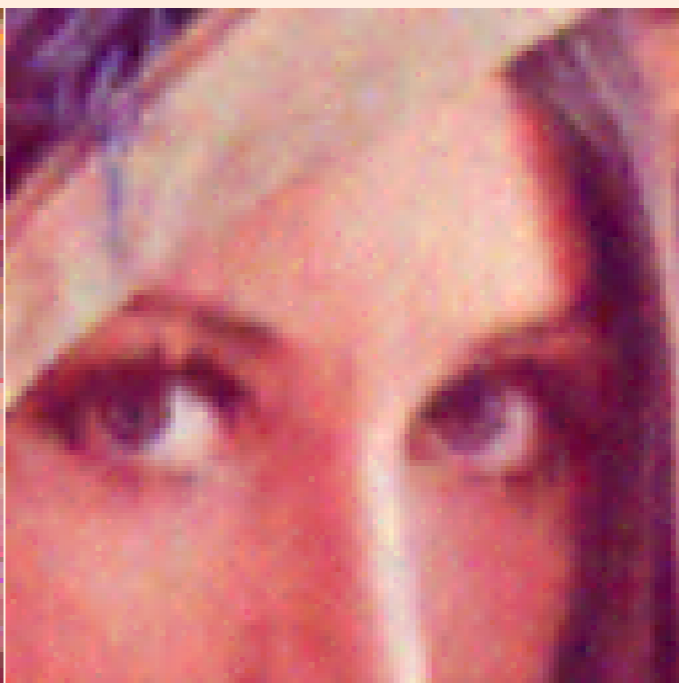
$$\sigma = 20$$



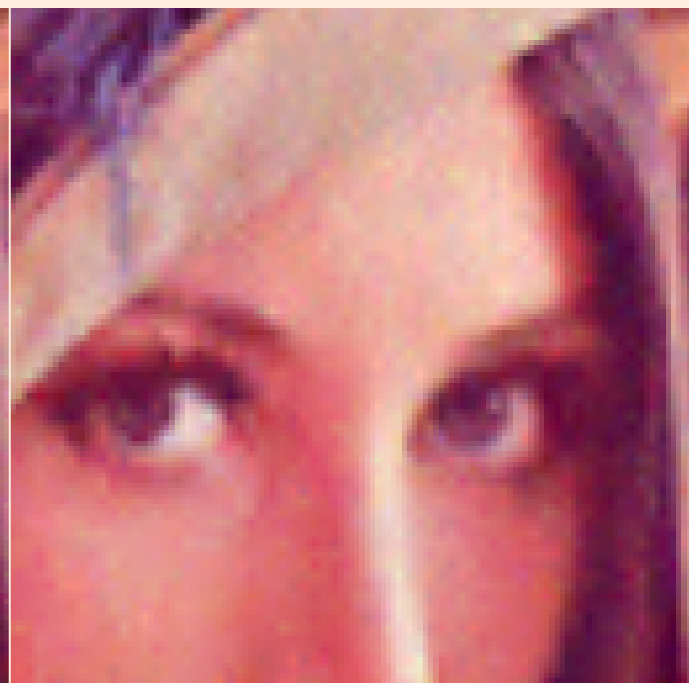
original RF
24.00 dB



original NC
23.76 dB



multiscale RF
27.54 dB



multiscale NC
27.11 dB

PSNR Comparison [dB]

method	original RF	original NC	WLS [3]	L0 [2]	multiscal RF	multiscal NC
<i>Pepper</i>	24.00	23.76	26.45	27.13	27.54	27.11
<i>Lena</i>	25.68	25.77	28.34	27.12	28.58	29.06
<i>House</i>	26.62	26.41	28.34	29.61	29.48	29.86
<i>Milkdrop</i>	26.02	26.21	28.12	28.27	28.52	28.83

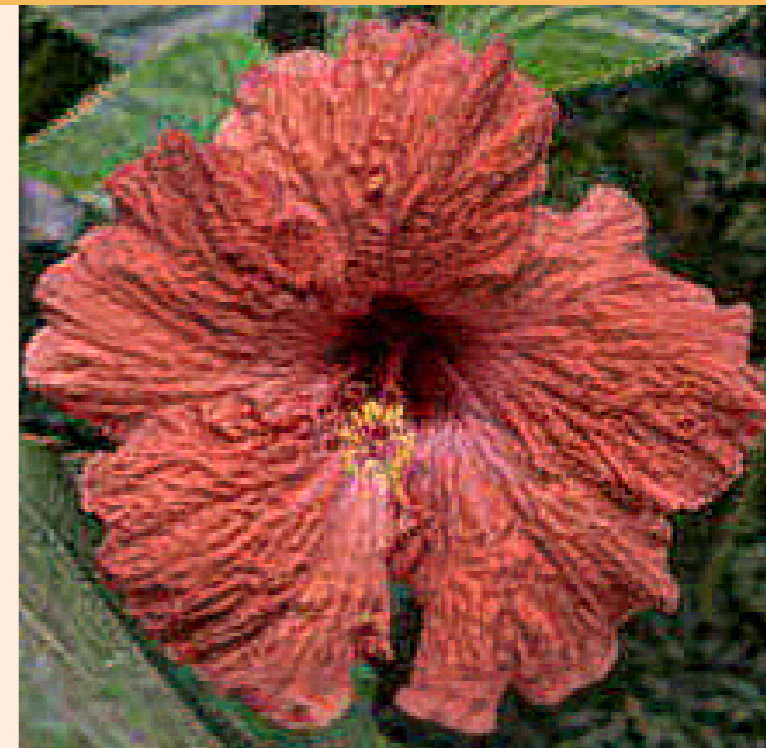
DETAIL ENHANCEMENT



input signal



original NC



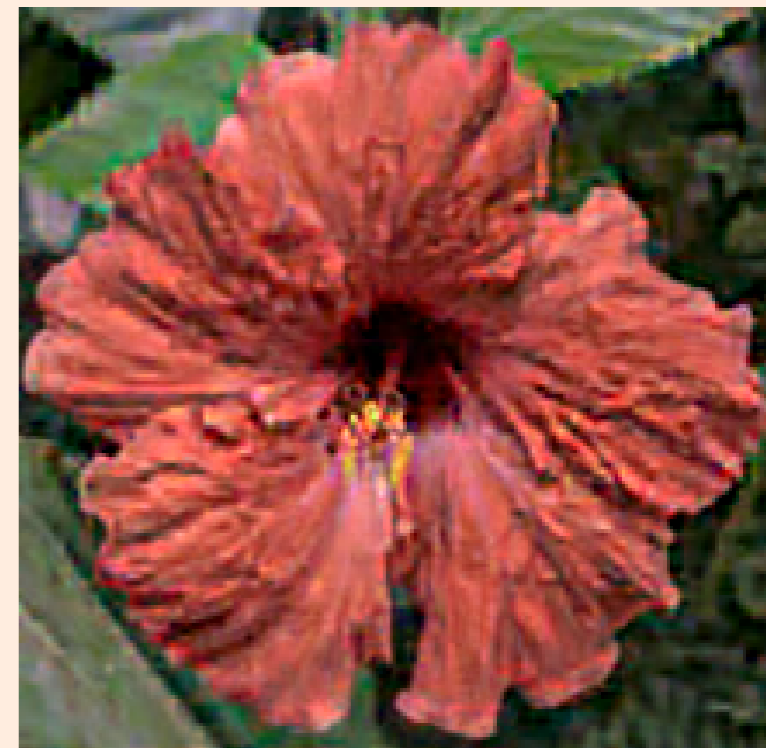
1st level



1st/2nd levels



1st/2nd/3rd levels



2nd level

objective

design of domain transform robust to noise

proposed method

**multiscale image decomposition method
based on the domain transform filter**

result

- **edge preserving smoothing**
→ **satisfactory even in the noisy environments**
- **detail enhancement**
→ **unique results due to multiscale decomposition**

OTHER APPLICATIONS

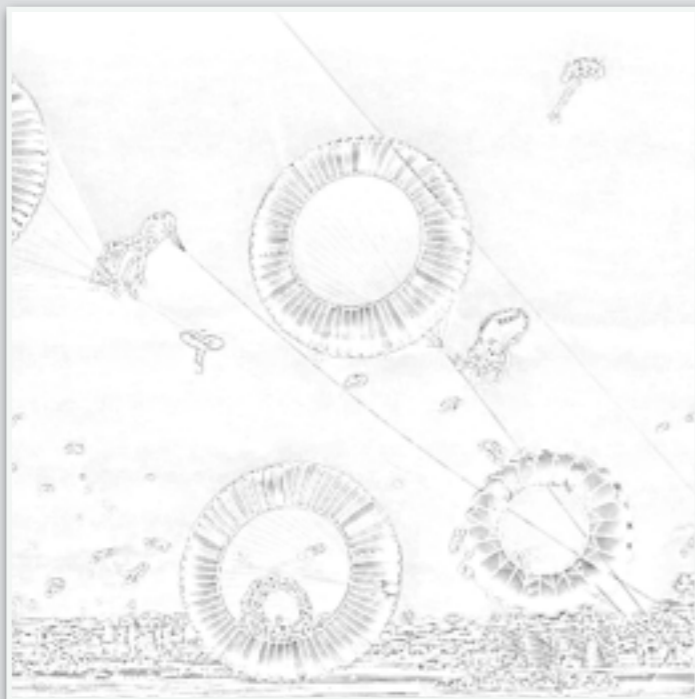
input image



stylization



pencil drawing



- [1] P. Perona and J. Malik, "Scale-space and edge detection using anisotropic diffusion," *IEEE Trans. Pattern Anal. Mach. Intel.*, vol. 12, no. 7, pp. 629 - 639, Jul. 1990.
- [2] C. Tomasi and R. Manduchi, "Bilateral filtering for gray and color images," in *Proc. IEEE Int. Conf. Computer Vision*, pp. 839 - 846, Jan. 1998.
- [3] L. Xu, C. Lu, Y. Xu, and J. Jia, "Image smoothing via L0 gradient minimization," *ACM Trans. Graph.*, vol. 30, no. 6, p. 174, Dec. 2011.
- [4] D. Min, S. Choi, J. Lu, B. Ham, K. SohnMin, and M. Do, "Fast global image smoothing based on weighted least squares," *IEEE Trans. Image Process.*, vol. 23, no. 12, pp. 5638 - 5653, Dec. 2014.
- [5] E. S. L. Gastal and M. M. Oliveira, "Domain transform for edge-aware image and video processing," in *Proc. ACM SIGGRAPH*, vol. 30, no. 4, p. 69, Sep. 2011.
- [6] Burt, Peter J., and Edward H. Adelson. "The Laplacian pyramid as a compact image code." *IEEE Trans. Commun.*, on 31.4 (1983): 532-540.