



Wideband Hybrid Precoder for Massive MIMO Systems

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Background

- Massive MIMO

High array gain, high throughput, low transmission power

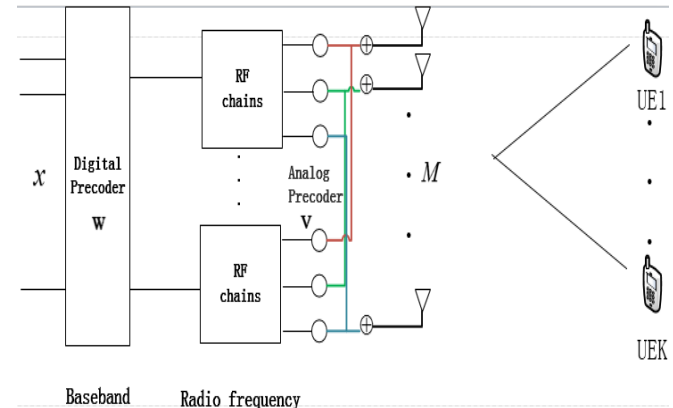
Full digital architecture

Excessive cost, complexity, and energy consumption

Hybrid architecture

Effectively reduce the number of RF chains

Analog precoder + Low-dimensional precoders



Hybrid architecture

Background

- Necessity of frequency-domain scheduling

Full digital architecture

Channel hardening; Plenty spatial degrees of freedom

Unnecessary!

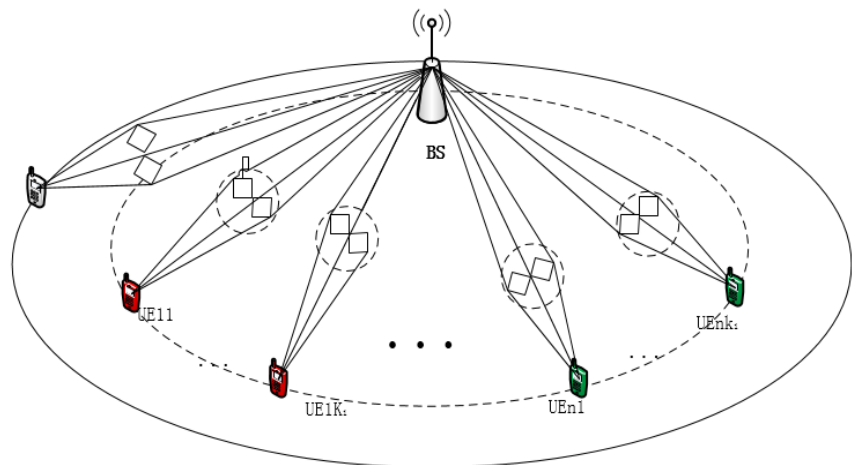
Hybrid architecture

Reduce the spatial degrees of freedom

Necessary!

BUT existing work on hybrid precoder mainly focus on **single-subcarrier**

System Model



Single-cell downlink SDMA-OFDMA massive MIMO system

M antennas ; L RF chains;
 N resource blocks(RBs) ;
 K users served N RBs

For data transmission, the received signal of the k -th user on the n -th RB (UE_{nk})

$$y_{nk} = \mathbf{h}_{nk}^H \mathbf{V} \mathbf{w}_{nk} x_{nk} + \sum_{\substack{j \in \mathcal{K}_n \\ j \neq k}} \mathbf{h}_{nk}^H \mathbf{V} \mathbf{w}_{nj} x_{nj} + z_{nk}$$

Analog Precoder : \mathbf{V}
Digital Precoders : $\{\mathbf{w}_{nk}\}$
Set of UE_{nk} : $\{\mathcal{K}_n\}$

Problem Formulation

Maximize the sum rate of all served users subject to the maximal transmit power of the BS

Joint optimization

non-convex

$$\max_{\mathbf{V}, \{\mathbf{w}_{nk}\}} \sum_{n=1}^N \sum_{k \in \mathcal{K}_n} \log(1 + \text{SINR}_{nk})$$

$$s.t. \sum_{n=1}^N \sum_{k \in \mathcal{K}_n} |\mathbf{V} \mathbf{w}_{nk}|^2 \leq P_{\max}$$

maximal transmit power of the BS

$$|[\mathbf{V}]_{ml}| = 1, m = 1, \dots, M, l = 1, \dots, L$$

Constant modulus

where

$$\text{SINR}_{nk} = \frac{|\mathbf{h}_{nk}^H \mathbf{w}_{nk}|^2}{\sum_{j=1, j \neq k}^K |\mathbf{h}_{nk}^H \mathbf{w}_{nj}|^2 + \sigma_{nk}^2}$$

Difficulties:

Joint optimization

Wideband analog precoder

Precoder Design

Alternating Optimization Algorithm

First, omit the phase-only constraint

Equivalence between sum rate maximization problem and weighted sum mean square error (MSE) minimization problem

$$\min_{\mathbf{V}, \{\mathbf{w}_{nk}, t_{nk}\}} \sum_{n=1}^N \sum_{k \in \mathcal{K}_n} t_{nk} \epsilon_{nk} - \log(t_{nk})$$

weight for the data of UE_{nk}

$$s.t. \sum_{n=1}^N \sum_{k \in \mathcal{K}_n} |\mathbf{V} \mathbf{w}_{nk}| \leq P_{\max}$$

MSE

where

$$\epsilon_{nk} = \sum_{j \in \mathcal{K}_n} \left| g_{nk} \mathbf{h}_{nk}^H \mathbf{V} \mathbf{w}_{nj} \right|^2 - 2 \Re \left\{ g_{nk} \mathbf{h}_{nk}^H \mathbf{V} \mathbf{w}_{nk} \right\} + \left| g_{nk} \right|^2 \sigma_{nk}^2 + 1$$

the receive filter of UE_{nk}

convex for each individual variable of \mathbf{V} , \mathbf{w}_{nk} , t_{nk} and g_{nk} when given the others

Precoder Design

standard alternating optimization method

1. Initialize \mathbf{V} and $\{\mathbf{w}_{nk}\}$ that satisfy the power constraint
2. Calculate g_{nk}
3. Calculate ϵ_{nk} and t_{nk}

4. Digital precoder:
$$\mathbf{w}_{nk} = t_{nk} g_{nk}^H \left(\sum_{j \in \mathcal{K}_n} t_{nj} |g_{nj}|^2 \mathbf{V}^H \mathbf{h}_{nj} \mathbf{h}_{nj}^H \mathbf{V} + \lambda_\omega \mathbf{V}^H \mathbf{V} \right)^{-1} \mathbf{V}^H \mathbf{h}_{nk}$$

the lagrangian multiplier

5. Analog precoder:
$$\mathbf{v} = \left(\sum_{n=1}^N \sum_{k \in \mathcal{K}_n} \left(t_{nk} |g_{nk}|^2 \sum_{j \in \mathcal{K}_n} (\mathbf{w}_{nj}^H \mathbf{w}_{nj})^T \otimes (\mathbf{h}_{nk}^H \mathbf{h}_{nk}) + \lambda_v (\mathbf{w}_{nk} \mathbf{w}_{nk}^H)^T \otimes \mathbf{I} \right) \right)^{-1} \sum_{n=1}^N \sum_{k \in \mathcal{K}_n} t_{nk} g_{nk}^H (\mathbf{w}_{nk}^H)^T \otimes \mathbf{h}_{nk}$$

6. Repeat steps 2~5 until convergence

Alternating!

7. Update

$$[\mathbf{V}]_{ml} \leftarrow \frac{[\mathbf{V}]_{ml}}{[\mathbf{V}]_{ml}}$$

Precoder Design

A low-complexity algorithm

First, omit the phase-only constraint

Optimize the analog precoder — uplink-downlink duality theory

$$\max_{\mathbf{V}} \max_{\{\mathbf{D}_n\}} \sum_{n=1}^N \log \det (\mathbf{D}_n \bar{\mathbf{H}}_n^H \mathbf{V} \mathbf{V}^H \bar{\mathbf{H}}_n + \mathbf{I})$$

sum capacity of the equivalent downlink channels $\mathbf{h}_{nk}^H \mathbf{V}$

$$s.t. \sum_{n=1}^N \text{Tr} (\mathbf{D}_n) \leq P_{\max}$$

$$\mathbf{V}^H \mathbf{V} = \mathbf{I}$$

Proposition :
An analog precoding matrix with orthogonal columns is optimal for sum capacity maximization

$\{\mathbf{D}_n\}$: transmit power matrix of UE_{nk} in the dual uplink

Optimize digital precoders

Steps 2~4 of alternating optimization algorithm

Decoupling

Precoder Design

First find \mathbf{D}_n

By assuming a full digital system and the channels of all users are orthogonal

$$[\mathbf{D}_n]_{ii} = \left(\mu - \frac{\sigma_{n\mathcal{K}_n(i)}^2}{\|\mathbf{h}_{n\mathcal{K}_n(i)}\|^2} \right)^+$$

μ : the water-level variable that is chosen to ensure $\sum_{n=1}^N \text{Tr}(\mathbf{D}_n) = P_{\max}$

Given \mathbf{D}_n and , optimize \mathbf{V}

Semi-definite relaxation (SDR) method $\mathbf{V}\mathbf{V}^H = \mathbf{Q}$

$$\max_{\mathbf{V}} \sum_{n=1}^N \log \det (\mathbf{D}_n \bar{\mathbf{H}}_n^H \mathbf{Q} \bar{\mathbf{H}}_n + \mathbf{I})$$

$$s.t. \text{Tr}(\mathbf{Q}) = L$$

$\mathbf{Q} \succ 0$ \rightarrow \mathbf{Q} is positive semi-definite

$$\text{rank}(\mathbf{Q}) = L$$

Employ the Gaussian randomization method to obtain the analog precoder \mathbf{V}

$$\text{Update } [\mathbf{v}]_{ml} \leftarrow \frac{[\mathbf{V}]_{ml}}{[\mathbf{V}]_{ml}}$$

Simulation results

- divide all RBs into B groups and schedule the same users for the RBs in each group
- $B=1$: SDMA-OFDM $B>1$:SDMA-OFDMA

antennas	64	RBs	32
P_{\max} of the BS	46 dBm	K	16
The cell radius	250 m	$\{\mathcal{K}_n\}$	8
The path loss model	$35.3+37.6\log_{10}(d)$		
SNR	10 dB		

Methods for comparing

- “Random scheduling” : select users randomly for each group
- “Greedy scheduling” : select users providing the maximal sum rate for each group

Channel Model

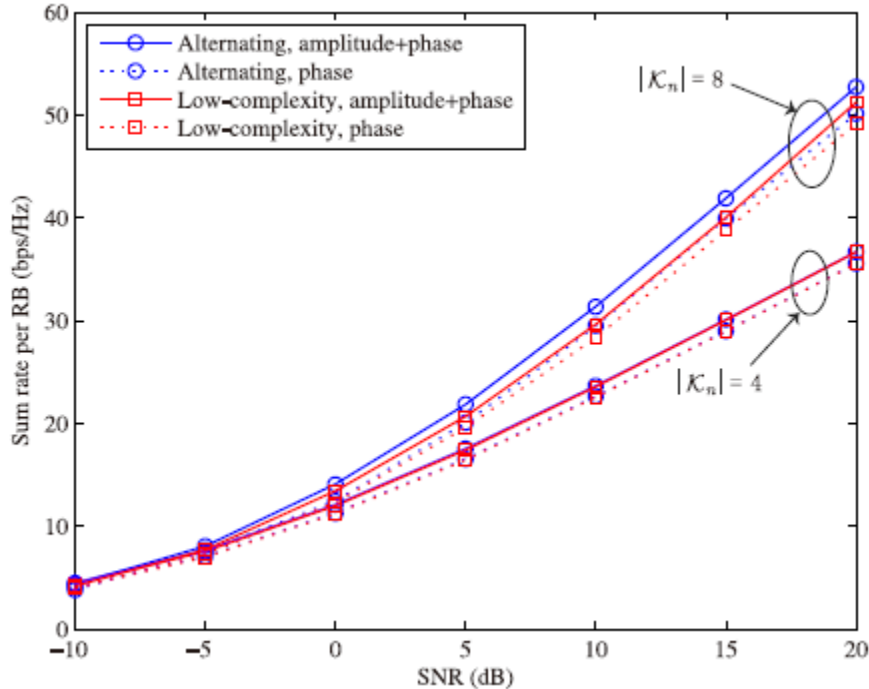
3GPP 36.873 UMa/NLOS

8×8 planar antenna array

elevation angle: $[-45^\circ, 45^\circ]$

azimuth angle: $[-60^\circ, 60^\circ]$

Simulation results



$L=8$

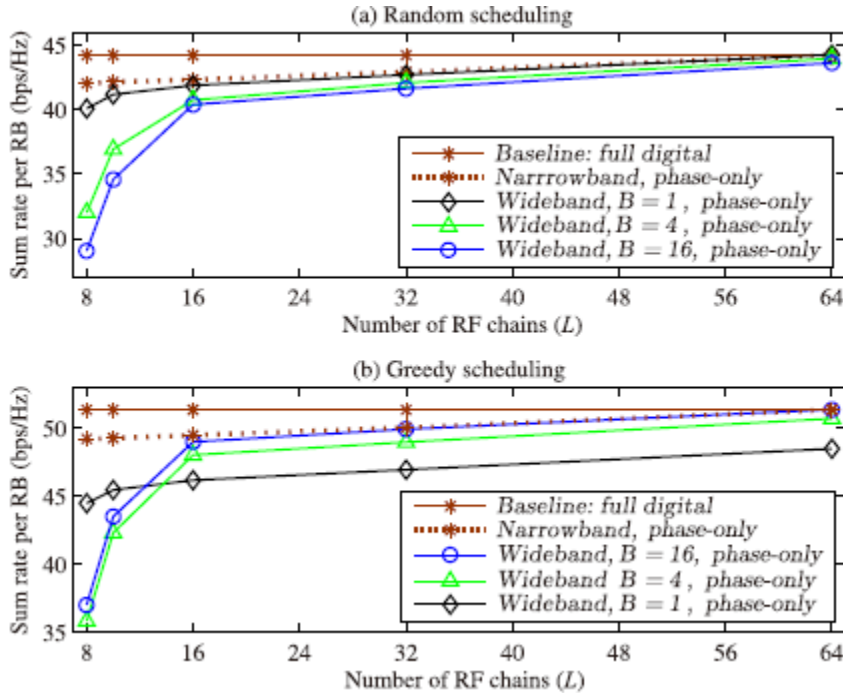
$B=16$

Random scheduling

1. low-complexity algorithm performs close to the alternating optimization algorithm no matter when $|\mathcal{K}_n| = 4$ or $|\mathcal{K}_n| = 8$.
2. Phase only constraint on analog precoder leads to slight performance loss for both algorithms.

Performance comparison of the proposed algorithms

Simulation results



Baseline: the per-RB performance of full digital precoder

1. “Random scheduling”:
larger performance gap between “hybrid” and “full digital” in wideband systems;
larger B , larger performance gap.
2. “Greedy scheduling”:
Increasing B increases the multiuser diversity gain but reduces the array gain.



With greedy scheduling, the performance can be improved, when both B and L are large

Impact of the number of RF chains and frequency-domain scheduling

Conclusions

- Optimized wideband hybrid precoder and investigated the necessity of frequency scheduling and the effectiveness of hybrid precoder in SDMA-OFDMA massive MIMO systems.
- Proposed a alternating optimization algorithm and an efficient non-iterative algorithm.
- Necessity of frequency scheduling and the effectiveness of wideband hybrid precoder depend on the employed scheduling method and the number of available RF chains

Thank you for your attention!